

TREES I



Today's content

- Trees Intro
- Naming convention
- Trees traversal
- Iterative inorder
- Level Order Traversal
- left view & right view

01. Arrays & ArrayList

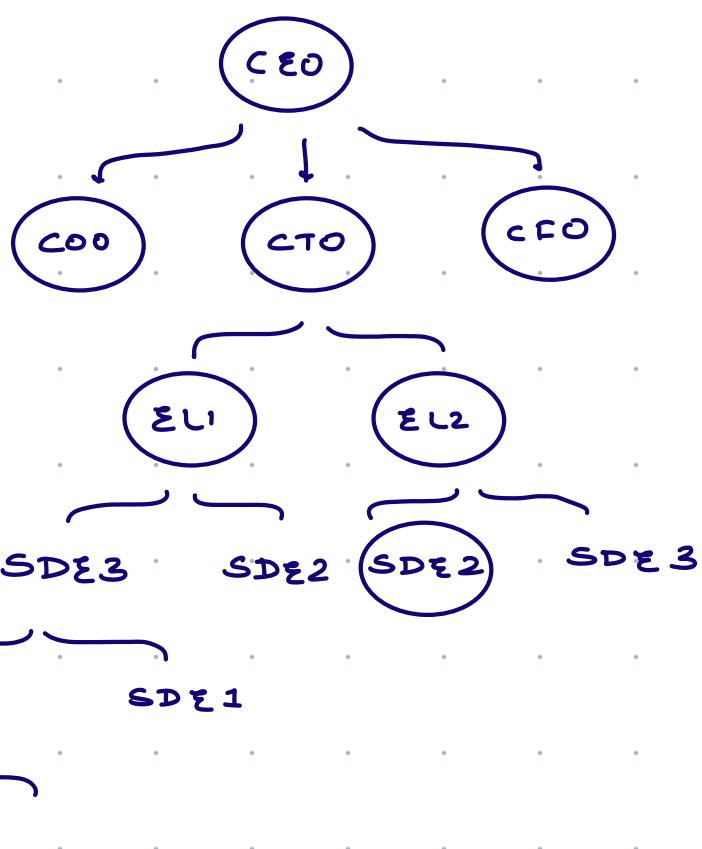
02. Stack & Queue

03. LinkedList

Linear data structures

Trees → Non linear data structure

↳ stores information in hierarchical order



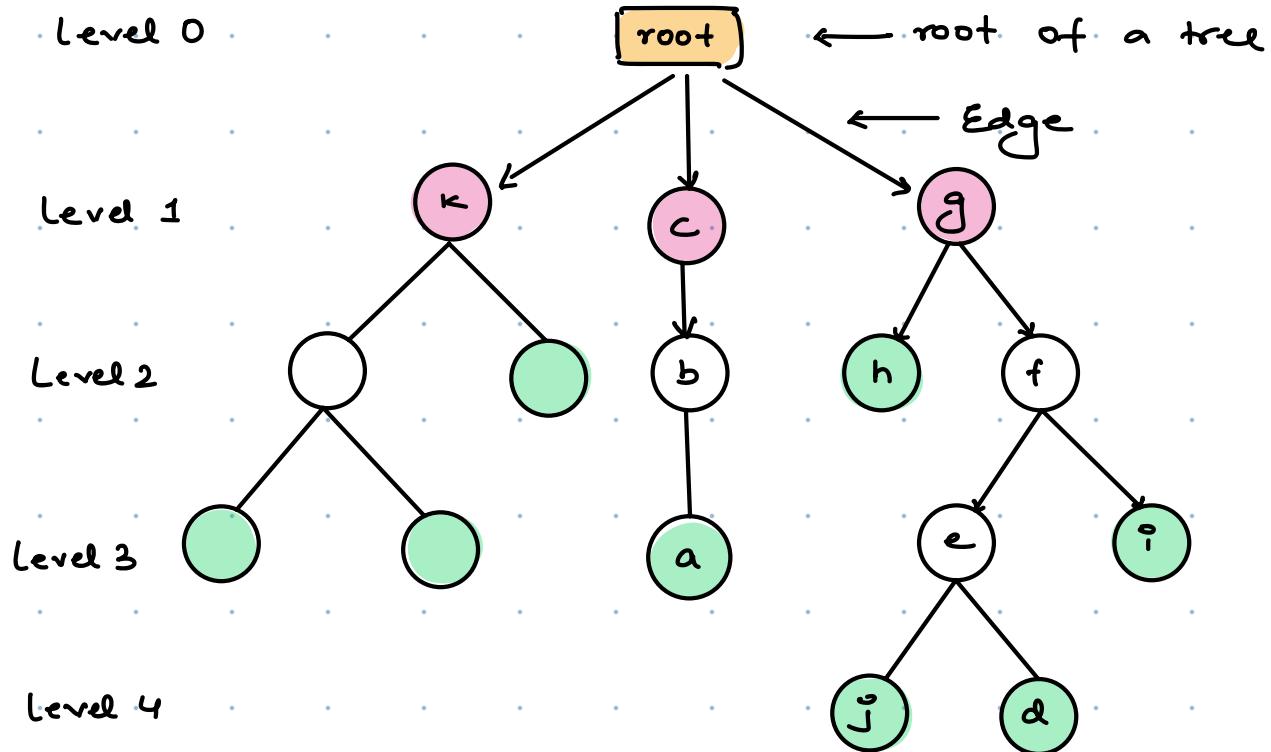
→ Family tree

→ Config tree in windows

→ File structure

→ MLM market

Naming convention for Trees



Node → An element of a tree that contains data & it may have some children

- sibling nodes → children of same parent
- leaf nodes → nodes with 0 child

Total no. of Nodes = N

No. of Edges = $N - 1$

Ancestor → All nodes from parent node to root node are going to be ancestor.

Ancestor(e) = f, g, root

Ancestor(b) = c, root

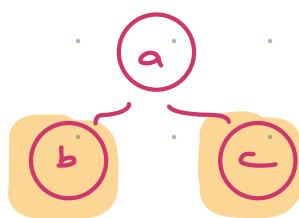
Descendant → All the nodes from child to leaf nodes along the same path will be descendants

Descendants(f) = d, e, i, j

Subtree → A part of a tree

→ Child along with descendants is a subtree.

Quiz 1 → Can leaf node be a subtree?



Leaf node is also a subtree.

Is single node a valid tree? → Yes



Quiz 2. Do all nodes have parent node?

↳ No, root node is an exception.

Height (Node) → Maximum distance (in terms of edges) between the node & its furthest leaf child node.

$$\text{Height}(b) = 1$$

$$\text{Height}(g) = 3$$

Depth (Node) → No. of edges b/w the given node to the root node.

$$\text{Depth}(g) = 1$$

$$\text{Depth}(\text{root}) = 0$$

Quiz 3 → Height of leaf Node → 0

Binary Tree

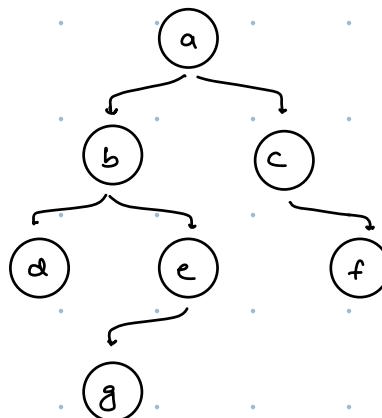
→ Each node can go & have at most 2 children.
0, 1, 2 ✓

class Node {

int val;

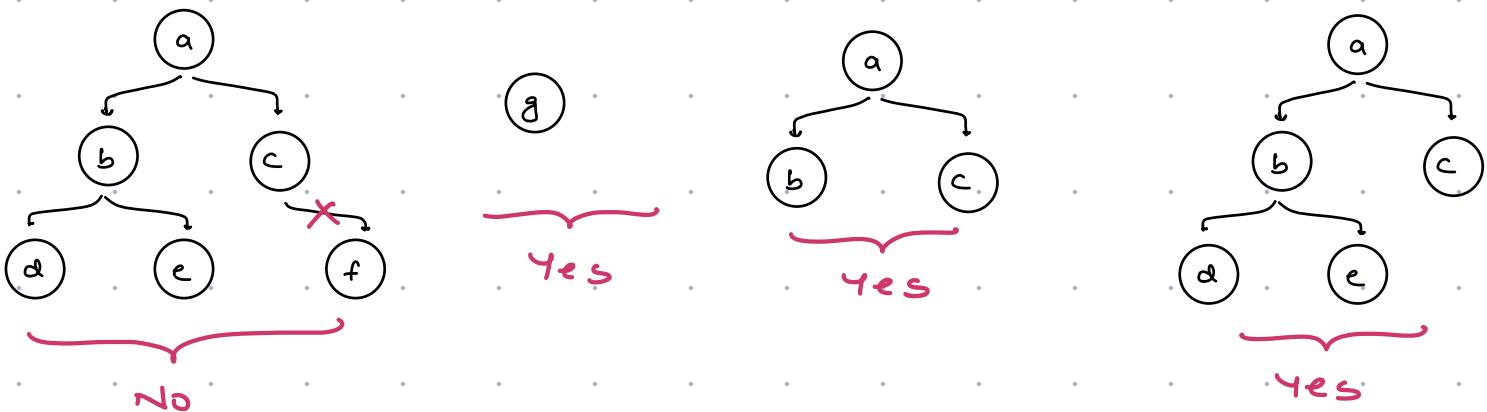
Node left;

Node right;

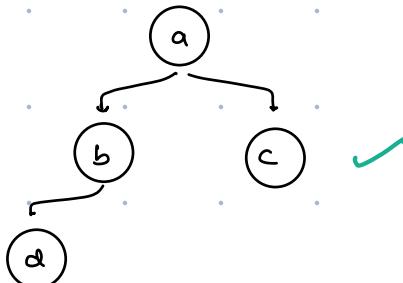
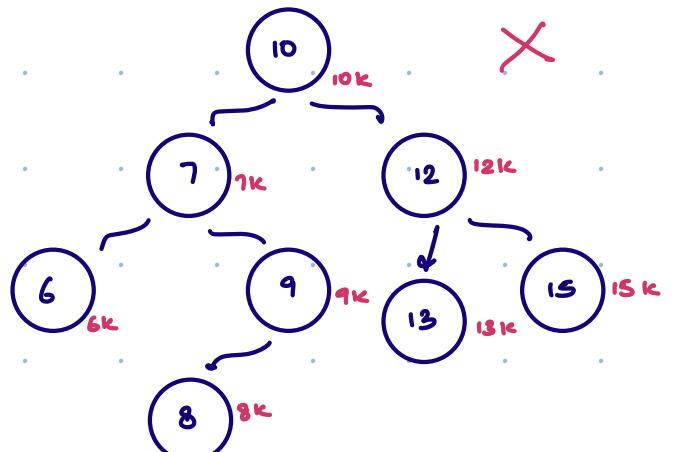
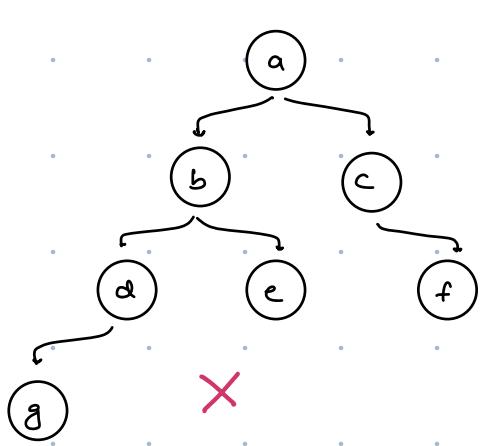


Types of Binary trees

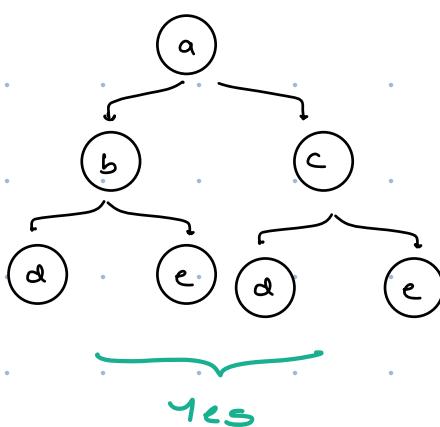
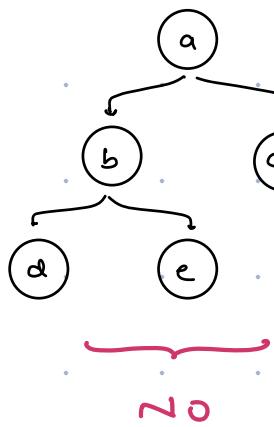
01. Proper binary tree → Every node will have either 0 or 2 children



02. Complete Binary tree → All the levels must be completely filled. the last level can be an exception but for last level as well, child should be added from left to right.



* Perfect binary tree → All internal nodes must have 2 children. All leaf nodes should lie on same level.

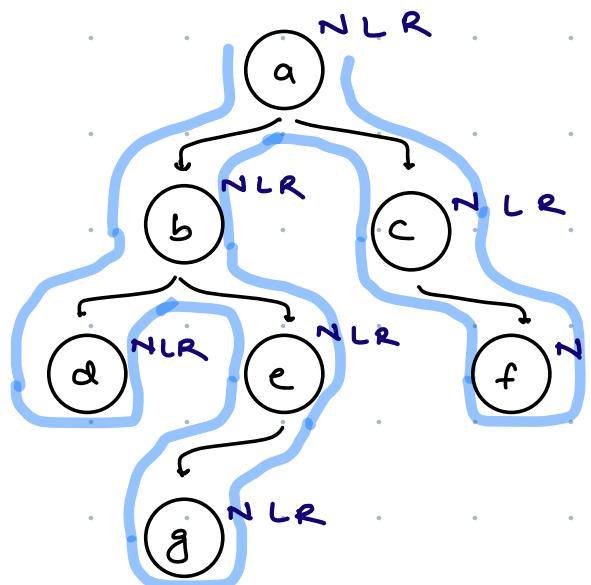


→ Perfect binary tree have property of both complete binary tree & proper binary tree

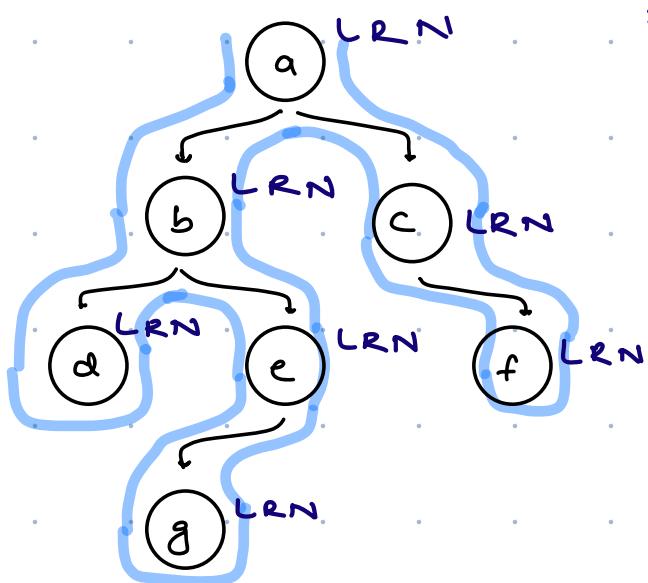
Traversals

- ⇒ Preorder (N L R)
- ⇒ Inorder (L N R)
- ⇒ Postorder (L R N)
- ⇒ Level Order → Breadth first Search

Depth first Traversal

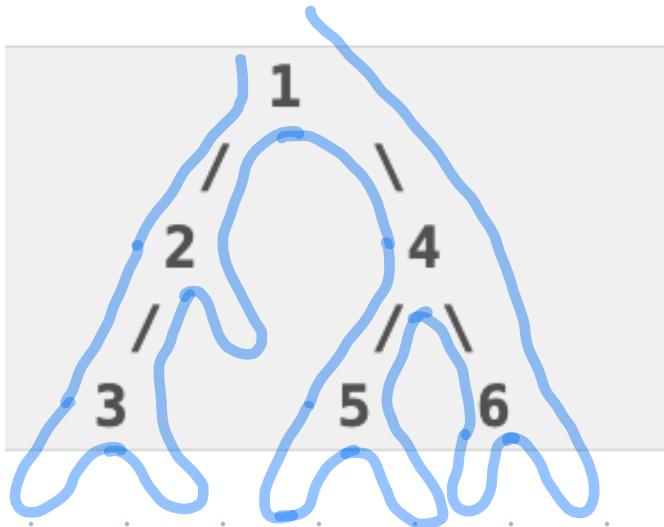


preorder = a b d e g c f
↳ NLR for every node



postorder = d g e b f c a
↳ LRN

Quiz 5 = Inorder Traversal → 3 2 1 5 4 6

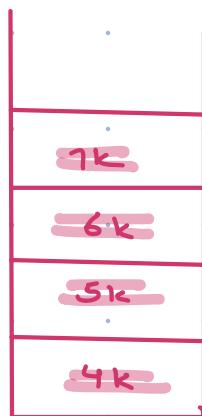
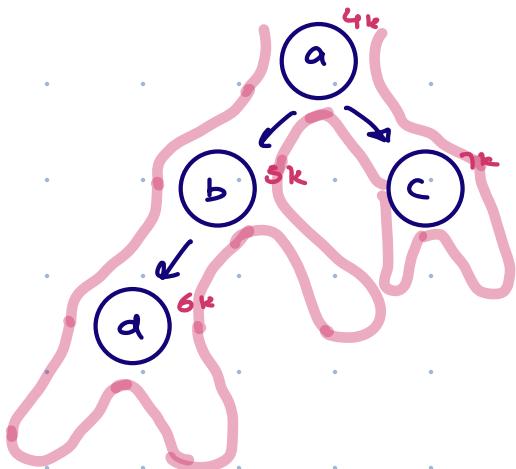


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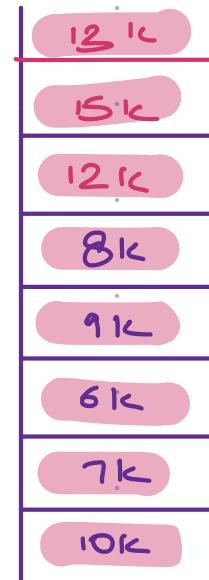
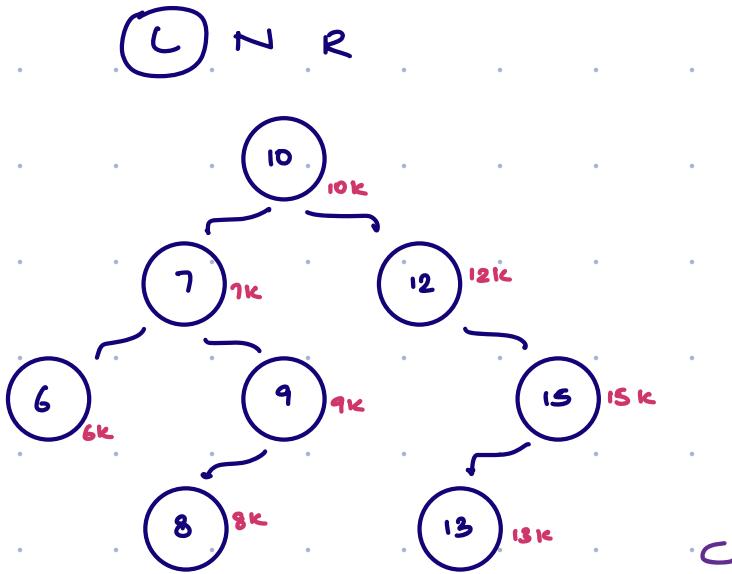
void inorder(Node *root)
{
    if (root == NULL) return;
    inorder(root.left);
    print (root.val);
    inorder (root.right);
}
  
```

$Tc: O(n)$
 $Sc: O(h)$

- d b a c



Iterative Inorder Traversal



6 7 8 9 10 12 13 15

Node curr = root

while (st.size() > 0 || curr != null)

 while (curr != null)

 st.push(curr);

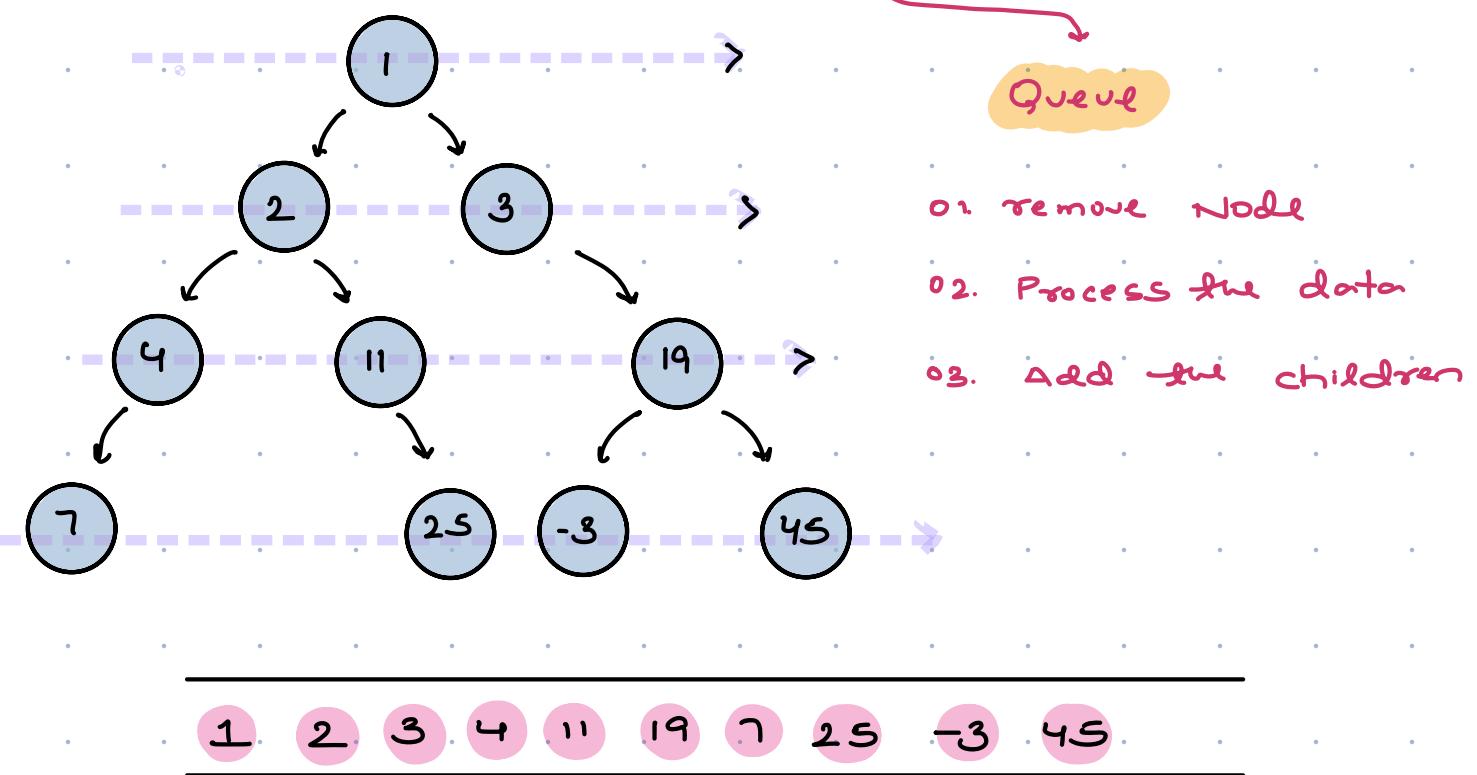
 curr = curr.left;

 curr = st.pop();

 print (curr.val);

 curr = curr.right;

Level Order Traversal (Breadth first search)



Output → 1 2 3 4 11 19 7 25 -3 45

Queue < Node > q :

q.add (root);

TC : O(n)
SC : O(n)

while (q.size () > 0)

 Node rem = q.remove();

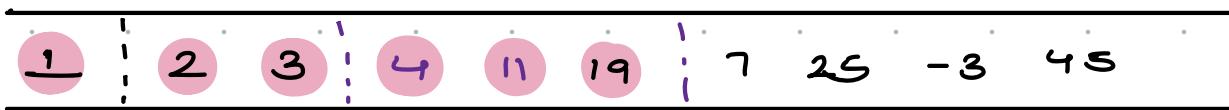
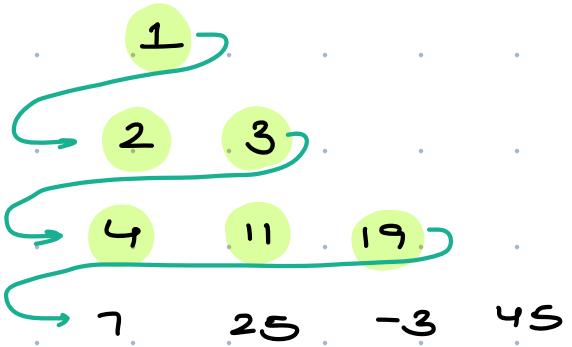
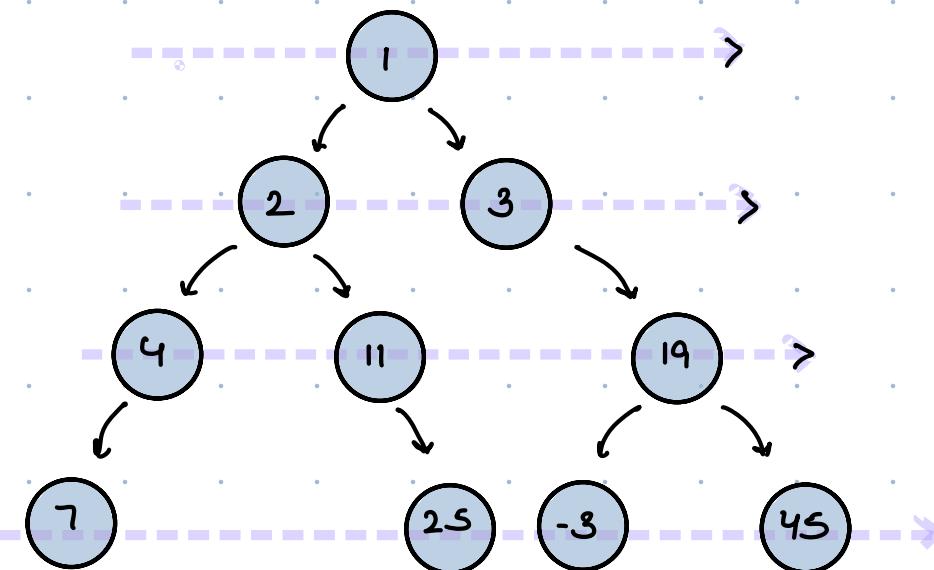
 print (rem.val);

 if (rem.left != null) q.add (rem.left);

 if (rem.right != null) q.add (rem.right);

}

* Level Order



$$\begin{array}{c} sz = 1 \\ | \\ 0 \end{array} \quad \begin{array}{c} sz = 2 \\ | \\ x \\ | \\ 0 \end{array} \quad \begin{array}{c} sz = 3 \\ | \\ x \\ + \\ 0 \end{array}$$

Queue < Node > q :

q.add (root);

while (q.size () > 0)

```
int sz = q.size ();
for (int i=1; i <= sz; i++) {
```

Node rem = q.remove ();

print (rem.val);

if (rem.left != null) q.add (rem.left);

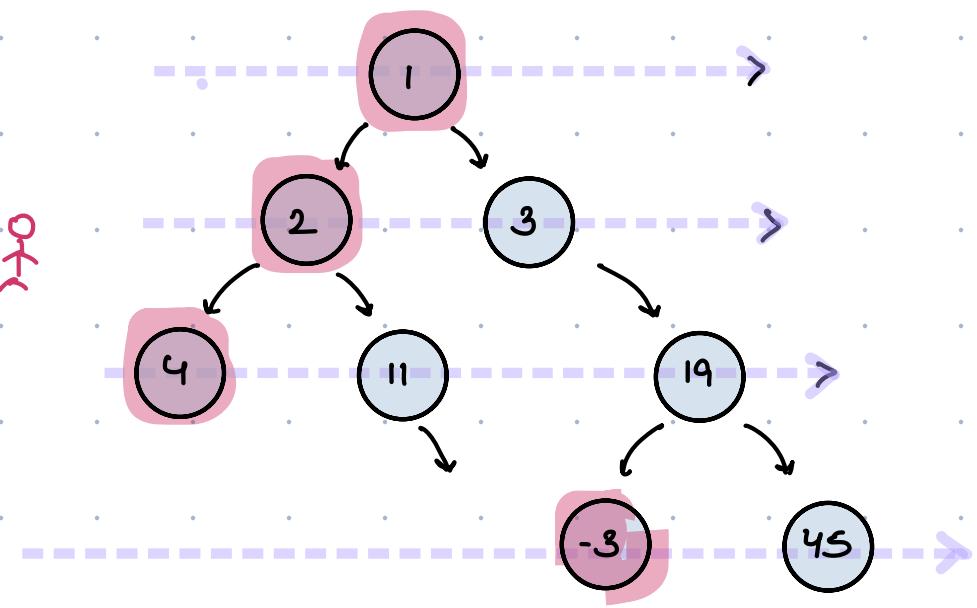
if (rem.right != null) q.add (rem.right);

}

Tc : O(n)

Sc : O(n)

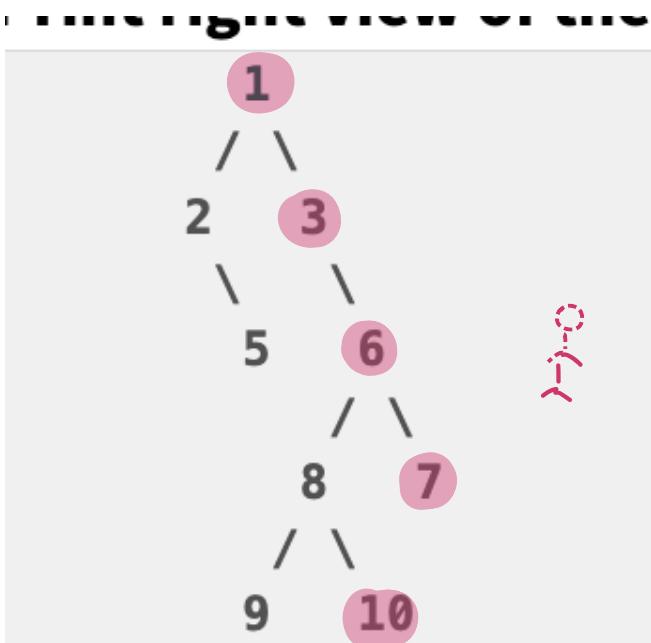
* left view



if ($i == 1$)

↓
print (rem.val);

right view



if ($i == sz$)

↓
print (rem.val)