Neural Networks: Old and New

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Logistics

Another great reference: Dive into Deep Learning
 by Aston Zhang and Zachary C. Lipton and Mu Li and Alexander J.
 Smola. Livebook online: https://d2l.ai/ (comprehensive coverage of recent developments and detailed implementations based on NumPy)



- Homework 0 will be posted tonight
- Waiting list

Outline

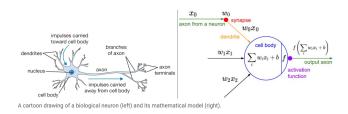
Start from neurons

Shallow to deep neural networks

A brief history of Al

Suggested reading

Model of biological neurons

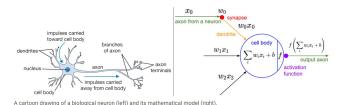


Credit: Stanford CS231N

Biologically ...

- Each neuron receives signals from its dendrites
- Each neuron outputs signals via its single axon
- The axon branches out and connects via synapese to dendrites of other neurons

Model of biological neurons



Credit: Stanford CS231N

Mathematically ...

- Each neuron receives x_i 's from its **dendrites**
- x_i 's weighted by w_i 's (synaptic strengths) and summed $\sum_i w_i x_i$
- The neuron fires only when the combined signal is above a certain threshold: $\sum_i w_i x_i + {\color{red}b}$
- Fire rate is modeled by an **activation function** f, i.e., outputting $f\left(\sum_{i} w_{i}x_{i} + b\right)$

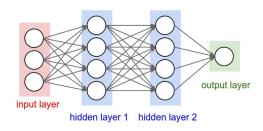
Artificial neural networks

Brain neural networks



Credit: Max Pixel

Artificial neural networks



Why called artificial?

- (Over-)simplification on neural level
- (Over-)simplification on connection level

In this course, neural networks are always artificial.

Outline

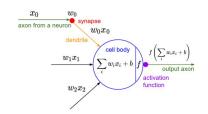
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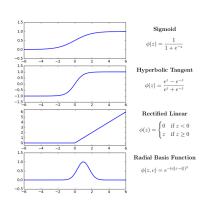
Artificial neurons



$$f\left(\sum_{i} w_{i} x_{i} + b\right) = f\left(\boldsymbol{w}^{\mathsf{T}} \boldsymbol{x} + b\right)$$

We shall use σ instead of f henceforth.

Examples of activation function σ

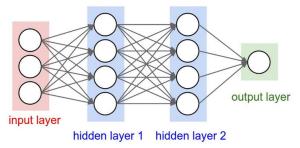


Credit: [Hughes and Correll, 2016]

Neural networks

One neuron: $\sigma\left(\boldsymbol{w}^{\mathsf{T}}\boldsymbol{x}+b\right)$

Neural networks (NN): **structured** organization of artificial neurons



 $m{w}$'s and $m{b}$'s are unknown and need to be learned Many models in machine learning $m{are}$ neural networks

A typical setup

Supervised Learning

- Gather training data $(oldsymbol{x}_1,oldsymbol{y}_1),\ldots,(oldsymbol{x}_n,oldsymbol{y}_n)$
- Choose a family of functions, e.g., \mathcal{H} , so that there is $f \in \mathcal{H}$ to ensure $m{y}_i pprox f\left(m{x}_i\right)$ for all i
- Set up a loss function ℓ to measure the approximation quality
- Find an $f \in \mathcal{H}$ to minimize the average loss

$$\min_{f \in \mathcal{H}} \frac{1}{n} \sum_{i=1}^{n} \ell\left(\boldsymbol{y}_{i}, f\left(\boldsymbol{x}_{i}\right)\right)$$

... known as **empirical risk minimization** (ERM) framework in learning theory

A typical setup

Supervised Learning from NN viewpoint

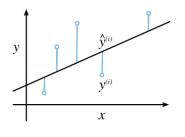
- Gather training data $(oldsymbol{x}_1,oldsymbol{y}_1),\ldots,(oldsymbol{x}_n,oldsymbol{y}_n)$
- Choose a NN with k neurons, so that there is a group of weights, e.g., $(\boldsymbol{w}_1,\ldots,\boldsymbol{w}_k,b_1,\ldots,b_k)$, to ensure

$$\boldsymbol{y}_i \approx \left\{ \mathsf{NN}\left(\boldsymbol{w}_1, \dots, \boldsymbol{w}_k, b_1, \dots, b_k \right) \right\} \left(\boldsymbol{x}_i \right) \quad \forall i$$

- Set up a loss function ℓ to measure the approximation quality
- Find weights $(w_1, \ldots, w_k, b_1, \ldots, b_k)$ to minimize the average loss

$$\min_{\boldsymbol{w}'s,b's} \frac{1}{n} \sum_{i=1}^{n} \ell\left[\boldsymbol{y}_{i}, \left\{\mathsf{NN}\left(\boldsymbol{w}_{1}, \ldots, \boldsymbol{w}_{k}, b_{1}, \ldots, b_{k}\right)\right\}\left(\boldsymbol{x}_{i}\right)\right]$$

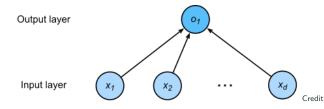
Linear regression



Credit: D2L

- Data: $({m x}_1, y_1), \ldots, ({m x}_n, y_n)$, ${m x}_i \in \mathbb{R}^d$
- Model: $y_i \approx \boldsymbol{w}^\intercal \boldsymbol{x}_i + b$
- Loss: $||y \hat{y}||_2^2$
- Optimization:

$$\min_{\boldsymbol{w},b} \ \frac{1}{n} \sum_{i=1}^{n} \|y_i - (\boldsymbol{w}^{\mathsf{T}} \boldsymbol{x}_i + b)\|_2^2$$

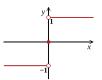


Perceptron



Frank Rosenblatt

- Data: $(\boldsymbol{x}_1, y_1), \dots, (\boldsymbol{x}_n, y_n)$, $\boldsymbol{x}_i \in \mathbb{R}^d$, $y_i \in \{+1, -1\}$
- Model: $y_i \approx \sigma \left(\boldsymbol{w}^\intercal \boldsymbol{x}_i + b \right)$, σ sign function

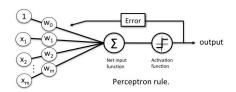


- Loss: $\mathbf{1}\left\{y \neq \hat{y}\right\}$
- Optimization:

$$\min_{\boldsymbol{w},b} \frac{1}{n} \sum_{i=1}^{n} \mathbf{1} \left\{ y_i \neq \sigma \left(\boldsymbol{w}^{\mathsf{T}} \boldsymbol{x}_i + b \right) \right\}$$

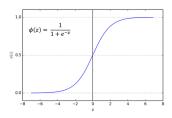
Perceptron

Perceptron is a single artificial neuron for binary classification



dominated early AI (50's - 70's)

Logistic regression is similar but with sigmod activiation



Softmax regression

- Data: $(x_1,y_1),\ldots,(x_n,y_n)$, $x_i\in\mathbb{R}^d$, $y_i\in\{L_1,\ldots,L_p\}$, i.e., multiclass classification problem
- Data preprocessing: labels into vectors via one-hot encoding

$$L_k \Longrightarrow [\underbrace{0,\ldots,0}_{k-1\,0's},1,\underbrace{0,\ldots,0}_{n-k\,0's}]^{\mathsf{T}}$$

So: $y_i \Longrightarrow \boldsymbol{y}_i$

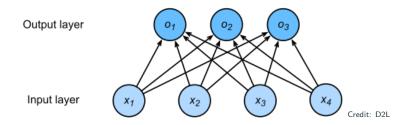
- Model: $y_i \approx \sigma (W^{\mathsf{T}} x_i + b)$, here σ is the softmax function (maps vectors to vectors): for $z \in \mathbb{R}^p$,

$$oldsymbol{z} \mapsto \left[rac{e^{z_1}}{\sum_j e^{z_j}}, \ldots, rac{e^{z_p}}{\sum_j e^{z_j}}
ight]^\intercal.$$

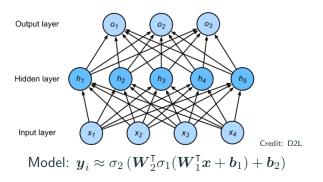
- Loss: cross-entropy loss $-\sum_j y_j \log \hat{y}_j$
- Optimization ...

Softmax regression

... for multiclass classification



Multilayer perceptrons



Also called feedforward networks

Modern NNs: many hidden layers (deep), refined connection structure and/or activations

They're all (shallow) NNs

- Linear regression
- Perception and Logistic regression
- Softmax regression
- Multilayer perceptron (feedforward NNs)
- Support vector machines (SVM)
- PCA (autoencoder)
- Matrix factorization

see, e.g., Chapter 2 of [Aggarwal, 2018].

Outline

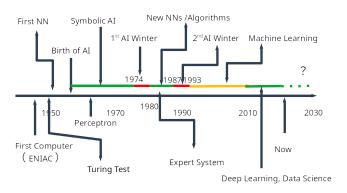
Start from neurons

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A brief history of AI

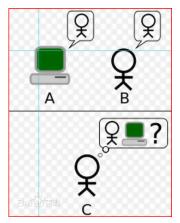
Suggested reading

Birth of Al



- Crucial precursors: first computer, Turing test
- 1956: Dartmouth Artificial Intelligence Summer Research
 Project Birth of Al

Turing test



Turing Test



Alan Turing (1912-1954)

First golden age



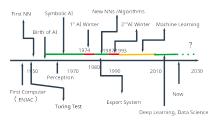
Symbolic AI: based on rules and logic

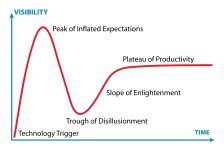




rules for recognizing dogs?

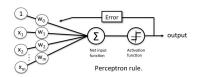
First Al winter





Gartner hype cycle

Perceptron



invented 1962



written in 1969, end of Perceptron era



Marvin Minsky (1927–2016)

Birth of computer vision

MASSACHUSETTS INSTITUTE OF TECHNOLOGY PROJECT MAC

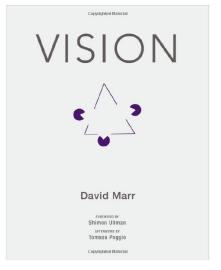
Artificial Intelligence Group Vision Memo. No. 100. July 7, 196

THE SUMMER VISION PROJE

Seymour Papert

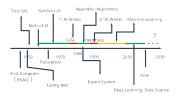
The numer vision project is an attempt to use our numer workers effectively in the construction of a significant part of a visual system. The particular task was chosen partly because it can be segmented into sub-problems which will allow individuals to work independently and yet participate in the construction of a system complex enough to be a real landmark in the development of "matters recognization".

1966

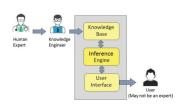


around 1980

Second golden age



expert system





Can we build comprehensive knowledge bases and know all rules?

26/32

Big bang in DNNs

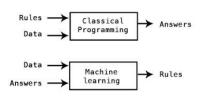
Key ingredients of DL have been in place for 25-30 years:

Landmark	Emblem	Epoch
Neocognitron	Fukushima	1980
CNN	Le Cun	mid 1980s'
Backprop	Hinton	mid 1980's
SGD	Le Cun, Bengio etc	mid 1990's
Various	Schmidhuber	mid 1980's
CTF	DARPA etc	mid 1980's

After 2nd Al winter



Machine learning takes over ...



Golden age of Machine learning

Starting 1990's

Support vector machines (SVM)

Adaboost

Decision trees and random forests

Deep learning

. . .

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Suggested reading

Suggested reading

- Chap 2, Neural Networks and Deep Learning.
- Chap 3-4, Dive into Deep Learning.
- Chap 1, Deep Learning with Python.

References i

[Aggarwal, 2018] Aggarwal, C. C. (2018). Neural Networks and Deep Learning. Springer International Publishing.

[Hughes and Correll, 2016] Hughes, D. and Correll, N. (2016). **Distributed machine** learning in materials that couple sensing, actuation, computation and communication. arXiv:1606.03508.