

Week 2

1.2 Determine the current flowing through an element if the charge flow is given by

(a) $q(t) = (3t+8) \text{ mC}$

$$(3t+8) \frac{d}{dt} = 3 \quad \text{Answer: } 3 \text{ mA}$$

(b) $q(t) = (8t^2+4t-2) \text{ C}$

$$(8t^2+4t-2) \frac{d}{dt} = 16t+4 \quad \text{Answer: } (16t+4) \text{ A}$$

1.3 Find the charge $q(t)$ flowing through a device if the current is:

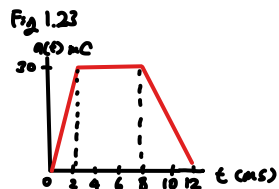
(a) $i(t) = 3 \text{ A}$, $q(0) = 1 \text{ C}$

$$\int 3 dt + 1 = 3t + 1 \quad \text{Answer: } (3t+1) \text{ C}$$

(b) $i(t) = (2t+5) \text{ mA}$, $q(0) = 0$

$$\int 2t+5 dt + 0 = t^2 + 5t \quad \text{Answer: } (t^2+5t) \text{ mC}$$

1.6 The charge entering a certain element is shown in Fig. 1.23. Find the current $i(t)$:



(a) $t = 1 \text{ ms}$

$$\frac{dq}{dt} = \frac{15}{1} = 15$$

(b) $t = 6 \text{ ms}$

$$\frac{dq}{dt} = \frac{0}{4} = 0$$

(c) $t = 10 \text{ ms}$

$$\frac{dq}{dt} = \frac{-30}{4} = -7.5$$

Answer
a) 15 A
b) 0 A
c) -7.5 A

1.10 A lightning bolt with 10 kA strikes an object for 15 μs .

How much charge is deposited on the object?

$$i = 10 \text{ kA} = 10 \times 10^3 \text{ A}$$

$$t = 15 \mu\text{s} = 15 \times 10^{-6} \text{ s}$$

$$q = i \cdot t = (10 \times 10^3) \times (15 \times 10^{-6}) \\ = 150 \times 10^{-3}$$

Answer: 150 mC

1.12 If the current flowing through an element is given by

$$i(t) = \begin{cases} 3t \text{ A}, & 0 \leq t < 6 \text{ s} \\ 18 \text{ A}, & 6 \leq t < 10 \text{ s} \\ -12 \text{ A}, & 10 \leq t < 15 \text{ s} \\ 0, & 15 \leq t \end{cases}$$

Plot the charge stored in the element over $0 < t < 20 \text{ s}$

$$0 \leq t < 6 \text{ s}$$

$$q(t) = \int_0^t 3t dt + q(0) = \left[\frac{3}{2} t^2 \right]_0^t + 0 \\ = 1.5 t^2$$

$$q(6) = 54$$

$$6 \leq t < 10 \text{ s}$$

$$q(t) = \int_6^t 18 dt + q(6) = [18t]_6^t + 54 \\ = 18t - 108 + 54 \\ = 18t - 54$$

$$q(10) = 126$$

$$10 \leq t < 15 \text{ s}$$

$$q(t) = \int_{10}^t (-12) dt + q(10) = [-12t]_{10}^t + 126 \\ = -12t + 120 + 126 \\ = -12t + 246$$

$$q(15) = -12 \times 15 + 246 \\ = 66$$

$$15 \leq t$$

$$q(t) = \int_{15}^t 0 dt + q(15) = 66$$

Answer

$$q(t) = \begin{cases} 1.5 t^2 & \text{C, } 0 \leq t < 6 \text{ s} \\ 18t - 54 & \text{C, } 6 \leq t < 10 \text{ s} \\ -12t + 246 & \text{C, } 10 \leq t < 15 \text{ s} \\ 66 & \text{C, } 15 \leq t < 20 \text{ s} \end{cases}$$