



## 4023 - Find a Minor

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In a graph  $G$ , contraction of an edge  $e$  with endpoints  $u, v$  is the replacement of  $u$  and  $v$  with a single vertex such that edges incident to the new vertex are the edges other than  $e$  that were incident with  $u$  or  $v$ . The resulting graph has one less edge than  $G$ . A graph  $H$  is a minor of a graph  $G$  if a copy of  $H$  can be obtained from  $G$  via repeated edge deletion, edge contraction and isolated node deletion.

Minors play an important role in graph theory. For example, every non-planar graph contains either the graph  $K_{3,3}$  (i.e., the complete bipartite graph on two sets of three vertices) or the complete graph  $K_5$  as a graph minor.

Write a program to find a graph minor  $K_{n,m}$  or  $K_n$  in an undirected connected simple graph.

### Input

The input consists of several test cases. The first line of each case contains an integers  $V$  ( $3 \leq V \leq 12$ ), the number of vertices in the graph, followed by a string in format " $K_n$ " or " $K_{n,m}$ " ( $1 \leq n, m \leq V$ ), the graph minor you're finding. The following  $V$  lines contain the adjacency matrix of the graph (1 means directly connected, 0 means not directly connected).

The diagonal elements of the matrix will always be 0, and the element in row  $i$  column  $j$  is always equal to the element in row  $j$  column  $i$ . The last test case is followed by a single zero, which should not be processed.

### Output

For each test case, print the case number and the string "Found" or "Not found".

### Sample Input

```
5 K2,2
0 1 1 1 1
1 0 0 0 0
1 0 0 0 0
1 0 0 0 0
1 0 0 0 0
4 K3
0 1 0 1
1 0 1 0
0 1 0 1
1 0 1 0
4 K2,2
0 1 0 1
1 0 1 1
0 1 0 1
1 1 1 0
5 K2,2
0 1 0 0 1
1 0 0 0 1
0 0 0 1 1
0 0 1 0 1
```

```
1 1 1 1 0
5 K4
0 1 0 1 1
1 0 1 1 0
0 1 0 1 1
1 1 1 0 1
1 0 1 1 0
0
```

## Sample Output

```
Case 1: Not found
Case 2: Found
Case 3: Found
Case 4: Not found
Case 5: Found
```

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**Problemsetter:** Rujia Liu

**Tests-Setter:** Rujia Liu

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