

Introduction to Software Testing

Chapter 2

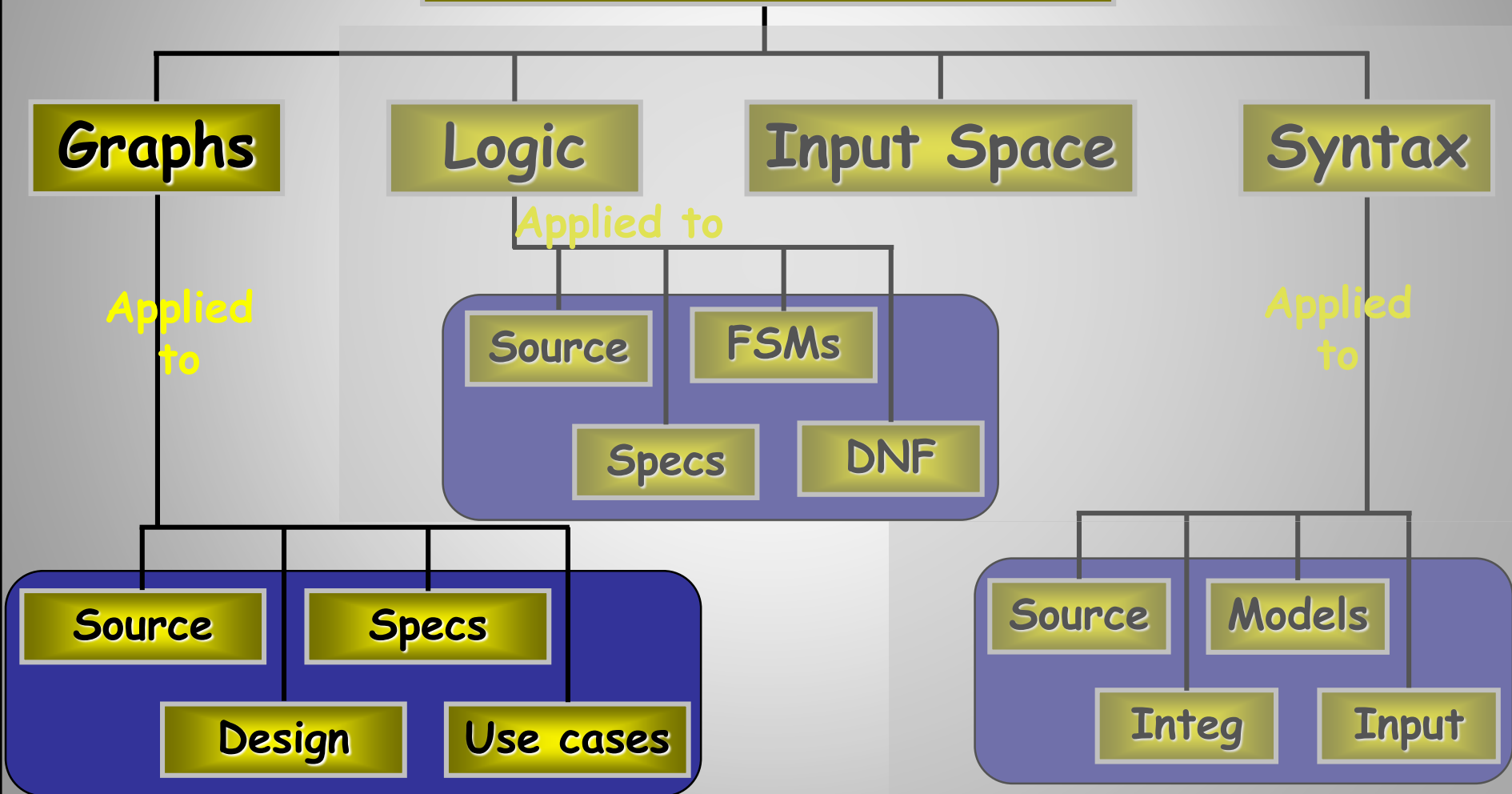
Overview Graph Coverage Criteria

Paul Ammann & Jeff Offutt

Updated by Sunae Shin

Ch. 02 : Graph Coverage

Four Structures for Modeling Software



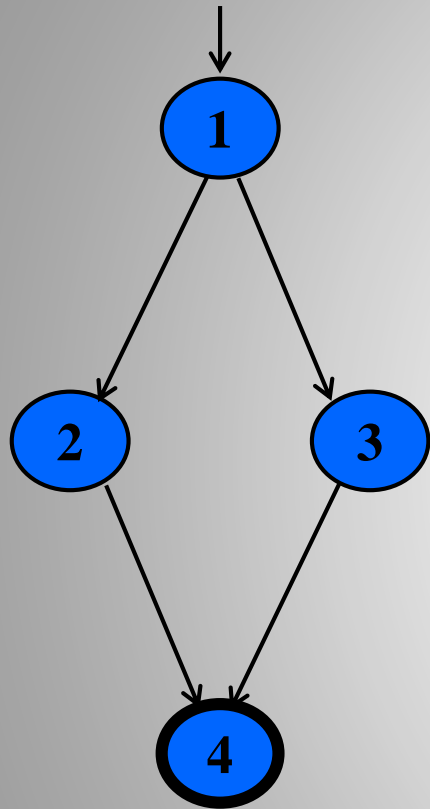
Covering Graphs

- Graphs are the most commonly used structure for testing
- Graphs can come from many sources
 - Control flow graphs
 - Design structure
 - FSMs and statecharts
 - Use cases
- Tests usually are intended to “cover” the graph in some way

Definition of a Graph

- A set N of nodes, N is not empty
- A set N_0 of initial nodes, N_0 is not empty
- A set N_f of final nodes, N_f is not empty
- A set E of edges, each edge from one node to another
 - (n_i, n_j) , i is predecessor, j is successor

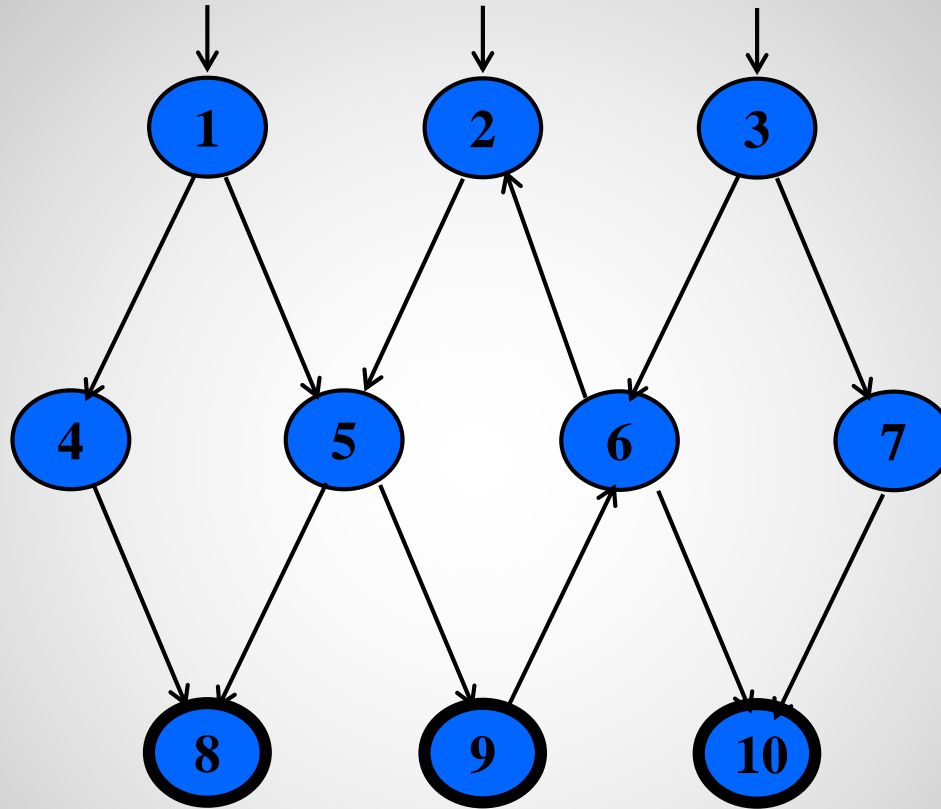
Three Example Graphs



$$N_0 = \{ 1 \}$$

$$N_f = \{ 4 \}$$

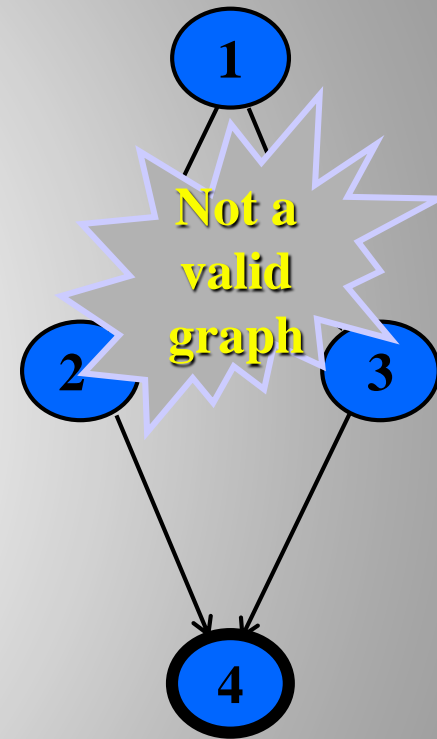
$$E = \{ (1,2), (1,3), \dots \}$$



$$N_0 = \{ 1, 2, 3 \}$$

$$N_f = \{ 8, 9, 10 \}$$

$$|E| = 12$$

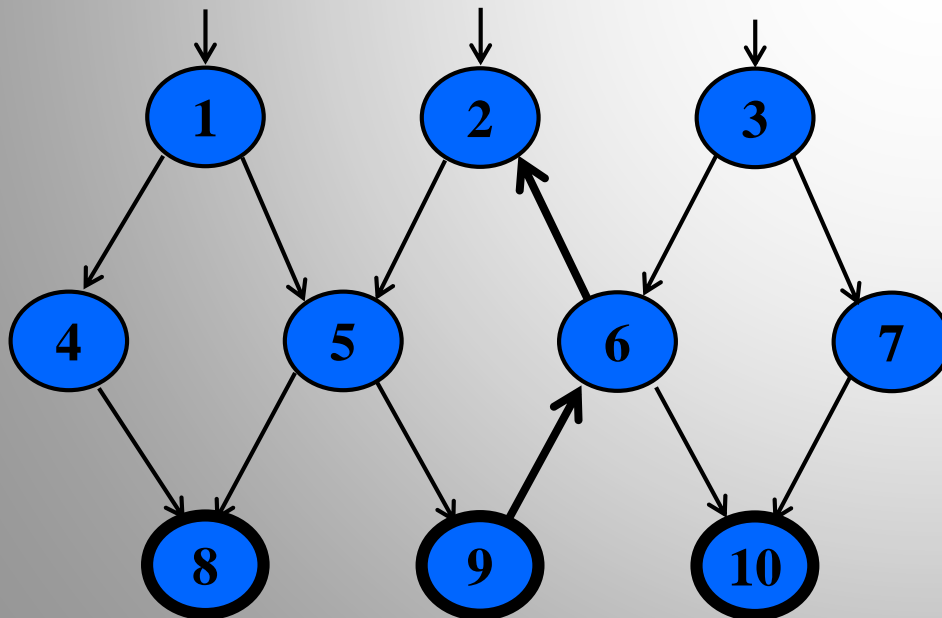


$$N_0 = \{ \}$$

$$N_f = \{ 4 \}$$

Paths in Graphs

- Path : A sequence of nodes – $[n_1, n_2, \dots, n_M]$
 - Each pair of nodes is an edge
- Length : The number of edges
 - A single node is a path of length 0
- Subpath : A subsequence of nodes in p is a subpath of p
- Reach (n) : Subgraph that can be reached from n (*includes the starting node*)



A Few Paths

[1, 4, 8]

[2, 5, 9, 6, 2]

[3, 7, 10]

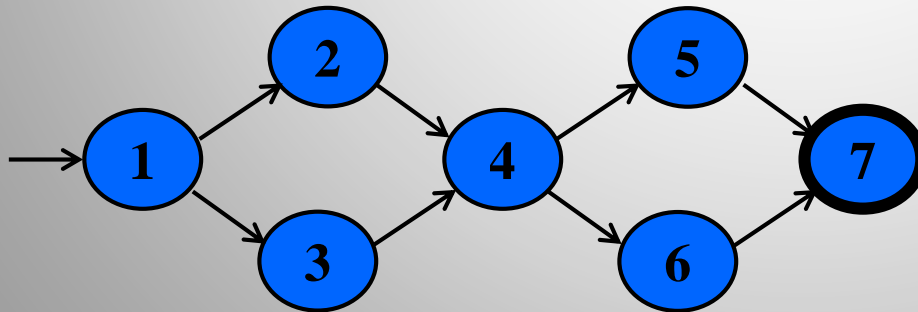
Reach (1) = { 1, 4, 5, 8, 9, 6, 2, 10 }

Reach (1, 3) = G

Reach([3,7]) = {3, 7, 10}

Test Paths and SESEs

- Test Path : A path that starts at an initial node and ends at a final node
- Test paths represent execution of test cases
 - Some test paths can be executed by many tests
 - Some test paths cannot be executed by any tests
- SESE graphs : All test paths start at a single node and end at another node
 - Single-entry, single-exit
 - N₀ and N_f have exactly one node



Double-diamond graph

Four test paths

[1, 2, 4, 5, 7]

[1, 2, 4, 6, 7]

[1, 3, 4, 5, 7]

[1, 3, 4, 6, 7]

Visiting and Touring

- Visit : A test path p visits node n if n is in p
A test path p visits edge e if e is in p
- Tour : A test path p tours subpath q if q is a subpath of p

Path [1, 2, 4, 5, 7]

Visits nodes 1, 2, 4, 5, 7

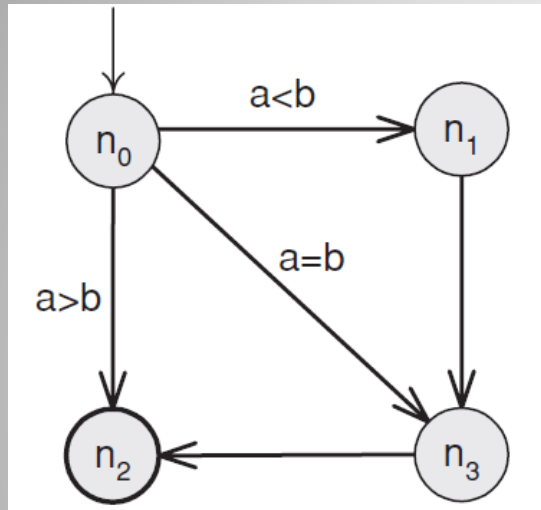
Visits edges (1, 2), (2, 4), (4, 5), (5, 7)

Tours subpaths [1, 2, 4], [2, 4, 5], [4, 5, 7], [1, 2, 4, 5], [2, 4, 5, 7]

Tests and Test Paths

- $\text{path}(t)$: The test path executed by test t
- $\text{path}(T)$: The set of test paths executed by the set of tests T

Test cases and Corresponding Test Paths



- Graph for testing the case with input integers a , b and output $(a+b)$

Test case $t_1 : (a=0, b=1)$ $\xrightarrow{\text{Map to}}$ [Test path $p_1 : n_0, n_1, n_3, n_2$]

Test case $t_2 : (a=1, b=1)$ $\xrightarrow{\text{Map to}}$ [Test path $p_2 : n_0, n_3, n_2$]

Test case $t_3 : (a=2, b=1)$ $\xrightarrow{\text{Map to}}$ [Test path $p_3 : n_0, n_2$]

Testing and Covering Graphs

- We use graphs in testing as follows :
 - Developing a model of the software as a graph
 - Requiring tests to visit or tour specific sets of nodes, edges or subpaths
- Test Requirements (TR) : Describe properties of test paths
 - ***Specific element of a software artifact that a test case must cover***
- Test Criterion : Rules that define test requirements

Testing and Covering Graphs

- **Structural Coverage Criteria** : Defined on a graph just in terms of nodes and edges
 - Has variously been called – statement coverage, block coverage, state coverage and **node coverage**
- **Data Flow Coverage Criteria** : Requires a graph to be annotated with references to variables

Structural Coverage Criteria

Node and Edge Coverage

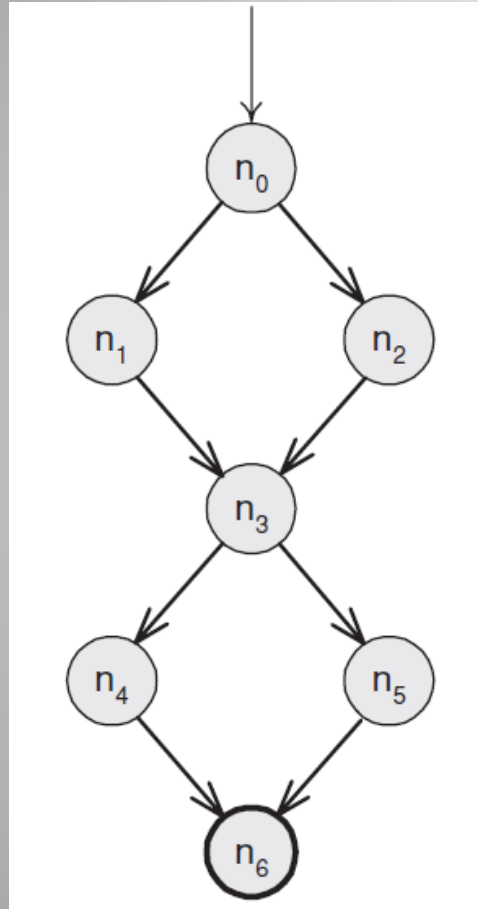
- The first (and simplest) two criteria require that each node and edge in a graph be executed

Node Coverage (NC) : Test set T satisfies node coverage on graph G iff for every syntactically reachable node n in N , there is some path p in $path(T)$ such that p visits n .

- This statement is a bit cumbersome, so we abbreviate it in terms of the set of test requirements

Node Coverage (NC) : TR contains each reachable node in G .

Node Coverage Definition Example



- $TR = \{n_0, n_1, n_2, n_3, n_4, n_5, n_6\}$
- Test path
 - $P_1 = [n_0, n_1, n_3, n_4, n_6]$
 - $P_2 = [n_0, n_2, n_3, n_5, n_6]$
- Therefore, if test set T contains $\{t_1, t_2\}$, where $\text{path}(t_1) = p_1$ and $\text{path}(t_2) = p_2$
- Then T satisfies node coverage on G

Node and Edge Coverage

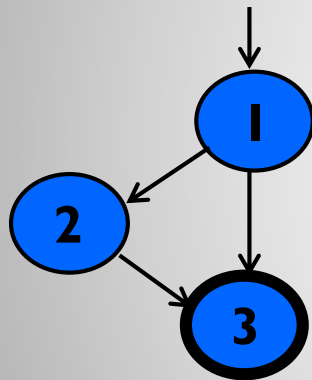
- Edge coverage is slightly stronger than node coverage

Edge Coverage (EC) : TR contains each reachable path of length up to l , inclusive, in G .

- The phrase “*length up to l* ” allows for graphs with one node and no edges

Node and Edge Coverage

- NC and EC are only different when there is an edge and another subpath between a pair of nodes (as in an “if-else” statement)



Node Coverage : $TR = \{ 1, 2, 3 \}$

Test Path = [1, 2, 3]

Edge Coverage : $TR = \{ (1, 2), (1, 3), (2, 3) \}$

Test Paths = [1, 2, 3]

[1, 3]

Covering Multiple Edges

- Edge-pair coverage requires pairs of edges, or subpaths of length 2

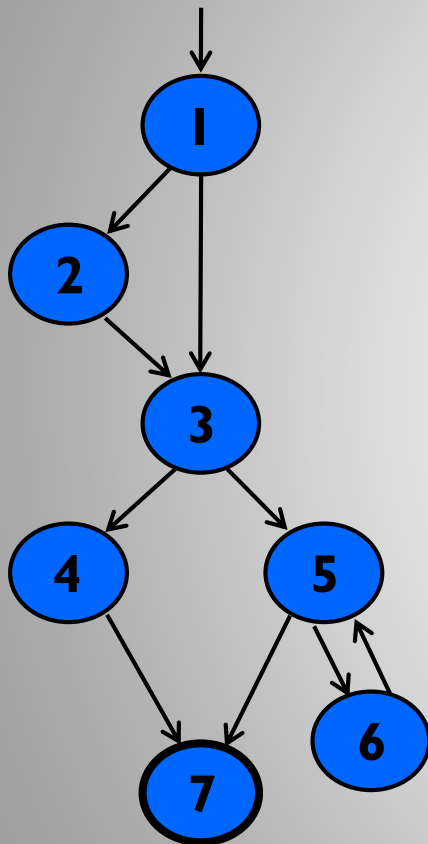
Edge-Pair Coverage (EPC) : TR contains each reachable path of length up to 2, inclusive, in G.

- The phrase “length up to 2” is used to include graphs that have less than 2 edges
- The logical extension is to require all paths ...

Complete Path Coverage (CPC) : TR contains all paths in G.

- Unfortunately, this is impossible if the graph has a loop, so a weak compromise is to make the tester decide which paths:

Structural Coverage Example



Node Coverage

TR = { 1, 2, 3, 4, 5, 6, 7 }

Test Paths: [1, 2, 3, 4, 7] [1, 2, 3, 5, 6, 5, 7]

Edge Coverage

TR = { (1,2), (1,3), (2,3), (3,4), (3,5), (4,7), (5,6), (5,7), (6,5) }

Test Paths: [1, 2, 3, 4, 7] [1, 3, 5, 6, 5, 7]

Edge-Pair Coverage

TR = { [1,2,3], [1,3,4], [1,3,5], [2,3,4], [2,3,5], [3,4,7], [3,5,6], [3,5,7], [5,6,5], [6,5,6], [6,5,7] }

Test Paths: [1, 2, 3, 4, 7] [1, 2, 3, 5, 7] [1, 3, 4, 7]
[1, 3, 5, 6, 5, 6, 5, 7]

Complete Path Coverage

Test Paths: [1, 2, 3, 4, 7] [1, 2, 3, 5, 7] [1, 2, 3, 5, 6, 5, 7]
[1, 2, 3, 5, 6, 5, 6, 5, 7] [1, 2, 3, 5, 6, 5, 6, 5, 6, 5, 7] ...

Loops in Graphs

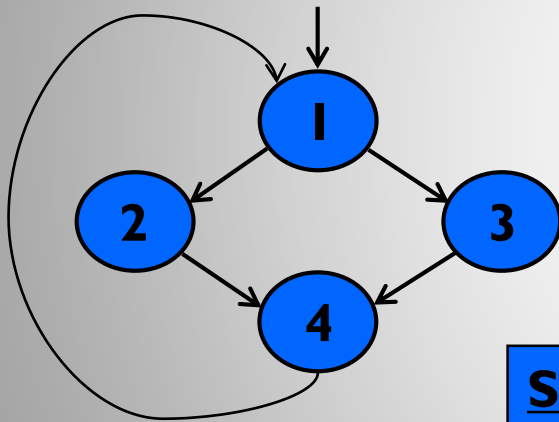
- If a graph contains a loop, it has an infinite number of paths
- Thus, CPC is not feasible
- Attempts to “deal with” loops:
 - 1970s : Execute cycles once ([4, 5, 4] in previous example, informal)
 - 1980s : Execute each loop, exactly once (formalized)
 - 1990s : Execute loops 0 times, once, more than once (informal description)
 - 2000s : Prime paths

Simple Paths and Prime Paths

- Simple Path: A path from node n_i to n_j is simple **if no node appears more than once**, except possibly the first and last nodes are the same
 - No internal loops
 - A loop is a simple path
- For a coverage criterion, we would like to avoid enumerating the entire set of simple paths
 - List only maximal length simple paths
- Prime Path: A simple path that does not appear as a proper subpath of any other simple path
 - **Maximal length simple path**

Simple Paths and Prime Paths

- Prime Path : A simple path that does not appear as a proper subpath of any other simple path
 - **Maximal length simple path**
 - Reduces the number of test cases for path coverage



Simple Paths : [1,2,4,1], [1,3,4,1], [2,4,1,2], [2,4,1,3], [3,4,1,2], [3,4,1,3], [4,1,2,4], [4,1,3,4], [1,2,4], [1,3,4], [2,4,1], [3,4,1], [4,1,2], [4,1,3], [1,2], [1,3], [2,4], [3,4], [4,1], [1], [2], [3], [4]

Prime Paths : [2,4,1,2], [2,4,1,3], [1,3,4,1], [1,2,4,1], [3,4,1,2], [4,1,3,4], [4,1,2,4], [3,4,1,3]

Prime Path Coverage

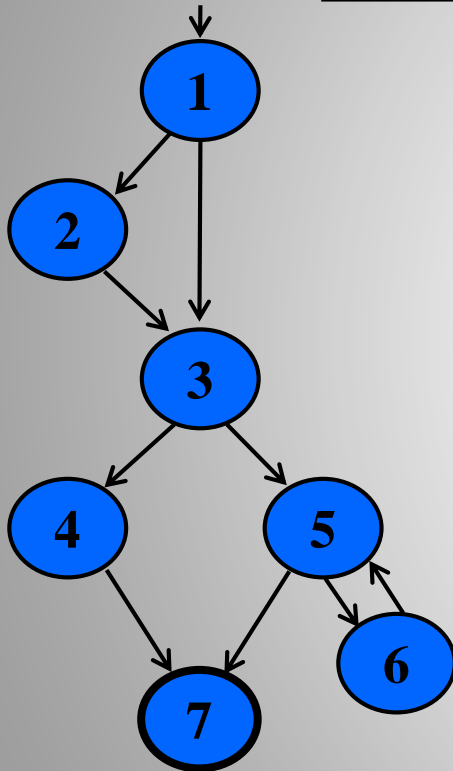
- A simple, elegant and finite criterion that requires loops to be executed as well as skipped

Prime Path Coverage (PPC) : TR contains each prime path in G.

- Will tour all paths of length 0, 1, ...
- That is, it subsumes node and edge coverage
- PPC does NOT subsume EPC
 - If a node n has an edge to itself, EPC will require $[n, n, m]$
 - $[n, n, m]$ is not prime

Simple & Prime Path Example

Simple
paths



Len 0

[1]
[2]
[3]
[4]
[5]
[6]
[7] !

Len 1

[1, 2]
[1, 3]
[2, 3]
[3, 4]
[3, 5]
[4, 7] !
[5, 7] !
[5, 6]
[6, 5]

Len 2

[1, 2, 3]
[1, 3, 4]
[1, 3, 5]
[2, 3, 4]
[2, 3, 5]
[3, 4, 7] !
[3, 5, 7] !
[3, 5, 6] !
[5, 6, 5] *
[6, 5, 7] !
[6, 5, 6] *

Len 3

[1, 2, 3, 4]
[1, 2, 3, 5]
[1, 3, 4, 7] !
[1, 3, 5, 7] !
[1, 3, 5, 6] !
[2, 3, 4, 7] !
[2, 3, 5, 6] !
[2, 3, 5, 7] !

Len 4

[1, 2, 3, 4, 7] !
[1, 2, 3, 5, 7] !
[1, 2, 3, 5, 6] !

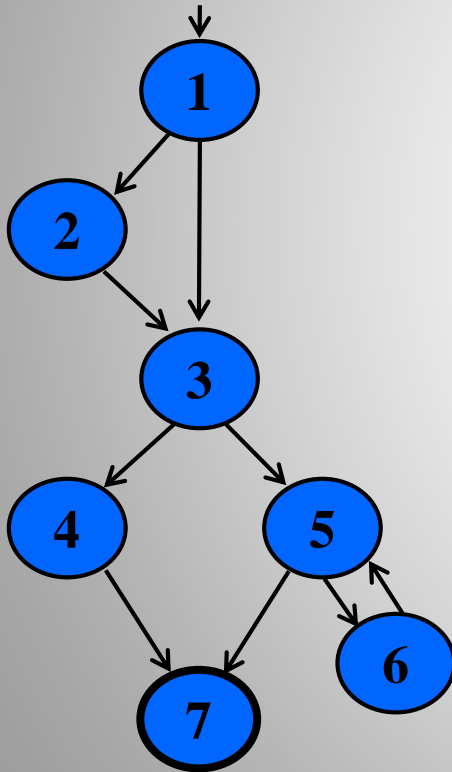
Prime Paths

6! means paths

is path
es

Prime Path Example

- The previous example has 38 simple paths
- Only nine *prime paths*



Prime Paths

[1, 2, 3, 4, 7]

[1, 2, 3, 5, 7]

[1, 2, 3, 5, 6]

[1, 3, 4, 7]

[1, 3, 5, 7]

[1, 3, 5, 6]

[6, 5, 7]

[6, 5, 6]

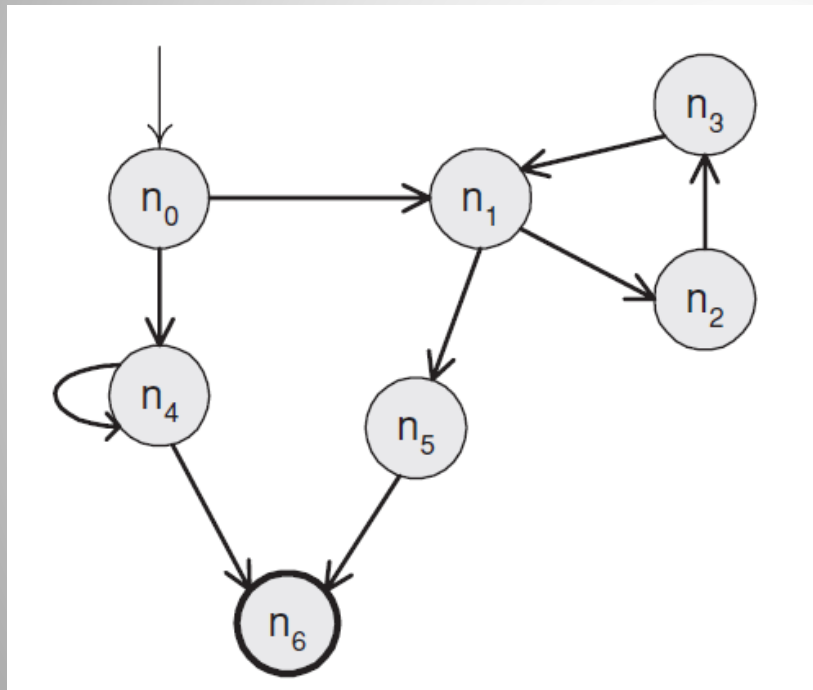
[5, 6, 5]

**Execute
loop 0 times**

**Execute
loop once**

**Execute loop
more than once**

Prime Path Example



Simple paths of length 0 (7):

- 1) [0]
- 2) [1]
- 3) [2]
- 4) [3]
- 5) [4]
- 6) [5]
- 7) [6] !

Simple paths of length 1 (9):

- 8) [0, 1]
- 9) [0, 4]
- 10) [1, 2]
- 11) [1, 5]
- 12) [2, 3]
- 13) [3, 1]
- 14) [4, 4] *
- 15) [4, 6] !
- 16) [5, 6] !

Prime Path Example (cont.)

Simple paths of length 2 (8):

17) [0, 1, 2]
18) [0, 1, 5]
19) [0, 4, 6] !
20) [1, 2, 3]
21) [1, 5, 6] !
22) [2, 3, 1]
23) [3, 1, 2]
24) [3, 1, 5]

Simple paths of length 3 (7):

25) [0, 1, 2, 3] !
26) [0, 1, 5, 6] !
27) [1, 2, 3, 1] *
28) [2, 3, 1, 2] *
29) [2, 3, 1, 5]
30) [3, 1, 2, 3] *
31) [3, 1, 5, 6] !

Prime paths of length 4 (1):

32) [2, 3, 1, 5, 6]!

- There are 8 prime paths

14) [4, 4] *
19) [0, 4, 6] !
25) [0, 1, 2, 3] !
26) [0, 1, 5, 6] !
27) [1, 2, 3, 1] *
28) [2, 3, 1, 2] *
30) [3, 1, 2, 3] *
32) [2, 3, 1, 5, 6]!

Round Trips

- Round-Trip Path : *A prime path that starts and ends at the same node*

Simple Round Trip Coverage (SRTC) : TR contains at least one round-trip path for each reachable node in G that begins and ends a round-trip path.

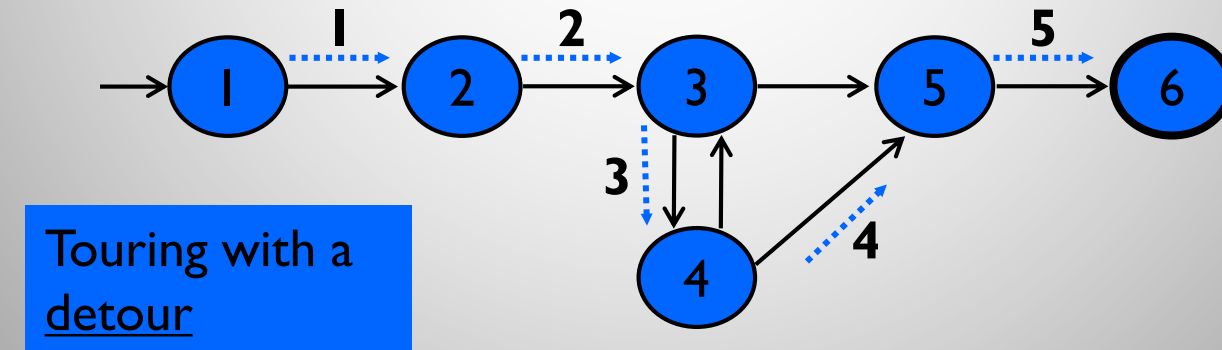
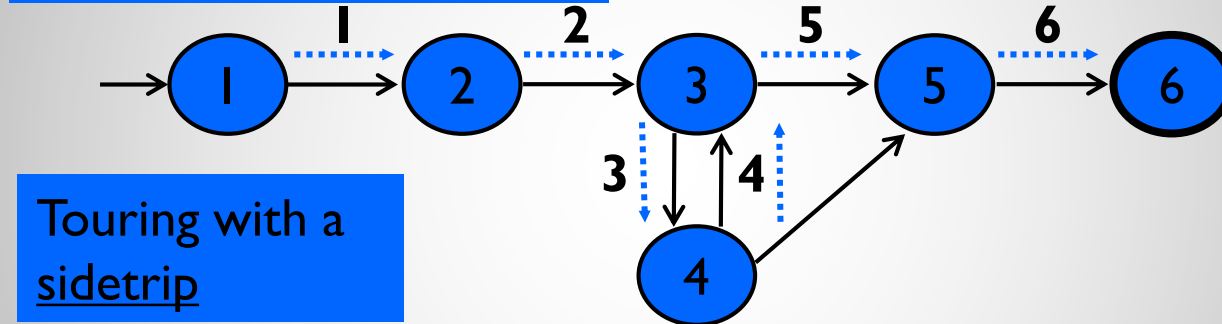
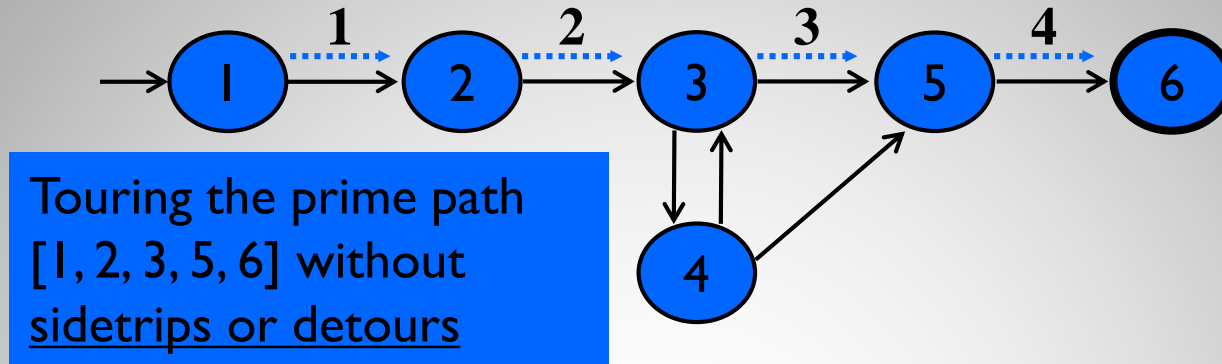
Complete Round Trip Coverage (CRTC) : TR contains all round-trip paths for each reachable node in G .

- These criteria omit nodes and edges that are not in round trips
- That is, they do not subsume edge-pair, edge, or node coverage

Touring, Sidetrips and Detours

- Prime paths do not have internal loops ... test paths might
- Tour : *A test path p tours subpath q if q is a subpath of p*
- Tour With Sidetrips : *A test path p tours subpath q with sidetrips iff every edge in q is also in p in the same order*
 - The tour can include a sidetrip, as long as it comes back to the same node
- Tour With Detours : *A test path p tours subpath q with detours iff every node in q is also in p in the same order*
 - The tour can include a detour from node ni , as long as it comes back to the prime path at a successor of ni

Sidetrrips and Detours Example

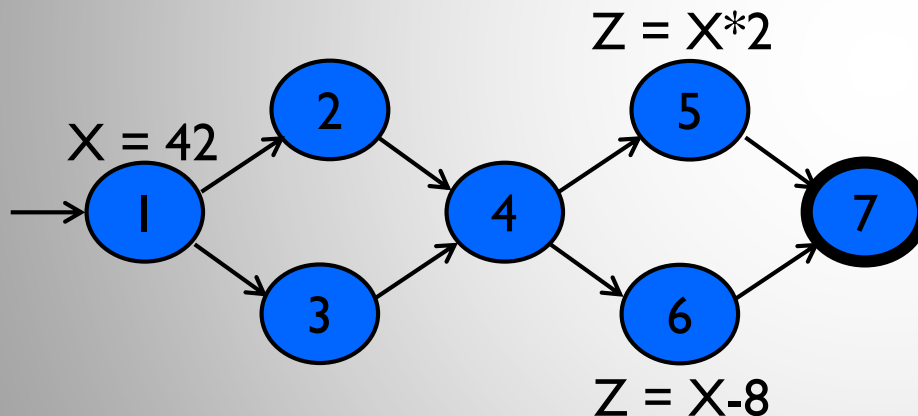


Data Flow Coverage Criteria

Data Flow Criteria

Goal: Try to ensure that values are computed and used correctly

- Definition (def) : A location where a value for a variable is stored into memory
- Use : A location where a variable's value is accessed



Defs: def (1) = {X}

def (5) = {Z}

def (6) = {Z}

Uses: use (5) = {X}

use (6) = {X}

The values given in defs should reach at least one, some, or all possible uses

DU Pairs and DU Paths

- $\text{def}(n)$ or $\text{def}(e)$: The set of variables that are defined by node n or edge e
 - $\text{use}(n)$ or $\text{use}(e)$: The set of variables that are used by node n or edge e
-
- DU pair : A pair of locations (l_i, l_j) such that a variable v is defined at l_i and used at l_j
-
- du-path : A simple subpath that is def-clear with respect to v from a def of v to a use of v
 - $\text{du}(n_i, n_j, v)$ – the set of du-paths from n_i to n_j
 - $\text{du}(n_i, v)$ – the set of du-paths that start at n_i

Data Flow Test Criteria

- First, we make sure every def reaches a use

All-defs coverage (ADC) : For each set of du-paths $S = du(n, v)$, TR contains at least one path d in S .

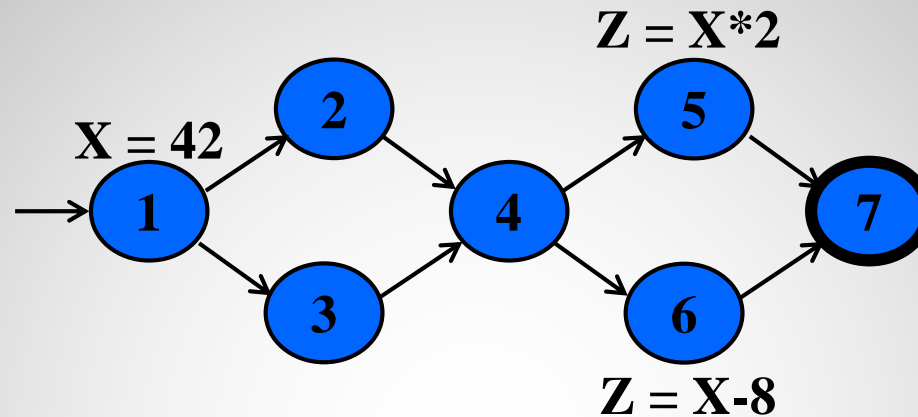
- Then we make sure that every def reaches all possible uses

All-uses coverage (AUC) : For each set of du-paths to uses $S = du(n_i, n_j, v)$, TR contains at least one path d in S .

- Finally, we cover all the paths between defs and uses

All-du-paths coverage (ADUPC) : For each set $S = du(n_i, n_j, v)$, TR contains every path d in S .

Data Flow Testing Example



All-defs for X

[1, 2, 4, 5]

All-uses for X

[1, 2, 4, 5]

[1, 2, 4, 6]

All-du-paths for X

[1, 2, 4, 5]

[1, 3, 4, 5]

[1, 2, 4, 6]

[1, 3, 4, 6]

Exercise

Graph I.

$$N = \{0, 1, 2, 3, 4, 5, 6, 7\}$$

$$N_0 = \{0\}$$

$$N_f = \{7\}$$

$$E = \{(0, 1), (1, 2), (1, 7), (2, 3), (2, 4), (3, 2), (4, 5), (4, 6), (5, 6), (6, 1)\}$$

$$def(0) = def(3) = use(5) = use(7) = \{x\}$$

- (a) Draw the graph.
- (b) List all of the du-paths with respect to x . (Note: Include all du-paths, even those that are subpaths of some other du-path).

Graph Coverage Criteria Subsumption

