Past Year JEE Questions

Questions

Quetion: 01

The sum of an infinite geometric series with positive terms is 3 and the sum of the cubes of its terms is $\frac{27}{19}$. Then the common ratio of this series is : A. $\frac{4}{9}$ B. $\frac{1}{3}$ C. $\frac{2}{3}$ D. $\frac{2}{9}$

Solutions

Solution: 01

Explanation

$$\frac{a}{1-r} = 3$$
(1)

$$\frac{a^3}{1-r^3} = \frac{27}{19} \Rightarrow \frac{27(1-r^2)}{1-r^3} = \frac{27}{19}$$

$$\Rightarrow 6r^2 - 13r + 6 = 0$$

$$\Rightarrow r = \frac{2}{3}$$

as
$$|r| < 1$$