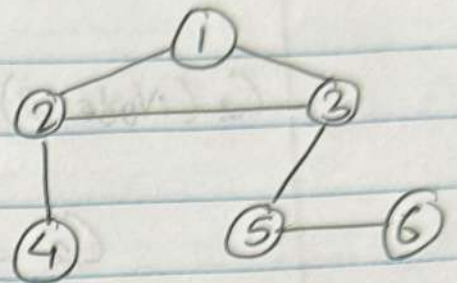


Nodes (V): $\{1, 2, 3, 4, 5, 6\}$
 Edges (E): $\{(1, 2), (1, 3), (2, 3), (2, 4), (3, 5), (5, 6)\}$

① Order (N): Total nodes = 6
 Size (M): Total edges = 6

② Degree Distribution $P(k)$:



$$k_1 \Rightarrow \{2, 3\} = 2$$

$$k_2 \Rightarrow \{1, 3, 4\} = 3$$

$$k_3 \Rightarrow \{1, 2, 5\} = 3$$

$$k_4 \Rightarrow \{2\} = 1$$

$$k_5 \Rightarrow \{3, 6\} = 2$$

$$k_6 \Rightarrow \{5\} = 1$$

$$\text{Average degree } \langle k \rangle = \frac{1}{N} \sum_{i=1}^N k_i$$

$$= \frac{2 + 3 + 3 + 1 + 2 + 1}{6} = \frac{12}{6} = 2$$

③ Local Clustering Coefficient (C_i)

$$C_i = \frac{2E_i}{k_i(k_i - 1)}$$

②

$$C_1(\text{Node 1}): E_1 = 1 \{2, 3\}$$

$$k_1 = 2$$

$$C_1 = \frac{2 \times 1}{2(2-1)} = 1$$

$$C_2(\text{Node 2}): E_2 = 1 \{1, 3, 4\} \Rightarrow \{1, 3\} \text{ exist}$$

$$k_2 = 3$$

$$C_2 = \frac{2 \times 1}{3(3-1)} = \frac{1}{3}$$

$$C_3(\text{Node 3}): E_3 = 1 \{1, 2, 5\} \Rightarrow \{1, 2\} \text{ exist}$$

$$k_3 = 3$$

$$C_3 = \frac{2 \times 1}{3(3-1)} = \frac{1}{3}$$

$$C_5(\text{Node 5}): E_5 = 0 \{3, 6\} \text{ no connection}$$

$$k_5 = 2$$

$$C_5 = \frac{2 \times 0}{2(2-1)} = 0$$

$$\textcircled{4} \text{ Network Average Clustering Coefficient } \langle C \rangle = \frac{1}{N} \sum_{i=1}^N C_i$$

$$\langle C \rangle = \{C_1, C_2, C_3\} = \frac{1 + \frac{1}{3} + \frac{1}{3}}{3}$$

$$= \frac{5}{9} \approx 0.556$$

(3)

$$\begin{aligned} \textcircled{5} \text{ Density } (p) &= \frac{M}{N(N-1)/2} = \frac{6}{6(6-1)/2} \\ &= \frac{2}{5} \text{ or } 0.4 \end{aligned}$$

homework-1

October 22, 2025

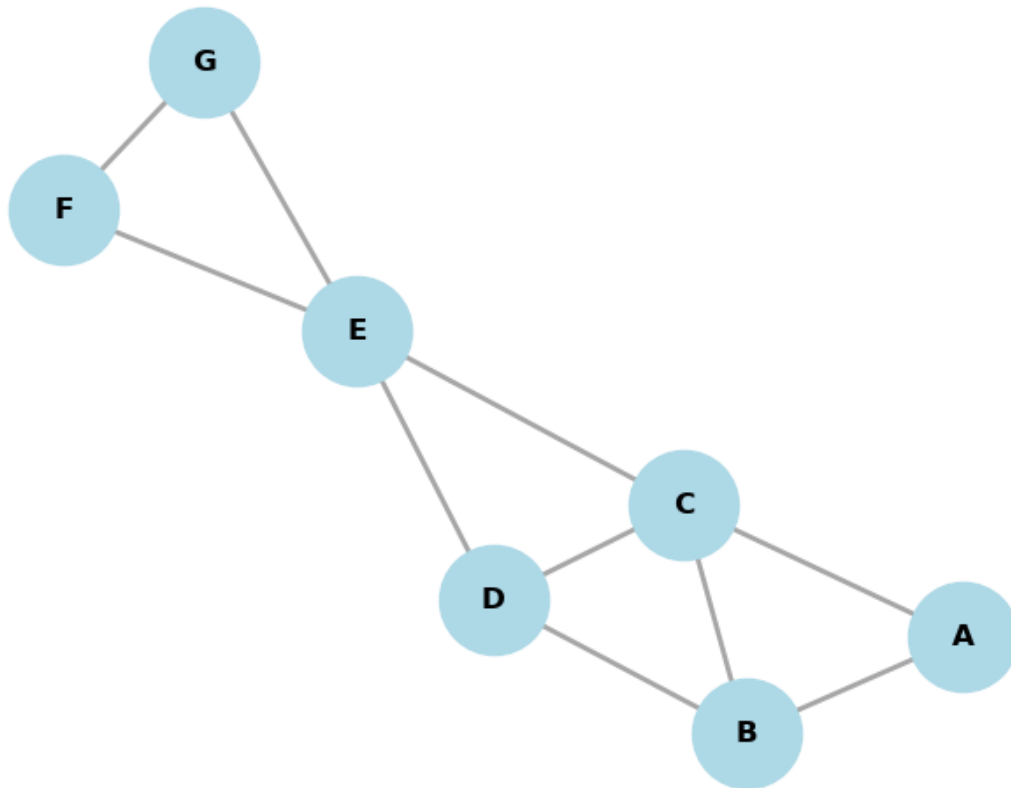
```
[1]: !pip install networkx igraph -q
```

```
[2]: import networkx as nx
import matplotlib.pyplot as plt
import numpy as np
```

```
[3]: edge_list = [
    ('A', 'B'), ('A', 'C'),
    ('B', 'C'), ('B', 'D'),
    ('C', 'D'), ('C', 'E'),
    ('D', 'E'),
    ('E', 'F'), ('E', 'G'),
    ('F', 'G')
]
G = nx.Graph()
G.add_edges_from(edge_list)

plt.figure(figsize=(8, 6))
pos = nx.spring_layout(G, k=0.5, iterations=50)
nx.draw_networkx_nodes(G, pos, node_color='lightblue', node_size=2000)
nx.draw_networkx_edges(G, pos, width=2, alpha=0.7, edge_color='gray')
nx.draw_networkx_labels(G, pos, font_size=12, font_weight='bold')
plt.axis('off')
plt.title('Graph B')
plt.show()
```

Graph B



```
[4]: order_N = G.number_of_nodes()
size_M = G.number_of_edges()
density = nx.density(G)
avg_degree = np.mean([d for n, d in G.degree()])
avg_path_length = nx.average_shortest_path_length(G)
avg_clustering = nx.average_clustering(G)

print(f"Order (N): {order_N}")
print(f"Size (M): {size_M}")
print(f"Density (p): {density:.4f}")
print(f"Average Degree <k>: {avg_degree:.2f}")
print(f"Average Path Length <d>: {avg_path_length:.2f}")
print(f"Average Clustering Coefficient <C>: {avg_clustering:.4f}")
```

```
Order (N): 7
Size (M): 10
Density (p): 0.4762
Average Degree <k>: 2.86
Average Path Length <d>: 1.71
Average Clustering Coefficient <C>: 0.7381
```

```
[5]: print("Degree (k) Distribution:")
degrees = dict(G.degree())
for node, deg in sorted(degrees.items()):
    print(f"Node {node}: {deg}")
```

```
Degree (k) Distribution:
Node A: 2
Node B: 3
Node C: 4
Node D: 3
Node E: 4
Node F: 2
Node G: 2
```

```
[6]: print('Local Clustering Coefficient Distribution:')
clustering = nx.clustering(G)
for node, coeff in sorted(clustering.items()):
    print(f"Node {node}: {coeff:.4f}")
```

```
Local Clustering Coefficient Distribution:
Node A: 1.0000
Node B: 0.6667
Node C: 0.5000
Node D: 0.6667
Node E: 0.3333
Node F: 1.0000
Node G: 1.0000
```

How does the density reflect the overall connectivity?

A density of ≈ 0.476 is moderately high. It indicates that the network is well-connected, with almost half of all possible connections being present. It is far from being a sparse network.

Does the Average Path Length suggest this is a “small world”?

Yes. An average path length of ≈ 1.71 is extremely short. It means that, on average, any node can reach any other node in the network in less than two “hops.” This high degree of closeness is a defining characteristic of a small-world network.

How does the Average Clustering Coefficient indicate the level of local community formation?

An average clustering coefficient of ≈ 0.738 is extremely high. This value (which measures the “cliquishness” of neighborhoods) shows a very strong tendency for nodes to form tight-knit local communities. The high values for C_A , C_F , and C_G (all 1.0) confirm that their immediate neighborhoods are perfect triangles. This high clustering, combined with the low path length, is the classic signature of a small-world network.

```
[ ]:
```