

K-7/11

B.C.A./ 2nd Sem  
Fundamentals of Mathematics  
Subject Code : BMATO-204  
Paper ID : May 2018

Max Marks: 60

Time allowed: 3 Hrs  
Important Instructions:

- Section A is compulsory.
- Attempt any five questions from section B and section C selecting at least two questions from each section.
- Assume any missing data
- Additional instructions, if any

**PART A (2marks × 10)**

Q. 1. Short-Answer Questions:

(a) Define upper triangular matrix with an example

(b) Find  $(AB)^T$  When  $A = \begin{bmatrix} 2 & 1 & -3 \\ 1 & 2 & 1 \\ 1 & -1 & 0 \end{bmatrix}$  and  $B = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 1 \end{bmatrix}$

(c) Solve  $2x + 5y = 1$  ,  $x - 3y = 5$

(d) Obtain the Median :  
X: 1 2 3 4 5 6 7 8 9  
F: 8 10 11 16 20 25 15 9 6

(e) What are the Demerits of median?

(f) Find  $\frac{dy}{dx}$  when  $y = \frac{\log(2x+3)}{x^2}$

(g) Find  $\frac{dy}{dx}$  when  $y = x^{-3} + x^{-5}$

(h) Evaluate  $\int_0^{\frac{\pi}{2}} \frac{\tan x}{\tan x + \cot x} dx$

(i) Evaluate  $\int \frac{(x+2)^3}{\sqrt{x}} dx$

(j) Write the formula for Trapezoidal method.

**PART B (8marks ×5)**

- Q. 2. Find the maximum and minimum value of  $Y = (x + 1)(x - 2)^2$   
OR

Compute  $\int_0^1 \frac{dx}{1+x^2}$  using Simpson's rule by dividing  $[0,1]$  into 4 equal parts.

- Q. 3. Solve by matrix method
- $$\begin{aligned} 2x + 5y - z &= 9 \\ 3x - 3y + 2z &= 7 \\ 2x - 4y + 3z &= 1 \end{aligned}$$

OR

Reduce the matrix to the normal form and hence, find its rank.

$$\begin{bmatrix} 2 & -1 & 3 & 4 \\ 0 & 3 & 4 & 1 \\ 2 & 3 & 7 & 5 \\ 2 & 5 & 11 & 6 \end{bmatrix}$$

- Q. 4. Calculate mode and standard deviation .

X :	1-10	11-20	21-30	31-40	41-50	51-60
F :	3	16	26	31	16	8

OR

The scores of 21 students in an intelligence test are shown in the frequency table below:

score	91	92	96	97	101	103	108
frequency	3	2	3	2	5	3	3

Calculate  $\sigma^2$

- Q. 5. Evaluate  $I = \int \frac{e^x(1+x)}{\sin^2 x e^x} dx$

OR

Evaluate  $\int_0^{\frac{\pi}{4}} \log(1 + \tan x) dx$

- Q. 6. If  $\sin y = x \sin(a+y)$ , then prove that  $\frac{dy}{dx} = \frac{\sin^2(a+y)}{\sin a}$

OR

Find  $\frac{dy}{dx}$  if  $x = a(1 - \cos \theta)$ ,  $y = a(1 + \sin \theta)$