

# Survey of Semi-supervised Learning (SSL) And Multi-Task Learning (MTL)

## Outline

- SSL
- MTL

Google doc: <https://docs.google.com/document/d/1LKojD6wUeHtxiyY4ogXW6ZejYikUNnxk-GJ5NHrdlyQ/edit>

# SSL-overview

## Realistic Evaluation of Deep Semi-Supervised Learning Algorithms

Avital Oliver\*, Augustus Odena\*, Colin Raffel\*, Ekin D. Cubuk & Ian J. Goodfellow  
Google Brain  
{avitalo,augustusodena,craffel,cubuk,goodfellow}@google.com

Table 1: Test error rates obtained by various SSL approaches on the standard benchmarks of CIFAR-10 with all but 4,000 labels removed and SVHN with all but 1,000 labels removed, using our proposed unified reimplementation. “Supervised” refers to using only 4,000 and 1,000 labeled datapoints from CIFAR-10 and SVHN respectively without any unlabeled data. VAT and EntMin refers to Virtual Adversarial Training and Entropy Minimization respectively (see section 3).

Dataset	# Labels	Supervised	II-Model	Mean Teacher	VAT	VAT + EntMin	Pseudo-Label
CIFAR-10	4000	$20.26 \pm .38\%$	$16.37 \pm .63\%$	$15.87 \pm .28\%$	$13.86 \pm .27\%$	$13.13 \pm .39\%$	$17.78 \pm .57\%$
SVHN	1000	$12.83 \pm .47\%$	$7.19 \pm .27\%$	$5.65 \pm .47\%$	$5.63 \pm .20\%$	$5.35 \pm .19\%$	$7.62 \pm .29\%$

# SSL overview

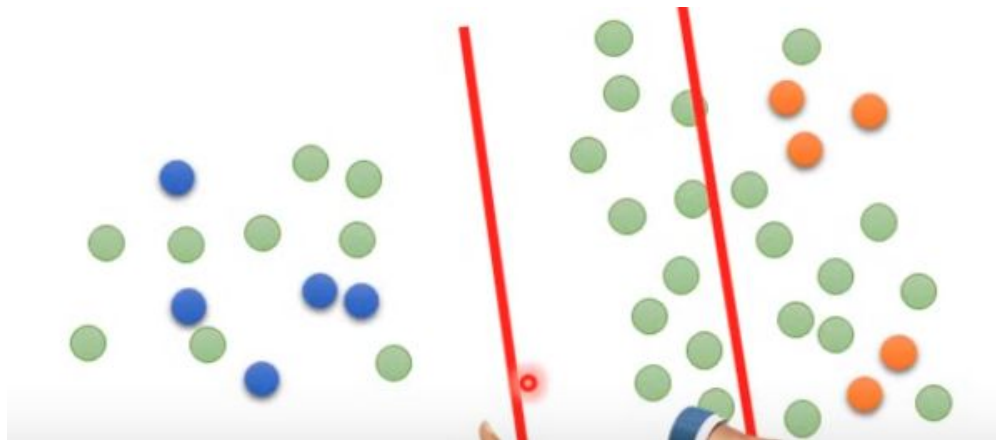
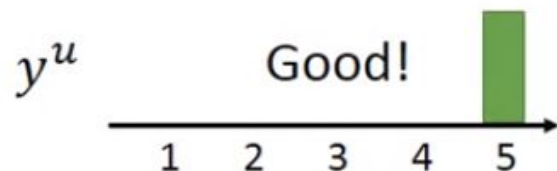
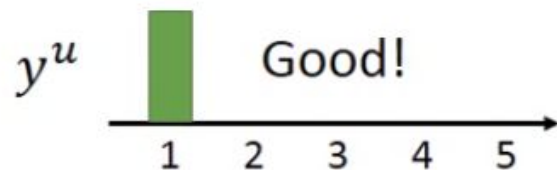
- Semi-supervised learning by **entropy minimization**. (2004) ([EntMin](#))
- **Pseudo-label**: The simple and efficient semi-supervised learning method for deep neural networks. (2013) ([Pseudo-label](#), [self-training](#))
- **Label Propagation** ([LP](#))
- **Temporal Ensembling** for Semi-Supervised Learning (ICLR 2017)
- **Mean teachers** are better role models: Weight-averaged consistency targets improve semi-supervised deep learning results (NIPS 2017) ([Mean Teachers](#))
- **Virtual Adversarial Training**: A Regularization Method for Supervised and Semi-Supervised Learning (IEEE) ([VAT](#))

# Semi-supervised Learning (SSL)

- Inductive bias / Assumption
  - Low density separation
  - Cluster assumption
  - Smoothness assumption

# Entropy Minimization

- Low density separation



# Pseudo-Label (self training, self supervision)

- For unlabeled data, Pseudo-Labels, just picking up the class which has the maximum predicted probability, are used as if they were true labels.
- Equivalent effect of entropy minimization
- Low density separation

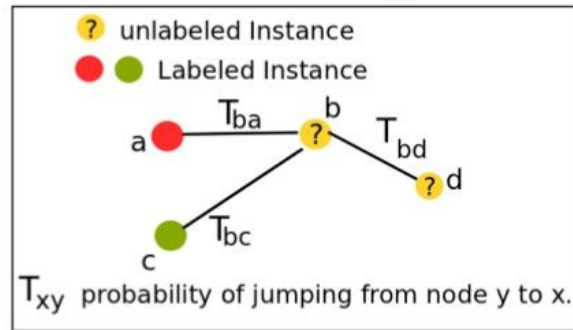
# Label Propagation graph based method

- Construct graph between data points according to some similarity function
- Propagate label (label are more likely to propagate through similar data points)
- Train and propagate until convergence
- Smoothness assumption

(“similar” x has “Similar” y)

## The Model

- A complete graph
  - Each Node is an instance
  - Each arc has a weight  $T_{xy}$

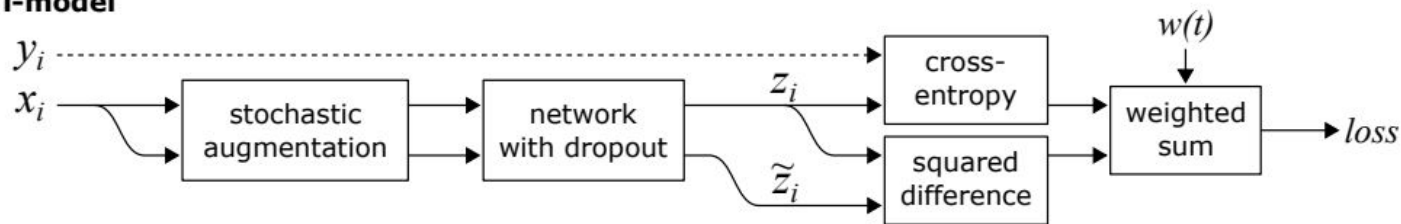


- $T_{xy}$  is high if Nodes x and y are similar.

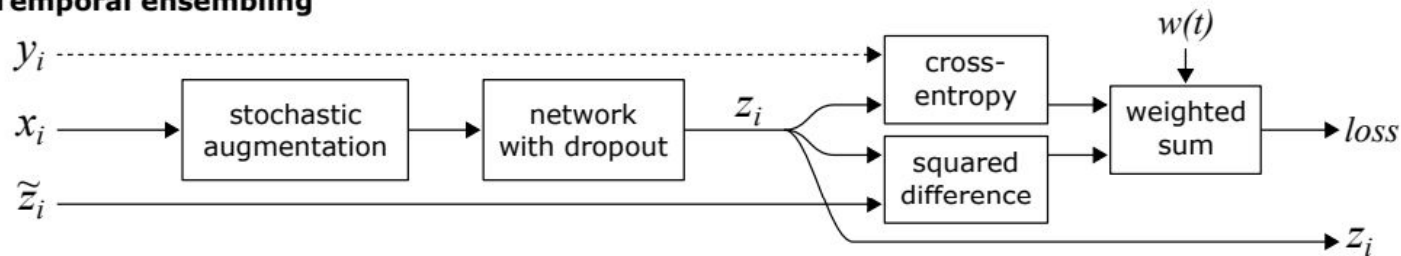
# Temporal Ensembling for Semi-Supervised Learning (ICLR 2017)

- This ensemble prediction can be expected to be a better predictor for the unknown labels than the output of the network at the most recent training epoch, and can thus be used as a target for training.

## $\Pi$ -model

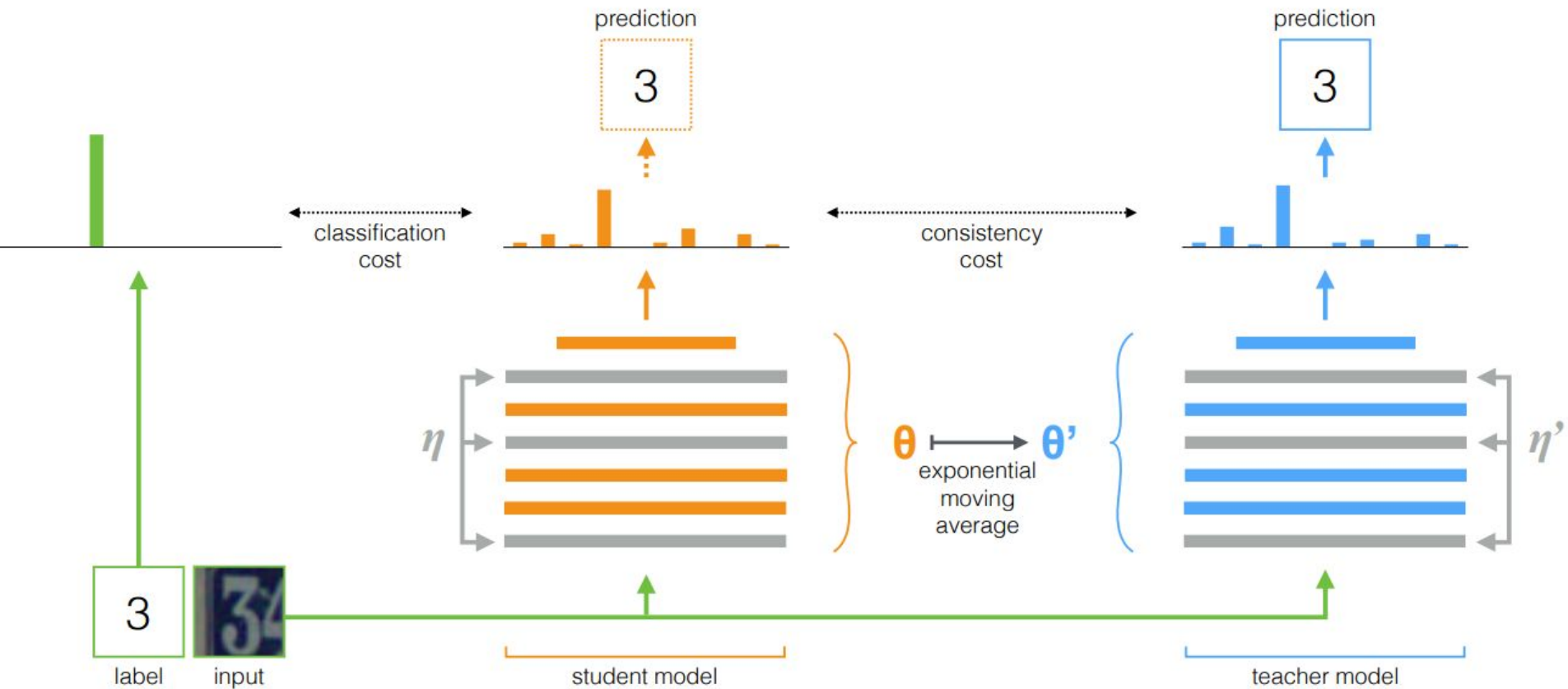


## Temporal ensembling





# Mean teachers (NIPS 2017)



# Virtual Adversarial Training - perturbation-based method (VAT)

## Adversarial Training

Our method is closely related to the adversarial training proposed by Goodfellow et al. [14]. We therefore formulate adversarial training before introducing our method. The loss function of adversarial training in [14] can be written as

$$L_{\text{adv}}(x_l, \theta) := D[q(y|x_l), p(y|x_l + r_{\text{adv}}, \theta)] \quad (1)$$

$$\text{where } r_{\text{adv}} := \arg \max_{r; \|r\| \leq \epsilon} D[q(y|x_l), p(y|x_l + r, \theta)], \quad (2)$$

## Virtual Adversarial Training

Therefore, in this study, we use the *current* estimate  $p(y|x, \hat{\theta})$  in place of  $q(y|x)$ . With this compromise, we arrive at our rendition of Eq.(2) given by

$$\text{LDS}(x_*, \theta) := D[p(y|x_*, \hat{\theta}), p(y|x_* + r_{\text{vadv}}, \theta)] \quad (5)$$

$$r_{\text{vadv}} := \arg \max_{r; \|r\|_2 \leq \epsilon} D[p(y|x_*, \hat{\theta}), p(y|x_* + r)], \quad (6)$$

# Smoothness Assumption

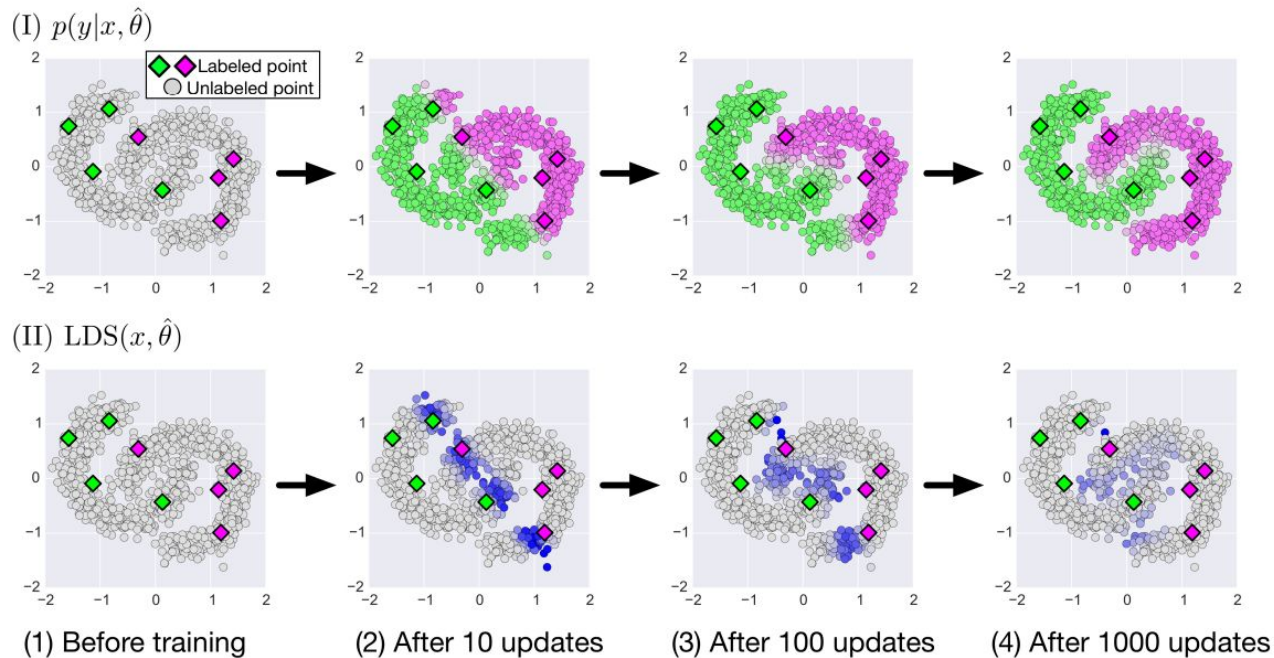


Fig. 1: Demonstration of how our VAT works on semi-supervised learning. We generated 8 labeled data points ( $y = 1$  and  $y = 0$  are green and purple, respectively), and 1,000 unlabeled data points in 2-D space. The panels in the first row (I) show the prediction  $p(y = 1|x, \theta)$  on the unlabeled input points at different stages of the algorithm. We used a continuous colormap to designate the predicted values of  $p(y = 1|x, \theta)$ , with Green, gray, and purple respectively corresponding to the values 1.0, 0.5, and 0.0. The panels in the second row (II) are heat maps of the regularization term  $LDS(x, \theta)$  on the input points. The values of  $LDS$  on blue-colored points are relatively high in comparison to the gray-colored points. We used KL divergence for the choice of  $D$  in Eq.(5). Note that, at the onset of training, all the data points have similar influence on the classifier. After 10 updates, the model boundary was still appearing *over* the inputs. As the training progressed, VAT pushed the boundary away from the labeled input data points.

# Review

Table 1: Test error rates obtained by various SSL approaches on the standard benchmarks of CIFAR-10 with all but 4,000 labels removed and SVHN with all but 1,000 labels removed, using our proposed unified reimplementation. “Supervised” refers to using only 4,000 and 1,000 labeled datapoints from CIFAR-10 and SVHN respectively without any unlabeled data. VAT and EntMin refers to Virtual Adversarial Training and Entropy Minimization respectively (see section 3).

Dataset	# Labels	Supervised	$\Pi$ -Model	Mean Teacher	VAT	VAT + EntMin	Pseudo-Label
CIFAR-10	4000	$20.26 \pm .38\%$	$16.37 \pm .63\%$	$15.87 \pm .28\%$	$13.86 \pm .27\%$	$13.13 \pm .39\%$	$17.78 \pm .57\%$
SVHN	1000	$12.83 \pm .47\%$	$7.19 \pm .27\%$	$5.65 \pm .47\%$	$5.63 \pm .20\%$	$5.35 \pm .19\%$	$7.62 \pm .29\%$

# Summarize: “Student - Teacher” framework

- Enforce consistency loss between student and teacher
  - Mean\_teacher
    - Student: original
    - Teacher: ensemble model (EMA)
  - VAT
    - Student output: perturbed input
    - Teacher output: original
  - Pseudo labelling
    - Student output: original
    - Teacher output: masks data point with high confident

# Semi-supervised Regression

**Semi-supervised Deep Kernel Learning: Regression with Unlabeled Data by Minimizing Predictive Variance - NIPS 2018 (SSDKL)**

## Baselines

- VAT
- Mean-teachers
- Label propagation
- CoREG (co-training)
  - Uses two k-nearest neighbor (kNN) regressors with different configuration
  - each of which generates labels for the other during the learning process

# Semi-supervised Deep Kernel Learning (**SSDKL**)

$$L_{semisup}(\bar{\theta}) = -\frac{1}{n} \log p(\mathbf{y}_L | X_L, \bar{\theta}) + \frac{\alpha}{m} \sum_{x \in X_U} \text{Var}_{f \sim p}(f(x))$$

## Intuition

- Unlabeled data tend to cluster around these label supports (as it's trained jointly)
- Semi-supervised objective serves as a regularizer that reduces overfitting, improve model generalization

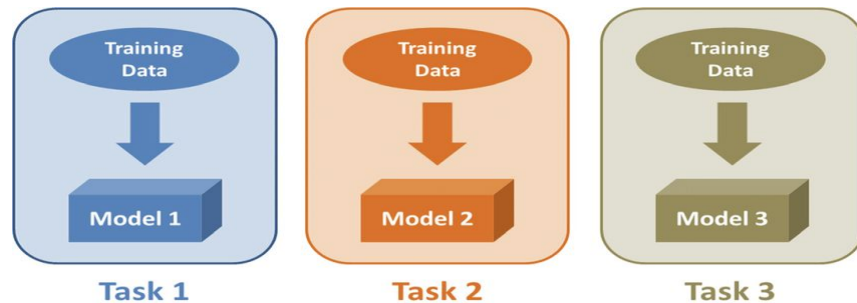
# Multi-Task Learning (MTL)



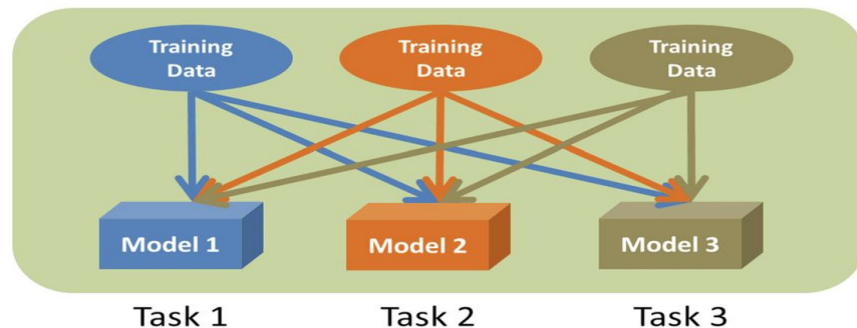
# Multi-Task Learning (MTL)

**Loose Definition:** Anytime we optimize more than one loss function at the same time.

**Definition:** Given  $m$  learning tasks  $\{T_i\}_{i=1}^m$  where all the tasks or a subset of them are related, *multi-task learning* aims to help improve the learning of a model for  $T_i$  by using the knowledge contained in all or some of the  $m$  tasks



(a)



(b)

	Training		Testing	
Transfer Learning	Task 1		Task 2	
Multi-task Learning	Task 1	... Task N	Task 1	... Task N
Lifelong Learning	Task 1	... Task N	Task N+1	

# Why Does MTL Work?

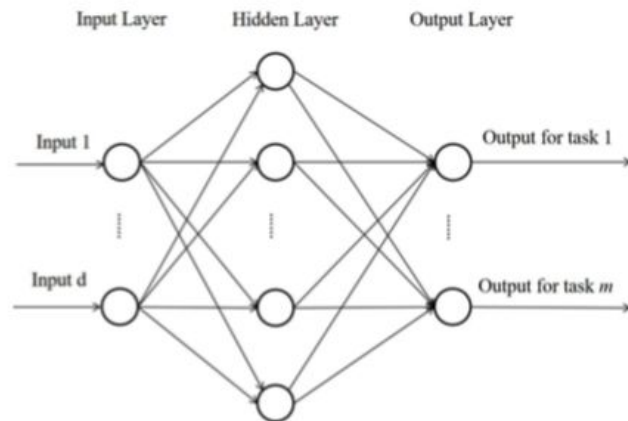
- **Implicit Data Augmentation** - Increase sample size
- **Feature Selection Double Check** - Features that carry across tasks are important
- **Eavesdropping** - Information transfer from different tasks
- **Representation Bias** - Generate flexible representations
- **Regularization** - Reduce risk of overfitting

# What to Share?

- **Feature**: Learn common features among different tasks as a way to share knowledge
- **Instance**: Identify useful data instances in a task for other tasks and then shares knowledge via the identified instances
- **Parameter**: Uses model parameters (e.g., coefficients in linear models) in a task to help learn model parameters in other tasks in some ways, for example, regularization.

# Feature Based

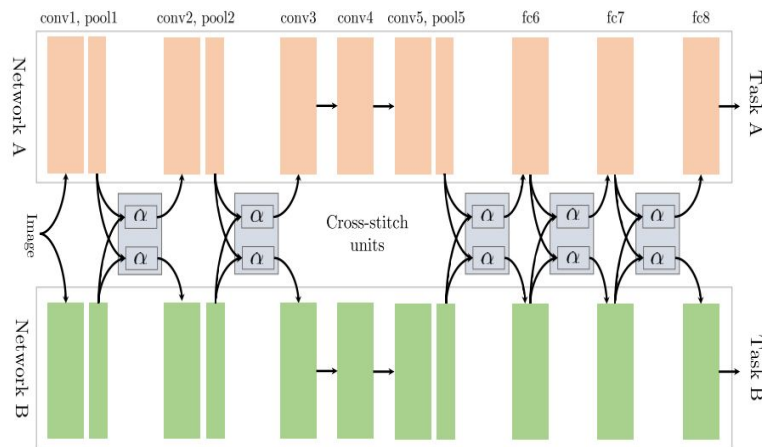
- **Feature Transformation**: The learned representation is a linear or non-linear transformation of the original representation. Each feature in the learned representation is different from the original.
- **Feature Selection**: Select a subset of the original features as the learned representation. Learned representation is similar to the original by eliminating useless features.



# Cross Stitch Network (Misra et al., 2016)

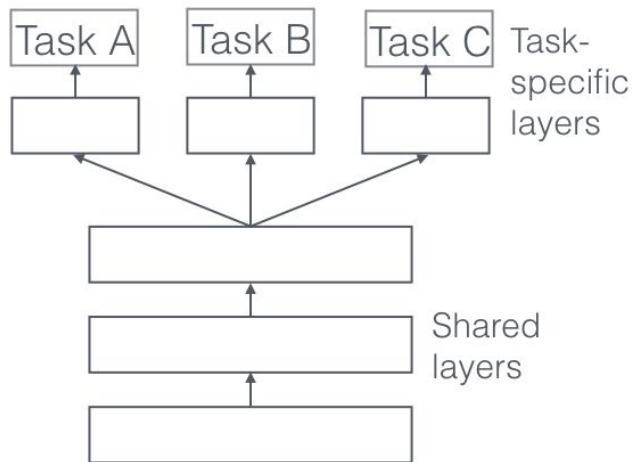
$$\begin{pmatrix} \tilde{x}_A^{i,j} \\ \tilde{x}_B^{i,j} \end{pmatrix} = \begin{pmatrix} \alpha_{AA} & \alpha_{AB} \\ \alpha_{BA} & \alpha_{BB} \end{pmatrix} \begin{pmatrix} x_A^{i,j} \\ x_B^{i,j} \end{pmatrix}$$

When  $\alpha_{AB}$  and  $\alpha_{BA}$  are both equal to 0 then training the two networks jointly is equivalent to training them independently.

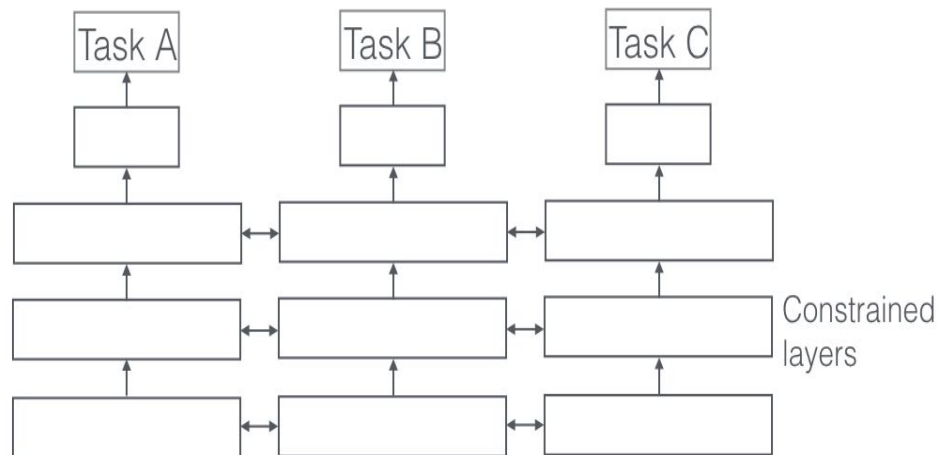


# Parameter Based

## Hard Parameter Sharing



## Soft Parameter Sharing



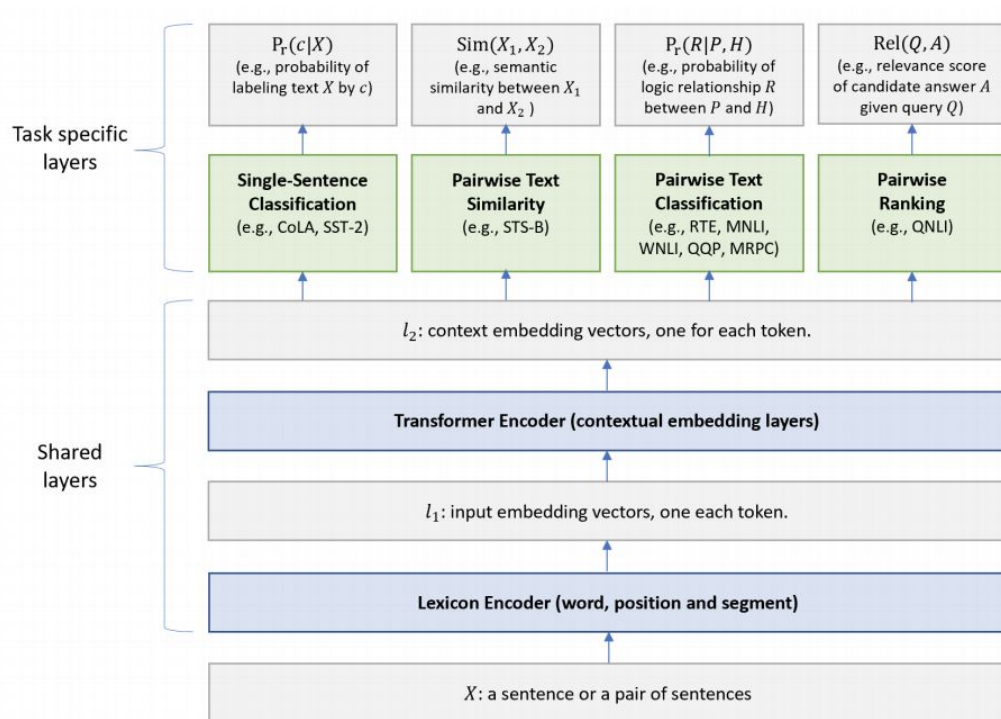
Auxiliary Tasks	Use case
<b>Related Tasks</b>	Similar tasks learn in a group
<b>Adversarial Tasks</b>	Domain Adaptation
<b>Hints</b>	Use easier tasks to help learn complex tasks
<b>Representation Learning</b>	Explicitly create a learned representation(Eg: Language Modelling)



# Learning General Purpose Sentence Representations (2018)

- **Idea:** Generate representations of sentences which are generalized and not task specific
- **Method:** Use diverse sentence-representation learning objectives and combine into a single multi-task framework.
  - Skip-thought vectors
  - Neural Machine Translation
  - Constituency Parsing
  - Natural Language Inference
- **Observation:** By utilizing multiple weakly related objectives, the representation encodes the inductive biases of each objective without becoming task-specific.

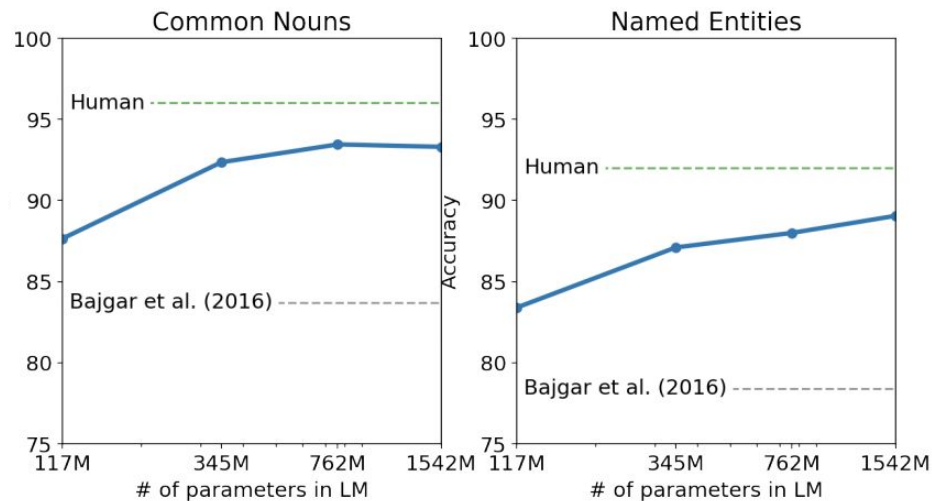
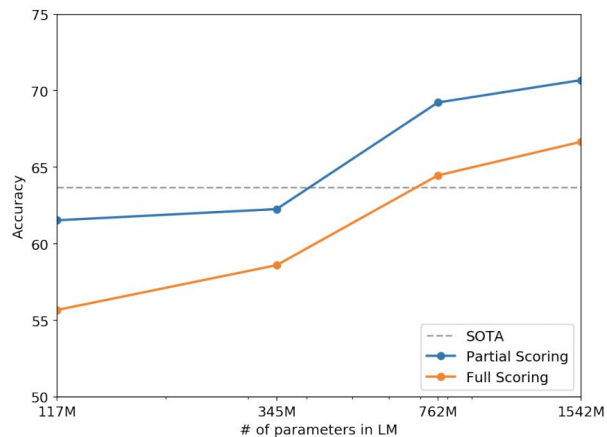
# Multi-Task Deep Neural Networks for Natural Language Understanding(2019)



# OpenAI GPT-2 (2019)

Parameters	Layers	$d_{model}$
117M	12	768
345M	24	1024
762M	36	1280
1542M	48	1600

Table 2. Architecture hyperparameters for the 4 model sizes.



***In a shocking finding, scientist discovered a herd of unicorns living in a remote, previously unexplored valley, in the Andes Mountains. Even more surprising to the researchers was the fact that the unicorns spoke perfect***

***English.*** The scientist named the population, after their distinctive horn, Ovid's Unicorn. These four-horned, silver-white unicorns were previously unknown to science. Now, after almost two centuries, the mystery of what sparked this odd phenomenon is finally solved. Dr. Jorge Pérez, an evolutionary biologist from the University of La Paz, and several companions, were exploring the Andes Mountains when they found a small valley, with no other animals or humans. Pérez noticed that the valley had what appeared to be a natural fountain, surrounded by two peaks of rock and silver snow. Pérez and the others then ventured further into the valley. "By the time we reached the top of one peak, the water looked blue, with some crystals on top," said Pérez. Pérez and his friends were astonished to see the unicorn herd. These creatures could be seen from the air without having to move too much to see them – they were so close they could touch their horns. While examining these bizarre creatures the scientists discovered that the creatures also spoke some fairly regular English. Pérez stated, "We can see, for example, that they have a common 'language,' something like a dialect or dialectic." Dr. Pérez believes that the unicorns may have originated in Argentina, where the animals were believed to be descendants of a lost race of people who lived there before the arrival of humans in those parts of South America. While their origins are still unclear, some believe that perhaps the creatures were created when a human and a unicorn met each other in a time before human civilization. According to Pérez, "In South America, such incidents seem to be quite common." However, Pérez also pointed out that it is likely that the only way of knowing for sure if unicorns are indeed the descendants of a lost alien race is through DNA. "But they seem to be able to communicate in English quite well, which I believe is a sign of evolution, or at least a change in social organization," said