

Stack

- stack is a linear data structure in which data is stored sequentially.
- in stack, data insertion and deletion is allowed from only one end (top).
- stack follows the principle of "Last In First Out"
- all operations of stack are done in $O(1)$ time
- stack can be implemented using array or linked list

size = 5



Operations:

1. Add/Insert/Push

- reposition top (inc)
- add data at top index

2. Delete/Remove/Pop

- reposition top (dec)

3. Peek (Collect)

- read data from top index

Conditions:

Empty

$\text{top} == -1$

Full

$\text{top} == \text{size} - 1$

Stack Application

Expression Evaluation and Conversion

1. Postfix Evaluation
2. Prefix Evaluation
3. Infix to Postfix Conversion
4. Infix to Prefix Conversion

Expression:

- combination of operators and operands
 - operators are mathematical operations like +, -, *, /, % or power
 - operands are values/numbers/variables

e.g. $a + b - c$, $a + b * c$, a

Types

- | | | |
|------------|---------|------------|
| 1. Infix | $a + b$ | - human |
| 2. Prefix | $+ a b$ | - computer |
| 3. Postfix | $a b +$ | - computer |

Priorities:

()
power \$
* / %
+ -



Postfix Evaluation

Postfix : 4 5 6 * 3 / + 9 + 7 -

left \longrightarrow right

⑤ $23 - 7 = 16$

Result = 16

④ $14 + 9 = 23$

③ $4 + 10 = 14$

② $30 / 3 = 10$

① $5 * 6 = 30$

Stack

| |
|---------------|
| |
| |
| 16 |
| 7 |
| 23 |
| 9 |
| 14 |
| 10 |
| 3 |
| 30 |
| 6 |
| 5 |
| 4 |

top

ele
'0' - ascii 48 $\Rightarrow 48 - 48 = 0$
'1' - ascii 49 $\Rightarrow 49 - 48 = 1$
'2' - ascii 50 $\Rightarrow 50 - 48 = 2$
'3' - ascii 51 $\Rightarrow 51 - 48 = 3$
'4' - 52 $\Rightarrow 52 - 48 = 4$
.
|

Prefix Evaluation

Prefix : - + + 4 / * 5 6 3 9 7

left ← right $23 - 7$
 $= 16$

$$14 + 9 = 23$$

Result = 16

$$4 + 10 = 14$$

$$30 / 3 = 10$$

$$5 * 6 = 30$$

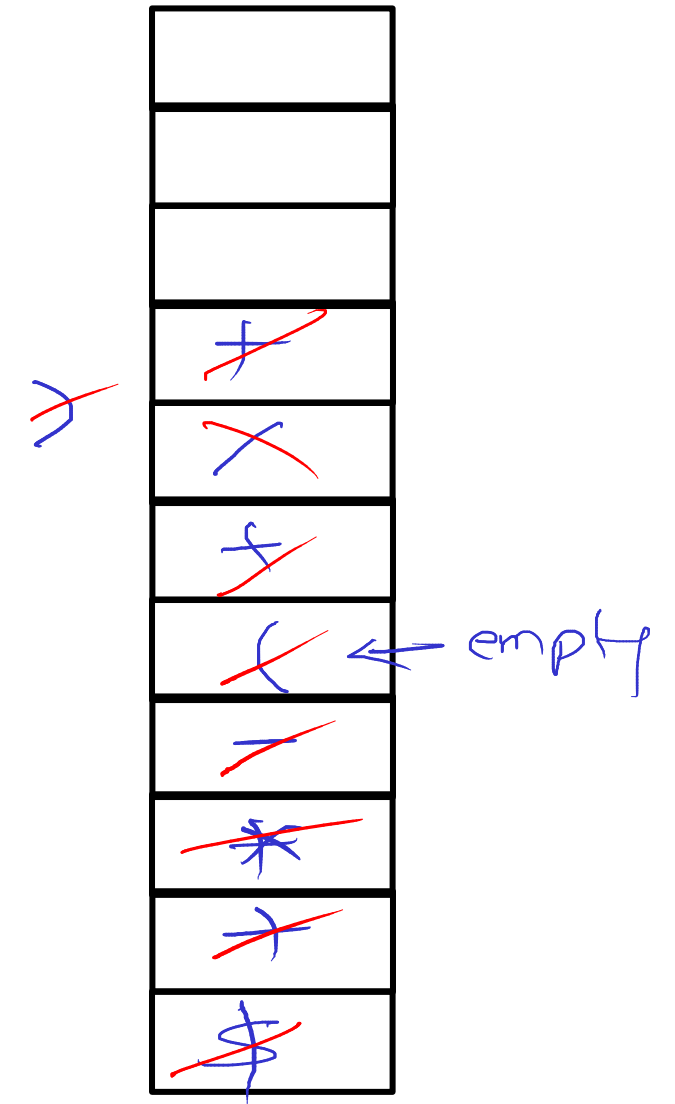
| |
|---------------|
| 16 |
| 23 |
| 14 |
| 4 |
| 10 |
| 30 |
| 5 |
| 6 |
| 3 |
| 9 |
| 7 |

Infix to Postfix conversion

Infix : $1 \$ 9 + 3 * 4 - (6 + 8 / 2) + 7$

left \longrightarrow **right**

Postfix : $1 9 \$ 3 4 * + 6 8 2 / + - 7 +$



Infix to Prefix conversion

Infix : $1 \$ 9 + 3 * 4 - (6 + 8 / 2) + 7$

left \longleftarrow right

Expression : $7 2 8 / 6 + 4 3 * 9 1 \$ + - +$

Prefix : $+ - + \$ 1 9 * 3 4 + 6 / 8 2 7$

| |
|--------------|
| |
| |
| |
| \$ |
| + |
| * |
| - |
| + |
| X |
|) |
| + |

Infix to postfix and prefix conversion

Postfix

Infix : 1 \$ 9 + 3 * 4 - (6 + 8 / 2) + 7

1 \$ 9 + 3 * 4 - (6 + 8 2 /) + 7

1 \$ 9 + 3 * 4 - 6 8 2 / + + 7

1 9 \$ + 3 * 4 - 6 8 2 / + + 7

1 9 \$ + 3 4 * - 6 8 2 / + + 7

1 9 \$ 3 4 * + - 6 8 2 / + + 7

1 9 \$ 3 4 * + 6 8 2 / + - + 7

1 9 \$ 3 4 * + 6 8 2 / + - 7 +

Prefix

Infix : 1 \$ 9 + 3 * 4 - (6 + 8 / 2) + 7

\$ 1 9 + * 3 4 - (6 + 8 2 /) + 7

\$ 1 9 + * 3 4 - + 6 8 2 / + 7

+ \$ 1 9 * 3 4 - + 6 8 2 / + 7

- + \$ 1 9 * 3 4 + 6 8 2 / + 7

+ - + \$ 1 9 * 3 4 + 6 8 2 /