

## Basic Stats - 2

Given Data:

No. of Samples = 15

data =

$x_i$	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
1.13	$(1.13 - 1.24) = -0.11$	0.012
1.55	0.31	0.096
1.43	0.19	0.036
0.42	-0.32	0.102
1.25	0.01	0
1.36	0.12	0.014
1.32	0.08	0.06
0.85	-0.39	0.152
1.07	-0.17	0.028
1.48	0.24	0.057
1.20	-0.04	0.01
1.33	0.09	0.08
1.18	-0.06	0.03
1.22	-0.02	0
1.44	0.05	0.02

$$\sum x_i = 18.58$$

~~$$\sum (x_i - \bar{x})$$~~

$$\sum (x_i - \bar{x})^2 = 0.522$$

$$\bar{x} = \frac{\sum x_i}{n}$$

$$= \frac{18.58}{15} = 1.24$$

$$\text{Sample deviation (S)} = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}}$$

$$= \sqrt{\frac{0.522}{14}}$$

$$\approx 0.19$$

$$s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n}}$$

$$= \sqrt{\frac{0.522}{15}}$$

$$\approx 0.18$$

a. 99% Confidence using Sample Standard deviation.

$$t = 2.977 \dots (\text{from table})$$

$$\text{Error Margin} = t \times \frac{s}{\sqrt{n}}$$

$$= 2.977 \times \frac{0.18}{\sqrt{15}}$$

$$= 0.14$$

$$\text{Confidence Interval} = (\bar{x} - E, \bar{x} + E)$$

$$= (1.24 - 0.14, 1.24 + 0.14)$$

$$\boxed{CI = (1.1, 1.38)}$$

b. 99% Confidence using Population Std. deviation.

$$Z = 2.576 \quad \dots \quad (\text{from table})$$

$$\text{Error Margin} = \frac{Z \times \sigma}{\sqrt{n}}$$

$$= \frac{2.576 \times 0.18}{\sqrt{15}}$$

$$= 0.11$$

$$\text{Confidence Interval} = (\bar{x} - E, \bar{x} + E)$$

$$= (1.24 - 0.11, 1.24 + 0.11)$$

$$\boxed{CI = (1.13, 1.35)}$$