Trigonometry Functions - Class XI

Past Year JEE Questions

Questions

Quetion: 01

The value of $\cot \frac{\pi}{24}$ is :

A.
$$\sqrt{2} + \sqrt{3} + 2 - \sqrt{6}$$

B.
$$\sqrt{2} + \sqrt{3} + 2 + \sqrt{6}$$

C.
$$\sqrt{2} - \sqrt{3} - 2 + \sqrt{6}$$

D.
$$3\sqrt{2} - \sqrt{3} - \sqrt{6}$$

Solutions

Solution: 01

Explanation

$$\cot \theta = \frac{1 + \cos 2\theta}{\sin 2\theta} = \frac{1 + \left(\frac{\sqrt{2} + 1}{2\sqrt{2}}\right)}{\left(\frac{\sqrt{2} - 1}{2\sqrt{2}}\right)}$$

$$\theta = \frac{\pi}{24}$$

$$\Rightarrow \cot\left(\frac{\pi}{24}\right) = \frac{1 + \left(\frac{\sqrt{9} + 1}{2\sqrt{2}}\right)}{\left(\frac{\sqrt{9} - 1}{2\sqrt{2}}\right)}$$

$$=\frac{(2\sqrt{2}+\sqrt{3}+1)}{(\sqrt{3}-1)}\times\frac{(\sqrt{3}+1)}{(\sqrt{3}+1)}$$

$$= \frac{2\sqrt{6}+2\sqrt{2}+3+\sqrt{3}+\sqrt{3}+1}{2}$$

$$=\sqrt{6}+\sqrt{2}+\sqrt{3}+2$$