

Assignment-9

18KUN05H1

Momentum gradient descent

Step-1 Read $[x, y]$, $m=1$, $c=-1$, $\eta=0.1$, $\gamma=0.9$,
epochs = 2, $V_m = V_c = 0$

Step-2 $i = 1$ Step-3 = sample = 1

Step-4 $E = \frac{1}{2} (y_i - mx_i - c)^2$

$$\frac{\partial E}{\partial m} = (3.4 - (1)(0.2) + 1)(0.2) = (4.2)(0.2) = -0.84$$

$$\frac{\partial E}{\partial c} = -(4.2) = -4.2$$

Step-5 $V_m = \gamma V_m - \eta \frac{\partial E}{\partial m} = (0.9)(0) - (0.1)(-0.84)$
 $= 0.084$

$$V_c = (0.9)(0) - (0.1)(4.2) = -0.42$$

Step-6 $m = 1 + 0.084 = 1.084$

$$c = -1 + 0.42 = -0.58$$

Step-7 sample = 1 + 1 = 2

Step-8 If sample > ns \Rightarrow 2 > 2 - false
goto step 4

Step-9 $\frac{\partial E}{\partial m} = -(3.8 - (1.084 \times 0.4) + 0.58) \times 0.4$
 $= -(3.9464) \times 0.4 = -1.5785$

$$\frac{\partial E}{\partial c} = -(3.94) =$$

step-10 $V_m = (0.9)(0.084) - (0.1)(1.5 + 85) = 0.0822$

$V_c = (0.9)(0.42) - (0.1)(-3.9464) = 0.77264$

step-11 $m = 1.084 + 0.0822 = 1.1662$

$c = -0.58 + 0.77264 = 0.1926$

step-12 $\text{Sample} = 2 + 1 = 3.$

step-13 $\text{If Sample} > n_s = 3 > 2 = \text{true}$
 goto step 14

step-14 $\text{Iter} = 1 + 1 = 2$

step-15 $\text{If Iter} > \text{epoch} = 2 > 2 = \text{false}$
 goto step 3.

step-16 $\text{Sample} = 1$

step-17 $E = \frac{1}{2} (y - mx - c)^2$

$\frac{\partial E}{\partial m} = -(3.4 - (1.16625 \times 0.2) - 0.19264) \times 0.2$

Step-18 $V_m = (0.9)(0.08225) - (0.1)(-0.5111)$
 $= 0.133507$
 $V_c = (0.9)(0.7726) - (0.1)(-2.92411)$
 $= 0.992787$

Step-19
 $m = 1.16625 + 0.133507 = 1.299757$
 $c = 0.19264 + 0.992787 = 1.185427$

Step-20 Sample = $1+1=2$

Step-21 If Sample $ns = 272 = \text{false}$
 goto step 4

Step-22 $\frac{\partial E}{\partial m} = -(3.8 - (1.2997) \times (0.4) - (1.1854) \times 0.6)$
 $= -(2.09467) \times 0.4 = -0.83786$

$\frac{\partial E}{\partial c} = -2.09467$

Step-23 $V_m = (0.9)(0.13350) - (0.1)(-0.83786)$
 $= 0.20394$

$V_c = (0.9)(0.992787) - (0.1)(-2.09467)$
 $= 1.10297$

step 24 $m = 1.2997 + 0.2039 = 1.50369$

$C = 1.10297 + 1.185127 = 2.28839$

step 25 $eta = 2 + 1 = 3$

step 26 $\text{if } eta > epochs = 372 = \text{false}$
goto step 27

step 27 $\text{print}(m, C)$
 $= 1.50369, 2.288397.$