

# **Introduction to Software Testing**

## **Chapter 5.2** **Program-based Grammars**

**Paul Ammann & Jeff Offutt**

Updated by Sunae Shin

# Applying Syntax-based Testing to Programs

- **Syntax-based criteria originated with programs and have been used most with programs**
  - **BNF criteria are most commonly used to test compilers**
  - **Mutation testing criteria are most commonly used for unit testing and integration testing of classes**

# Program-based Grammars

- The original and most widely known application of syntax-based testing is to **modify programs**
  - Operators modify a ground string (program under test) to create mutant programs
  - Mutant programs must compile correctly
  - Mutants are not tests, but used to find tests
  - Once mutants are defined, tests must be found to cause mutants to fail when executed
  - This is called “**killing mutants**”

# Program-based Grammars

## Original Method

```
int Min (int A, int B)
{
    int minVal;
    minVal = A;
    if (B < A)
    {
        minVal = B;
    }
    return (minVal);
} // end Min
```

6 mutants

Each represents a  
separate program

## With Embedded Mutants

```
int Min (int A, int B)
{
    int minVal;
    minVal = A;
    Δ 1 minVal = B;
    if (B < A)
    Δ 2 if (B > A)
    Δ 3 if (B < minVal)
    {
        minVal = B;
    Δ 4 Bomb ();
    Δ 5 minVal = A;
    Δ 6 minVal = failOnZero (B);
    }
    return (minVal);
} // end Min
```

*Replace one variable  
with another*

*Changes operator*

*Immediate runtime  
failure ... if reached*

*Immediate runtime  
failure if B==0 else  
does nothing*

# Syntax-Based Coverage Criteria

**Mutation Coverage (MC)** : For each  $m \in M$ , TR contains exactly one requirement, to kill  $m$ .

## 1) Strongly Killing Mutants:

Given a mutant  $m \in M$  for a program  $P$  and a test  $t$ ,  $t$  is said to *strongly kill*  $m$  if and only if the output of  $t$  on  $P$  is different from the output of  $t$  on  $m$

## 2) Weakly Killing Mutants:

Given a mutant  $m \in M$  that modifies a location  $l$  in a program  $P$ , and a test  $t$ ,  $t$  is said to *weakly kill*  $m$  if and only if the state of the execution of  $P$  on  $t$  is different from the state of the execution of  $m$  immediately on  $t$  after  $l$

- Weakly killing satisfies reachability and infection, but not propagation

# Weak Mutation

**Weak Mutation Coverage (WMC) : For each  $m \in M$ , TR contains exactly one requirement, to weakly kill  $m$ .**

- “Weak mutation” is so named because it is easier to kill mutants under this assumption
- Weak mutation also requires less analysis
- A few mutants can be killed under weak mutation but not under strong mutation (no propagation)

# Weak Mutation Example

- Mutant 1 in the Min( ) example is:

```
minVal = A;  
Δ 1 minVal = B;  
    if (B < A)  
        minVal = B;
```

```
int Min (int A, int B)  
{  
    int minVal;  
    minVal = A;  
Δ 1 minVal = B;  
    if (B < A)  
Δ 2 if (B > A)  
Δ 3 if (B < minVal)  
    {  
        minVal = B;  
Δ 4 Bomb ();  
Δ 5 minVal = A;  
Δ 6 minVal = failOnZero(B);  
    }  
    return (minVal);  
} // end Min
```

- The complete test specification to kill mutant 1:
  - Reachability: *true* // Always get to that statement (mutant is on the first statement)
  - Infection :  $A \neq B$  // In order to infect, the value B must be different from A
  - Propagation:  $(B < A) = \text{false}$  // Skip the next assignment
  - Full Test Specification:  $\text{true} \wedge (A \neq B) \wedge ((B < A) = \text{false})$   
 $\equiv (A \neq B) \wedge (B \geq A)$   
 $\equiv (B > A)$
- The test case (A = 5, B = 7) should cause mutant 1 to result in a failure

# Equivalent Mutation Example

- Mutant 3 in the Min() example is equivalent:

```
minVal = A;  
if (B < A)  
Δ 3 if (B < minVal)
```

```
int Min (int A, int B)  
{  
    int minVal;  
    minVal = A;  
Δ 1 minVal = B;  
    if (B < A)  
Δ 2 if (B > A)  
Δ 3 if (B < minVal)  
    {  
        minVal = B;  
Δ 4 Bomb ();  
Δ 5 minVal = A;  
Δ 6 minVal = failOnZero(B);  
    }  
    return (minVal);  
} // end Min
```

- Reachability: true
- The infection condition is “ $(B < A) \neq (B < \text{minVal})$ ”
- However, the previous statement was “ $\text{minVal} = A$ ”
  - Substituting, we get: “ $(B < A) \neq (B < A)$ ”
  - This is a logical contradiction !
- Thus no input can kill this mutant



# Mutation example

```
...  
found := FALSE; TRUE  
i := 1;  
while(not(found)) and (i <= x) do begin // x is the length  
    if a[i] = c then  
        found := TRUE  
    else  
        i := i + 1  
    end  
end  
if (found)  
    print("Character %c appears at position %i");  
else  
    print("Character is not present in the string");  
end  
...
```

- **Replace Found := FALSE; with Found := TRUE;**
- **Note: It is better in Mutation Testing to make only one small change at a time to avoid the danger of introduced faults with interfering effects**

# Mutation example

```
...  
found := FALSE; TRUE  
i := 1;  
while(not(found)) and (i <= x) do begin // x is the length  
    if a[i] = c then  
        found := TRUE  
    else  
        i := i + 1  
    end  
end  
if (found)  
    print("Character %c appears at position %i");  
else  
    print("Character is not present in the string");  
end  
...
```

- **Failure:** “character a appears at position 1” instead of saying “character is not present in the string”
- **Mutant is killed**

# Why Mutation Works

## Fundamental Premise of Mutation Testing

**If the software contains a fault, there will usually be a set of mutants that can only be killed by a test case that also detects that fault**

- **This is not an absolute !**
- **The mutants guide the tester to an effective set of tests**
- **A very challenging problem :**
  - **Find a fault and a set of mutation-adequate tests that do not find the fault**
- **Of course, this depends on the mutation operators ...**

# Designing Mutation Operators

- Mutation operators do one of two things :
  - Mimic typical programmer mistakes ( incorrect variable name )
  - Encourage common test heuristics ( cause expressions to be 0 )
- Researchers design lots of operators, then experimentally *select* the most useful

## Effective Mutation Operators

If tests that are created specifically to kill mutants created by a collection of mutation operators  $O = \{o1, o2, \dots\}$  also kill mutants created by all remaining mutation operators with very high probability, then  $O$  defines an *effective* set of mutation operators

# Mutation Operators for Java

## 1. *ABS* — *Absolute Value Insertion*:

Each arithmetic expression (and subexpression) is modified by the functions *abs()*, *negAbs()*, and *failOnZero()*.

Examples:

```
a = m * (o + p);
```

```
Δ1 a = abs (m * (o + p));
```

```
Δ2 a = m * abs ((o + p));
```

```
Δ3 a = failOnZero (m * (o + p));
```

## 2. *AOR* — *Arithmetic Operator Replacement*:

Each occurrence of one of the arithmetic operators  $+$ ,  $-$ ,  $*$ ,  $/$ , and  $\%$  is replaced by each of the other operators. In addition, each is replaced by the special mutation operators *leftOp*, and *rightOp*.

Examples:

```
a = m * (o + p);
```

```
Δ1 a = m + (o + p);
```

```
Δ2 a = m * (o * p);
```

```
Δ3 a = m / (o + p);
```

# Mutation Operators for Java (2)

## 3. *ROR* — *Relational Operator Replacement*:

Each occurrence of one of the relational operators ( $<$ ,  $\leq$ ,  $>$ ,  $\geq$ ,  $=$ ,  $\neq$ ) is replaced by each of the other operators and by *falseOp* and *trueOp*.

Examples:

if (X  $\leq$  Y)

$\Delta 1$  if (X  $>$  Y)

$\Delta 2$  if (X  $<$  Y)

$\Delta 3$  if (X  $\neq$  Y)

## 4. *COR* — *Conditional Operator Replacement*:

Each occurrence of one of the logical operators (and -  $\&\&$ , or -  $\parallel$ , and with no conditional evaluation -  $\&$ , or with no conditional evaluation -  $|$ , not equivalent -  $\wedge$ ) is replaced by each of the other operators; in addition, each is replaced by *falseOp*, *trueOp*, *leftOp*, and *rightOp*.

Examples:

if (X  $\leq$  Y  $\&\&$  a  $>$  0)

$\Delta 1$  if (X  $\leq$  Y  $\parallel$  a  $>$  0)

$\Delta 2$  if (X  $\leq$  Y  $\wedge$  a  $>$  0)

# Mutation Operators for Java (4)

## 5. *SOR* — *Shift Operator Replacement*:

Each occurrence of one of the shift operators <<, >>, and >>> is replaced by each of the other operators. In addition, each is replaced by the special mutation operator *leftOp*.

Examples:

```
byte b = (byte) 16;
```

```
b = b << 2;
```

```
Δ1 b = b >> 2;
```

```
Δ2 b = b >>> 2;
```

## 6. *LOR* — *Logical Operator Replacement*:

Each occurrence of one of the logical operators (bitwise and - &, bitwise or - |, exclusive or - ^) is replaced by each of the other operators; in addition, each is replaced by *leftOp* and *rightOp*.

Examples:

```
int a = 60; int b = 13;
```

```
int c = a & b;
```

```
Δ1 int c = a | b;
```

```
Δ2 int c = a;
```

# Mutation Operators for Java (5)

## 7. ASR — *Assignment Operator Replacement*:

Each occurrence of one of the assignment operators (`+=`, `-=`, `*=`, `/=`, `%=`, `&=`, `|=`, `^=`, `<<=`, `>>=`, `>>>=`) is replaced by each of the other operators.

Examples:

`a = m * (o + p);`

$\Delta 1$  `a += m * (o + p);`

$\Delta 2$  `a *= m * (o + p);`

## 8. UOI — *Unary Operator Insertion*:

Each unary operator (arithmetic `+`, arithmetic `-`, conditional `!`, logical `~`) is inserted in front of each expression of the correct type.

Examples:

`a = m * (o + p);`

$\Delta 1$  `a = m * -(o + p);`

$\Delta 2$  `a = -(m * (o + p));`



# Mutation Operators for Java (6)

## 9. UOD — *Unary Operator Deletion*:

Each unary operator (arithmetic +, arithmetic -, conditional !, logical~) is deleted.

Examples:

if !(X <= Y && !Z)

Δ1 if (X > Y && !Z)

Δ2 if !(X < Y && Z)

## 10. SVR — *Scalar Variable Replacement*:

Each variable reference is replaced by every other variable of the appropriate type that is declared in the current scope.

Examples:

a = m \* (o + p);

Δ 1 a = o \* (o + p);

Δ 2 a = m \* (m + p);

Δ 3 a = m \* (o + o);

Δ 4 p = m \* (o + p);

# Mutation Operators for Java (7)

## 11. BSR — *Bomb Statement Replacement*:

Each statement is replaced by a special Bomb() function.

Example:

```
a = m * (o + p);
```

```
Δ1 Bomb() // Raises exception when reached
```

# Summary : Subsumption of Other Criteria

- **Mutation is widely considered the strongest test criterion**
  - And most expensive !
  - By far the most test requirements (each mutant)
  - Not always the most tests
- **Subsumption can only be defined for weak mutation – other criteria impose local requirements, like weak mutation**
  - Node coverage
  - Edge coverage
  - Clause coverage
  - General active clause coverage
  - Correlated active clause coverage
  - All-defs data flow coverage

# Example 1

```
//Effects: If numbers null throw NullPointerException
//  else return LAST occurrence of val in numbers[]
//  If val not in numbers[] return -1
1. public static int findVal (int numbers[], int val)
2. {
3.     int findVal = -1;
4.
5.     for (int i=0; i<numbers.length; i++)
5'.// for (int i=(0+1); i<numbers.length; i++)
6.         if (numbers [i] == val)
7.             findVal = i;
8.     return (findVal);
9. }
```

- Find a test input that kills mutant *m*.
- Sol: Any input with val only in numbers[0] works. An example is: (numbers, val) = ([1, 0], 1)

# Example 2

```
//Effects: If x null throw NullPointerException
//      else return the sum of the values in x

1. public static int sum (int[] x)
2. {
3.     int s = 0;
4.     for (int i=0; i < x.length; i++) {
5.         {
6.             s = s + x[i];
6'.        // s = s - x[i]; //AOR
7.         }
8.     return s;
9. }
```

- Find a test input that kills mutant *m*.
- Sol: Any input with a nonzero sum works.  
An example is:  $x = [1, 2, 3]$