



Sunbeam Institute of Information Technology

Pune and Karad

Module – Data Structures and Algorithms

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Stack

- Parenthesis balancing
- Expression conversion and evaluation
- Function calls
- Used in advanced data structures for traversing
- **Expression conversion and evaluation:**
 - Infix to postfix
 - Infix to prefix
 - Postfix evaluation
 - Prefix evaluation

Expression : combination of operands & operator

Type :

1) Infix : $a + b$

2) Prefix : $+ a b$

3) Postfix : $a b +$

(human)

? (computer)

↓
CPU

↓
ALU

Queue

- Jobs submitted to printer
- In Network setups – file access of file server machine is given to First come First serve basis
- Calls are placed on a queue when all operators are busy
- Used in advanced data structures to give efficiency.
- Process waiting queues in OS

operation:

()
\$
* / %
+ -



Postfix Evaluation

- Process each element of postfix expression from left to right
- If element is operand
 - Push it on a stack
- If element is operator
 - Pop two elements (Operands) from stack, in such a way that
 - Op2 – first popped element
 - Op1 – second popped element
 - Perform current element (Operator) operation between Op1 and Op2
 - Again push back result onto the stack
- When single value will remain on stack, it is final result
- e.g. 4 5 6 * 3 / + 9 + 7 -

Postfix evaluation

Postfix expression : 4 5 6 * 3 / + 9 + 7 -

l \longrightarrow r

Result : 16

- ⑤ $23 - 7 = 16$
- ④ $14 + 9 = 23$
- ③ $4 + 10 = 14$
- ② $30 / 3 = 10$
- ① $5 * 6 = 30$

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| |
| |
| |
| 16 |
| 7 |
| 23 |
| 9 |
| 14 |
| 10 |
| 3 |
| 30 |
| 6 |
| 5 |
| 4 |

stack

$$'4' = 4$$

$$'0' = 48$$

$$'0' - '0' = 0$$

$$'1' = 49$$

$$'1' - '0' = 1$$

$$'2' = 50$$

$$'2' - '0' = 2$$

Prefix Evaluation

- Process each element of prefix expression from right to left
- If element is operand
 - Push it on a stack
- If element is operator
 - Pop two elements (Operands) from stack, in such a way that
 - Op1 – first popped element
 - Op2 – second popped element
 - Perform current element (Operator) operation between Op1 and Op2
 - Again push back result onto the stack
- When single value will remain on stack, it is final result
- e.g. - + + 4 / * 5 6 3 9 7

Prefix expression : - + + 4 / * 5 6 3 9 7

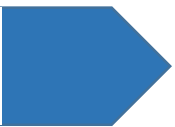
l ← ————— 8

Result = 16

- ⑤ $23 - 7 = 16$
- ④ $14 + 9 = 23$
- ③ $4 + 10 = 14$
- ② $30 / 3 = 10$
- ① $5 * 6 = 30$

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| |
| 16 |
| 23 |
| 14 |
| 4 |
| 10 |
| 30 |
| 5 |
| 6 |
| 3 |
| 9 |
| 7 |

- Process each element of infix expression from left to right
- If element is Operand
 - Append it to the postfix expression
- If element is Operator
 - If priority of topmost element (Operator) of stack is greater or equal to current element (Operator), pop topmost element from stack and append it to postfix expression
 - Repeat above step if required
 - Push element on stack
- Pop all remaining elements (Operators) from stack one by one and append them into the postfix expression
- e.g. $a * b / c * d + e - f * h + i$

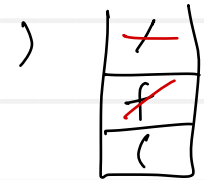
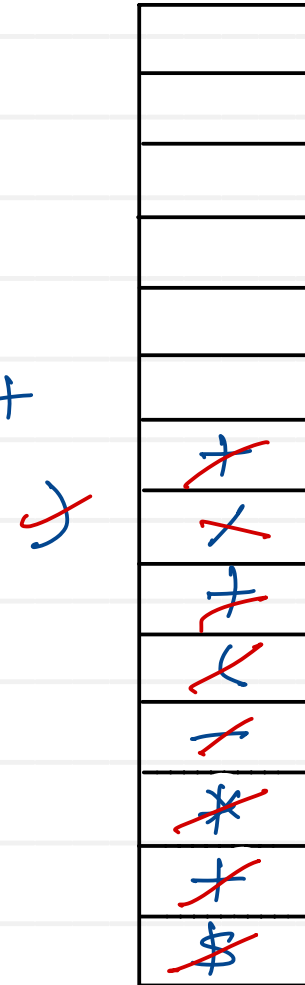


Infix to Postfix conversion

Infix expression : $1 * 9 + 3 * 4 - (6 + 8 / 2) + 7$

$$d \longrightarrow r$$

Postfix expression : $19\ 34\ * + 68\ 2\ / + - 7\ +$



```
while(st.peek() != 'c')
    st.pop();
st.pop();
```



Infix to Prefix Conversion

- Process each element of infix expression from right to left
- If element is Operand
 - Append it to the prefix expression
- If element is Operator
 - If priority of topmost element of stack is greater than current element (Operator), pop topmost element from stack and append it to prefix expression
 - Repeat above step if required
 - Push element on stack
- Pop all remaining elements (Operators) from stack one by one and append them into the prefix expression
- Reverse prefix expression
- e.g. $a * b / c * d + e - f * h + i$

Infix to Prefix conversion

Infix expression : $1 \$ 9 + 3 * 4 - (6 + 8 / 2) + 7$

\hookleftarrow

Expression : $7 2 8 / 6 + 4 3 * 9 1 \$ + - +$

Prefix expression : $+ - + \$ 1 9 * 3 4 + 6 / 8 2 7$

\hookleftarrow

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| \$ |
| + |
| * |
| / |
| + |
| + |
| + |
|) |
| + |

Prefix to Postfix

- Process each element of prefix expression from right to left
- If element is an Operand
 - Push it on to the stack
- If element is an Operator
 - Pop two elements (Operands) from stack, in such a way that
 - Op1 – first popped element
 - Op2 – second popped element
 - Form a string by concatenating Op1, Op2 and Opr (element)
 - String = “Op1+Op2+Opr”, push back on to the stack
- Repeat above two steps until end of prefix expression.
- Last remaining on the stack is postfix expression
- e.g. $* + a b - c d$

Postfix to Infix

- Process each element of postfix expression from left to right
- If element is an Operand
 - Push it on to the stack
- If element is an Operator
 - Pop two elements (Operands) from stack, in such a way that
 - Op2 – first popped element
 - Op1 – second popped element
 - Form a string by concatenating Op1, Opr (element) and Op2
 - String = “Op1+Opr+Op2”, push back on to the stack
- Repeat above two steps until end of postfix expression.
- Last remaining on the stack is infix expression
- E.g. a b c - + d e - f g - h + / *

Valid Parantheses

Given a string s containing just the characters '(', ')', '{', '}', '[' and ']', determine if the input string is valid.

An input string is valid if:

- Open brackets must be closed by the same type of brackets.
- Open brackets must be closed in the correct order.
- Every close bracket has a corresponding open bracket of the same type.

Example 1:

Input: $s = "()"$

Output: true

~~(~~) == (✓

Example 2:

Input: $s = "()[]{}"$

Output: true

~~(~~) == (✓
~~[~~] == [✓
~~{~~ } == { ✓

Example 3:

Input: $s = "()"$

Output: false

~~(~~] != (✗

Example 4:

Input: $s = "([])"$

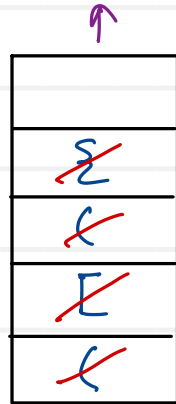
Output: true

~~(~~] == [✓
~~[~~) == (✓

```
boolean isValid(String s) {
    Stack<Character> st = new Stack<>();
    for (i = 0; i < s.length(); i++) {
        char ele = s.charAt(i);
        if (ele == '(' || ele == '[' || ele == '{')
            st.push(ele);
        else if (ele == ')' && !st.isEmpty() && st.peek() == '(')
            st.pop();
        else if (ele == ']' && !st.isEmpty() && st.peek() == '[')
            st.pop();
        else if (ele == '}' && !st.isEmpty() && st.peek() == '{')
            st.pop();
        else
            return false;
    }
    if (!st.isEmpty())
        return false;
    return true;
}
```

$5 + ([9 - 4] * (8 - \{6 / 2\}))$

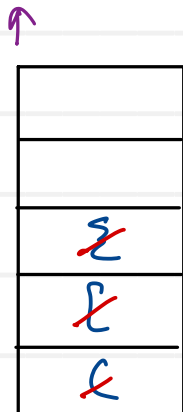
$] == [$
 $\} == \{$
 $) == ($
 $) == ($



stack

$5 + ([9 - 4] * 8 - \{6 / 2\}))$

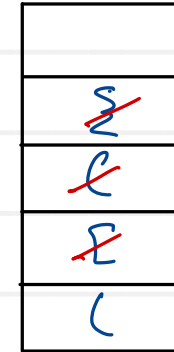
$] == [$
 $\} == \{$
 $) == ($
 $) == ?$



stack

$5 + ([9 - 4] * (8 - \{6 / 2\}])$

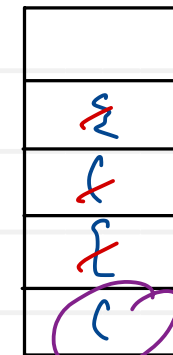
$] == [$
 $\} == \{$
 $] != ($



stack

$5 + ([9 - 4] * (8 - \{6 / 2\}))$

$] == [$
 $\} == \{$
 $) == ($



stack

opening

| | | |
|---|---|---|
| (| [| { |
| 0 | 1 | 2 |

closing

| | | |
|---|---|---|
|) |] | } |
| 0 | 1 | 2 |

String

↓
indexOf()

↓
returns index of char
returns -1 if char
not found



Thank you!!!

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