Paper / Subject Code: 40521 / Engineering Mathematics-IV Time: 3 hrs Note: 1) O. No. 01 is compulsory. 2) Solve any three from Q. No. 92 to 06. 3) Numbers to the right indicate full marks. Use of statistical tables is allowed. Q. 1. Solve. find the sum and product of Eigen values A. Integrate the function  $f(z) = z^2$  from A(0, 0) to B(1, 1) along straight line AB b) A transmission channel has a per-digit error probability p = 0.01. Calculate the probability of more than 1 error in 10 received digits using Poisson distribution Find the Eigenvalues and Eigenvectors of the matrix A Find the Z-Transform of  $Cos\left(\frac{k\pi}{4} + \alpha\right) k \ge 0$ Use the dual simplex method to solve the LPP  $Min \cdot Z = 2X_1 + 2X_2 + 4X_3$ 8 Verify Caley-Hamilton theorem and hence find  $A^{-1}$  and  $A^4$  where A =6 Solve the LPP by Big -M method Maximize  $Z = 3X_1 - 2X_2$ 8 subject to 2X<sub>1</sub> Page 1 of 2

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Q. 4.

- a) Find inverse Z transform of  $F(z) = \frac{1}{(z-1)(z-3)}$  for i) |z| < 1, ii) 1 < |z| < 3.
- b) The following data represent the marks obtained by 12 students in two tests, one held before the coaching and the other after the coaching.

Test I : 55, 60, 65, 75, 49, 25, 18, 30, 35, 51, 61, 72.

Test II : 63, 70, 70, 81, 54, 29, 21, 38, 32, 50, 70, 80.

Do the data indicate that the coaching was effective in improving the performance of the students?

Find all possible Laurent's series expansions of the function  $f(z) = \frac{1}{(z-1)(z+2)}$  about z=0 indicating the region of convergence in each case.

Q. 5.

a) Determine all basic solutions to the following problem

Max.  $Z = x_1 - 2x_2 + 4x_3$ 

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- $x_1 + 2x_2 + 3x_3 = 7$ ,  $3x_1 + 4x_2 + 6x_3 = 15$ ,  $x_1, x_2, x_3 \ge 0$
- b) Using Normal distribution, find the probability of getting 55 heads in the toss of 100 fair coins.
- c) Solve the NLPP Optimize  $Z = 10x_1 + 8x_2 + 6x_3 + 2x_1^2 + x_2^2 + 3x_3^2 100$ Subject to  $x_1 + x_2 + x_3 = 20$ ,  $x_1, x_2, x_3 \ge 0$

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Q. 6.

a) Show that the given matrix is diagonalizable and hence find diagonal form and

transforming matrix where  $A = \begin{bmatrix} 4 & 6 & 6 \\ 1 & 3 & 2 \\ -1 & -5 & -2 \end{bmatrix}$ .

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- b) Of the 64 off springs of a certain cross between guinea pigs 34 were red, 10 were black and 20 were white. According to the generic model these numbers should be in the ratio 9:3:4. Use 2- test to check whether the data are consistent with the model.
- c) Max.  $Z = 4x_1 + 6x_2 x_1^2 x_2^2 x_3^2$ , Subject to  $x_1 + x_2 \le 2$  and  $2x_1 + 3x_2 \le 12$ ,  $x_1, x_2 \ge 0$  by K-T condition.

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