

Assignment 1

1. 'openblas' is used in the program.
2. (1) 'S' means single, 'D' means double, 'C' means complex, 'Z' means double complex.
(2) 'SSPR2' is to calculate $\mathbf{A} \leftarrow \mathbf{A} + \alpha \mathbf{xy}^T + \alpha \mathbf{yx}^T$, which alpha is a scalar, A is a symmetric matrix, x & y are vector, and, \mathbf{y}^T \mathbf{x}^T are the transpose of vector x and y.
'ZGERC' is to calculate $\mathbf{A} \leftarrow \mathbf{A} + \alpha \mathbf{xy}^H$, which A is an m by n matrix, alpha is a scalar, x is a vector of length m, \mathbf{y}^H is the conjugate transpose of vector y of length n.
'DGBSVX' is to compute the solution of $\mathbf{AX}=\mathbf{B}$, which A can be \mathbf{A}^T or \mathbf{A}^H , and B is matrix, X is the solution.
'CHEEVR' is to compute the eigenvalues and the eigenvectors of a matrix.
3. To check the correctness of the calculation, we can use both lapack function and numpy function, then check if the answer is equal.
4. To use block matrix operation to evaluate $\mathbf{Ax} = \mathbf{b}$, we can evaluate $\mathbf{x} = (\mathbf{A}-1)\mathbf{b}$. Then partitioning $\mathbf{A}-1$ into smaller block matrix. We can partitioning it every 2 rows and 2 columns. Then we can get a 2 * 2 partitioning $\mathbf{A}-1$ matrix.
We can accelerate the compute speed because if there are some O or I matrix, it will be more convenient to calculate it.
5. Strassen Matrix–Matrix Multiplication algorithm is using the block matrix operation to calculate, and the matrix should be $2^n * 2^n$. By partitioning the matrix, it can reduce the calculate time, and reduce the time complexity.
But by this method, the matrix should be $2^n * 2^n$. Although we can extend the matrix to fit it, if the matrix is too big, still can't increase the efficiency a lot.