

Union find :

(P, q, value)

let, say $P[] \rightarrow$ stores Parent info.

$w[] \rightarrow$ weight from th element to its Parent.

$$\boxed{\frac{P}{q} = \text{value}} \quad - (1)$$

let, say Parent of $P[P] \rightarrow x$ - ultimate Parent of P .
 $P[q] \rightarrow y$ - ultimate Parent of q .

x, y are Parents.

$$\therefore \frac{w[q]}{w[P]} = \frac{(q/y)}{(P/x)} = \frac{q}{P} \cdot \frac{x}{y}$$

weight from q to y
weight from P to x

$$\frac{w_q}{w_p} = \frac{q}{P} \cdot \frac{x}{y} \Rightarrow$$

$$\boxed{\frac{x}{y} = \frac{w_q}{w_p} \cdot \frac{P}{q}} \quad - (2)$$

\therefore If we change, $P(x)$ to $y \Rightarrow$ ultimate Parent of x is y .
then $w[x] \Rightarrow \frac{x}{y} \rightarrow$ from (2)

$$w[x] = \frac{x}{y} = \frac{w_q}{w_p} \cdot \frac{P}{q} \Rightarrow \frac{w[q]}{w[P]} \cdot \text{value}$$