

Deep Image Prior (and Its Cousin) for Inverse Problems: the Untold Stories

Ju Sun

Computer Science & Engineering, UMN

Imaging & Vision Seminar, Rice University

Nov 18, 2022



UNIVERSITY OF MINNESOTA
Driven to DiscoverSM

Thanks to



<https://glovex.umn.edu/>



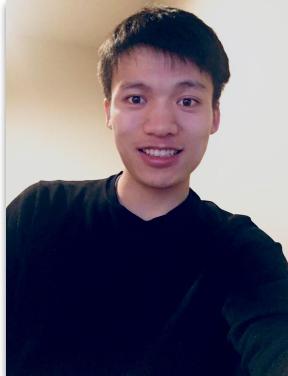
Taihui Li (CS&E)



Zhong Zhuang (ECE)



Hengkang Wang (CS&E)



Le Peng (CS&E)



Hengyue Liang (ECE)

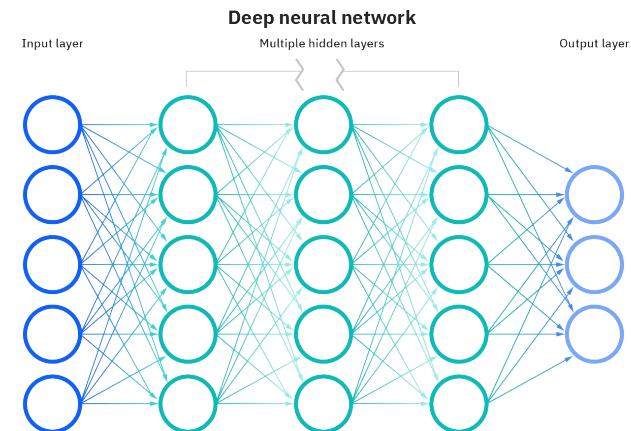


Tiancong Chen (CS&E)

Research in the group



(Machine) **Learning**, (Numerical) **Optimization**, (Computer) **Vision**, healthcar**E**, + **X**

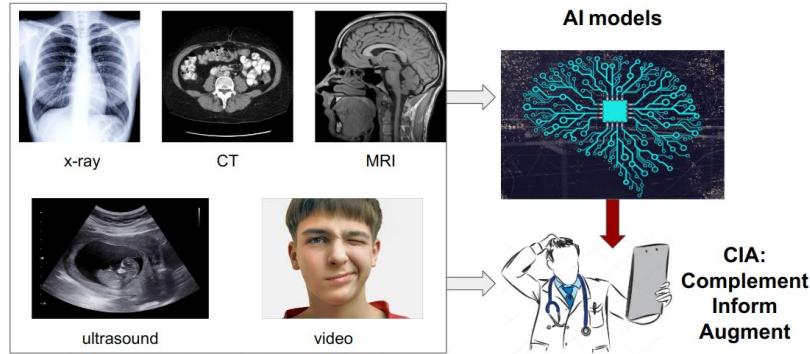
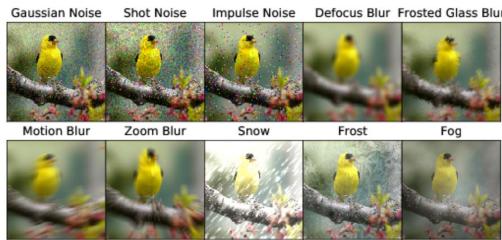
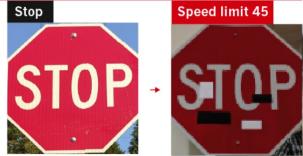


Our research themes

FOOLING THE AI

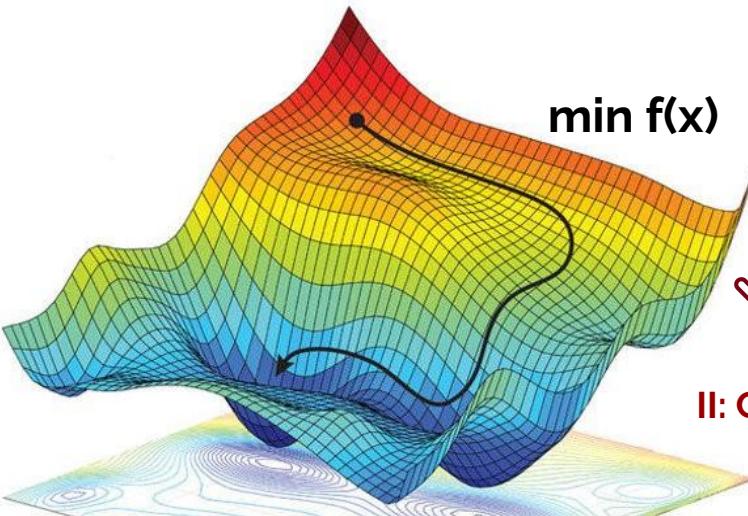
Deep neural networks (DNNs) are brilliant at image recognition — but they can be easily hacked.

These stickers made an artificial-intelligence system read this stop sign as 'speed limit 45'.



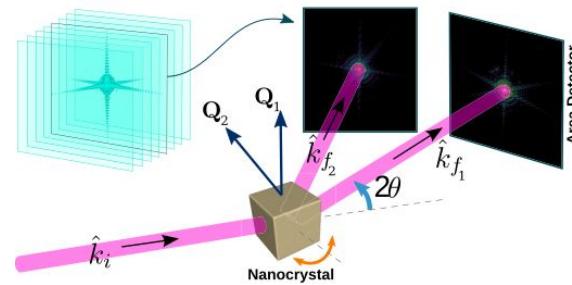
I: Trustworthy AI

$$\min f(x) \quad \text{s.t.} \quad g(x) \leq 0$$



II: Computation for AI

III: AI for Healthcare



IV: AI for Science and Engineering

Visual inverse problems

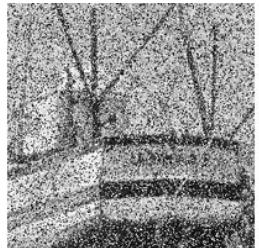
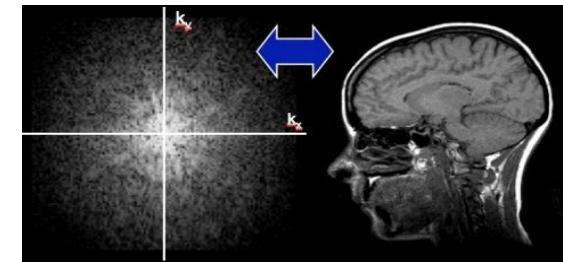
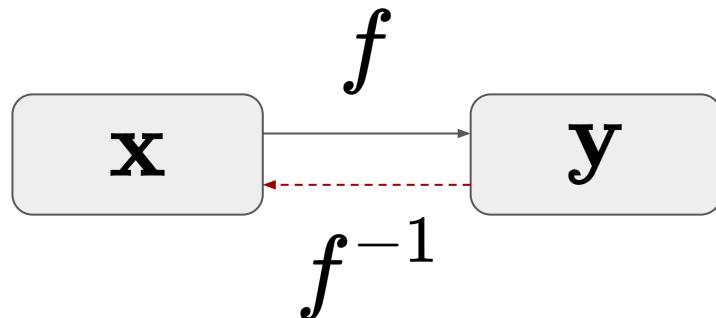


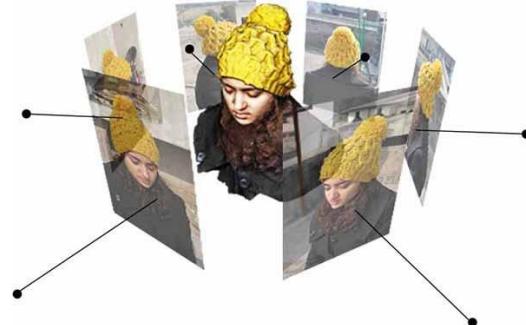
Image denoising



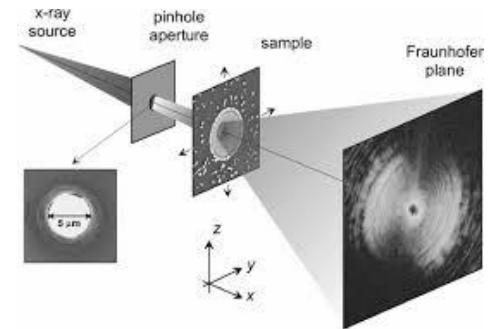
MRI reconstruction



Image super-resolution



3D reconstruction



Coherent diffraction imaging (CDI)

Traditional methods

Inverse problem: given $\mathbf{y} = f(\mathbf{x})$, recover \mathbf{x}

$$\min_{\mathbf{x}} \underbrace{\ell(\mathbf{y}, f(\mathbf{x}))}_{\text{data fitting}} + \lambda \underbrace{R(\mathbf{x})}_{\text{regularizer}}$$

RegFit

Limitations:

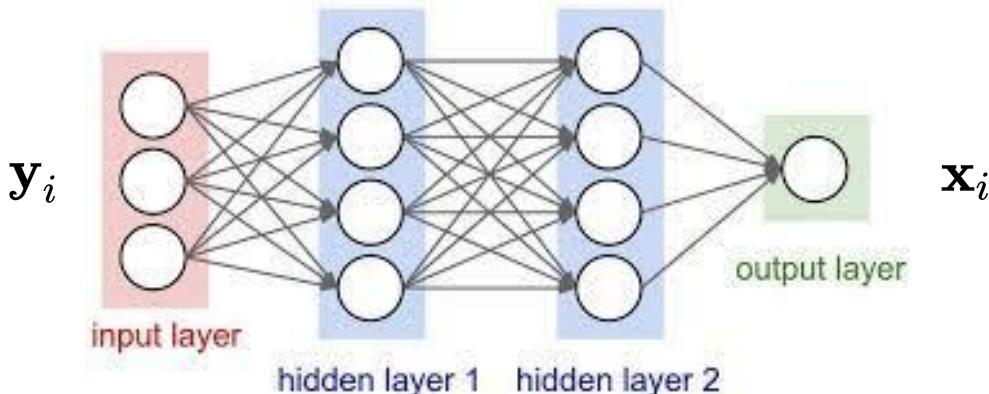
- Which ℓ ? (e.g., unknown/compound noise)
- Which R ? (e.g., structures not amenable to math description)
- Speed

How has deep learning (DL)
changed the story?

DL methods: the radical way

Inverse problem: given $\mathbf{y} = f(\mathbf{x})$, recover \mathbf{x}

Learn the f^{-1} with a training set $\{(\mathbf{y}_i, \mathbf{x}_i)\}$



Limitations:

- Wasteful: not using f
- Representative data?
- Not always straightforward
(see, e.g., Tayal et al. **Inverse Problems, Deep Learning, and Symmetry Breaking**.
<https://arxiv.org/abs/2003.09077>)

DL methods: the middle way

Inverse problem: given $\mathbf{y} = f(\mathbf{x})$, recover \mathbf{x}

$$\min_{\mathbf{x}} \underbrace{\ell(\mathbf{y}, f(\mathbf{x}))}_{\text{data fitting}} + \lambda \underbrace{R(\mathbf{x})}_{\text{regularizer}}$$

RegFit

Recipe: revamp numerical methods for RegFit with **pretrained/trainable DNNs**

DL methods: the middle way

Algorithm unrolling

$$\min_{\mathbf{x}} \underbrace{\ell(\mathbf{y}, f(\mathbf{x}))}_{\text{data fitting}} + \lambda \underbrace{R(\mathbf{x})}_{\text{regularizer}}$$

If R proximal friendly

$$\mathbf{x}^{k+1} = \mathcal{P}_R(\mathbf{x}^k - \eta \nabla^\top f(\mathbf{x}^k) \ell'(\mathbf{y}, f(\mathbf{x}^k)))$$

Idea: make \mathcal{P}_R trainable, using $\{(\mathbf{x}_i, \mathbf{y}_i)\}$

E.g.,

$$\ell(\mathbf{y}, f(\mathbf{x})) = \|\mathbf{y} - \mathbf{A} \mathbf{x}\|_2^2$$

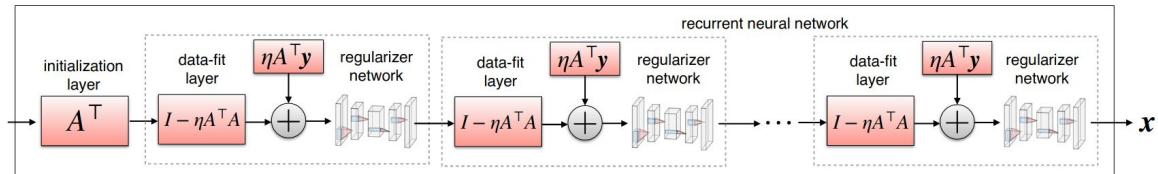


Fig credit: Deep Learning Techniques for Inverse Problems in Imaging <https://arxiv.org/abs/2005.06001>

DL methods: the middle way

Using $\{\mathbf{x}_i\}$ only

$$\min_{\mathbf{x}} \underbrace{\ell(\mathbf{y}, f(\mathbf{x}))}_{\text{data fitting}} + \lambda \underbrace{R(\mathbf{x})}_{\text{regularizer}}$$

Plug-and-Play

$$\mathbf{x}^{k+1} = \mathcal{P}_R(\mathbf{x}^k - \eta \nabla^\top f(\mathbf{x}^k) \ell'(\mathbf{y}, f(\mathbf{x}^k)))$$

E.g. replace \mathcal{P}_R with pretrained denoiser

Deep generative models

Pretraining: $\mathbf{x}_i \approx G_\theta(\mathbf{z}_i) \quad \forall i$

Deployment: $\min_{\mathbf{z}} \ell(\mathbf{y}, f \circ G_\theta(\mathbf{z})) + \lambda R \circ G_\theta(\mathbf{z})$

DL methods: a survey

Deep Learning Techniques for Inverse Problems in Imaging

Gregory Ongie,^{*} Ajil Jalal,[†] Christopher A. Metzler[‡]
Richard G. Baraniuk,[§] Alexandros G. Dimakis,[¶] Rebecca Willett^{||}

April 2020

Abstract

Recent work in machine learning shows that deep neural networks can be used to solve a wide variety of inverse problems arising in computational imaging. We explore the central prevailing themes of this emerging area and present a taxonomy that can be used to categorize different problems and reconstruction methods. Our taxonomy is organized along two central axes: (1) whether or not a forward model is known and to what extent it is used in training and testing, and (2) whether or not the learning is supervised or unsupervised, i.e., whether or not the training relies on access to matched ground truth image and measurement pairs. We also discuss the tradeoffs associated with these different reconstruction approaches, caveats and common failure modes, plus open problems and avenues for future work.

Focuses on **linear** inverse problems,
i.e., f linear

<https://arxiv.org/abs/2005.06001>

Limitations of middle ways:

- Representative data?
- Algorithm-sensitive
- Good initialization? (e.g., Manekar et al. **Deep Learning Initialized Phase Retrieval**.
<https://sunju.org/pub/NIPS20-WS-DL4F-PR.pdf>)

DL methods: the **economic (radical)** way

Deep image prior (DIP) $\mathbf{x} \approx G_\theta(\mathbf{z})$ G_θ (and \mathbf{z}) trainable

$$\min_{\mathbf{x}} \underbrace{\ell(\mathbf{y}, f(\mathbf{x}))}_{\text{data fitting}} + \lambda \underbrace{R(\mathbf{x})}_{\text{regularizer}}$$

No extra training data!

$$\min_{\theta} \ell(\mathbf{y}, f \circ G_\theta(\mathbf{z})) + \lambda R \circ G_\theta(\mathbf{z})$$

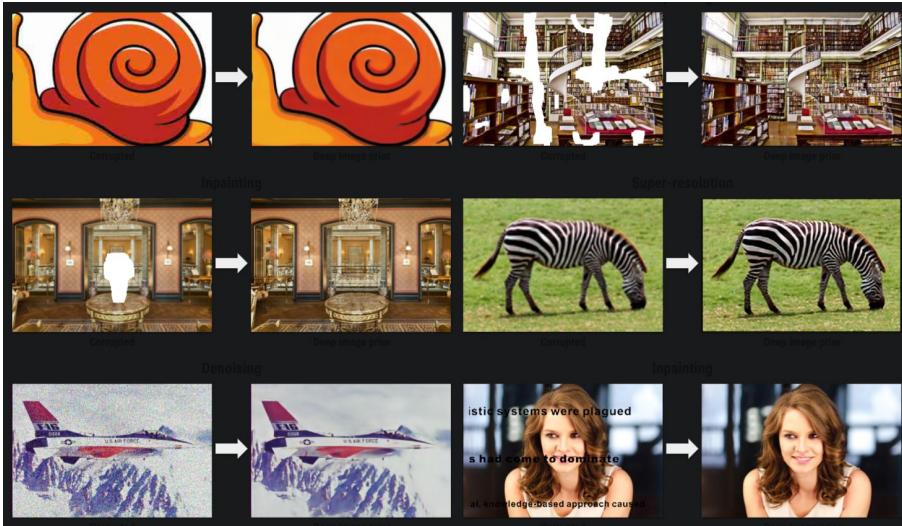
Ulyanov et al. **Deep image prior**. IJCV'20. <https://arxiv.org/abs/1711.10925>

Contrasting: Deep generative models

Pretraining: $\mathbf{x}_i \approx G_\theta(\mathbf{z}_i) \quad \forall i$

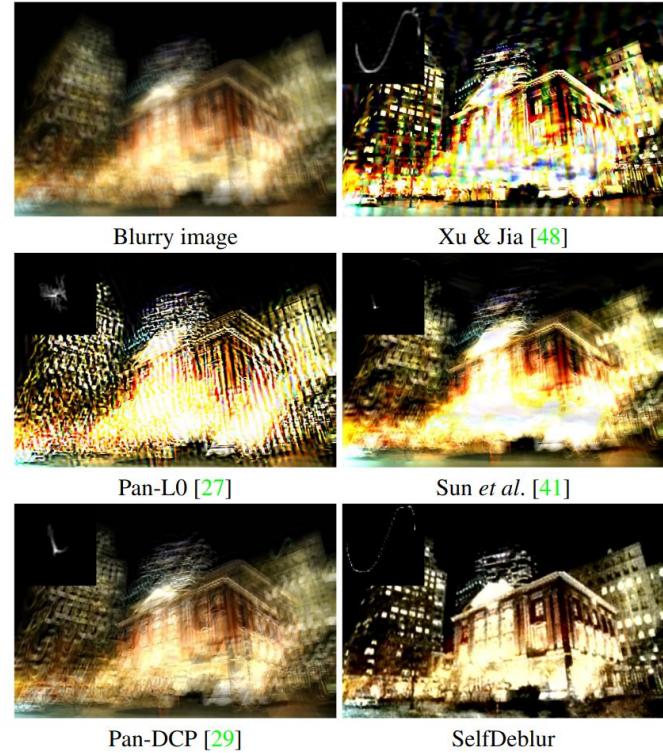
Deployment: $\min_{\mathbf{z}} \ell(\mathbf{y}, f \circ G_\theta(\mathbf{z})) + \lambda R \circ G_\theta(\mathbf{z})$

Successes of DIP



denoising/inpainting/super-resol/deJPEG/...

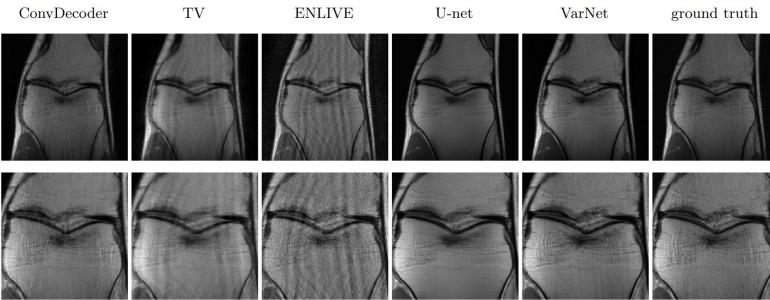
https://dmitryulyanov.github.io/deep_image_prior



Blind image deblurring (blind deconvolution)

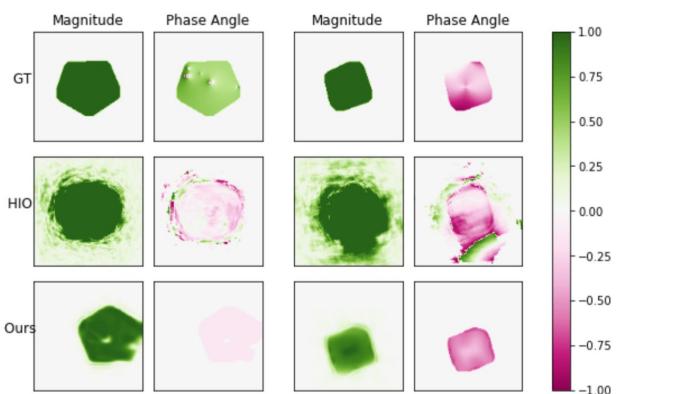
Ren et al. **Neural Blind Deconvolution Using Deep Priors**. CVPR'20. <https://arxiv.org/abs/1908.02197>

Zhuang et al. **Blind Image Deblurring with Unknown Kernel Size and Substantial Noise**. <https://arxiv.org/abs/2208.09483>



MRI reconstruction

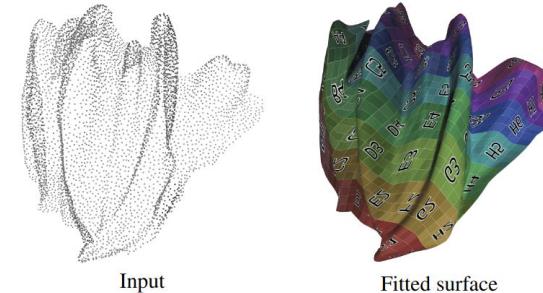
Darestani and Heckel. **Accelerated MRI with Un-trained Neural Networks.** <https://arxiv.org/abs/2007.02471> (ConvDecoder is a variant of DIP)



Phase retrieval

Tayal et al. **Phase Retrieval using Single-Instance Deep Generative Prior.** <https://arxiv.org/abs/2106.04812>

Zhuang et al. **Practical Phase Retrieval Using Double Deep Image Priors.** <https://arxiv.org/abs/2211.00799>



Surface reconstruction

Williams et al. **Deep Geometric Prior for Surface Reconstruction.** CVPR'19. <https://arxiv.org/abs/1811.10943>

Many others:

- PET reconstruction
- Audio denoising
- Time series

See recent survey

Oayyum et al. **Untrained neural network priors for inverse imaging problems: A survey.** T-PAMI'22.

<https://ieeexplore.ieee.org/document/9878048>

Deep image prior (DIP)

DIP's cousin(s)

$$\mathbf{x} \approx G_\theta(\mathbf{z}) \quad G_\theta \text{ (and } \mathbf{z} \text{) trainable}$$

Idea: (visual) objects as continuous functions

Neural implicit representation (NIR)

$$\mathbf{x} \approx \mathcal{D} \circ \bar{\mathbf{x}} \quad \mathcal{D} : \text{discretization} \quad \bar{\mathbf{x}} : \text{continuous function}$$

Physics-informed neural networks (PINN)

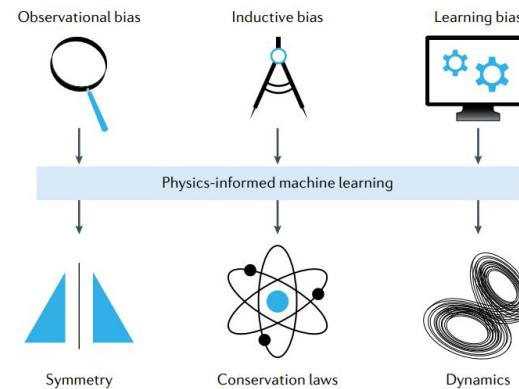
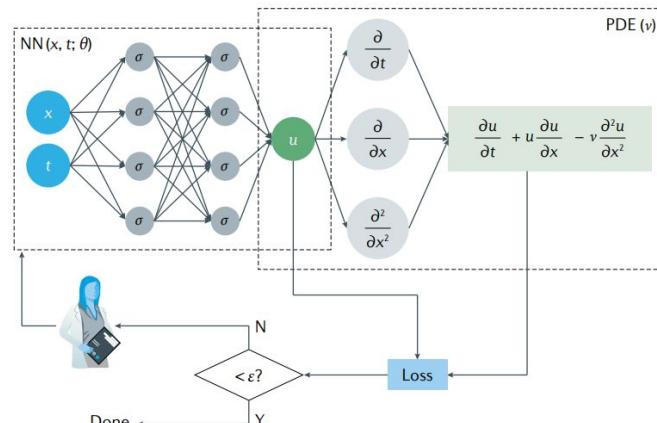
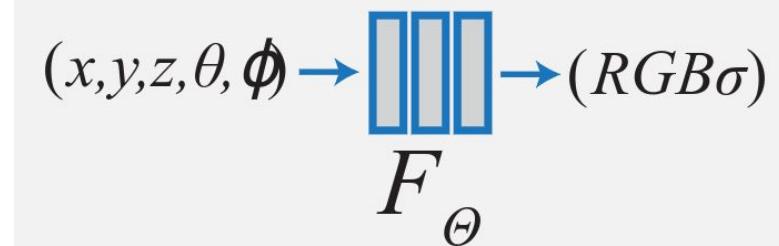
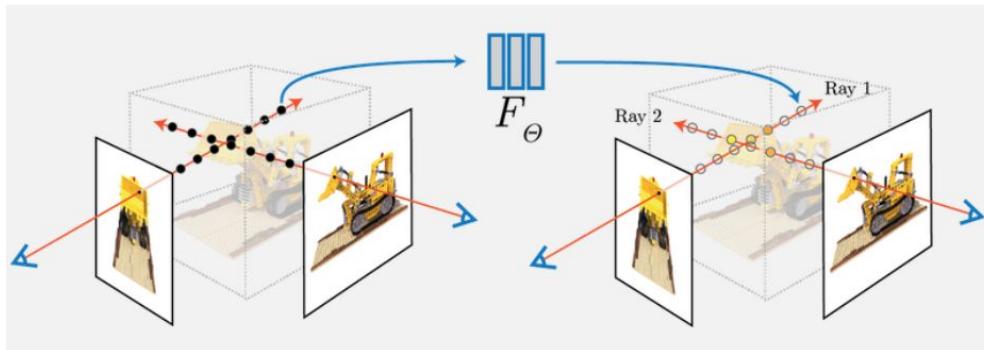
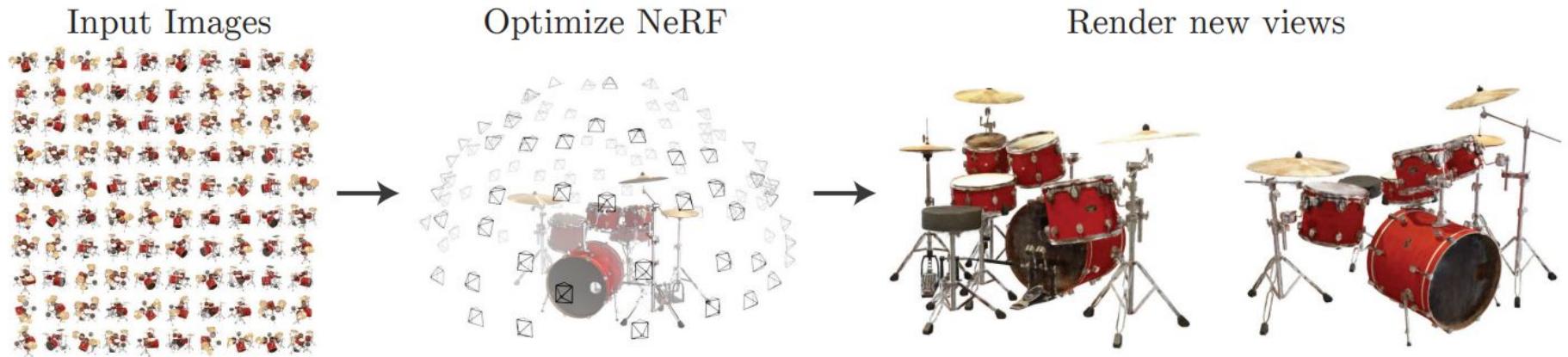


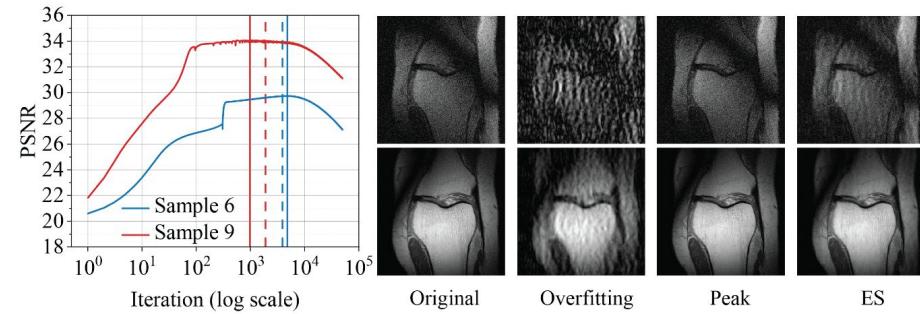
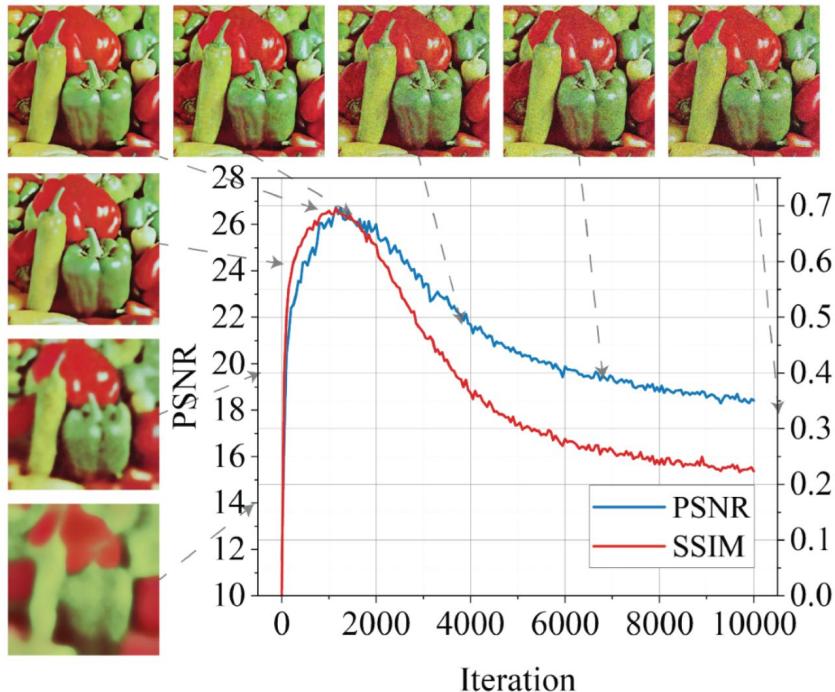
Figure credit: <https://www.nature.com/articles/s42254-021-00314-5>

NIR for 3D rendering and view synthesis



<https://www.matthewtancik.com/nerf>

Practical issues around DIP (and its cousin)



- 1) Early learning then overfitting (ELTO)
- 2) Slow in convergence
- 3) Which G_θ ?
- 4) ...

This talk

- Tackle early-learning-then-overfitting (ELTO) by **early stopping**
 - Li et al. **Self-Validation: Early Stopping for Single-Instance Deep Generative Priors** (BMVC'21)
<https://arxiv.org/abs/2110.12271>
 - Wang et al. **Early Stopping for Deep Image Prior** <https://arxiv.org/abs/2112.06074>
- **Practical** blind image deblurring (BID) /**Practical** phase retrieval (PR)
 - Zhuang et al. **Blind Image Deblurring with Unknown Kernel Size and Substantial Noise.**
<https://arxiv.org/abs/2208.09483>
 - Zhuang et al. **Practical Phase Retrieval Using Double Deep Image Priors.**
<https://arxiv.org/abs/2211.00799>
- Toward **fast** computation for DIP
 - Li et al. **Deep Random Projector: Accelerated Deep Image Prior**. Submitted to CVPR'23.

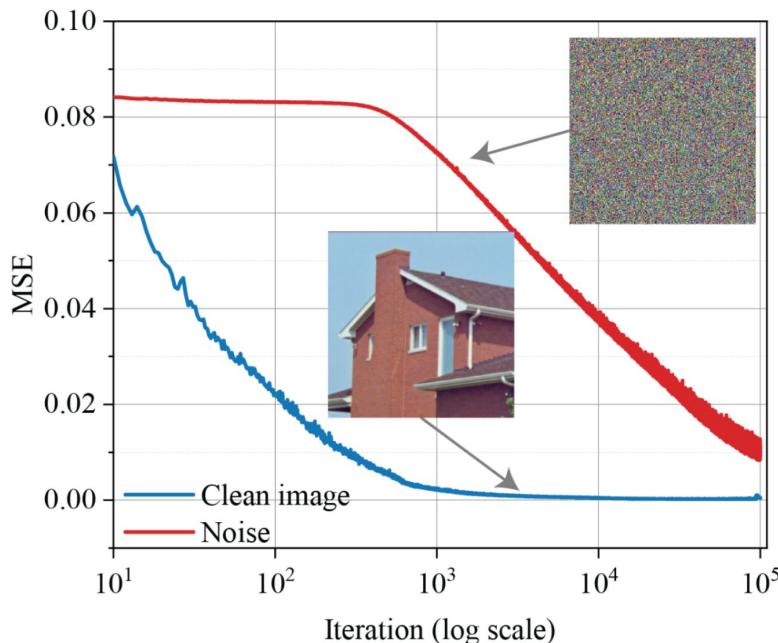
Early stopping for ELTO

- Li et al. **Self-Validation: Early Stopping for Single-Instance Deep Generative Priors** (BMVC'21) <https://arxiv.org/abs/2110.12271>
- Wang et al. **Early Stopping for Deep Image Prior** <https://arxiv.org/abs/2112.06074>

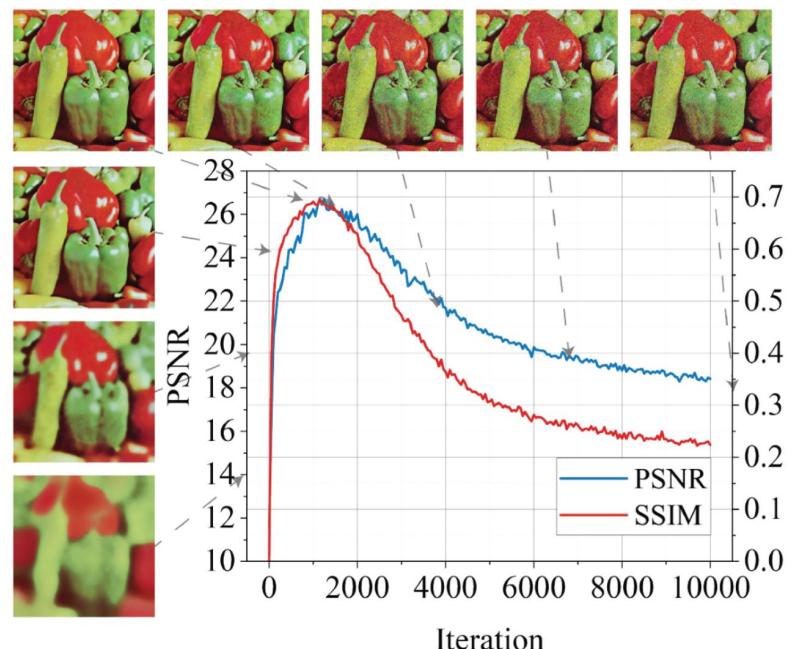
Why early-learning-then-overfitting (ELTO)?

$$\min_{\theta} \ell(\mathbf{y}, f \circ G_{\theta}(\mathbf{z}))$$

DIP learns signal **much faster than** learning noise



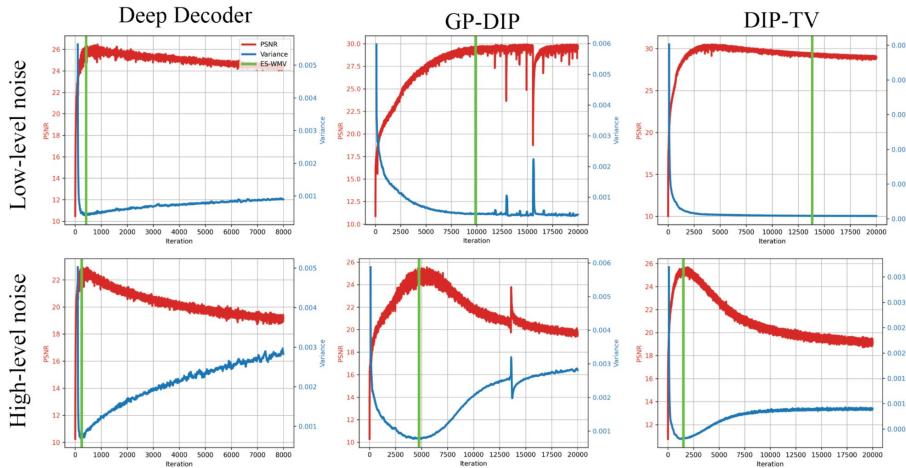
In practice, DIP heavily **over-parameterized**



Tackling ELTO via regularization

$$\min_{\theta} \ell(\mathbf{y}, f \circ G_{\theta}(\mathbf{z}))$$

- Regularize the network G_{θ}
- Regularize the estimation $G_{\theta}(\mathbf{z})$, i.e., bringing back $R \circ G_{\theta}(\mathbf{z})$



[Keckel & Hand'18]

[Cheng et al'19]

[Liu et al'18]

Cons: right regularization levels?

Detailed references: <https://arxiv.org/abs/2112.06074>

Tackling ELTO via noise modeling

- Noise modeling
 - Noise-specific regularizer
 - Explicit noise term

Double Over-parameterization:

$$\min_{\theta, \mathbf{g}, \mathbf{h}} \|\mathbf{y} - \phi(\theta) - (\mathbf{g} \circ \mathbf{g} - \mathbf{h} \circ \mathbf{h})\|_F^2$$

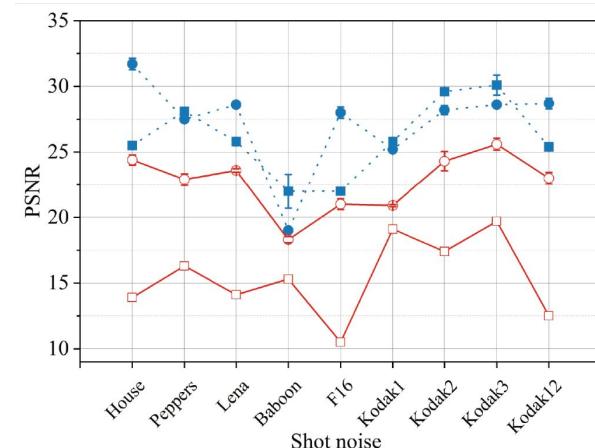
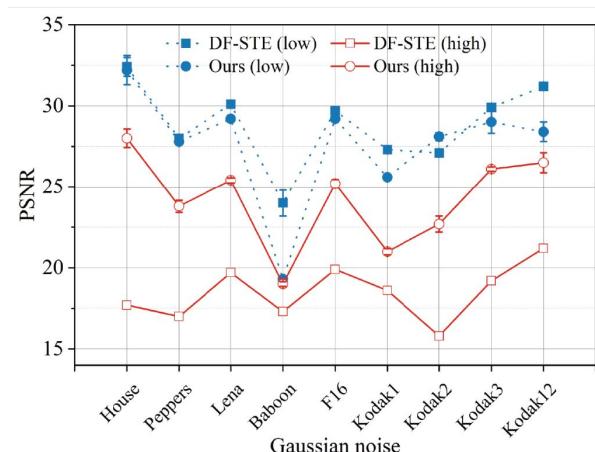
[You et al'20]

Rethinking DIP for denoising:

$$\eta(\mathbf{h}(\mathbf{y}), \mathbf{y}) = \mathcal{L}(\mathbf{y}, \mathbf{h}(\mathbf{y})) + \underbrace{\frac{2\sigma^2}{N} \sum_{i=1}^N \frac{\partial \mathbf{h}_i(\mathbf{y})}{\partial (\mathbf{y})_i}}_{\text{divergence term}} - \sigma^2$$

[Jo et al'21]

Cons: need detailed noise info

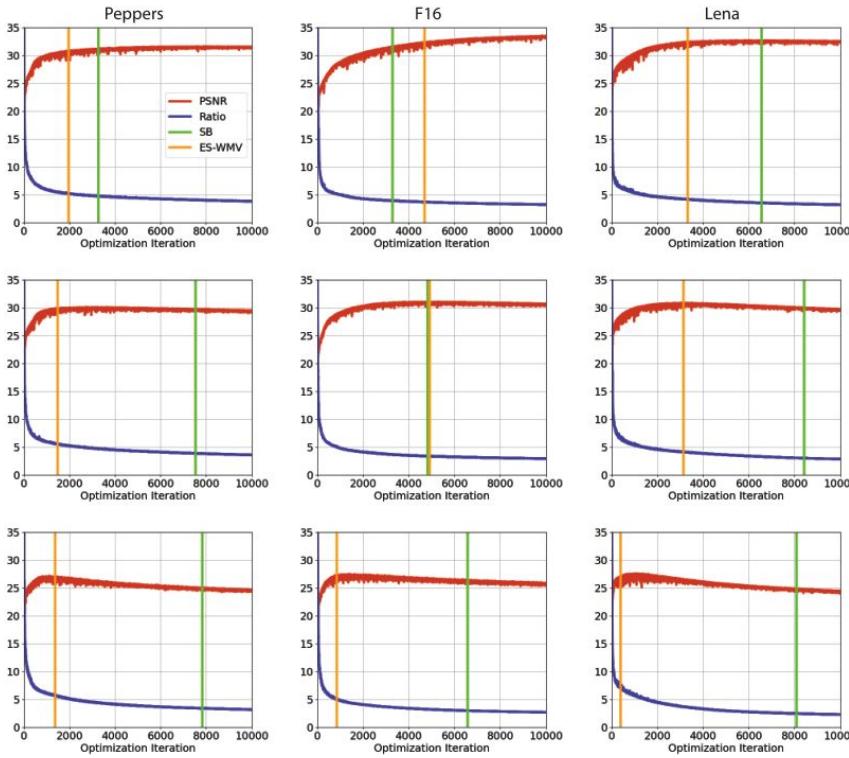


Detailed references: <https://arxiv.org/abs/2112.06074>

Tackling ELTO via early stopping

Cons: model- or noise-specific

[Shi et al'21]

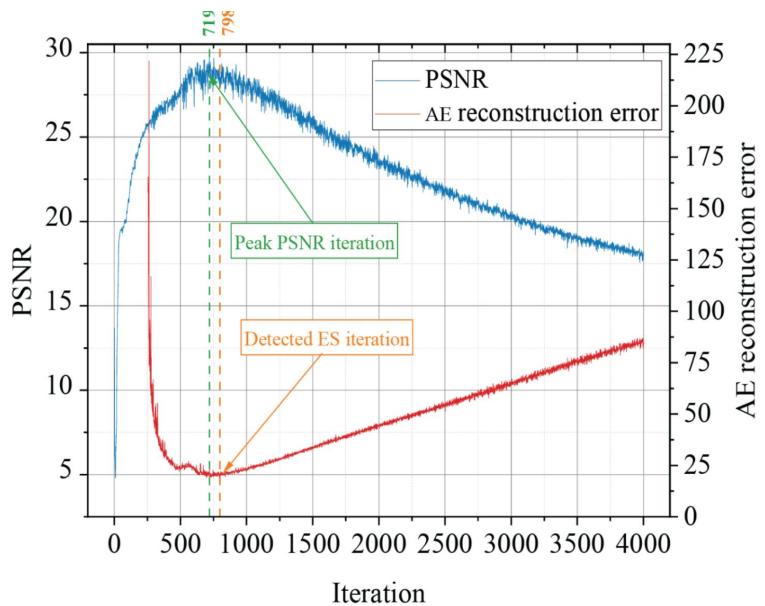


On Measuring and Controlling
the Spectral Bias of the Deep
Image Prior.

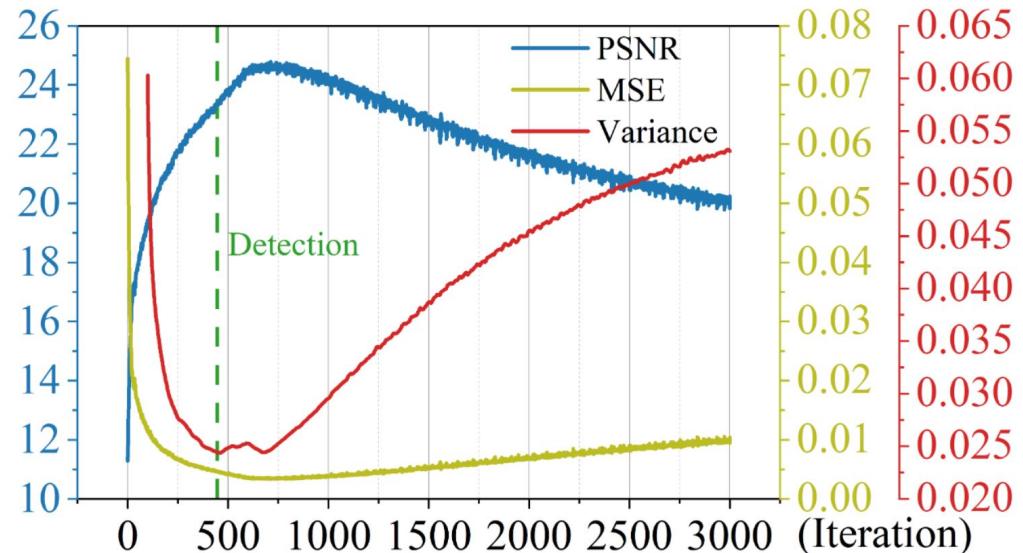
<https://link.springer.com/article/10.1007/s11263-021-01572-7>

Detailed references: <https://arxiv.org/abs/2112.06074>

An interesting observation



ES Ver 1.0: based on autoencoder Rec Err



ES Ver 2.0: based on running variance

ES base on moving variance (MV)

Algorithm 1 DIP with ES-WMV

Input: random seed \mathbf{z} , randomly-initialized G_θ , window size W , patience number P , empty queue \mathcal{Q} , iteration counter $k = 0$

Output: reconstruction \mathbf{x}^*

```

1: while not stopped do
2:   update  $\theta$  via Eq. (2) to obtain  $\theta^{k+1}$  and  $\mathbf{x}^{k+1}$ 
3:   push  $\mathbf{x}^{k+1}$  to  $\mathcal{Q}$ , pop queue front if  $|\mathcal{Q}| > W$ 
4:   if  $|\mathcal{Q}| = W$  then
5:     calculate VAR of elements in  $\mathcal{Q}$ 
6:     update  $\text{VAR}_{\min}$  and the corresponding  $\mathbf{x}^*$ 
7:     if no decrease of  $\text{VAR}_{\min}$  in  $P$  consecutive iterations
       then
8:       stop and return  $\mathbf{x}^k$ 
9:     end if
10:   end if
11:    $k = k + 1$ 
12: end while

```

Algorithm 2 DIP with ES-EMV

Input: random seed \mathbf{z} , randomly-initialized G_θ , forgetting factor $\alpha \in (0, 1)$, patience number P , iteration counter $k = 0$, $\text{EMA}^0 = 0$, $\text{EMV}^0 = 0$,

Output: reconstruction \mathbf{x}^*

```

1: while not stopped do
2:   update  $\theta$  via Eq. (2) to obtain  $\theta^{k+1}$  and  $\mathbf{x}^{k+1}$ 
3:    $\text{EMA}^{k+1} = (1 - \alpha)\text{EMA}^k + \alpha\mathbf{x}^{k+1}$ 
4:    $\text{EMV}^{k+1} = (1 - \alpha)\text{EMV}^k + \alpha(1 - \alpha)\|\mathbf{x}^{k+1} - \text{EMA}^k\|_2^2$ 
5:   update  $\text{EMV}_{\min}$  and the corresponding  $\mathbf{x}^*$ 
6:   if no decrease of  $\text{EMV}_{\min}$  in  $P$  consecutive iterations then
7:     stop and return  $\mathbf{x}^k$ 
8:   end if
9:    $k = k + 1$ 
10: end while

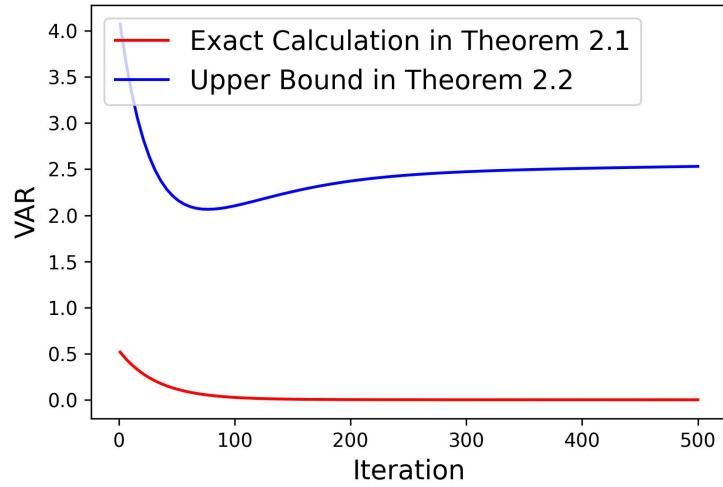
```

Table 5. Wall-clock time of DIP, SV-ES, ES-WMV and ES-EMV per epoch on *NVIDIA Tesla K40 GPU*: mean and (std).

	DIP	SV-ES	ES-WMV	ES-EMV
Time(secs)	0.448 (0.030)	13.027 (3.872)	0.301 (0.016)	0.003 (0.003)

Very little overhead

A bit of justification



Theorem 2.1. Let σ_i 's and w_i 's be the singular values and left singular vectors of $J_G(\theta^0)$, and suppose we run gradient descent with step size η on the linearized objective $\hat{f}(\theta)$ to obtain $\{\theta^t\}$ and $\{x^t\}$ with $x^t \doteq G_{\theta^0}(z) + J_G(\theta^0)(\theta^t - \theta^0)$. Then provided that $\eta \leq 1/\max_i(\sigma_i^2)$, the running variance of $\{x^t\}$ is

$$\text{DISP}_2^2(t) = \sum_i C_{m,\eta,\sigma_i} \langle w_i, \hat{y} \rangle^2 (1 - \eta\sigma_i^2)^{2t}, \quad (7)$$

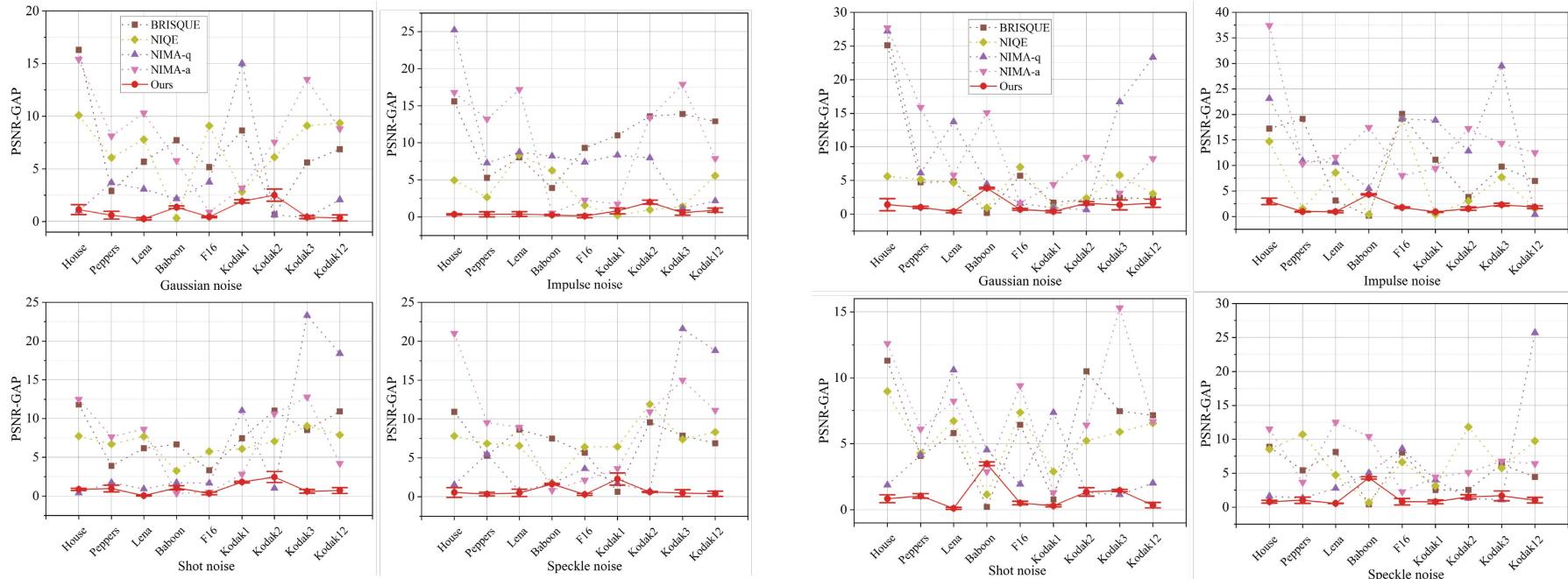
where $\hat{y} = y - G_{\theta^0}(z)$, and $C_{W,\eta,\sigma_i} \geq 0$ only depends on W , η , and σ_i for all i .

Theorem 2.2. Assume the same setting as Theorem 2 of [16]. Our WMV is upper bounded by

$$\begin{aligned} & \frac{12}{W} \|x\|_2^2 \frac{(1 - \eta\sigma_p^2)^{2t}}{1 - (1 - \eta\sigma_p^2)^2} + \\ & 12 \sum_{i=1}^n \left((1 - \eta\sigma_i^2)^{t+W-1} - 1 \right)^2 (w_i^\top n)^2 + 12\varepsilon^2 \|y\|_2^2. \end{aligned}$$

with high probability.

Effective across types\levels of noise



High-Level

Low-Level

Typical detection gap: around 1 PSNR point

Effective on real-world denoising

NTIRE 2020 Real Image Denoising Challenge (RGB track) for **1024** Images

- Unknown noise types and levels

Table 7. ES-WMV on real image denoising: mean and (std).

	Detected PSNR	PSNR Gap	Detected SSIM	SSIM Gap
DIP (MSE)	34.04 (3.68)	0.92 (0.83)	0.92 (0.07)	0.02 (0.04)
DIP (ℓ_1)	33.92 (4.34)	0.92 (0.59)	0.93 (0.05)	0.02 (0.02)
DIP (Huber)	33.72 (3.86)	0.95 (0.73)	0.92 (0.06)	0.02 (0.03)

Effective on advanced tasks

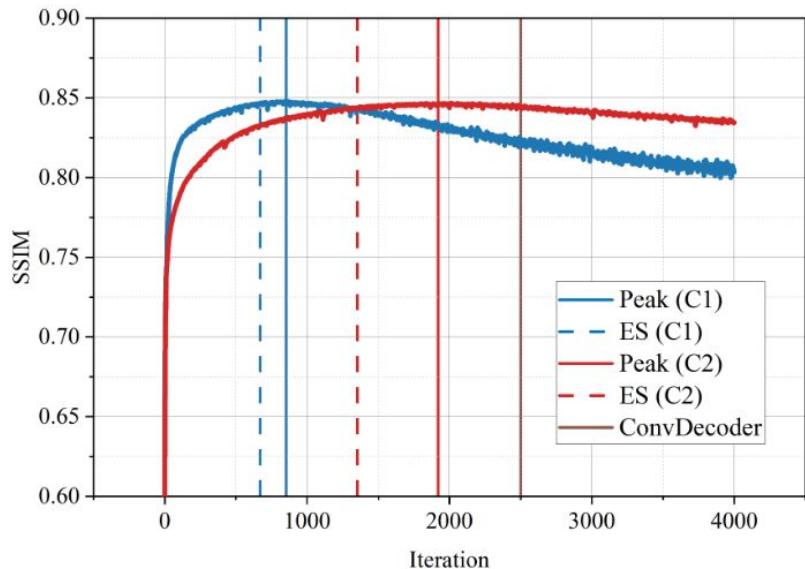
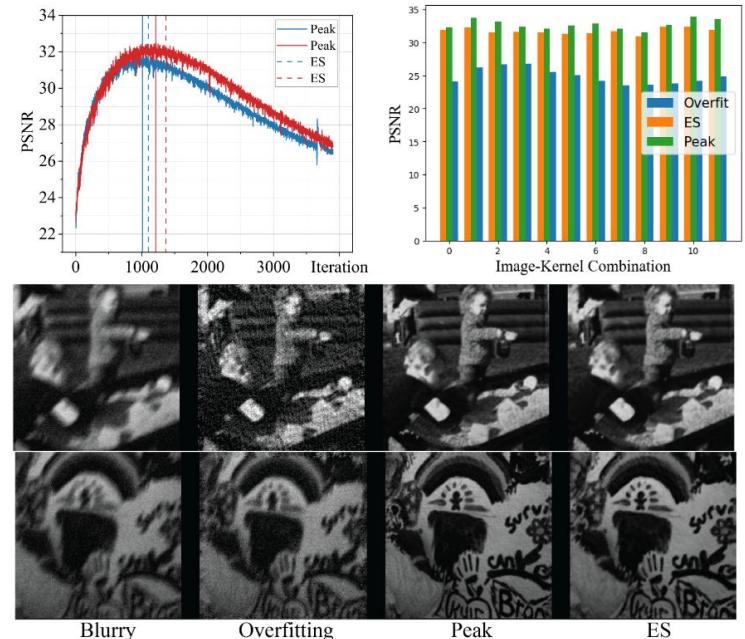


Figure 5. Detection performance on MRI reconstruction



Code available at: https://github.com/sun-umn/Early_Stopping_for_DIP

Toward practical blind image deblurring

- Zhuang et al. **Blind Image Deblurring with Unknown Kernel Size and Substantial Noise.** <https://arxiv.org/abs/2208.09483>

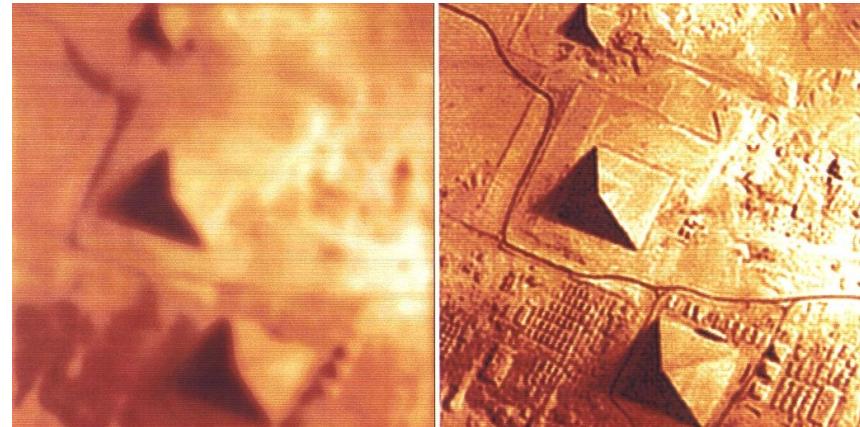
Blind image deblurring (BID)

$$\underbrace{\mathbf{y}}_{\text{blurry and noisy image}} = \overbrace{\mathbf{k}}^{\text{blur kernel}} * \underbrace{\mathbf{x}}_{\text{clean image}} + \overbrace{\mathbf{n}}^{\text{noise}}$$

Mostly due to optical deficiencies (e.g., defocus) and motions

Given \mathbf{y} ,
recover \mathbf{x} (and/or \mathbf{k})

Also **Blind Deconvolution**



Landmark surveys

- 1996: Kundur and Hatzinakos. **Blind image deconvolution.** <https://doi.org/10.1109/79.489268>
- 2011: Levin et al. **Understanding blind deconvolution algorithms.** <https://doi.org/10.1109/TPAMI.2011.148>
- 2012: Kohler et al. **Recording and playback of camera shake: Benchmarking blind deconvolution with a real-world database.** https://doi.org/10.1007/978-3-642-33786-4_3
- 2016: Lai et al. **A comparative study for single image blind deblurring.** <https://doi.org/10.1109/CVPR.2016.188>
- 2021: Koh et al. **Single image deblurring with neural networks: A comparative survey** <https://doi.org/10.1016/j.cviu.2020.103134>
- 2022: Zhang et al. **Deep image blurring: A survey** <https://doi.org/10.1007/s11263-022-01633-5>

See also: **Awesome Deblurring**

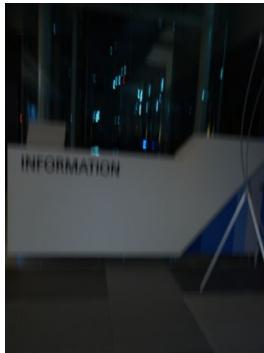
<https://github.com/subeeshvasu/Awesome-Deblurring>

Key challenge of data-driven approach:

obtaining sufficiently expressive data (Koh et al'21. Zhang et al'22)

Practicality challenges

- 1) Unknown kernel size
- 2) Substantial noise
- 3) Model stability



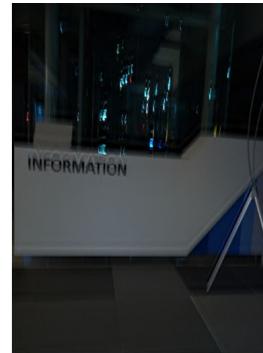
Blurry Image



Sun13



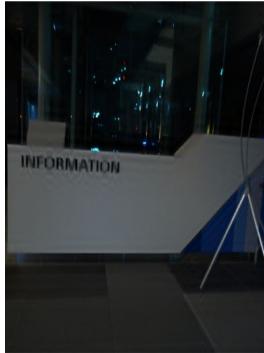
Pan16



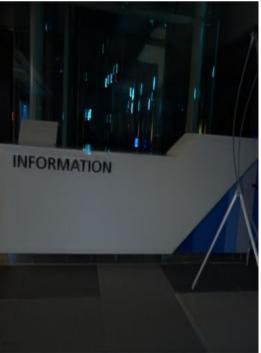
Xu13



SelfDeblur



Dong17



SRN



DeblurGAN-v2



Zhang20



Our

Double DIPs

$$\underbrace{\mathbf{y}}_{\text{blurry and noisy image}} = \underbrace{\mathbf{k}}_{\text{blur kernel}} * \underbrace{\mathbf{x}}_{\text{clean image}} + \underbrace{\mathbf{n}}_{\text{noise}}$$

$$\min_{\mathbf{k}, \mathbf{x}} \underbrace{\ell(\mathbf{y}, \mathbf{k} * \mathbf{x})}_{\text{data fitting}} + \lambda_k \underbrace{R_{\mathbf{k}}(\mathbf{k})}_{\text{regularizing } \mathbf{k}} + \lambda_x \underbrace{R_{\mathbf{x}}(\mathbf{x})}_{\text{regularizing } \mathbf{x}}$$

Idea: parameterize both \mathbf{k} and \mathbf{x} as DIPs

- CNN + CNN (Wang et al'19, <https://doi.ieeecomputersociety.org/10.1109/ICCVW.2019.00127>; Tran et al'21, <https://arxiv.org/abs/2104.00317>)
- MLP + CNN (SelfDeblur; Ren et al'20, <https://arxiv.org/abs/1908.02197>)

Still problematic with

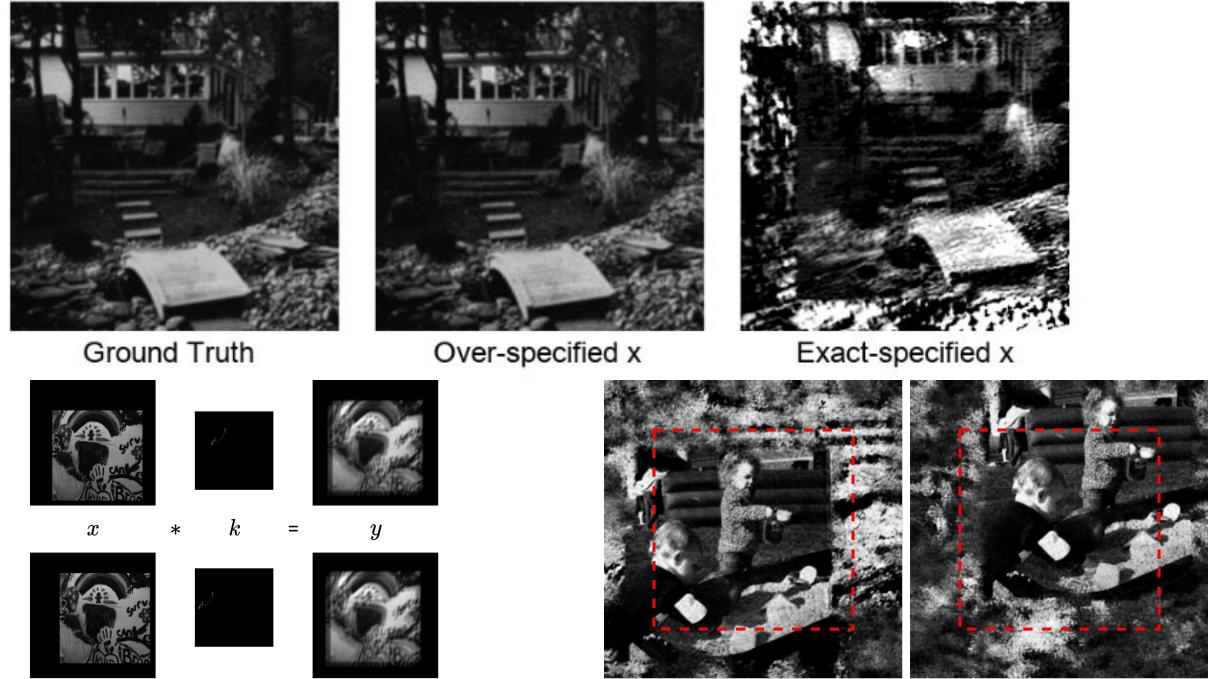
- 1) kernel size over-specification
- 2) substantial noise

A glance of our modifications

Over-specify k
Over-specify x

$k \sim$ half of the image sizes

Handle bounded shift



$$\min_{\theta_k, \theta_x} \|y - G_{\theta_k}(z_k) * G_{\theta_x}(z_x)\|_2^2 + \lambda \frac{\|\nabla G_{\theta_x}(z_x)\|_1}{\|\nabla G_{\theta_x}(z_x)\|_2}$$

ℓ_1/ℓ_2 vs ℓ_1

Table 1: ℓ_1/ℓ_2 vs TV for noise: mean and (std).

	Low Level		High Level	
	PSNR	λ	PSNR	λ
$\frac{L_1}{L_2}$	32.64 (0.69)	0.0001 (0.018)	27.74 (0.23)	0.0002 (0.0019)
TV	31.12 (0.52)	0.002 (0.07)	24.34 (0.78)	0.02 (0.10)

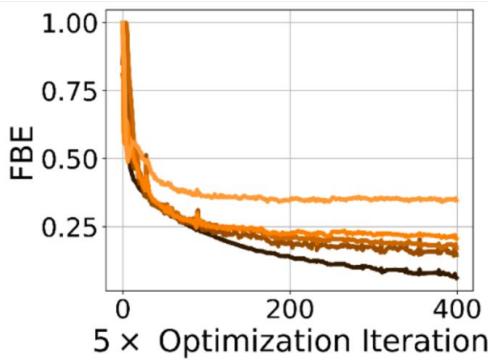
A glance of our modifications (continue)

— Frequency band (1,lowest)
— Frequency band (2)

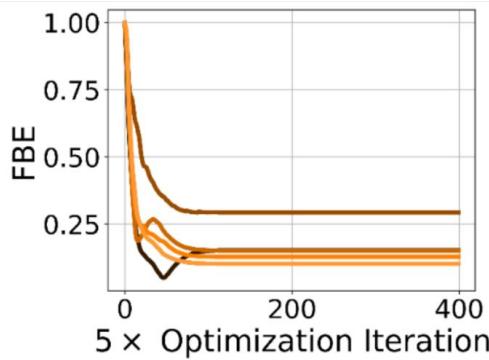
— Frequency band (3)
— Frequency band (4)

— Frequency band (5, highest)

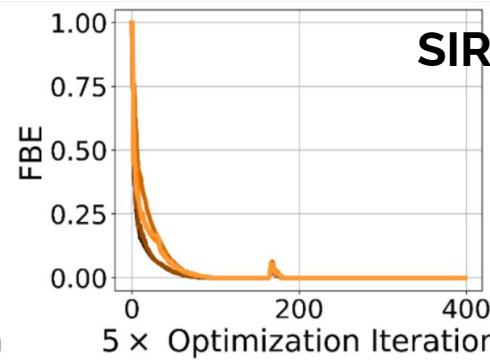
DIP



DIP-MLP

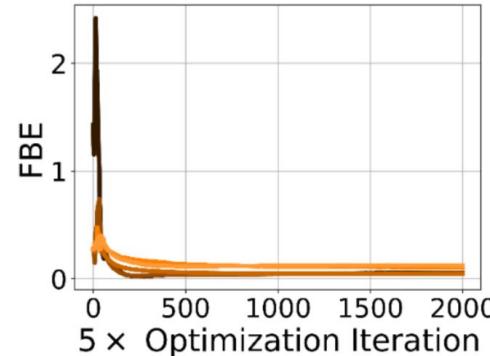
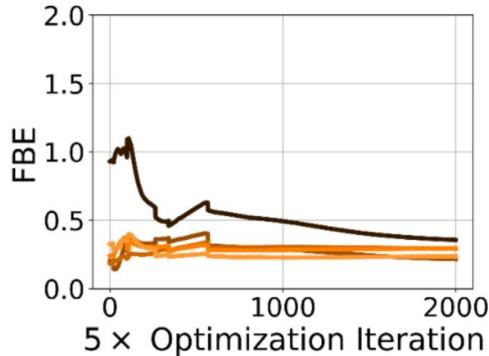
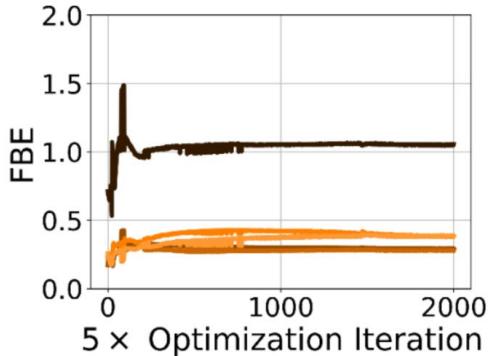


SIREN



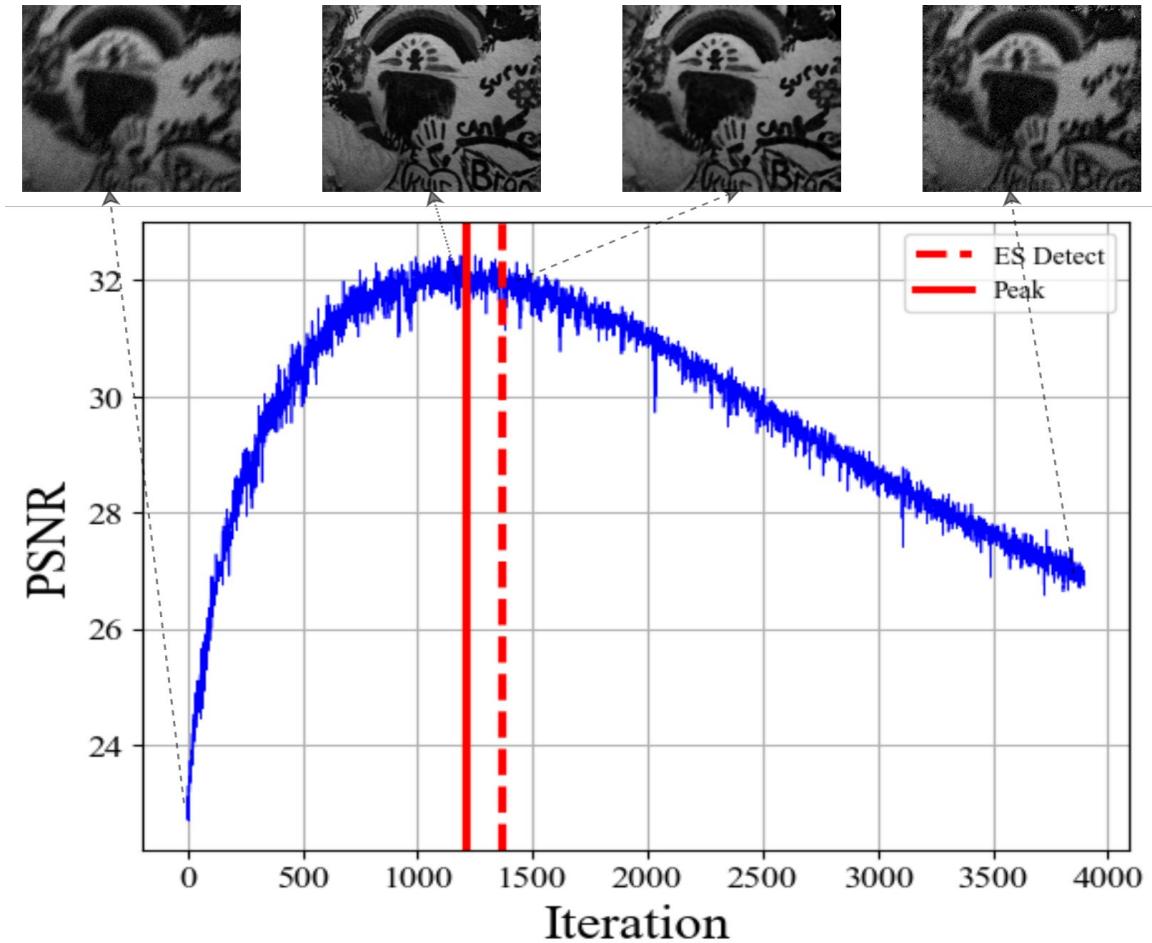
DIP models matter!

SIREN for k!



A glance of our modifications (continue)

- Early Stopping



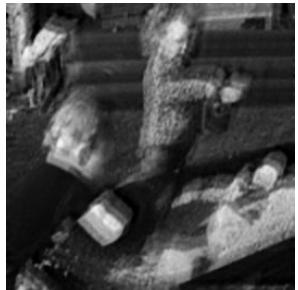
SelfDeblur vs our method



Clean



Blurry and noisy



SelfDeblur



Ours



Clean



Blurry and noisy

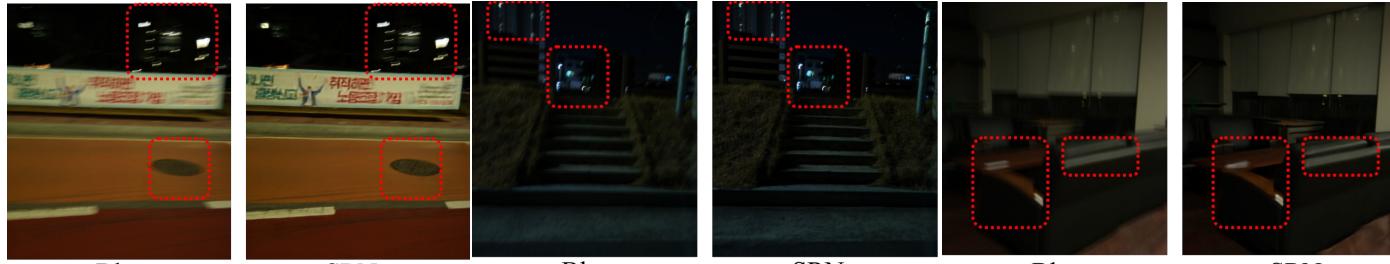


SelfDeblur



Ours

Real world results



Blur

SRN

Blur

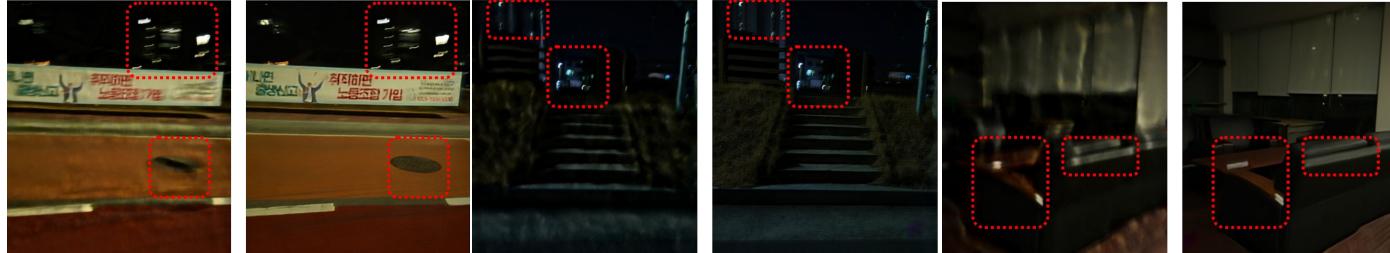
SRN

Blur

SRN

Difficult cases

- 1) High depth contrast
- 2) High brightness contrast



ZHANG20

DeblurGAN-v2

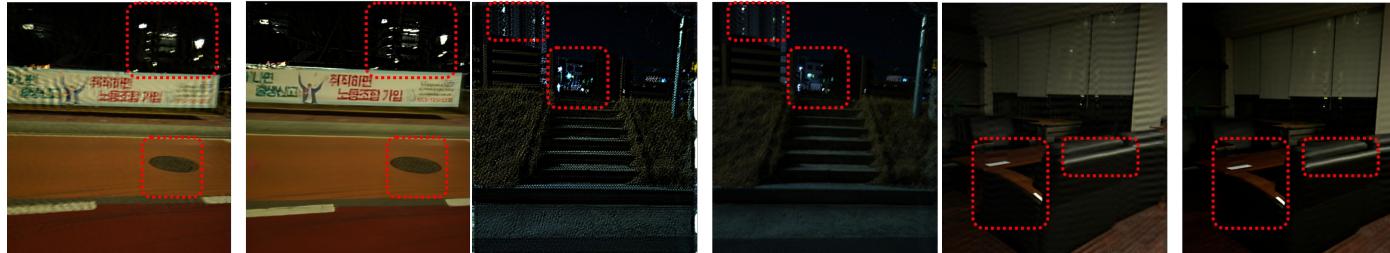
ZHANG20

DeblurGAN-v2

ZHANG20

DeblurGAN-v2

Outperform SOTA
data-driven methods!



SelfDeblur

Our

SelfDeblur

Our

SelfDeblur

Our

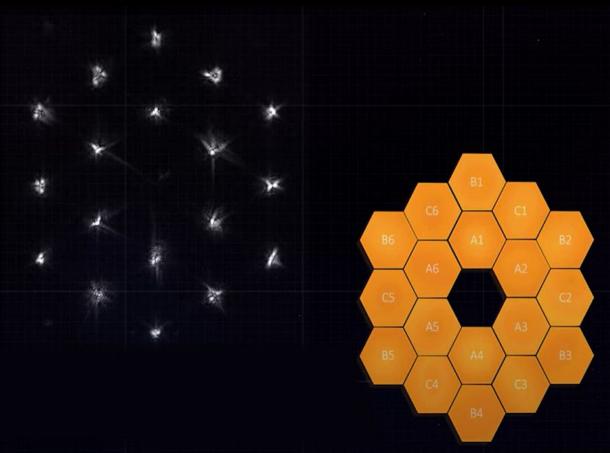
Toward practical phase retrieval

- Zhuang et al. **Practical Phase Retrieval Using Double Deep Image Priors.**
<https://arxiv.org/abs/2211.00799>

Why phase retrieval (PR)?

Phase Retrieval (PR): $Y = |\mathcal{A}(X)|^2$, recover X

Thumbnails



Segment Alignment

Step 2

Nominal Event Time: Starts - Launch + ~2 Months

Status: Completed

After we have the image array, we can perform Segment Alignment, which corrects most of the large positioning errors of the mirror segments.

We begin by defocusing the segment images by moving the secondary mirror slightly. Mathematical analysis, called Phase Retrieval, is applied to the defocused images to determine the precise positioning errors of the segments. Adjustments of the segments then result in 18 well-corrected "telescopes." However, the segments still don't work together as a single mirror.

VIDEO: [First Photons | Step 2 Segment Alignment](#)

READ: [About First Photons | Step 2 Complete](#)

REPLAY: [Media Telecon](#)

WEBB
SPACE TELESCOPE



James Webb telescope

Demo:

<https://webbtelescope.org/news/first-images/gallery/zoomable-image-carina-nebula>

Which phase retrieval?

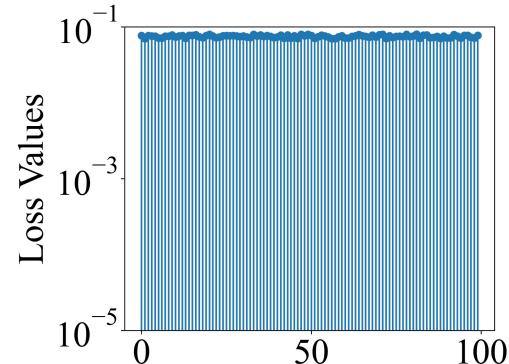
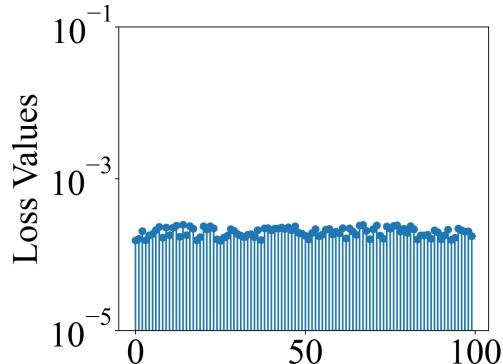
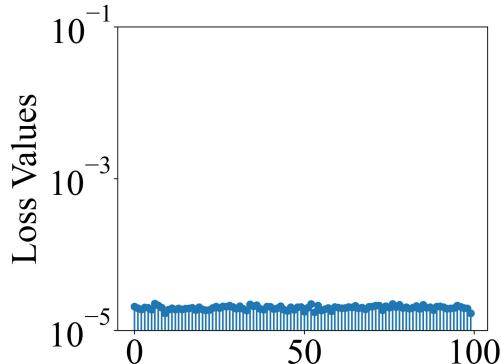
$$Y = |\mathcal{A}(X)|^2 \quad \text{Consider} \quad \min_X \|Y - |\mathcal{A}(X)|^2\|_F^2$$

	Gaussian PR	Fresnel PR	Fraunhofer PR
$\mathcal{A}(X)$	$\{\langle G_i, X \rangle\}_{i=1}^m$	$\mathcal{F}(X) \odot [e^{i\pi C(m^2+n^2)}]_{m,n}$	$\mathcal{F}(X)$
Symmetries	Global phase	Global phase	Shift, flipping, global phase

LS-solvable

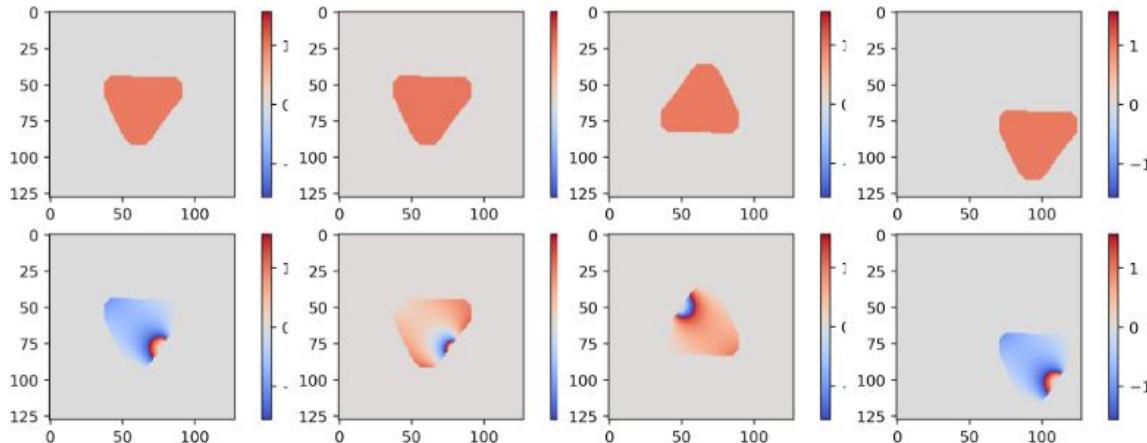
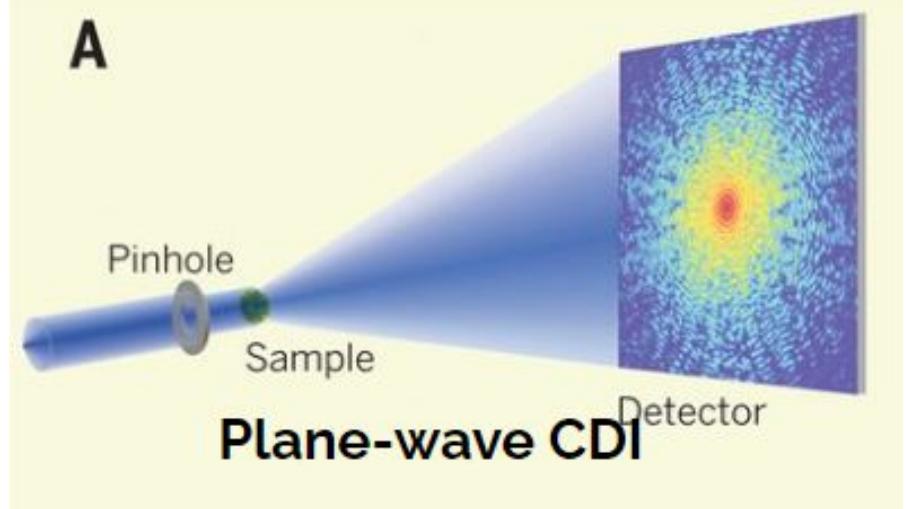


**un LS-solvable
(proliferation of local mins)**



Focus here: plane-wave CDI (Fraunhofer PR)

$$Y = |\mathcal{F}(X)|^2$$



X complex-valued

Three symmetries:

- **global phase**
- **conjugate flipping**
- **shift**

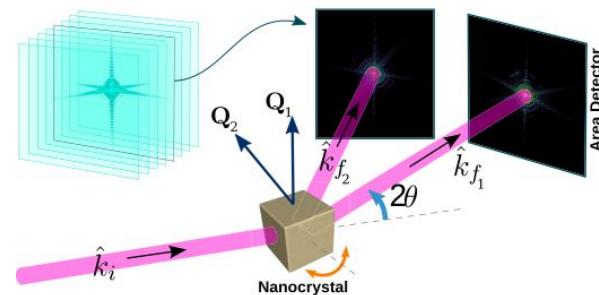
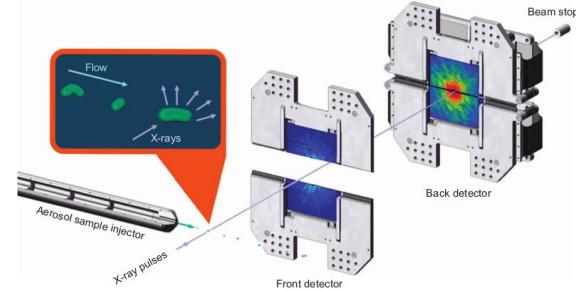
Limitations of SOTA methods on PR

Global issues

- Sensitivity to initial support estimation
- Sensitivity to **multiple hyperparameters** (e.g., **Coherent Diffraction Imaging (CDI)**
HIO+ER+Shrikwrap)
- Low reconstruction quality (e.g., phases with singularities in BCDI)

Local issues

- Beamstop (i.e., missing data)
- Shot noise



Bragg Coherent Diffraction Imaging (BCDI)

Double DIPs

$$\min_{\mathbf{X} \in \mathbb{C}^{n \times n}} \| \mathbf{Y} - |\mathcal{F}(\mathbf{X})|^2 \|_F^2$$

Reparameterizing X using two DIPs

$$\mathbf{X} = \mathbf{X}^{mag} e^{1j * \mathbf{X}^{phase}} = G_{\theta_1}^{mag}(z_1) e^{1j * G_{\theta_2}^{phase}(z_2)}$$

e.g., for BCDI on crystals, **magnitude known to be uniform**

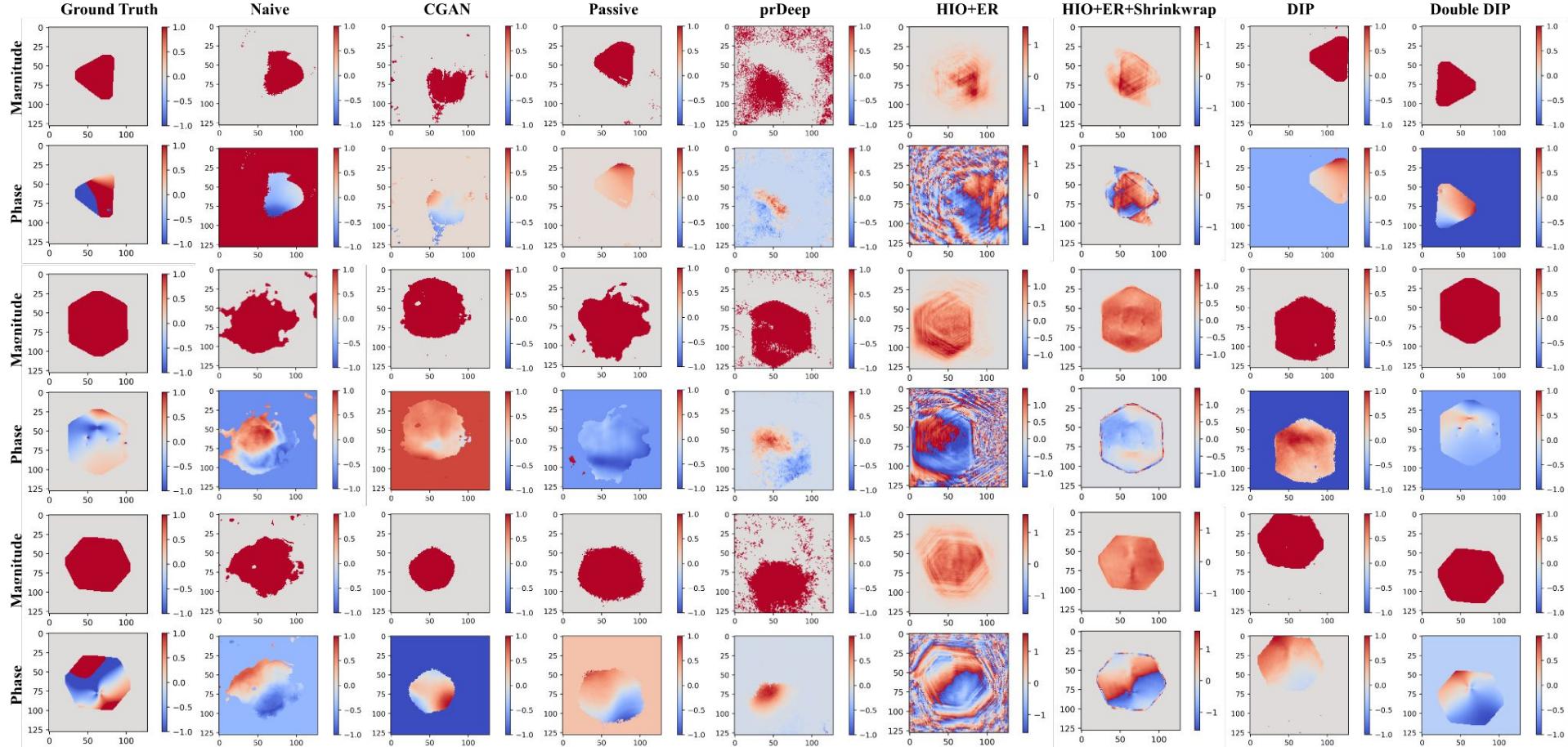
OR $\mathbf{X} = \mathbf{X}^{real} + 1j * \mathbf{X}^{imag} = G_{\theta_1}^{real}(z_1) + 1j * G_{\theta_2}^{imag}(z_2)$

e.g., for CDI on certain bio-specimen, real part **known to be nonnegative**

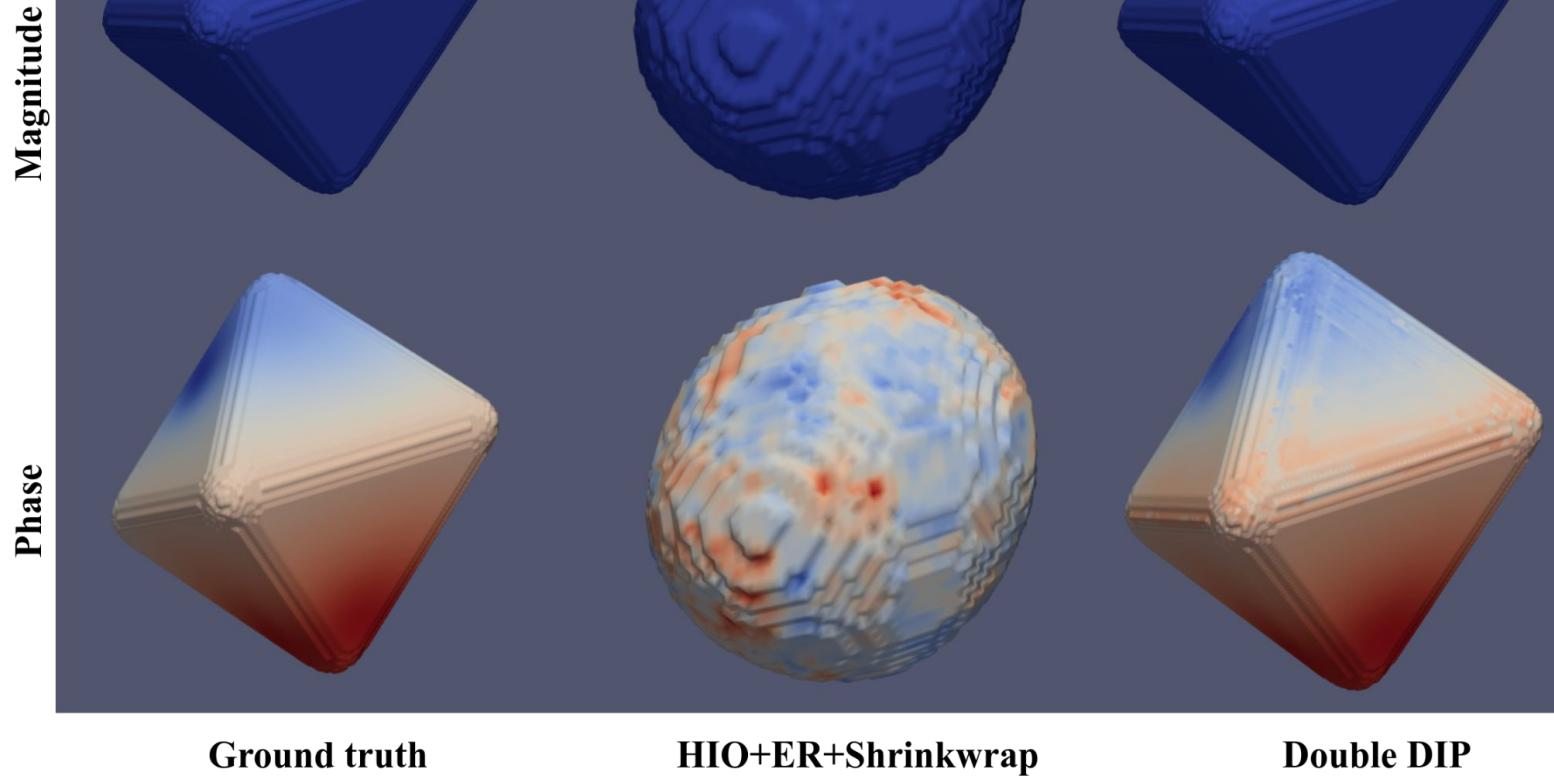
X half of the size of Y in any dimension: no tight support needed, and information-theoretic limit

Results on 2D simulated data

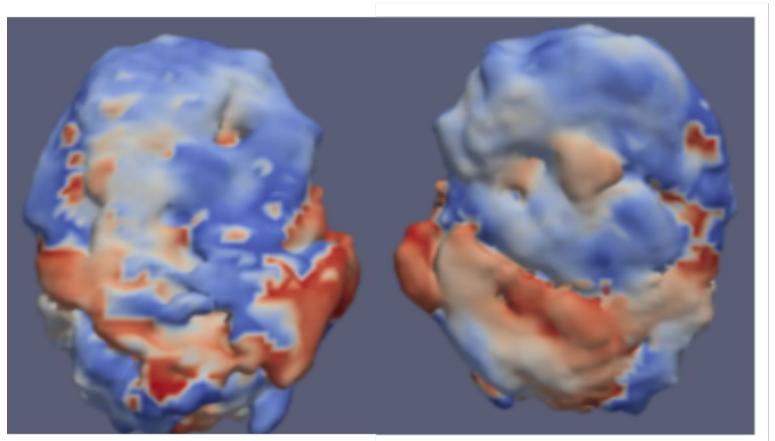
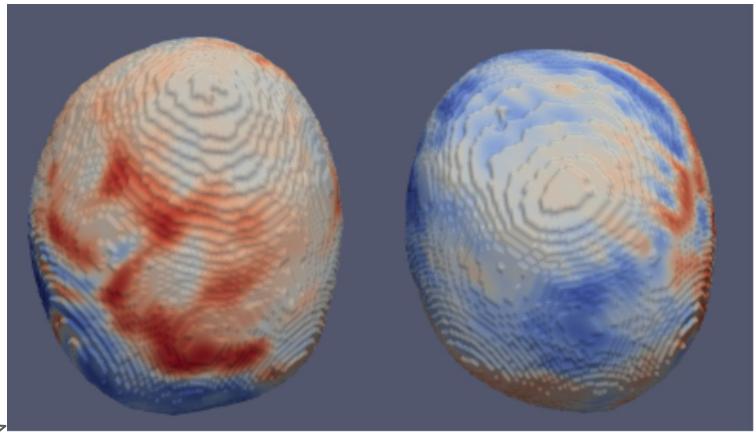
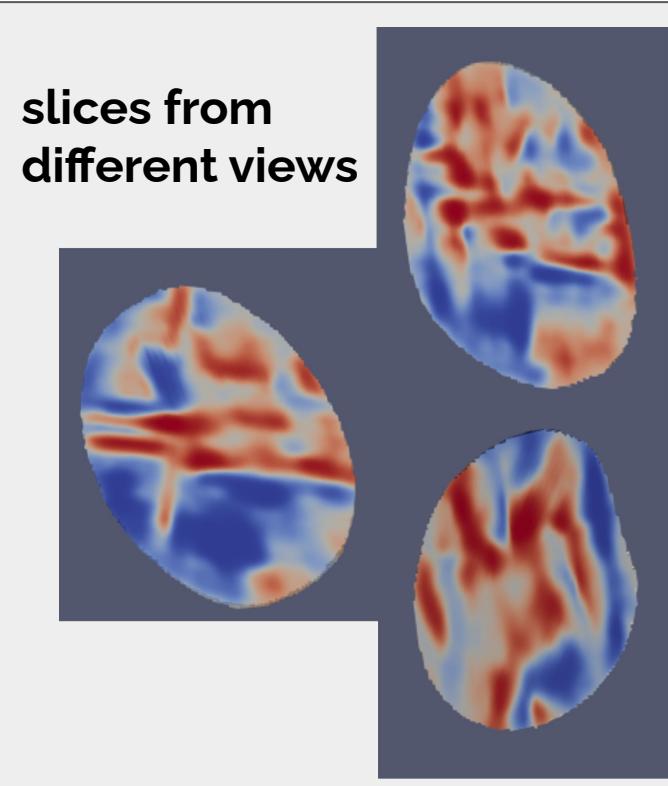
No training data!



Results on simulated 3D data



Results on realistic 3D results



HIO+ER with Shrinkwrap

Deep random projector to accelerate DIP

- Li et al. **Deep Random Projector: Accelerated Deep Image Prior**. Submitted to CVPR'23.

DRP vs. DIPs: a glance

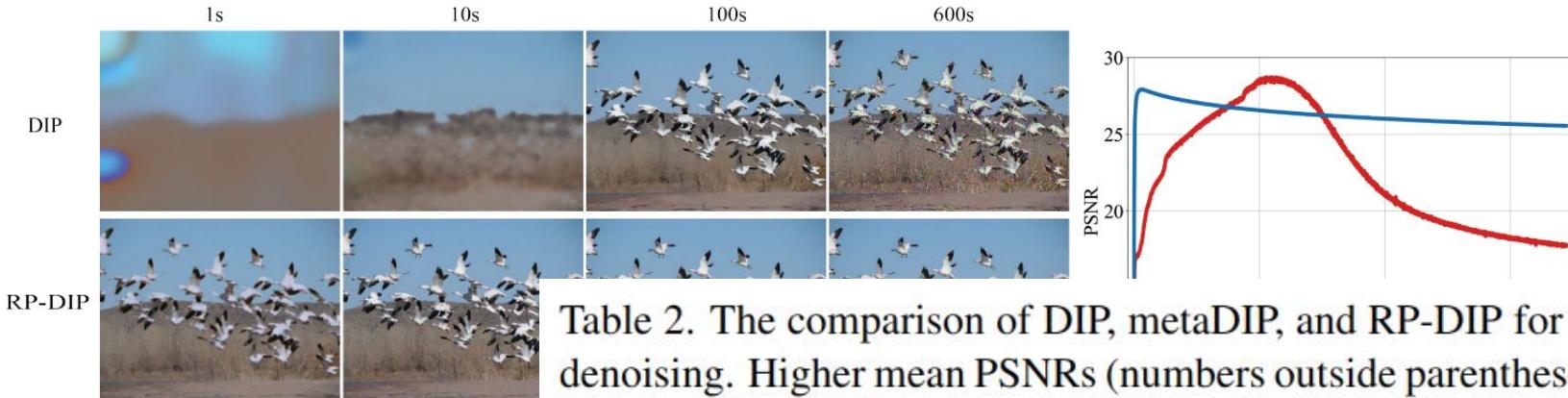


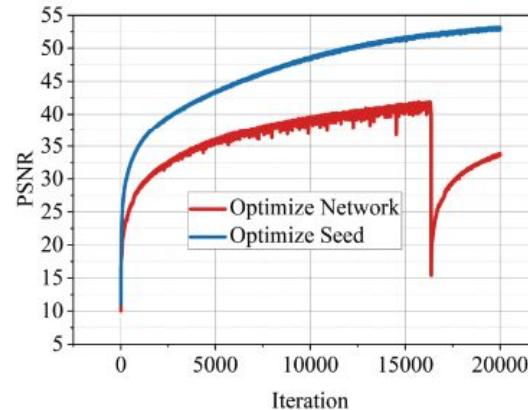
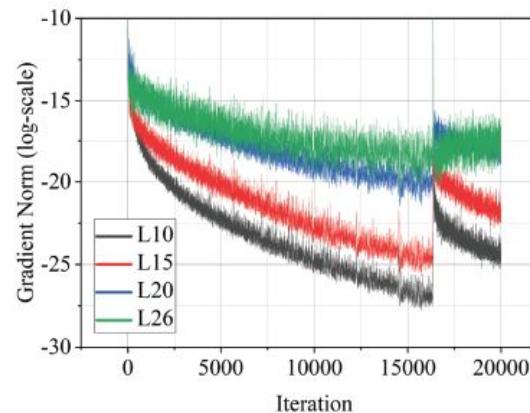
Table 2. The comparison of DIP, metaDIP, and RP-DIP for image denoising. Higher mean PSNRs (numbers outside parentheses) are in **red** and less OPT time (numbers inside parentheses) is in **blue**.

	CelebA		CBSD68	
	L	H	L	H
DIP	27.27 (9.44)	23.04 (3.95)	26.05 (9.44)	22.55 (3.67)
MetaDIP20	27.27 (7.59)	23.02 (3.24)	26.16 (8.89)	22.54 (3.99)
MetaDIP50	27.31 (7.01)	23.09 (2.69)	26.10 (8.50)	22.51 (3.39)
RP-DIP	27.99 (0.49)	23.70 (0.18)	26.86 (0.73)	23.07 (0.34)

Key(s) to accelerating optimization

- **Optimizing the input seed, not the network** → improve the convergence

$$\min_{\theta} \ell(\mathbf{y}, f \circ G_{\theta}(\mathbf{z})) \longrightarrow \min_{\mathbf{z}} \ell(\mathbf{y}, f \circ G_{\theta}(\mathbf{z}))$$



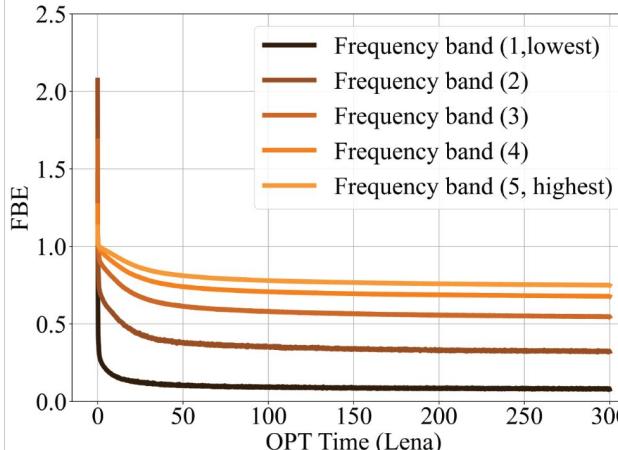
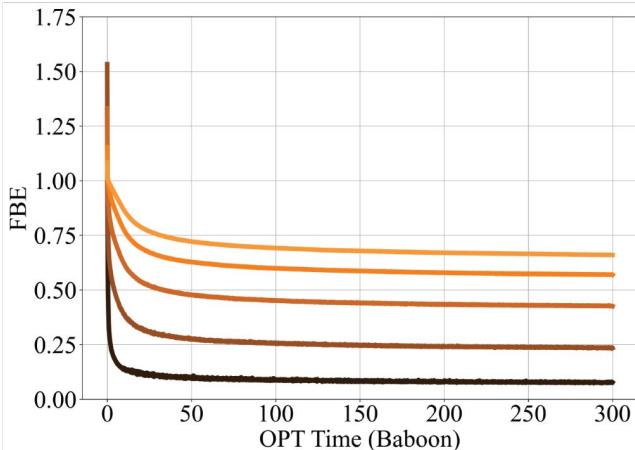
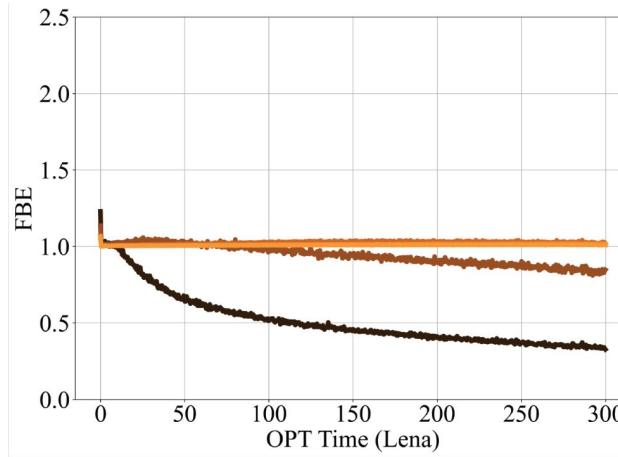
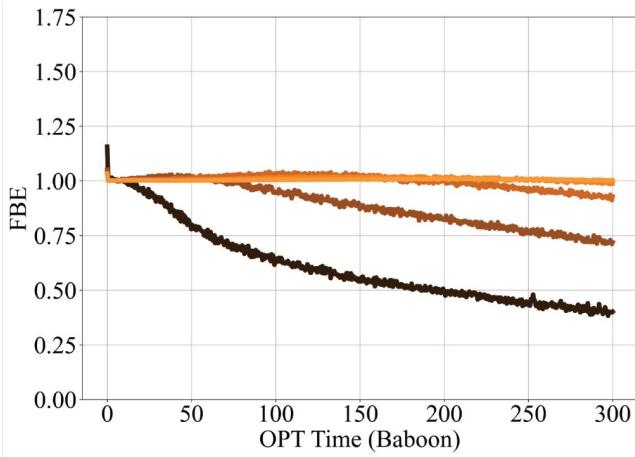
- **Cutting down the network depth** → improve per-iteration cost

Key(s) to retaining restoration quality

- Adopting an explicit regularizer

$$\min_z \underbrace{\|\mathbf{y} - G_{\hat{\theta}}(\mathbf{z})\|}_{\text{fidelity term}} + \lambda \underbrace{\text{TV}_{aniso}(G_{\hat{\theta}}(\mathbf{z}))}_{\text{regularization}}$$

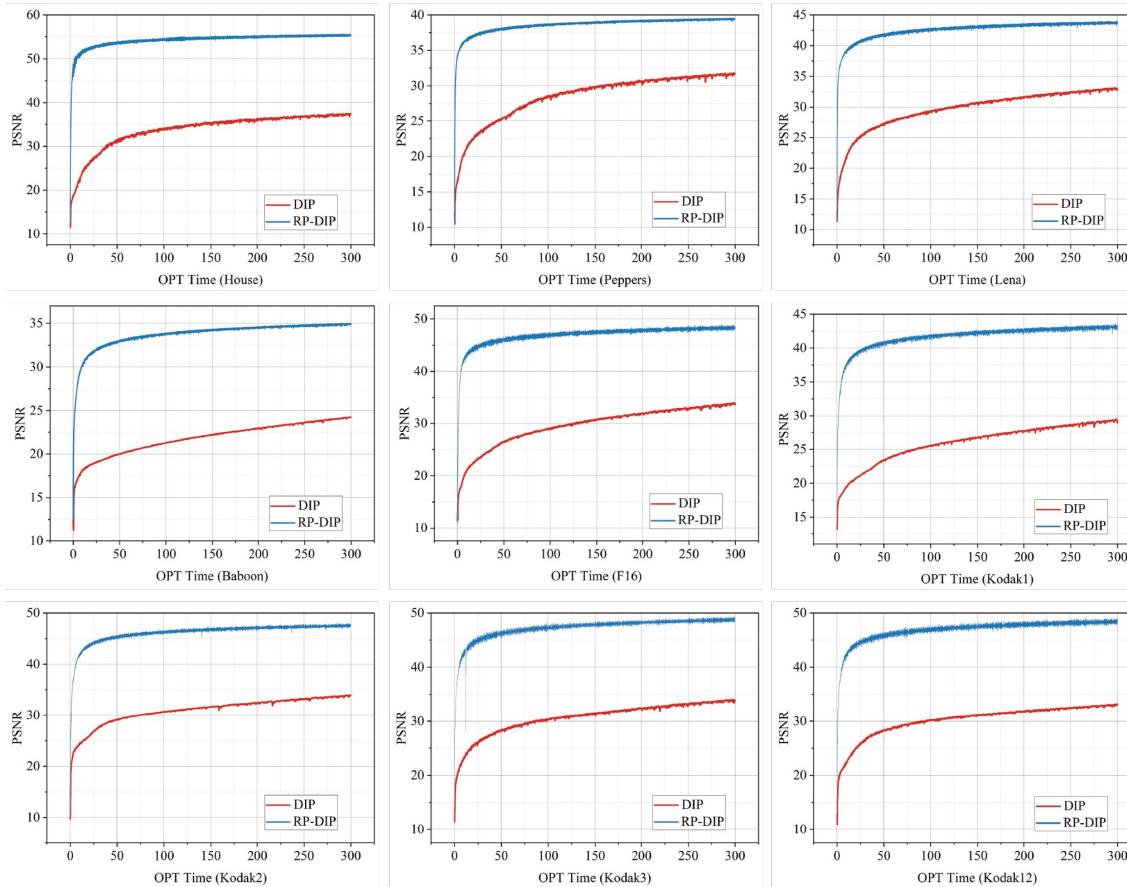
Spectral bias analysis



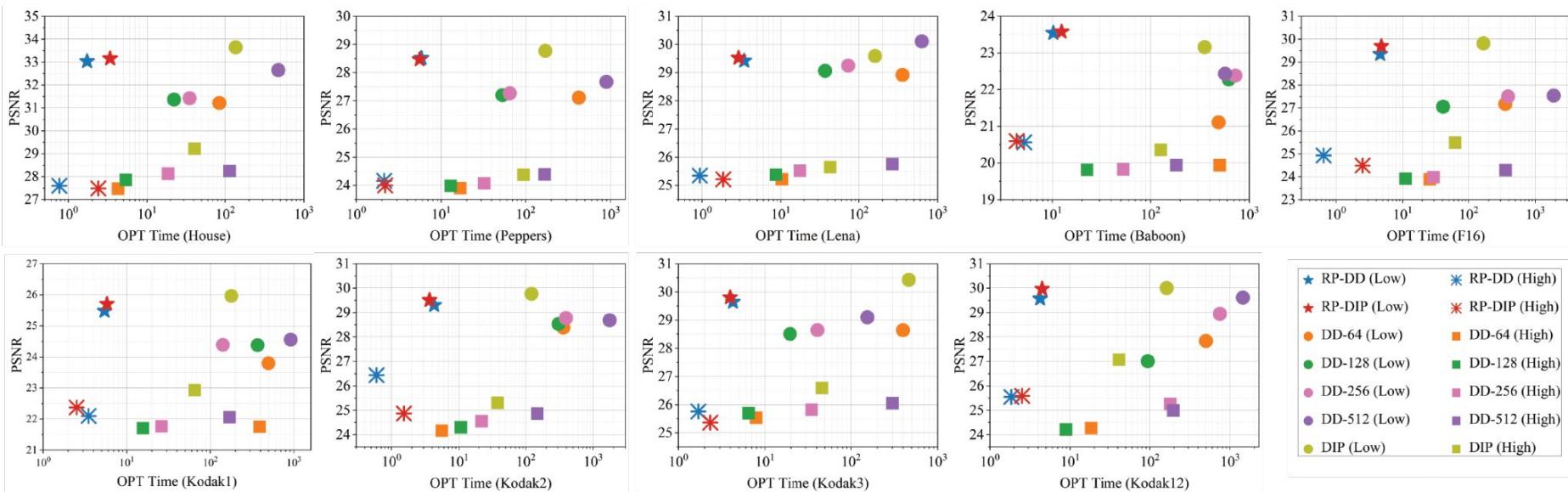
DIP

DRP

DRP vs. DIP: denoising/reconstruct a “clean” image



RP vs. DIPs: denoising/reconstruct a noisy image



Closing

$$\min_{\theta} \ell(\mathbf{y}, f \circ G_{\theta}(\mathbf{z})) + \lambda R \circ G_{\theta}(\mathbf{z})$$

Addressing practicality issues around DIP

- **Early stopping** to tackle early-learning-then-overfitting (ELTO)
- Careful customization makes **blind image denoising** and **phase retrieval** work in unprecedented regimes
- (brief) **Deep random projector**—toward efficient DIP

Papers

- Li et al. **Self-Validation: Early Stopping for Single-Instance Deep Generative Priors** (BMVC'21) <https://arxiv.org/abs/2110.12271>
- Wang et al. **Early Stopping for Deep Image Prior** <https://arxiv.org/abs/2112.06074> (Under review for ICLR'23)
- Zhuang et al. **Blind Image Deblurring with Unknown Kernel Size and Substantial Noise.** <https://arxiv.org/abs/2208.09483> (Under review for IJCV)
- Zhuang et al. **Practical Phase Retrieval Using Double Deep Image Priors.** <https://arxiv.org/abs/2211.00799> (Under review for ICCASP'23)
- Li et al. **Deep Random Projector: Toward Efficient Deep Image Prior.** (Under review for CVPR'23)



computer
SCIENCE & ENGINEERING



glovex.umn.edu

GROUP OF LEARNING, OPTIMIZATION,
VISION, HEALTHCARE, AND X

UNIVERSITY OF MINNESOTA
Driven to DiscoverSM

