

Problem 1:

(2) : inorder traversal of BST is always sorted

(4)(5): Tree is empty or only root exists

(6)(11): preorder: print(value), traverse(left), traverse(right)  
inorder: traverse(left), print(value), traverse(right)  
postorder: traverse(left), traverse(right), print(value)

(12):  $2^{(L-1)}$

(13):  $P=Q+1$

```
int BinarySearchTree::getMax(Node *ptr) {
    if (ptr == nullptr)
        return(-1); // empty
    while ( ptr->right != nullptr )
        ptr = ptr->right;
    return(ptr->value);
}
```

```
void BinarySearchTree::insert(int value, node * ptr) {
    if (ptr == nullptr) {
        ptr = new node(value);
    }else if (value < ptr->value)
        insert(value, tree->left);
    else if (value > ptr->value)
        insert(value, tree->right);
}
```

```
bool BinarySearchTree::find(int value, node * ptr) {
    if (ptr == nullptr) return false;
    if(ptr->value == value) return true;
    if (value < ptr->value)
        find(value, tree->left);
    else if (value > tree->value)
        insert(value, tree->right);
}
```

```
bool BinarySearchTree::remove()
//if the node to_be_removed has no child or have only one child
if (to_be_removed->left==NULL|| to_be_removed->right==NULL){
    TreeNode<ItemType,cmp>*new_child;
    if (to_be_removed->left==NULL)
        new_child=to_be_removed->right;
    else new_child=to_be_removed->left;
```

```

    if (parent==NULL)
        root=new_child;
    else if(parent->left==to_be_removed)
        parent->left=new_child;
    else parent->right=new_child;
    delete to_be_removed;
    return;
}
//Neither subtree is empty
//Find the largest element of the left subtree
TreeNode<ItemType,cmp>*largest_parent=to_be_removed;
TreeNode<ItemType,cmp>*largest=to_be_removed->left;
while (largest->right!=NULL){
    largest_parent=largest;
    largest=largest->right;
}
//largest contains the largest child in the left subtree
//move contents, unlink child
to_be_removed->data=largest->data;
if (largest_parent==to_be_removed)
    largest_parent->left=largest->left;
else largest_parent->right=largest->left;
delete largest;

```

10-17

20-24

10 11 12 13 14 15 16 17 -1 -1

no room left in hash table!!!

no room left in hash table!!!

10 11 12 13 14 15 16 17 20 21

max insert/buckets

speed  $O(1)$ ,  $O(\log n)$

load factor unlimited space

waste memory, use as much as needed

no ordering, ordering