

Binomial Theorem - Class XI

Related Questions with Solutions

Questions

Question: 01

In questions below, If $C_0, C_1, C_2, \dots, C_n$ are the combinatorial coefficients in the expansion of $(1+x)^n$, $n \in \mathbb{N}$, then

$$C_0 C_r + C_1 C_{r+1} + C_2 C_{r+2} + \dots + C_{n-r} C_n =$$

A. ${}^{2n}C_{n-r}$

B. ${}^{2n}C_n$

C. $\left({}^{2n}C_n\right)^2$

D. $\left({}^{2n}C_{n-r}\right) + 1$

Solutions

Solution: 01

$$[1+x]^n = {}^nC_0 + {}^nC_1 x + {}^nC_2 x^2 + \dots + {}^nC_n x^n \quad [x+1]^n = {}^nC_0 x^n + {}^nC_1 x^{n-1} + \dots + {}^nC_n$$

multiply

$$[1+x]^{2n} = [{}^nC_0 + {}^nC_1 x + \dots + {}^nC_n x^n] [{}^nC_0 x^n + \dots + {}^nC_n]$$

$${}^nC_0 {}^nC_r + {}^nC_1 {}^nC_{r+1} + \dots + {}^nC_{n-r} {}^nC_n =$$

$$\text{coefficient of } x^{n-r} \text{ in } [1+x]^{2n} = {}^{2n}C_{n-r}$$

Correct Options

Answer:01

Correct Options: A