

Approach

Iterative

We use loops

```
int fact(int n){  
    int fact = 1;  
    for(int i = 1 ; i <= n ; i++)  
        fact *= i;  
    return fact;  
}
```

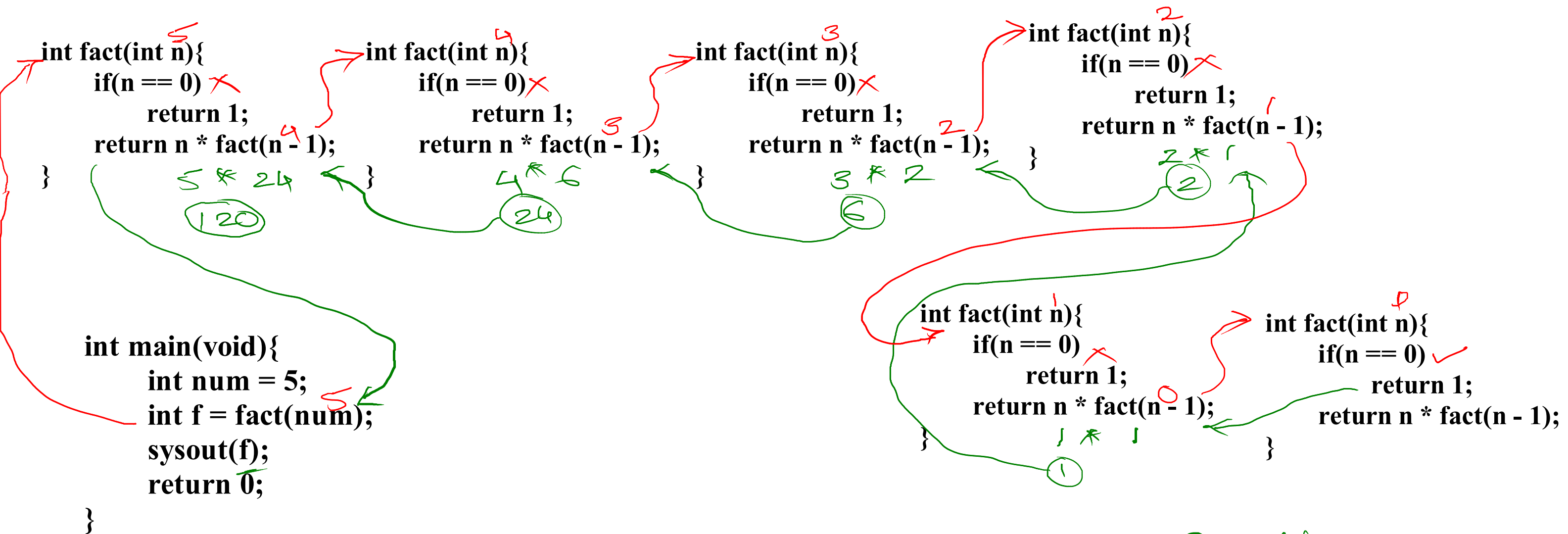
Recursive

Recursive function

$n! = n * (n - 1)!$

$n = 0$, then stop

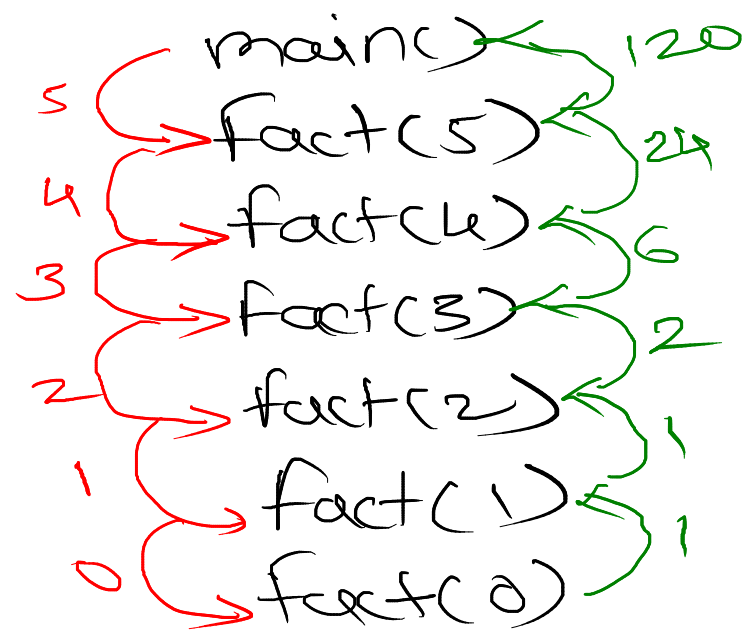
```
int fact(int n){  
    if(n == 0)  
        return 1;  
    return n * fact(n - 1);  
}
```



For every function call, Function Activation Record is created stack.

FAR

- ① Return Addr
- ② Formal Argument
- ③ local variable



```
int binarySearch(int arr[], int key, int left, int right) {  
    0) stop if partition is invalid  
    if (left > right)  
        return -1;
```

1) Find middle element of array
 $mid = (left + right) / 2$

2) Compare middle element with key
if (key == arr[mid])
 return mid; — if key is matching

3) if key < middle element
 — search key into left partition
 return binarySearch(arr, key, left, mid-1);

4) if key > middle element
 — search key into right partition.
 return binarySearch(arr, key, mid+1, right);

}

binarySearch(arr, 66, 0, 8) m = 4
binarySearch(arr, 66, 5, 8) m = 6
binarySearch(arr, 66, 5, 5) m = 5



Algorithm Analysis

- find out the number of resources required to execute the algorithm
- resources are time and space

Exact Analysis

- finding out the exact time and space required to execute
- time (nS, uS, mS) - time is dependent on processor type, number of processes running at that time
- space (Bytes, Kb, Mb, Gb) - space is dependent on datatypes, processor type [Space required to store FAR vary from arch to arch]

Approximate Analysis

- finding out the approximate time and space required to execute
- Asymtotic analysis - mathematical way of finding out time and space required
- Big O / $O()$ notation is used to indicate complexities(time and space)

Time Analysis

- unit time required to execute the algorithm
- time is equal to number of iterations of the loop

1. factorial of given number

```
int fact(int n){  
    int fact = 1;  
    for(int i = 1 ; i <= n ; i++)  
        fact *= i;  
    return fact;  
}
```

$\sum \text{itr} = n$

Time \propto itr

Time $\propto n$

$$T(n) = O(n)$$

2. Print 2D array on console

```
void print2DArray(int arr[][], int row, int col){  
    for(int i = 0 ; i < row ; i++){  
        for(int j = 0 ; j < col ; j++){  
            sysout(arr[i][j]);  
        }  
    }  
}
```

$\overset{n}{\text{itr}} = n$
 $\overset{n}{\text{itr}} = n$

Total itr = $n * n = n^2$

Time \propto itr

Time $\propto n^2$

$$T(n) = O(n^2)$$

3. Add two numbers

```
int sum(int num1 , int num2){  
    int res = num1 + num2;  
    return res;  
}
```

Time requirement of
this algorithm is constant

$$T(n) = O(1)$$

4. Print table of given number

```
void printTable(int num){
    for(int i = 1 ; i <= 10 ; i++)
        sysout(num * i);
}
```

$$\sum_{i=1}^{10} i = 10$$

$$\text{Time} \propto \text{itr}$$

$$\text{Time} \propto 10$$

$$T(n) = O(1)$$

5. Print binary of given decimal

```
void decToBinary(int num){
    while(num > 0){
        sysout(num % 2);
        num /= 2;
    }
}
```

$$n = 9, 4, 2, 1$$

$$n = 9, 9/2, 4/2, 2/2$$

$$= n, n/2, n/4, n/8, \dots$$

$$= \frac{n}{2^0}, \frac{n}{2^1}, \frac{n}{2^2}, \frac{n}{2^3}, \dots, \frac{n}{2^{i(\text{itr})}}$$

for last value 1, condition of loop will be true

$$\frac{n}{2^{\text{itr}}} = 1$$

$$n = 2^{\text{itr}}$$

$$\log 2^{\text{itr}} = \log n$$

$$\text{itr} = \frac{\log n}{\log 2}$$

$$\text{Time} \propto \frac{\log n}{\log 2}$$

$$T(n) = O(\log n)$$

| | | | | |
|----------|---|--------------|---|---|
| 9 | - | 9 % 2 | - | 1 |
| | - | 9/2=4 | | |
| 4 | - | 4 % 2 | - | 0 |
| | - | 4/2=2 | | |
| 2 | - | 2 % 2 | - | 0 |
| | - | 2/2=1 | | |
| 1 | - | 1 % 2 | - | 1 |
| <u>1</u> | - | <u>1/2=0</u> | | |