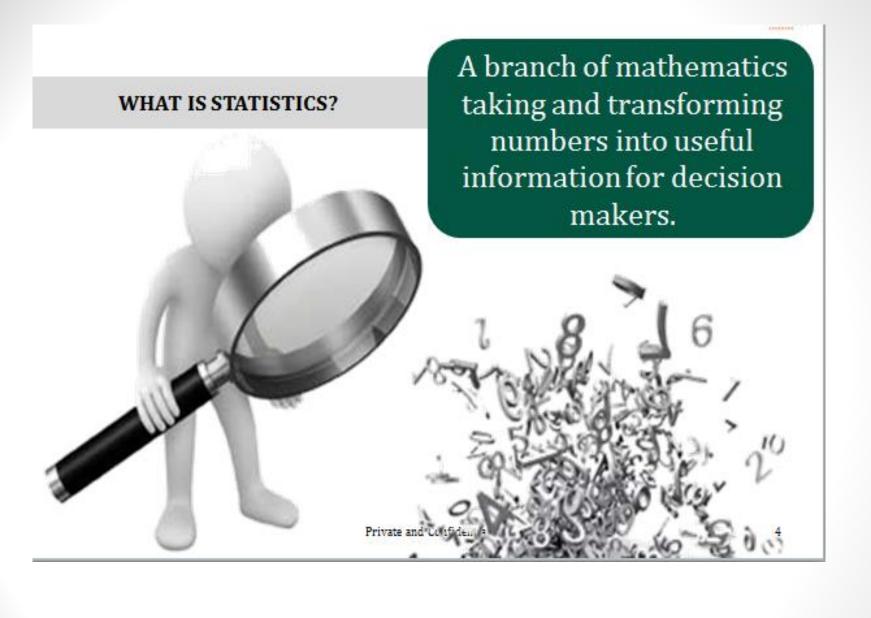
# Statistics & Probablities

#### What is Statistics?



## How Much Ambani Spent On Isha Ambani Wedding?

## How Much Ambani Spent On Isha Ambani Wedding?

- 110 Crores

## We spend more than Ambani in our Marriages?

## Ambani has just spent <u>0.2%</u> of his net worth in Isha's wedding

## Ambani has just spent <u>0.2%</u> of his net worth in Isha's wedding

- How much do we spend?

### Let's talk about some interesting statistics?

#### About cricket

- No team who scored more than <u>597 in first innings</u> of a test has lost
- 400+ score in second innings has been chased only 3 times in the history of test cricket

- You can add more ...

#### **Descriptive Statistics**

Agenda-

In this session you will learn about

- Basics of Statistics
- > Types of Variables
- Measure of Central Tendancy
- Measure of Dispersion
- Case studies of Central tendencies and Dispersion
- Percentile/Quartile & Correlation and Covariance
- Central Limit Theorem
- Data Visualization and distribution

#### Case 1 - Answer in 5 seconds!

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A college in US has students from the following countries for a Masters degree. Which country is in majority?

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A college in US has students from the following countries. Which country is in majority?

US	China	US	Sweden	China
Canada	China	Japan	Mexico	US
China	Germany	India	India	Japan
US	US	US	China	China
India	Japan	England	India	Japan
England	India	China	Mexico	US
Mexico	US	Canada	Pakistan	India
Japan	China	US	Japan	Germany
China	India	India	China	China
Germany	Japan	China	US	Japan

#### Frequency Table

Country	Frequency	
Canada	2	
China	12	
England	2	
Germany	3	
India	8	
Japan	8	
Mexico	3	
Pakistan	1	
Sweden	1	
US	10	

#### Case 2

#### **Problem**

A parent changes school of their Son who is studying in 11<sup>th</sup> standard since his academic results are not good in 10<sup>th</sup> Standard in his current School.

They change Student A from ABC school to XYZ school

#### Case 2

#### **Problem**

A parent changes school of their Son who is studying in 11<sup>th</sup> standard since his academic results are not good in 10<sup>th</sup> Standard in his current School.

They change Student A from ABC school to XYZ school

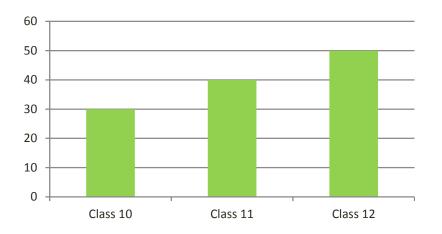
#### Results

- 1. Ranked 15<sup>th</sup> in ABC school
- 2. Ranked 2<sup>nd</sup> in XYZ school

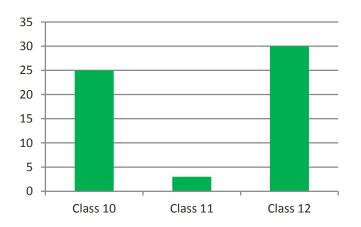
#### What can we say from this?

#### **Number of Students**

#### No of Students in ABC School



#### No of Students in XYZ School



Knowledge of Statistics allows you to make better sense of the ubiquitous use of numbers.

#### Decision Makers Use Statistics for Various Purposes:

Present and describe business data and information properly

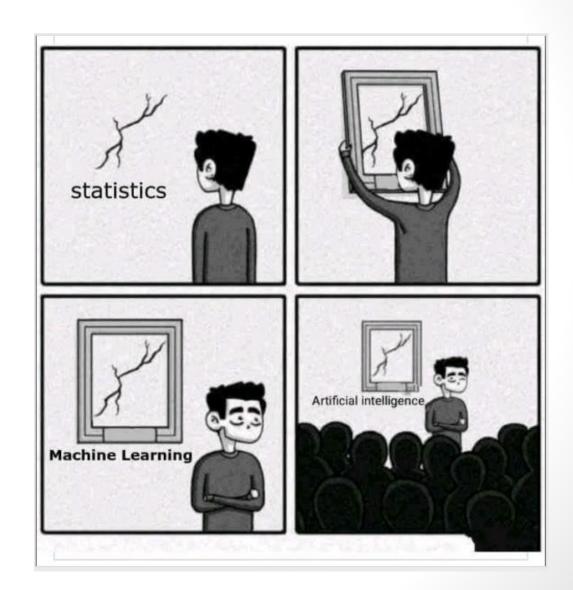
Draw conclusions about large sets using information collected from subsets



#### Statistics is ...

- 1. Collecting Data
- 2. Analyzing Data
- 3. Interpreting Data
- 4. Presenting Data

#### What does it Tell?



#### Classification

**Statistics** 

Descriptive Statistics

Presenting, organizing and summarizing data Inferential Statistics

Drawing conclusions about a population based on data observed in a sample

#### **Population and Sample**

## **POPULATION SAMPLE**

SOLO 1 SON

#### **Census and Survey**

Census: Gathering data from the whole population of interest.

For example, elections, 10-year census, etc.

**Survey:** Gathering data from the **sample** in order to make conclusions about the population.

For example, opinion polls, quality control checks in manufacturing units, etc.

#### Statistical Notations

#### **Greek – Population Parameter**

Mean – μ

Variance –  $\sigma^2$ 

Standard Deviation - σ

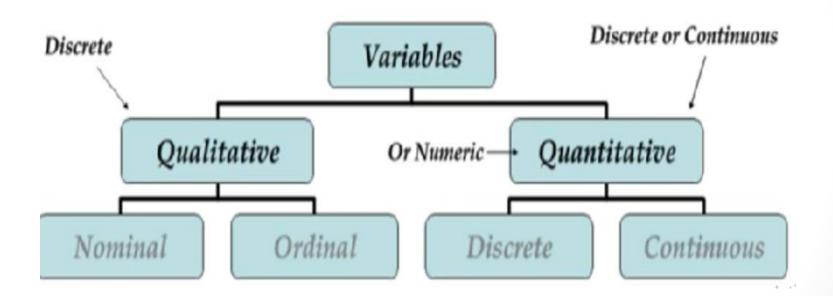
#### Roman – Sample Statistic

Mean  $-\bar{x}$ 

Variance – s<sup>2</sup>

Standard Deviation - s

#### Variables



#### Categorical Data (Qualitative)

#### Nominal Examples

- Employee ID
- Gender
- Religion
- Ethnicity
- Pin codes
- Place of birth
- Aadhaar numbers

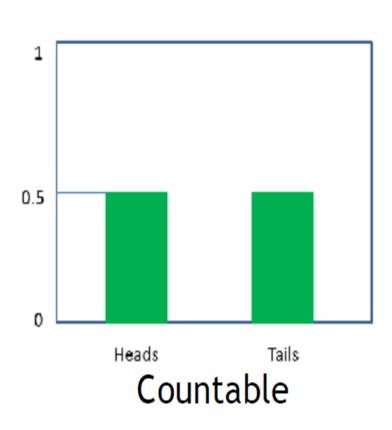
#### Ordinal

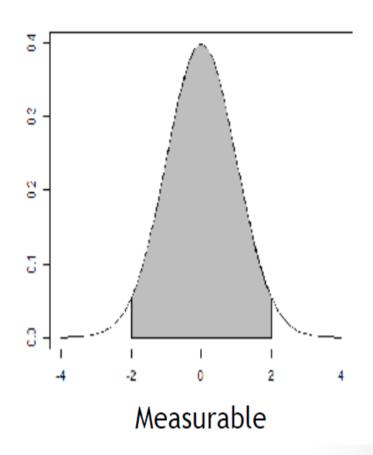
#### Examples

- Mutual fund risk ratings
   Fortune 50 rankings
- Movie ratings

While there is an order, difference between consecutive levels are not always equal.

#### **Discrete and Continuous**





#### **Discrete or Continuous?**

- Time between customer arrivals at a retail outlet Continuous
- Sampling 100 voters in an exit poll and determining how many voted for the winning candidate
   Discrete
- Lengths of newly designed automobiles -Continuous
- No. of customers arriving at a retail outlet during a five- minute period
   Discrete
- No. of defects in a batch of 50 items

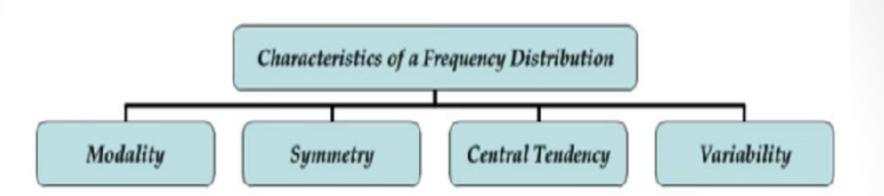
Discrete

#### Variables - Dependent and Independent

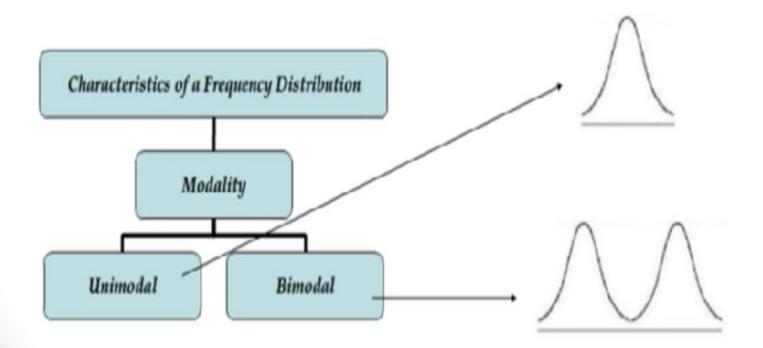
#### Summarizing Data

- Frequency distribution

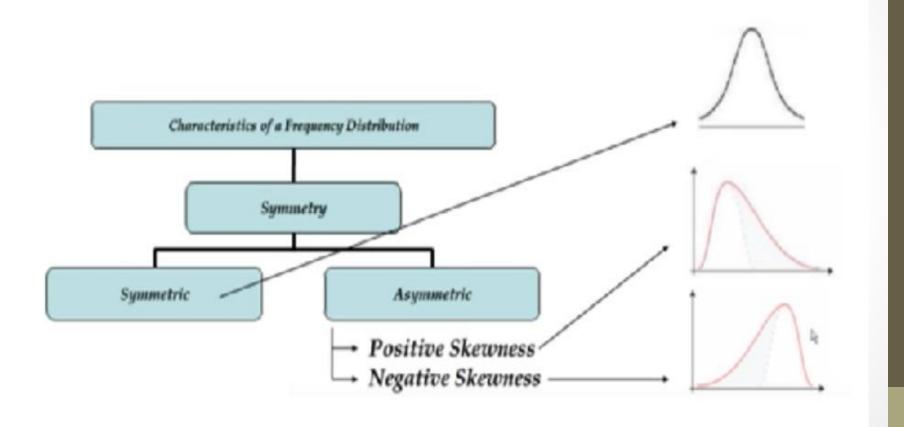
frequency distribution is a table or graph that displays the frequency of various outcomes in a sample



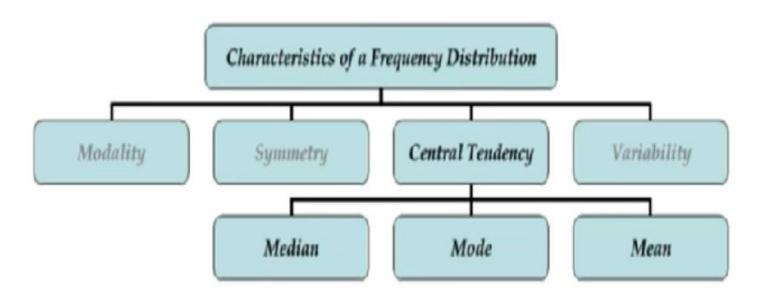
#### Modality



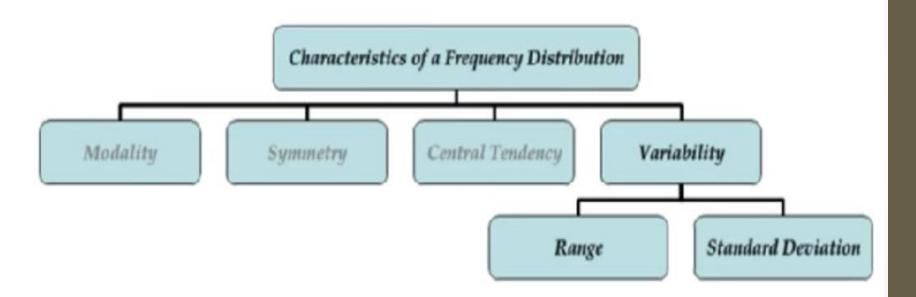
## Symmetry



## Central Tendency



## Variability



#### Central Tendency

A measure of **Central Tendency** is a single value that attempts to describe a set of data **by identifying the central position** within that set of data. In other words, the Central Tendency computes the "center" around which the data is distributed.

The reliable quantity

#### Mean

Mean, 
$$\mu = \frac{\Sigma x}{n}$$



Alan went for a trek. On the way, he had to cross a stream. As Alan did not know swimming, he started exploring alternate routes to cross over.

Suddenly he saw a sign-post, which said "Average depth 3 feet". Alan was 5'7" tall and thought he could safely cross the stream.

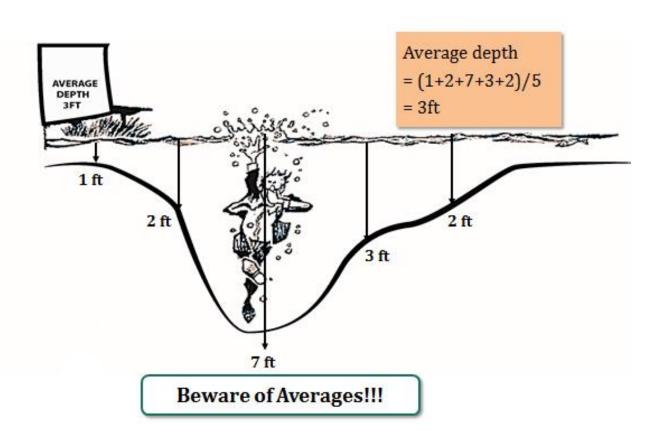




Alan never reached the other end and drowned in the stream.

#### Why did Alan Drown?

#### Why did Alan Drown?



#### The "Hotshot" Sales Executive



Kurt works as a sales manager at vsellhomes.com. In the monthly sales review, Kurt reports that he will achieve his quarterly target of \$1M.

Kurt claims his average deal size is \$100,000 and he has 10 deals in his pipeline. Kurt's boss Ross is very delighted with his numbers.





At the end of quarter, even after closing 8 deals Kurt fails to meet his target number and falls short by more than \$500,000.

#### Discussion





#### The Reality of the "Hotshot" Salesman

- Average deal size in pipeline
  - = \$100,000

Deal #	Deal Value	Deal Status
1	70,000	Open
2	50,000	Closed
3	55,000	Closed
4	60,000	Closed
5	55,000	Closed
6	50,000	Closed
7	50,000	Closed
8	60,000	Closed
9	50,000	Closed
10	5,00,000	Open

#### The Reality of the "Hotshot" Salesman

- Average deal size in pipeline
   = \$100,000
- Deal #10 is of significantly higher value than all the other deals and impacts the average calculation

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7	50,000	Closed
8	60,000	Closed
9	50,000	Closed
10	5,00,000	Open

## Median

#### Median

Median: Arrange data in increasing order and find the mid-point  $\frac{(n+1)}{2}$ .

#### The Reality of the "Hotshot" Salesman

- Average deal size in pipeline
   = \$100,000
- Deal #10 is of significantly higher value than all the other deals and impacts the average calculation
- Median = \$55,000 more realistic measure

Deal #	Deal Value	Deal Status
1	70,000	Open
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9	50,000	Closed
10	5,00,000	Open

Median is less susceptible to the influence of Outliers.

## Mode

#### Mode

Mode – the most frequently occurring

#### Central Tendency: Example

- Timing for the Men's 500-meter Speed Skating event in Winter Olympics is tabulated.
- The Central Tendency measures are computed below:

Year	Time		Year	Time		Year	Time	
1928	43.4	Mean	1988	36.4	Median	36.4	1	Mode
1932	43.4	=	1980	38.03	= (7 <sup>th</sup> + 8 <sup>th</sup>	50.1		= Value with
1936	43.4	(43.4++36.4)/1	1984	38.19	Value)/2	38.03	1	highest
1948	43.1	4 = 568.53/14	1976	39.17	= (40.2+40.2)/2	38.19	1	frequency = 43.4
1952	43.2	= 40.61	1972	39.44	= 40.2	39.17	1	
1956	40.2		1964	40.1		39.44	1	
1960	40.2		1956	40.2				
1964	40.1		1960	40.2		40.1	1	
1968	40.3		1968	40.3		40.2	2	
1972	39.44		1948	43.1		40.3	1	
1976	39.17		1952	43.2		42.1	1	
			1928	43.4		43.1	1	
1980	38.03		1932	43.4		43.2	1	
1984	38.19		1936	43.4		43.4	3	
1988	36.4		1350	10.4	1	70.7	J	l

## Player\_A Vs Player\_B – Who is Better?

Match	Player A	Player B
1	40	40
2	40	35
3	7	45
4	40	52
5	0	30
6	90	40
7	3	29
8	11	43
9	120	37

## Player\_A Vs Player\_B – Who is Better?

Match	Player A	Player B
1	40	40
2	40	35
3	7	45
4	40	52
5	0	30
6	90	40
7	3	29
8	11	43
9	120	37
SUM	351	351

#### Player\_A Vs Player\_B – Who is Better?

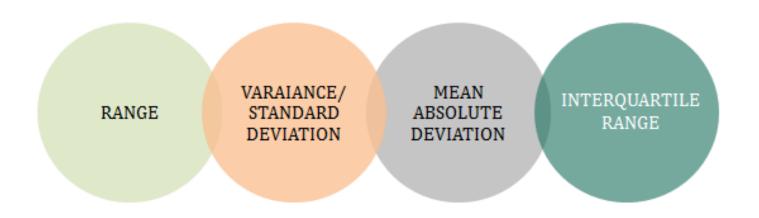
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7	3	29
8	11	43
9	120	37
SUM	351	351
MEAN	39	39

### Player\_A Vs Player\_B - Who is Better?

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5	0	30
6	90	40
7	3	29
8	11	43
9	120	37
SUM	351	351
MEAN	39	39
MEDIAN	40	40

#### Dispersion Measures

**Measures of Dispersion** describe the data spread or how far the measurements are from the center.



## **Spread of Data - Range**

Range = Max - Min

### Spread of Data - SD and Variance

Variance = 
$$\frac{\Sigma(x-\mu)^2}{n}$$

Standard Deviation,  $\sigma = \sqrt{Variance}$ 

#### Who's Best?

Match	Player A	Player B
1	40	40
2	40	35
3	7	45
4	40	52
5	0	30
6	90	40
7	3	29
8	11	43
9	120	37
SUM	351	351
MEAN	39	39
MEDIAN	40	40
STANDARD DEVIATION	41.5180683558376	7.28010988928052

#### Who's Best?

- What if I say Player A is Virat Kohli and Player B is Dhoni

### Measuring Variability and Spread

Basketball coach Statson is in a dilemma choosing between 3 players all having the same average scores.

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

Points scored per game	3	6	7	10	11	13	30
Frequency, f	2	1	2	3	1	1	1

#### Measuring Variability and Spread

Basketball coach Statson is in a dilemma choosing between 3 players all having the same average scores.

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

Points scored per game	3	6	7	10	11	13	30
Frequency, f	2	1	2	3	1	1	1

Mean = Median = Mode = 10 for all 3.

#### **Measuring Variability and Spread**

Range = Max - Min

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
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Points scored per game	3	6	7	10	11	13	30
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Frequency, f	2	1	2	3	1	1	1

MEAN = MEDIAN = MODE = 10 RANGE = 5,5,27

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

Points scored per game	3	6	7	10	11	13	30
Frequency, f	2	1	2	3	1	1	1

MEAN = MEDIAN = MODE = 10 RANGE = 5, 5, 27 Reject Player 3

# Basketball coach Statson is in a dilemma choosing between 3 players all having the same average scores.

Points scored per game	7	8	9	10	11	12	13
Frequency, f	1	1	2	2	2	1	1

Points scored per game	7	9	10	11	13
Frequency, f	1	2	4	2	1

#### STANDARD DEVIATION

Player 1 = 1.7873008824606

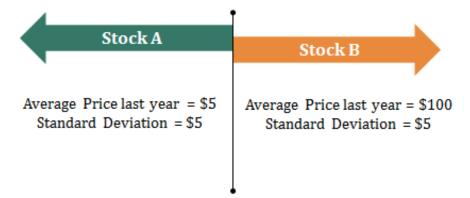
Player 2 = 3.30823887354653

What is your Decision?????????

A

#### **Coefficient of Variation**

Coeff of Variation = (Standard deviation/ Mean) \* 100 %



#### Coefficient of Variation:

**Stock A: CV = 100%** 

(5/5\*100=100%)

Stock B: CV = 5%

(5/100\*100=5%)

$$CV = \left(\frac{S}{\overline{X}}\right) \cdot 100\%$$

## **Case Study**

In an Under 19 World Cup selection squad for 2018 the BCCI needs to select 1 player based on the current performance in 2017 – 2018 Ranji Trophy. There are 2 players with similar stats and the board is not sure whom to select.

- Can you help the board members with your analysis?

# Stats - Player X & Y

Runs scored by both players in last 14 matches

Player X	F	Player Y
	40	35
	20	40
	5	7
	20	23
	10	20
	75	26
	100	12
	25	30
	15	27
	15	102
	20	18
	17	17
	11	14
	5	7

# **Coefficient of Variation**

Calculate the descriptive statistics of both players and if the coefficient of variation is greater than <u>85%</u> then drop that player

# Percentile & Quartile

## Percentile

Percentile is comparing the value with the maximum value of a column.

#### Ex:

If you want to compare your marks with the rest of the students marks(else how many % students have got more than your mark), then percentile is the way.

# Percentile

Nth percentile states that there are atleast N% of values less than or equal to this value and (100-N) values are greater or equal to this value

$$i = (N/100)*n$$

- N The percentile you are interested
- n Number of values

#### **Key points**

- 1. If i is decimal then round off to next value
- 2. If i is integer then take average of i and i+1 value

### Let's calculate 85<sup>th</sup> percentile

#### Data:

3310 3355 3450 3480 3480 3490 3520 3540 3550 3650 3730 3925

Calculate 85<sup>th</sup> percentile?

# Quartile

#### Data:

3310 3355 3450 3480 3480 3490 3520 3540 3550 3650 3730 3925

#### **Quartile:**

#### <u>Dividing data into ¼ − 4 parts</u>

Q1 - First Quartile - 25<sup>th</sup> percentile

Q2 - Second Quartile - 50<sup>th</sup> percentile (Median)

Q3 - Third Quartile - 75<sup>th</sup> percentile

Q4 - Fourth Quartile - 100<sup>th</sup> percentile

# Inter Quartile Range

IQR (Inter Quartile Range) = Q3 - Q1

# **Bi-variate Analysis**

# Measures of association between 2 variables

- 1. Covariance
- 2. Correlation coefficient

# Covariance

$$Cov(X,Y) = \frac{\sum (X_i - \overline{X})^* (Y_i - \overline{Y})}{n}$$

Higher the value stronger the relation between them

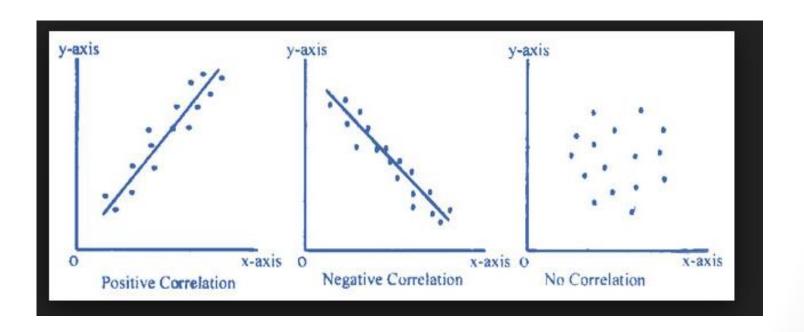
# **Correlation coefficient**

$$r_{xy} = \frac{\text{Cov}(x, y)}{S_x \times S_y}$$

#### **Key Points**

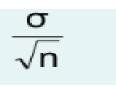
- 1. A measure of relationship not affected by the units of measurements
- 2. Ranges from -1 to +1

# **Types of Correlation**



# **Central Limit Theorem**

When samples of size  $\underline{n>=30}$  are drawn from a population and distributed with individual samples mean then any distribution changes to normal distribution



# **Key Points**

- Also called as Standard Error (SE)
   Standard deviation of sample mean = (population standard deviation/square root(n))
- 2. Mean of sample means distribution = **Population mean**

**NOTE:** As n increases SE decreases - SE is inversely proportional to n

# **Data Visualization**

### Answer in 5 seconds!

### Answer in 5 seconds

A college in US has students from the following countries for a Masters degree. Which country is in majority?

### Answer in 5 seconds

A college in US has students from the following countries. Which country is in majority?

US	China	US	Sweden	China
Canada	China	Japan	Mexico	US
China	Germany	India	India	Japan
US	US	US	China	China
India	Japan	England	India	Japan
England	India	China	Mexico	US
Mexico	US	Canada	Pakistan	India
Japan	China	US	Japan	Germany
China	India	India	China	China
Germany	Japan	China	US	Japan

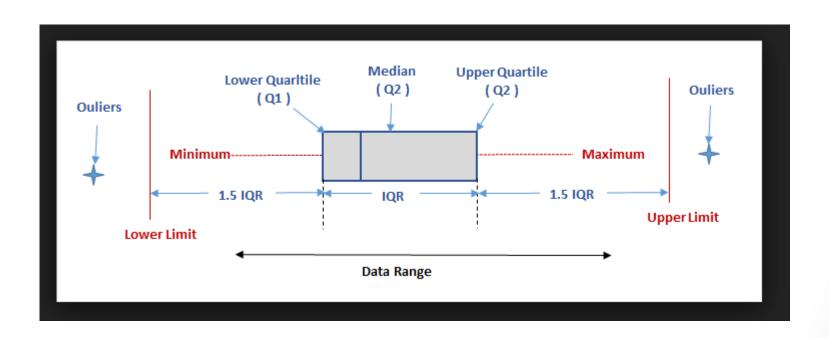
# Frequency Table

Country	Frequency
Canada	2
China	12
England	2
Germany	3
India	8
Japan	8
Mexico	3
Pakistan	1
Sweden	1
US	10

# **Data Visualization - Plots**

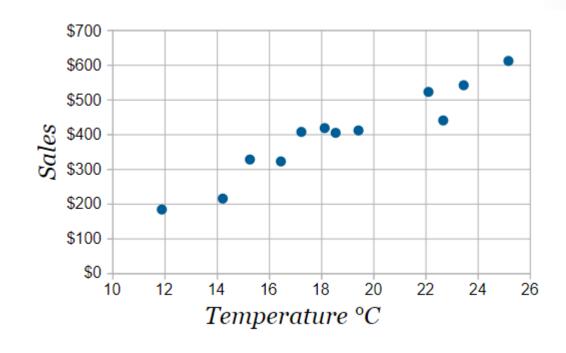
- 1. Box Plot
- 2. Scatter plot
- 3. Density Plot

# **Box Plot -** Shows the data spread for individual columns

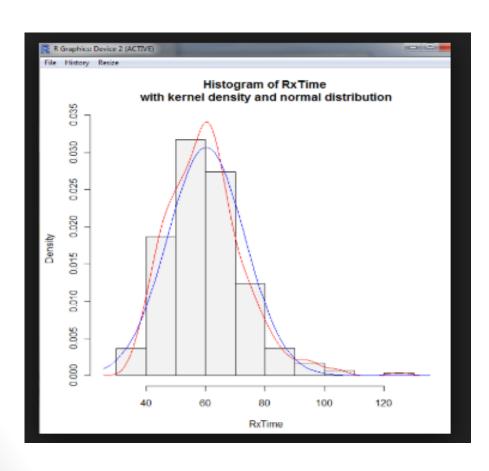


# **Scatter Plot** - Shows relationship between 2 columns

Ice Cream Sales vs Temperature			
Temperature °C	Ice Cream Sales		
14.2°	\$215		
16.4°	\$325		
11.9°	\$185		
15.2°	\$332		
18.5°	\$406		
22.1°	\$522		
19.4°	\$412		
25.1°	\$614		
23.4°	\$544		
18.1°	\$421		
22.6°	\$445		
17.2°	\$408		



# **Density Plot -** Shows the distribution of data



# Statistical simulation link

http://www.shodor.org/interactivate/activities/

# Mean Absolute Error vs Mean Squared Error

