

Electromagnetic Engineering (EC 21006)

TUTORIAL - IX

TRANSMISSION LINES -- FREQUENCY DOMAIN ANALYSIS

1. A lossless transmission line with $Z_0 = 60\Omega$ is being operated at 60 MHz. The velocity of the line is $3 \times 10^8 \text{ m/s}$. If the line is short-circuited at $z = 0$, find Z_{in} at $z =$: (a) -1m ; (b) -2m ; (c) -2.5m ; (d) -1.25m .
2. The characteristic impedance of a certain lossless transmission line is 72Ω . If $L = 0.5\mu\text{H}/\text{m}$, find: (a) C ; (b) v_p ; (c) β if $f = 80 \text{ MHz}$. (d) The line is terminated with a load of 60Ω . Find Γ and s .
3. A lossless transmission line having $Z_0 = 120\Omega$ is operating at $\omega = 5 \times 10^8 \text{ rad/s}$. If the velocity on the line is $2.4 \times 10^8 \text{ m/s}$, find: (a) L ; (b) C . (c) Let Z_L be represented by an inductance of $0.6\mu\text{H}$ in series with a 100Ω resistance. Find Γ and s .
4. Two characteristics of a certain lossless transmission line are $Z_0 = 50\Omega$ and $\gamma = 0 + j0.2\pi \text{ m}^{-1}$ at $f = 60 \text{ MHz}$: (a) find L and C for the line. (b) A load $Z_L = 60 + j80\Omega$ is located at $z = 0$. What is the shortest distance from the load to a point at which $Z_{in} = R_{in} + j0$?
5. A transmitter and receiver are connected using a cascaded pair of transmission lines. At the operating frequency, line 1 has a measured loss of $0.1\text{dB}/\text{m}$, and line 2 is rated at $0.2\text{dB}/\text{m}$. The link is composed of 40m of line 1 joined to 25m of line 2. At the joint, a splice loss of 2dB is measured. If the transmitted power is 100mW , what is the received power?
6. A 100MHz voltage source drives the series combination of an impedance, $Z_g = 25 + j25\Omega$ and a lossless transmission line of length $\lambda/4$, terminated by a load impedance, Z_L . The line characteristic impedance is 50Ω . (a) Determine the load impedance value required to achieve a net impedance (seen by the voltage source) of 50Ω . (b) If the inductance of the line is $L = 1\mu\text{H}/\text{m}$, determine the line length in meters.
7. A 1000-m -long communication line has the following per-unit-length parameters: $R_l = 22 \text{ m}\Omega/\text{m}$, $L_l = 0.63 \mu\text{H}/\text{m}$, $G_l = 0.1 \mu\text{S}/\text{m}$, $C_l = 31 \text{ pF}/\text{m}$. The resistive load at the receiving end of this line absorbs 10 W at 50 V (rms). Determine the sending-end voltage, current, and power for an operating frequency of 10 kHz .
8. A 10-m -long lossless transmission line feeds a load having an impedance of $35 + j10 \Omega$. The load voltage is $\sqrt{2} \times 50 \cos 10^8 t \text{ V}$. The voltage applied to the line is $\sqrt{2} \times 66 \cos(10^7 t + 31^\circ) \text{ V}$. Calculate the distributed inductance and capacitance of the line.
9. The incident voltage wave on a certain lossless transmission line for which $Z_0 = 50\Omega$ and $v_p = 2 \times 10^8 \text{ m/s}$ is $V^+(z, t) = 200 \cos(\omega t - \pi z) \text{ V}$. (a) Find ω . (b) Find $I^+(z, t)$. The section of the line for which $z > 0$ is replaced by a load $Z_L = 50 + j30\Omega$ at $z = 0$. Find (c) Γ_L ; (d) $V_s^-(z)$; (e) V_s at $z = -2.2 \text{ m}$.
10. A 50Ω lossless line is terminated with 60 and 30Ω resistors in parallel. The voltage at the input to the line is $v(t) = 100 \cos(5 \times 10^9 t)$ and the line is three-eighths of a wavelength long. What average power is delivered to each load resistor?
11. A lossless transmission line is 50 cm in length and operating at a frequency of 100 MHz . The line parameters are $L = 0.2 \mu\text{H}/\text{m}$ and $C = 80 \text{ pF}/\text{m}$. The line is terminated in a short circuit at $z = 0$, and there is a load $Z_L = 50 + j20\Omega$ across the line at location $z = -20\text{cm}$. What average power is delivered to Z_L if the input voltage is $100\angle 0^\circ \text{ V}$?