

Peer Graded Assignment: Statistical Inference Course Project

Sunday

May 7, 2017

Instructions

The project consists of two parts: 1. A simulation exercise. 2. Basic inferential data analysis. Part 1: Simulation Exercise Instructions Overview In this project you will investigate the exponential distribution in R and compare it with the Central Limit Theorem. The exponential distribution can be simulated in R with `rexp(n, lambda)` where `lambda` is the rate parameter. The mean of exponential distribution is $1/\lambda$ and the standard deviation is also $1/\lambda$. Set $\lambda = 0.2$ for all of the simulations. You will investigate the distribution of averages of 40 exponentials. Note that you will need to do a thousand simulations. Question 1 : Show the sample mean and compare it to the theoretical mean distribution

```
n <- 40
Simulations <- 1000
Lambda <- 0.2

SampleMean <- NULL
for(i in 1:Simulations) {
  SampleMean <- c(SampleMean, mean(rexp(n, Lambda)))
}
mean(SampleMean)
```

```
## [1] 4.992367
```

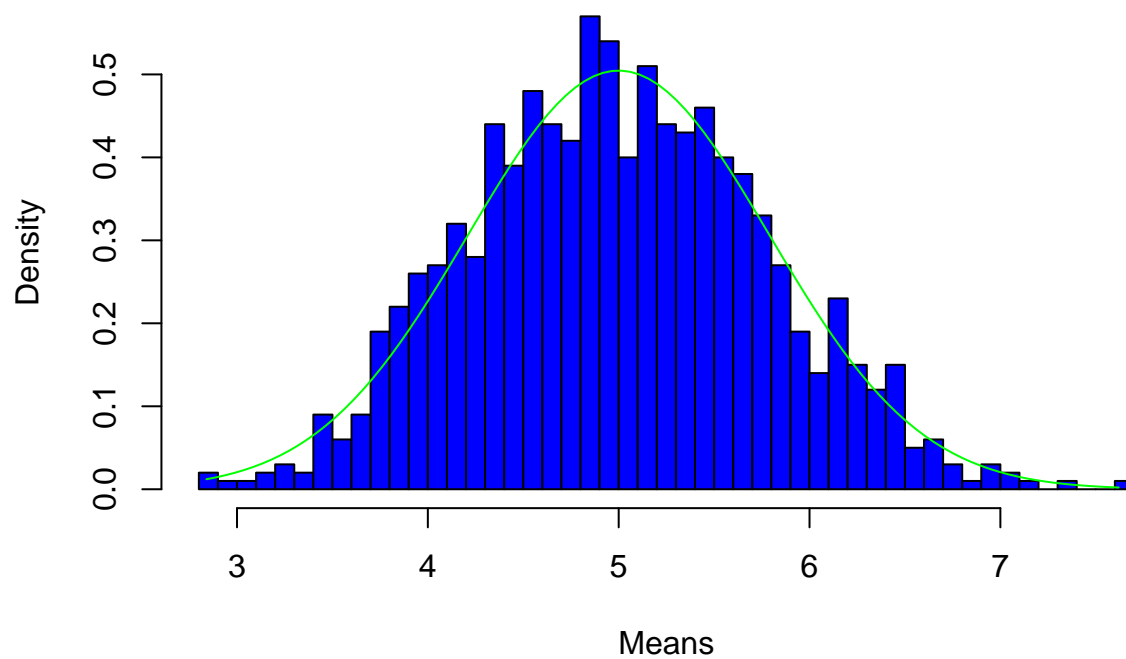
So, as we can see, compared to the theoretical mean distribution of 5, our mean 5 is close. Question 2: Show the sample is (via variance) and compares it to the theoretical variance of the distribution. The theoretical standard deviation of the distribution is also $1/\lambda$, which, for a λ of 0.2, equates to 5. The variance is the square of the standard deviation, which is 25.

```
Variance <- var(SampleMean)
```

0.6 is close to the theoretical distribution. Show that the distribution is approximately normal

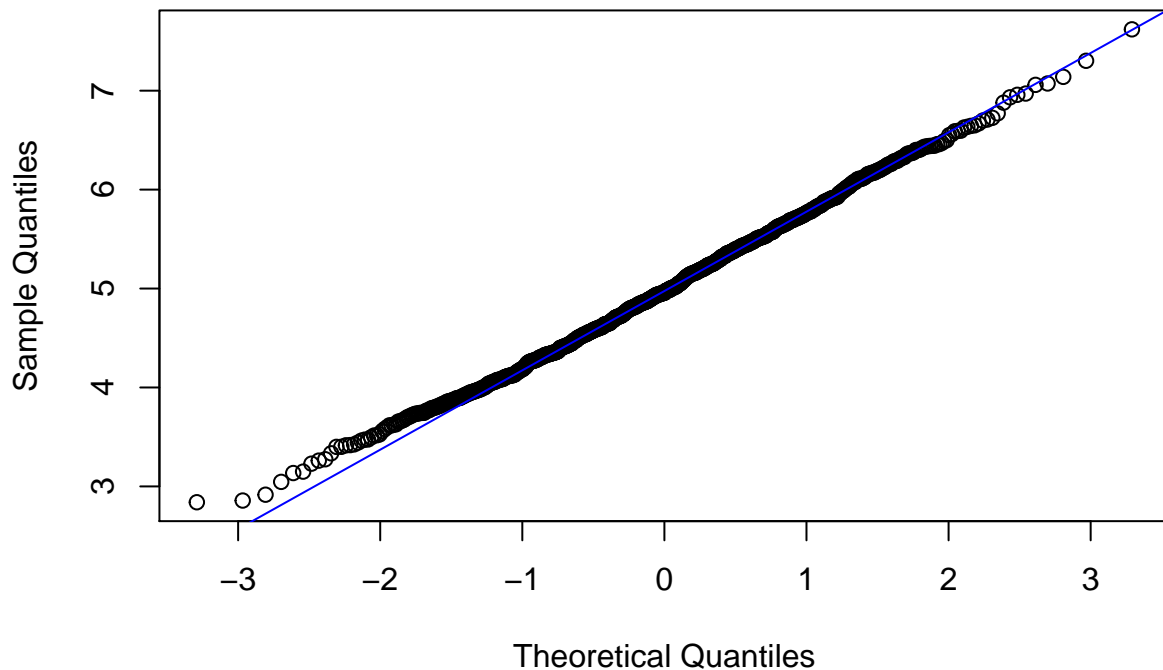
```
hist(SampleMean, breaks = n, prob = T, col = "blue", xlab = "Means")
x <- seq(min(SampleMean), max(SampleMean), length = 100)
lines(x, dnorm(x, mean = 1/Lambda, sd = (1/Lambda/sqrt(n))), pch = 25, col = "green")
```

Histogram of SampleMean



```
qqnorm(SampleMean)
qqline(SampleMean, col = "blue")
```

Normal Q-Q Plot



The distribution averages of 40 exponentials is very close to a normal distribution Part 2: Basic Inferential Data Analysis Instructions Now in the second portion of the project, we're going to analyze the ToothGrowth data in the R datasets package. 1. Load the ToothGrowth data and perform some basic exploratory data analysis

```
library(datasets)
data(ToothGrowth)
library(ggplot2)
```

```
## Warning: package 'ggplot2' was built under R version 3.3.3
```

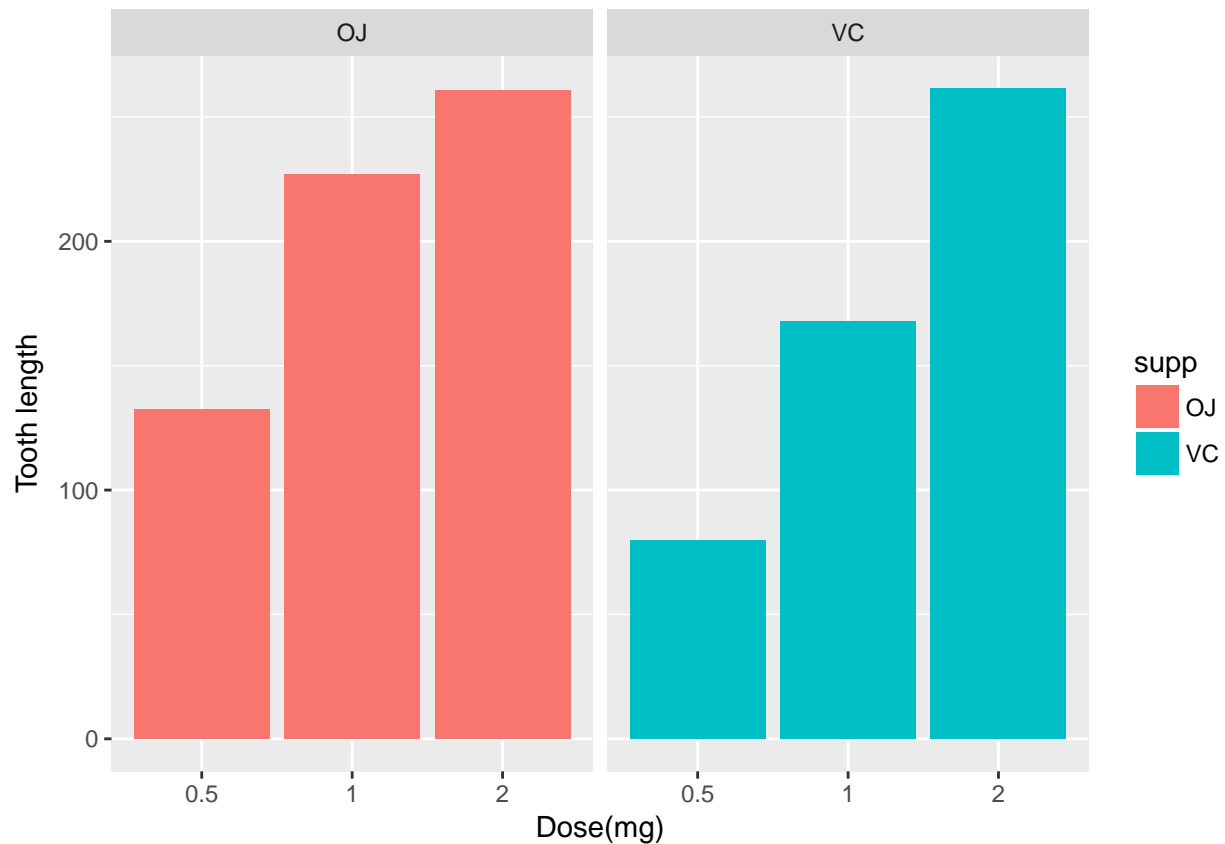
```
str(ToothGrowth)
```

```
## 'data.frame': 60 obs. of 3 variables:
## $ len : num 4.2 11.5 7.3 5.8 6.4 10 11.2 11.2 5.2 7 ...
## $ supp: Factor w/ 2 levels "OJ","VC": 2 2 2 2 2 2 2 2 2 2 ...
## $ dose: num 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 ...
```

```
summary(ToothGrowth)
```

```
##      len      supp      dose
## Min.   : 4.20    OJ:30    Min.    :0.500
## 1st Qu.:13.07    VC:30    1st Qu.:0.500
## Median :19.25                Median :1.000
## Mean   :18.81                Mean   :1.167
## 3rd Qu.:25.27                3rd Qu.:2.000
## Max.   :33.90                Max.   :2.000
```

```
ggplot(data=ToothGrowth, aes(x=as.factor(dose), y=len, fill=supp)) +
  geom_bar(stat="identity") +
  facet_grid(. ~ supp) +
  xlab("Dose(mg)") +
  ylab("Tooth length")
```



3. Use confidence intervals and/or hypothesis tests to compare tooth growth by supp and dose. (Only use the techniques from class, even if there's other approaches worth considering)

```
hypoth1 <- t.test(len ~ supp, data = ToothGrowth)
hypoth1$conf.int
```

```
## [1] -0.1710156 7.5710156
## attr("conf.level")
## [1] 0.95
attr("conf.level")
```

```
hypoth1$p.value
```

```
## [1] 0.06063451
```

```
hypoth2<-t.test(len ~ supp, data = subset(ToothGrowth, dose == 0.5))
hypoth2$conf.int
```

```
## [1] 1.719057 8.780943
## attr("conf.level")
## [1] 0.95
```

```
hypoth2$p.value
```

```
## [1] 0.006358607
```

```
hypoth3<-t.test(len ~ supp, data = subset(ToothGrowth, dose == 1))
```

```
hypoth3$conf.int
```

```
## [1] 2.802148 9.057852
```

```
## attr(,"conf.level")
```

```
## [1] 0.95
```

```
attr("conf.level")
```

```
hypoth3$p.value
```

```
## [1] 0.001038376
```

```
hypoth4<-t.test(len ~ supp, data = subset(ToothGrowth, dose == 2))
```

```
hypoth4$conf.int
```

```
## [1] -3.79807 3.63807
```

```
## attr(,"conf.level")
```

```
## [1] 0.95
```

```
attr("conf.level")
```

```
hypoth4$p.value
```

```
## [1] 0.9638516
```

Conclusions OJ ensures more tooth growth than VC for dosages 0.5 & 1.0. OJ and VC gives the same amount of tooth growth for dose amount 2.0 mg/day. For the entire trail we cannot conclude OJ is more effective than VC for all scenarios.