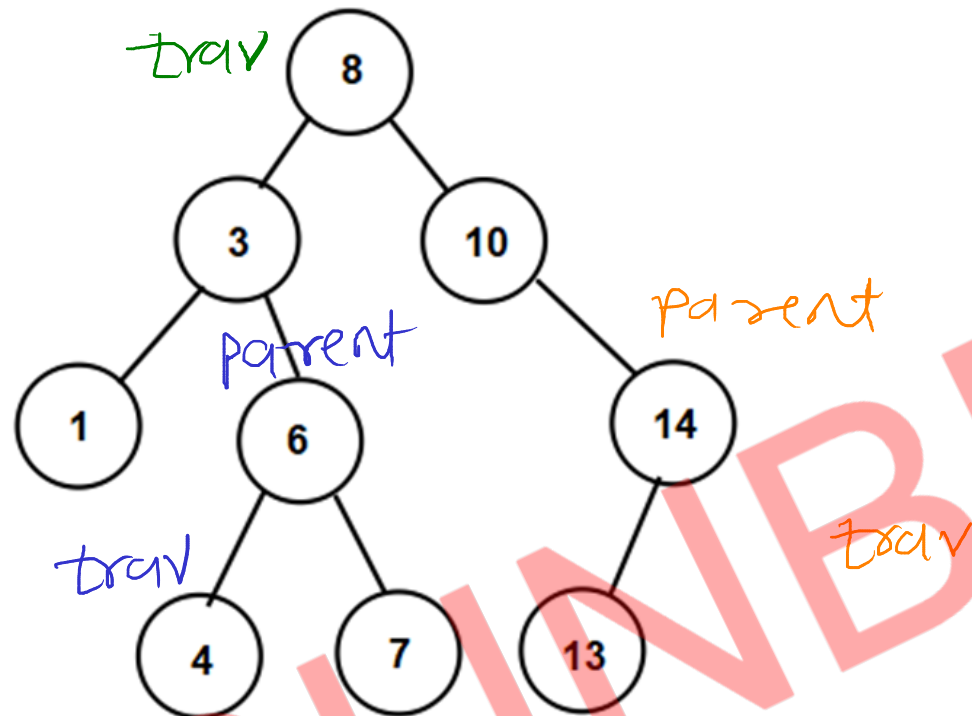


# parent BST - Search with Parent



Key = 15

trav	parent
\$8	null
\$10	\$8
\$14	\$10
null	\$14

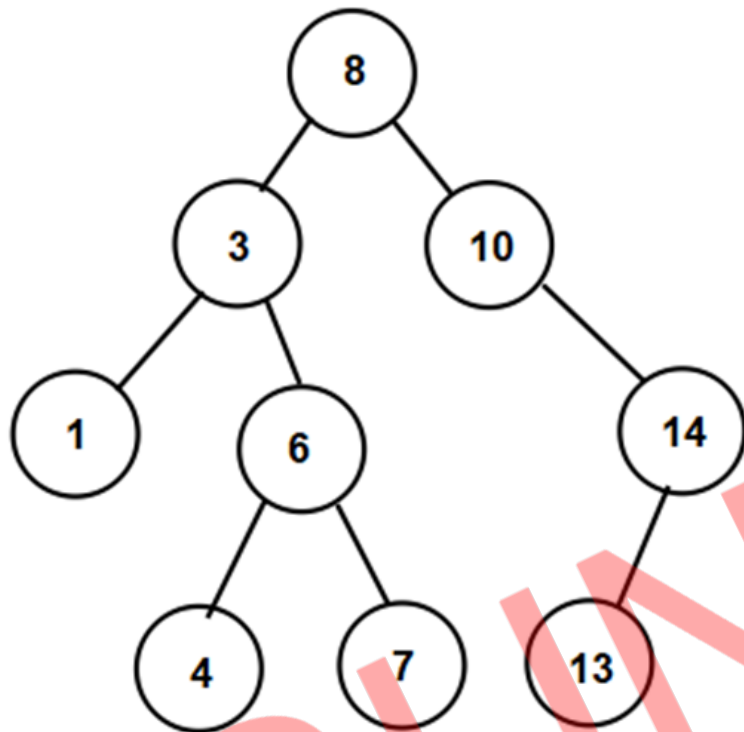
Key = 4

trav	parent
\$8	null
\$3	\$8
\$4	\$3
	\$6

Key = 8

trav	parent
\$8	null

## BST - Delete Node



Parent's left      root      Parent's right

Node

Non leaf

Leaf

two child

single child

right child

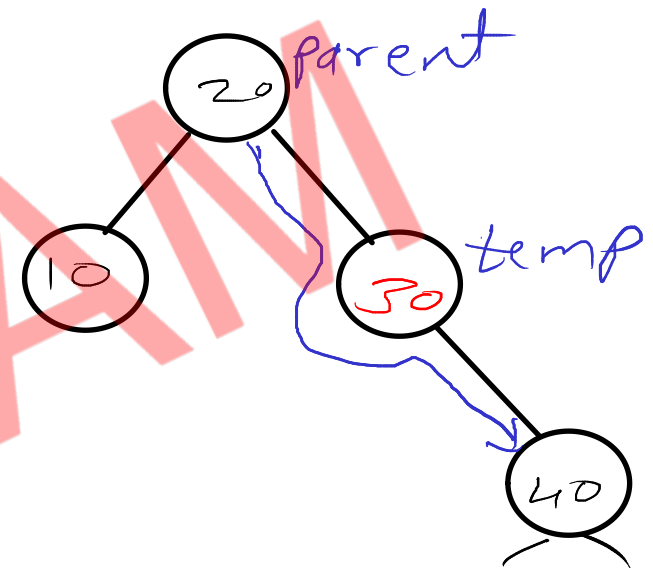
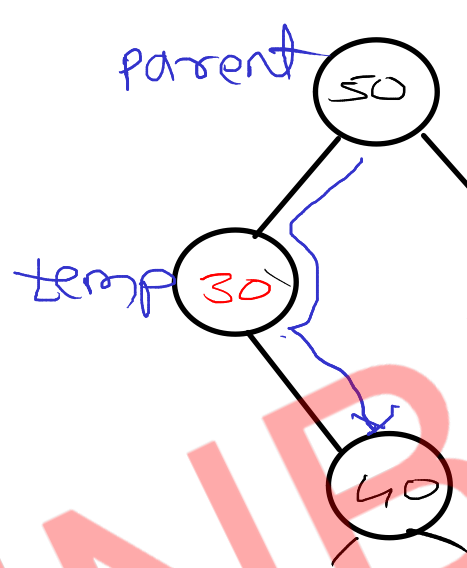
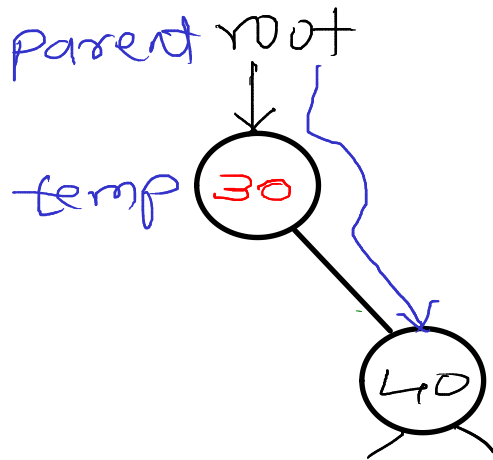
left child

## BST - Delete node which has single child (right child)

Ⓐ root node

Ⓑ Parent's left

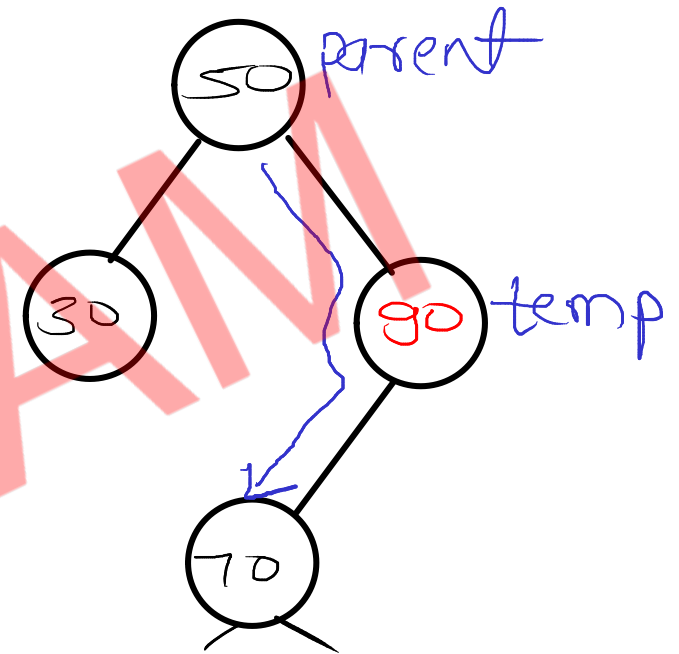
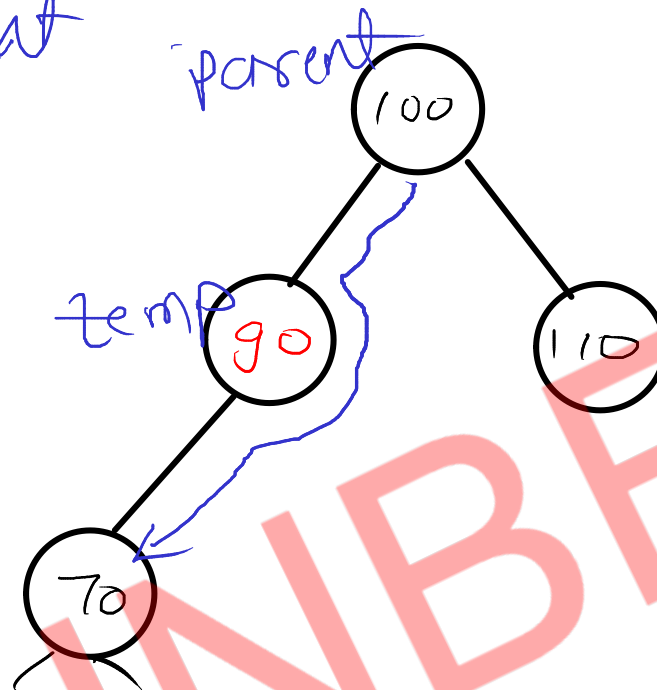
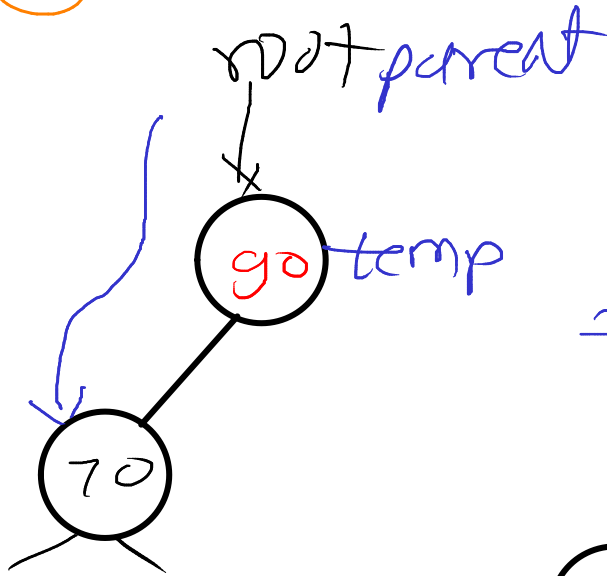
Ⓒ Parent's right



```
if(temp.left == null){  
    if(temp == root)                // root node  
        root = temp.right;  
    else if(temp == parent.left)    // Parent's left  
        parent.left = temp.right;  
    else if(temp == parent.right)  // Parent's right  
        parent.right = temp.right;  
}
```

## BST - Delete node which has single child (left child)

(a) root Node      (b) Parent's left      (c) Parent's right



```
if(temp.right == null){
```

```
    if(temp == root)
```

```
        root = temp.left;
```

```
    else if(temp == parent.left)
```

```
        parent.left = temp.left;
```

```
    else if(temp == parent.right)
```

```
        parent.right = temp.left;
```

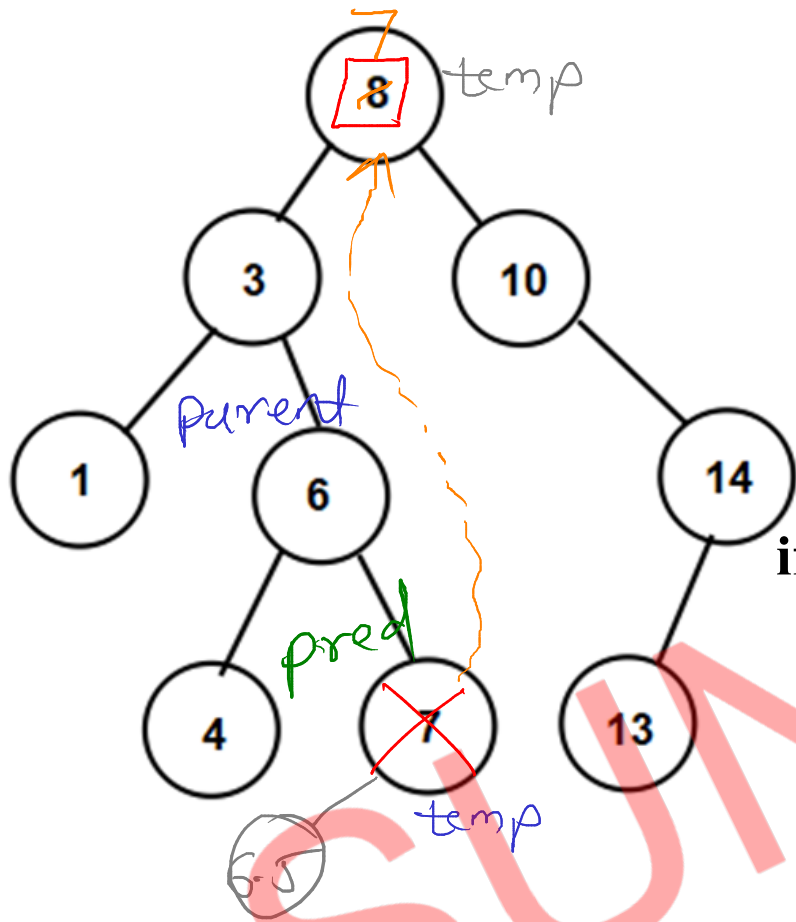
```
}
```

```
// root node
```

```
// parent's left
```

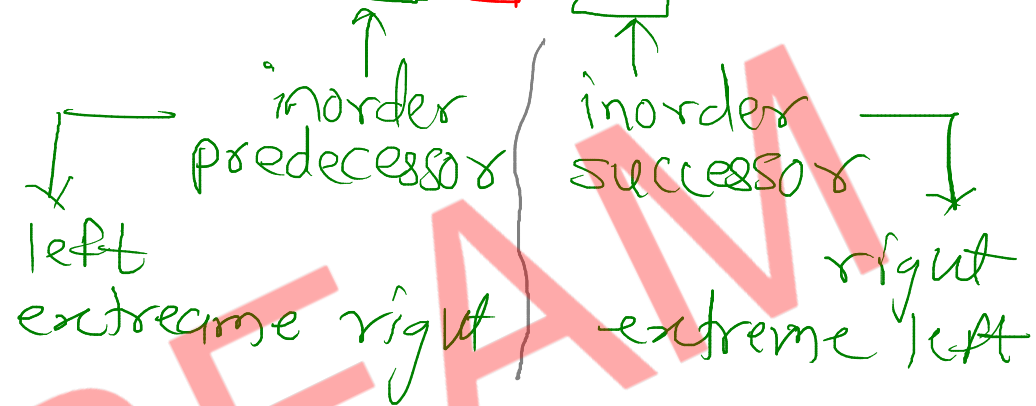
```
// parent's right
```

## BST - Delete node which has two childs



Inorder:

1 3 4 6 7 8 10 13 14



```
if(temp.left != null && temp.right != null){
```

```
//1. find inorder predecessor of temp
```

```
Node pred = temp.left;
```

```
parent = temp;
```

```
while(pred.right != null){
```

```
    parent = pred;
```

```
    pred = pred.right;
```

```
}
```

```
//2. replace predecessor's value at temp's value
```

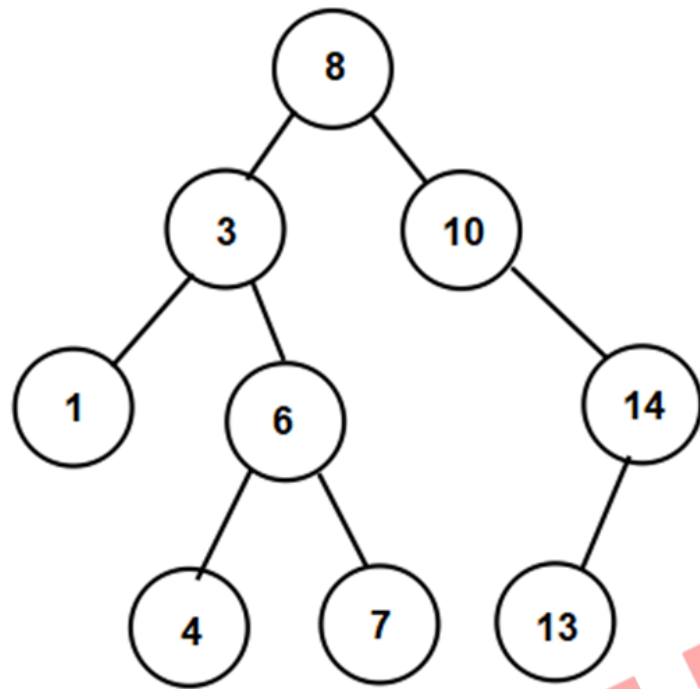
```
temp.data = pred.data;
```

```
//3. delete space of predecessor
```

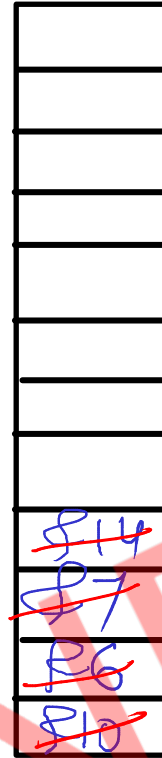
```
temp = pred;
```

```
}
```

## BST - Preorder



stack



Traversal:

8, 3, 1, 6, 4, 7, 10, 14, 13

$$AS(n) = O(n)$$

//1. start traversing from root

//2. visit trav

//3. if trav has right, push trav->right on stack

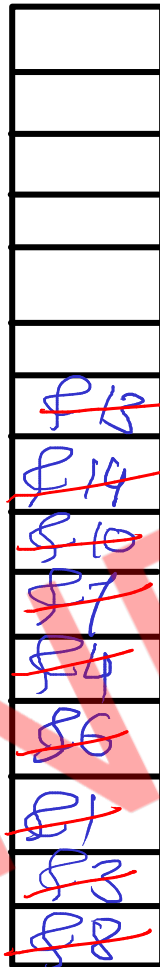
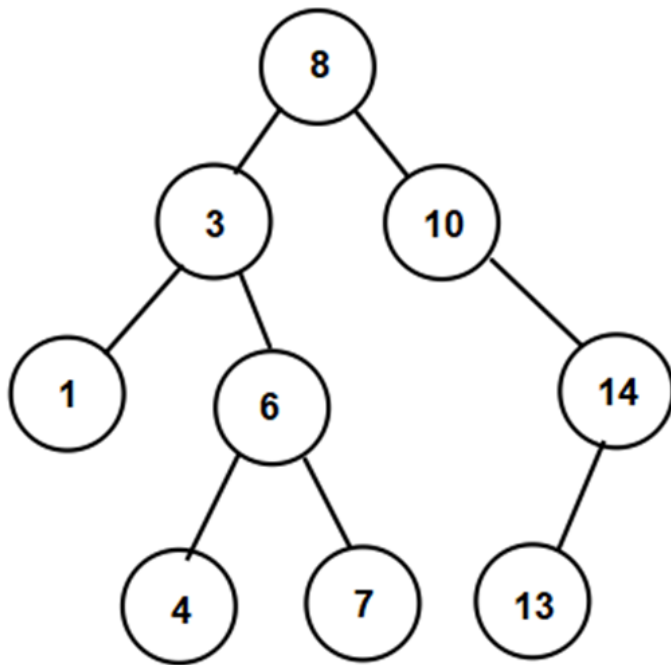
//4. go to left of trav

//5. repeat 2-4 until trav is null

//6. pop node from stack into trav

//7. repeat 2-6, until trav is null or stack is empty

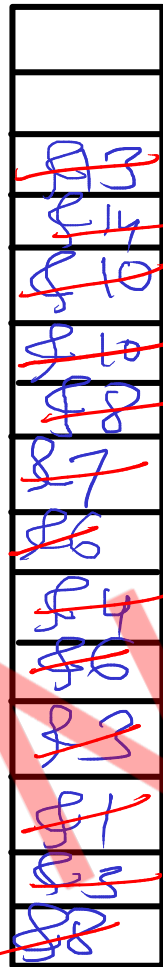
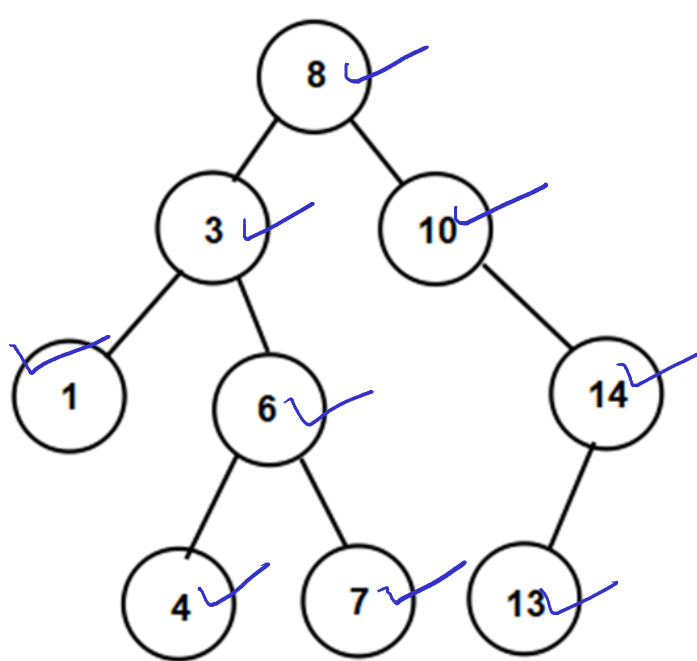
## BST - Inorder



Traversal:  
1, 3, 4, 6, 7, 8, 10, 13, 14

- //1. start traversing from root
- //2. push trav on stack
- //3. go to left of trav
- //4. repeat 2-3 until trav is null ←
- //5. pop node from stack into trav
- //6. visit trav
- //7. go to the right
- //8. repeat 2-7, until trav is null or stack is empty

## BST - Postorder



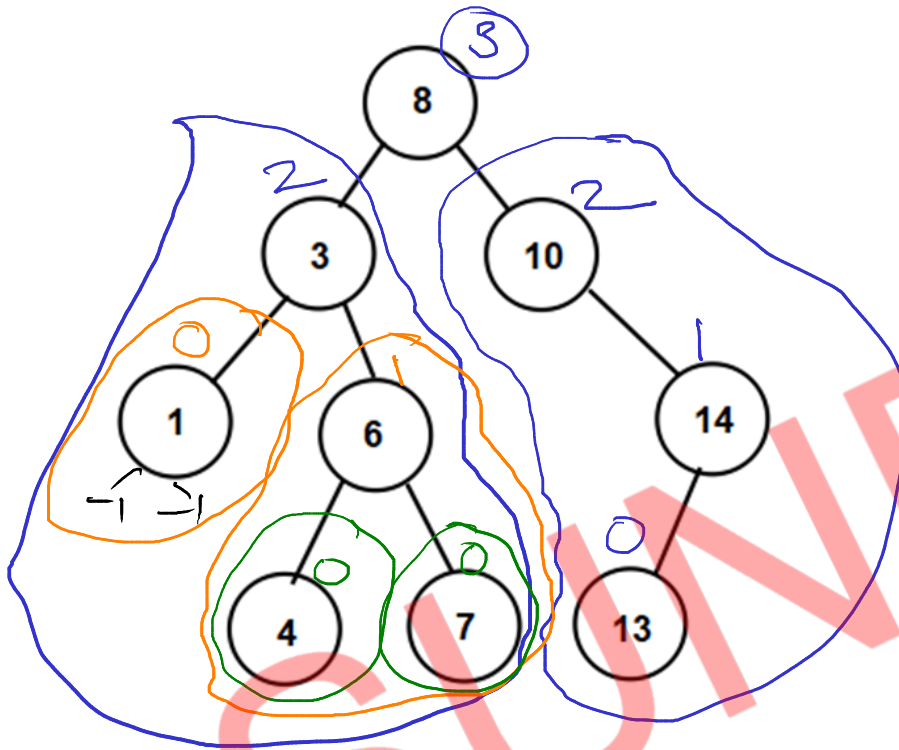
1, 4, 7, 6, 8, 13, 14, 10, 8

```
// start trav from root
// while trav is not null or stack is not empty
//   until null is reached
//     push trav on stack
//     go to trav's left
//   if stack is not empty
//     pop node from stack into trav
//   if trav's right is not present or visited
//     visit trav & mark it as visited
//     make trav null (so that next node
//       will be popped from stack)
//   otherwise
//     push node on stack
//     go to its right
```



# BST - Height

$$\text{Height(Node)} = \text{MAX}(\text{Height}(\text{left sub tree}), \text{Height}(\text{right sub tree})) + 1$$



- //1. if sub tree is absent(empty) then return -1;
- //2. find height of left subtree
- //3. find height of right subtree
- //4. find max of both heights
- //5. return max height + 1

root  
↓  
null ← empty tree  
Null tree  
↓  
height = -1