Determinants - Class XII

Past Year JEE Questions

Questions

Quetion: 01

Let
$$A = \begin{pmatrix} [x+1] & [x+2] & [x+3] \\ [x] & [x+3] & [x+3] \\ [x] & [x+2] & [x+4] \end{pmatrix}$$
, where [t] denotes the greatest integer less than or equal to

t. If det(A) = 192, then the set of values of x is the interval:

A. [68, 69)

B. [62, 63)

C. [65, 66)

D. [60, 61)

Solutions

Solution: 01

Explanation

$$\begin{vmatrix} [x+1] & [x+2] & [x+3] \\ [x] & [x+3] & [x+3] \\ [x] & [x+2] & [x+4] \end{vmatrix} = 192$$

$$\mathsf{R}_1 \to \mathsf{R}_1 - \mathsf{R}_3 \And \mathsf{R}_2 \to \mathsf{R}_2 - \mathsf{R}_3$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & -1 \\ [x] & [x] + 2 & [x] + 4 \end{bmatrix} = 192$$

$$2[x] + 6 + [x] = 192 \Rightarrow [x] = 62$$