

# Enhanced Sampling & Metadynamics

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# Molecular Dynamics reminder

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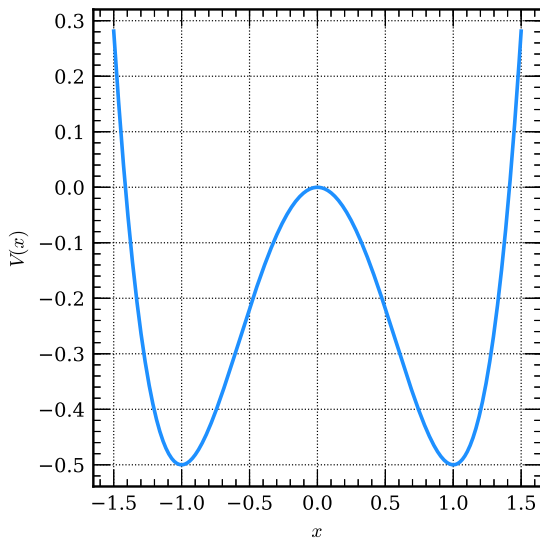
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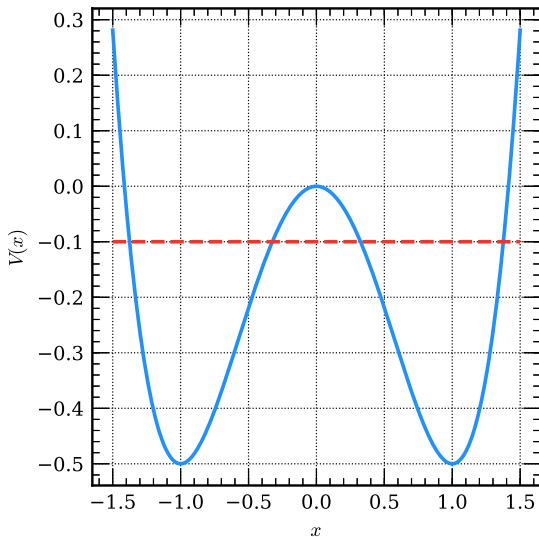
$$v(t + \Delta t) = v(t) + \frac{1}{2}(a(t) + a(t + \Delta t))\Delta t$$

$$x(t + \Delta t) = x(t) + v(t)\Delta t + \frac{1}{2}a(t)\Delta t^2$$

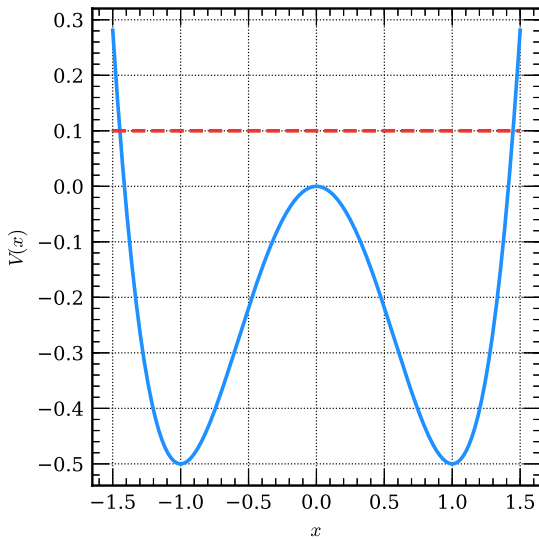
# Potential Energy Surface



# Impossible events



# Rare events





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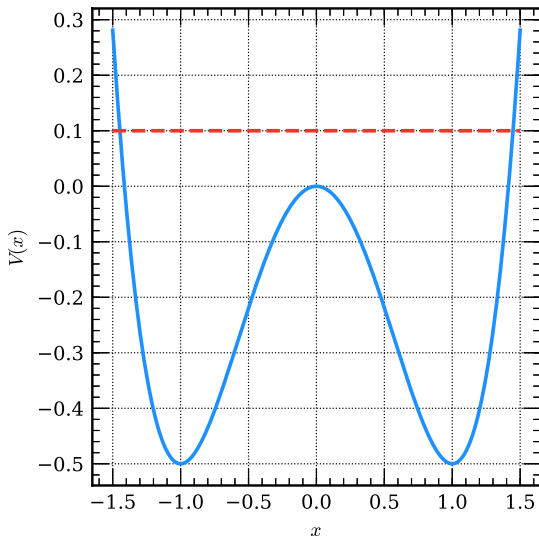
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Enhanced sampling lets us simulate more of the interesting chemistry in the same amount of simulation time.

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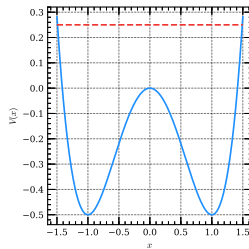
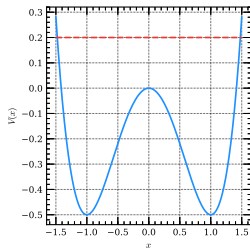
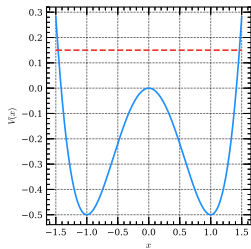
We can control  $T$  and the PES.<sup>1</sup>

- **Temperature** - “Tempering” methods control the temperature to overcome barriers
- **PES:**
  - Bias the PES by adding another potential to limit sampling of the same area
  - Modify the forcefield to raise minima

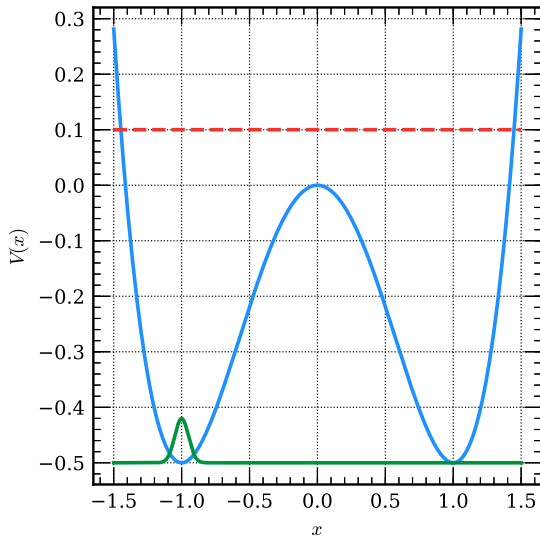
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<sup>1</sup>Abrams, C.; Bussi, G. *Entropy* **2014**, *16*, 163–199, Miao, Y.; McCammon, J. A. *Molecular Simulation* **2016**, *42*, 1046–1055.

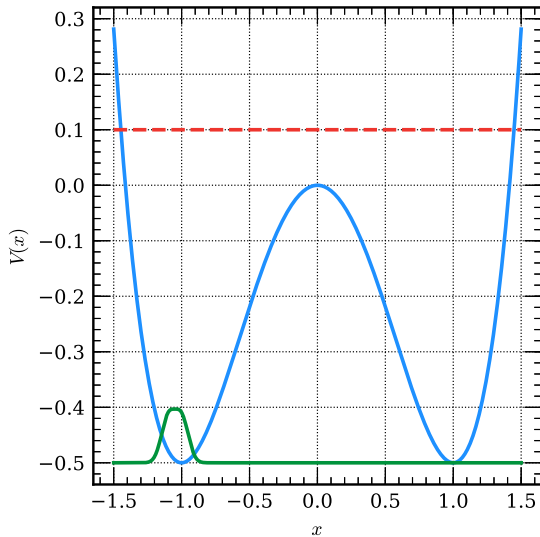
# Replica Exchange/Parallel Tempering



# Metadynamics

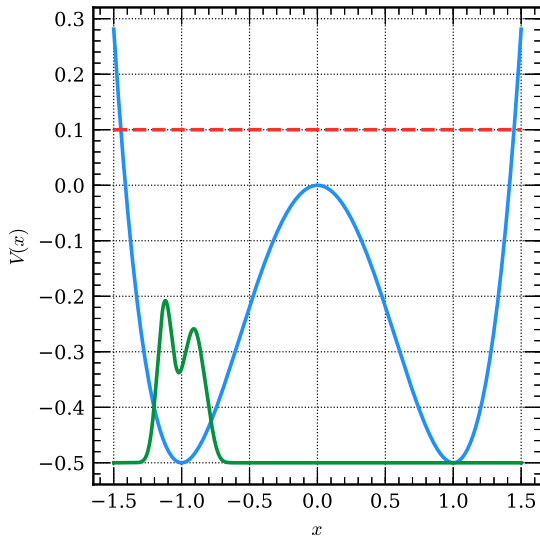


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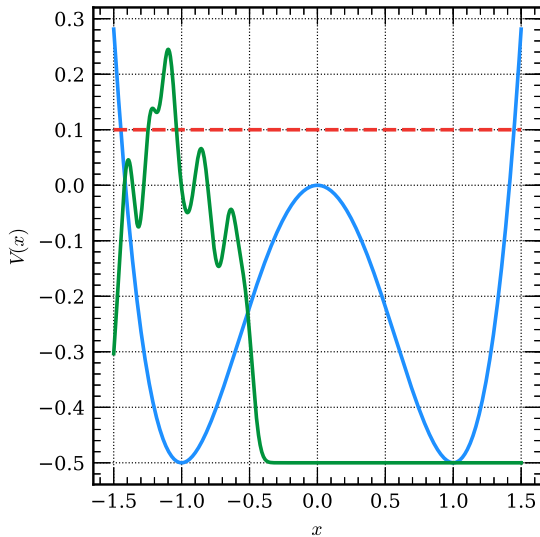




# Metadynamics



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# Accelerated Molecular Dynamics

