#### **Table of Contents**

A.1		. 1
A.2		. 2
A.3	(x1)	. 2
A.3	(x2)	. 3
A.3	(x3)	. 4
A.4	(x1a)	. 5
A.4	(x1b)	. 6
A.4	(x1c)	. 7
A.4	(x1d)	. 8
A.4	(x2a)	. 9
A.4	(x2b)	10
A.4	(x2c)	11
A.4	(x2d)	12
A.4	(x3a)	13
A.4	(x3b)	14
A.4	(x3c)	15
A.4	(x3d)	16
A5	(x1)	17
A5	(x2)	17
A5	(x3)	18
A6	(x1a)	18
A6	(x1b)	19
A6	(x1c)	20
A6	(x1d)	21
A6	(x2a)	22
A6	(x2b)	23
A6	(x2c)	24
A6	(x2d)	25
A6	(x3a)	26
A6	(x3b)	27
A6	(x3c)	28
A6	(x3d)	29
B1		30
B2		30
В3		30
B4		30
B5		30
B6		31
В7		31

### **A.1**

```
I = imread("A1.jpg");
imshow(I)
```

X <sub>1</sub> (t)= cos(張t)+迄ros(犹t) = 名e <sup>j 麗t</sup> +名e <sup>j 羅t</sup> +名e <sup>-j 蓋t</sup> +名e <sup>j 蓋t</sup>					W. = 7/10	
~~	D3= 1/2	~~~	0, = 1/4	GCF = T/10	To = 27 = 20	
					for 30, n=3	
					for the n=1	

### **A.2**

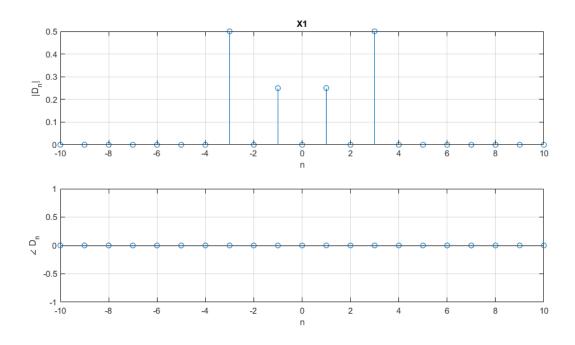
```
I2 = imread("A2.jpg");
imshow(I2)
```

x <sub>2</sub> (+)		<u>X<sub>5</sub>(+)</u>
To = 20		To = 40
Wo = 27 = T/10		$W_0 = \frac{2\pi}{90} = \frac{7}{20}$
Pn= 1/20 5(1) e-jk 1/4 dt		Pn= 40 Sa) eix 36t dt
= 1/20 [ -10 5 ev du]	U= - Tjkt du= - Tjk	$= V_{40} \left[ -\frac{2\sigma}{\pi_0^2 K} \int_{-\infty}^{\infty} e^{u} du \right] \qquad V = -\frac{\pi_0^2 K^4}{2\sigma}  du = -\frac{\pi_0^2 K}{2\sigma}$
= 1/20 [-10 (ev  -5)]		$= \frac{1}{40} \left( \frac{20}{\pi_1^2 \pi} \right) \left[ e^{v} \right]_{-5}^{5}$
= -10 [e snjk   e snjk   e snjk		$= -\frac{20}{40\pi i k} \left( e^{-\frac{5\pi i k}{20}} - e^{-\frac{5\pi i k}{6\pi}} \right)$
$= -\frac{1}{2\pi i} \kappa \left[ e^{-\frac{\pi i k}{2}} - e^{\frac{\pi i \kappa}{2}} \right]$		$= -\frac{1}{2X_{jk}} \left( e^{\frac{\pi j k}{4k}} - e^{\frac{\pi j k}{4k}} \right)$
	$\sin(x) = \frac{e^{x} - e^{-x}}{j^2}$	$= \underbrace{e^{\frac{\pi_{3}k}{q_{1}}} - e^{-\frac{\pi_{3}k}{q_{1}}}}_{2\pi_{3}k}$
= \(\lambda\pi \sin\left(\frac{\sin}{\sin}\right)		$= \frac{1}{\sqrt{n}} \sin\left(\frac{n\pi}{n}\right)$
~~~~		~~~

# A.3 (x1)

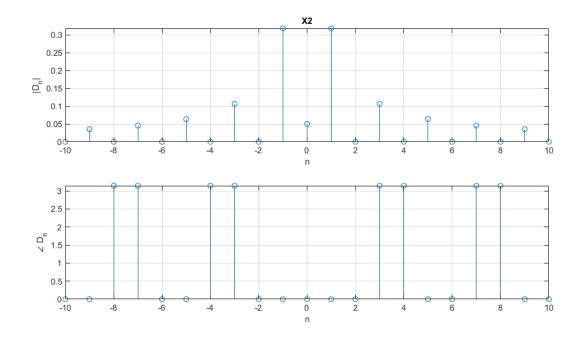
```
\begin{array}{lll} n = (-10:10); \\ D_{-}n = (n==1).*(1/4)+(n==-1).*(1/4)+(n==3).*(1/2)+(n==-3).*(1/2); \\ \text{subplot}(2,1,1); \\ \text{stem}(n,abs(D_{-}n)); \\ \text{title } ('X1'); \\ \text{xlabel } ('n'); \\ \text{ylabel } ('|D_{-}n|'); \end{array}
```

```
grid;
subplot(2,1,2);
stem(n,angle(D_n));
xlabel('n');
ylabel('\angle D_n');
grid;
```



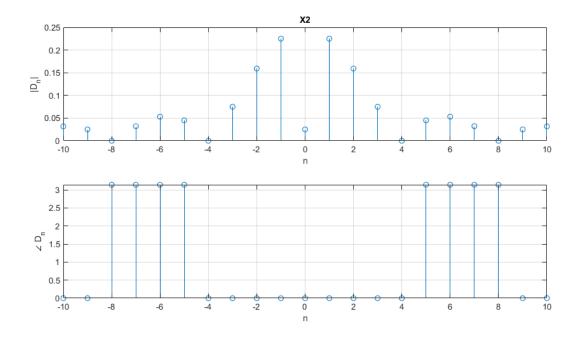
## A.3 (x2)

```
n=(-10:10);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.05;
else
D_n((i+abs(min(n))+1))=(sin((i*pi)/2))./(i*pi);
end
end
subplot (2,1,1);
stem(n,abs(D_n));
title ('X2');
xlabel ('n'); ylabel ('D_n');
grid;
subplot(2,1,2);
stem(n,angle(D_n));
xlabel('n');
ylabel('\angle D_n');
grid;
```



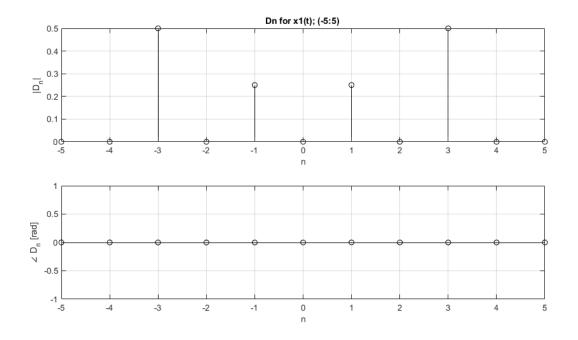
## A.3 (x3)

```
n=(-10:10);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.025;
D_n((i+abs(min(n))+1))=(sin((i*pi)/4))./(i*pi);
end
end
subplot (2,1,1);
stem(n,abs(D_n));
title ('X2');
xlabel ('n'); ylabel ('|D_n|');
grid;
subplot(2,1,2);
stem(n,angle(D_n));
xlabel('n');
ylabel('\angle D_n');
grid;
```



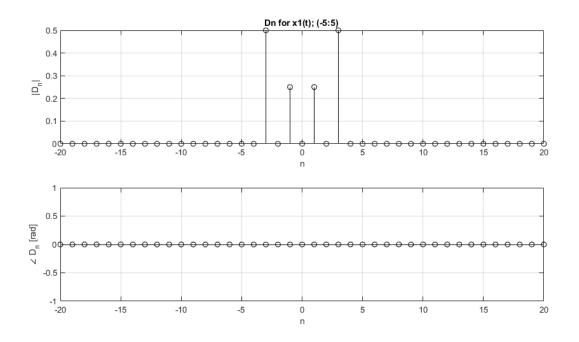
## A.4 (x1a)

```
n = (-5:5);
D_n = (n==1).*(1/4)+(n==-1).*(1/4)+(n==3).*(1/2)+(n==-3).*(1/2);
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x1(t); (-5:5) ');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



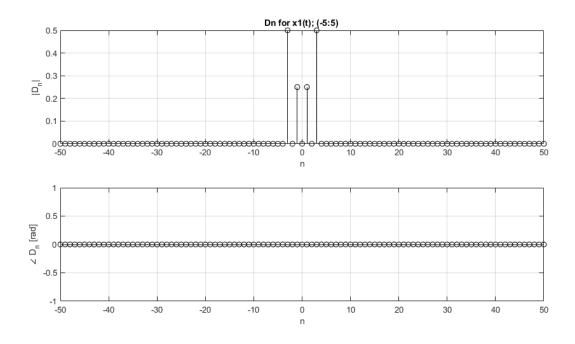
## A.4 (x1b)

```
n = (-20:20);
D_n = (n==1).*(1/4)+(n==-1).*(1/4)+(n==3).*(1/2)+(n==-3).*(1/2);
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x1(t); (-5:5) ');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



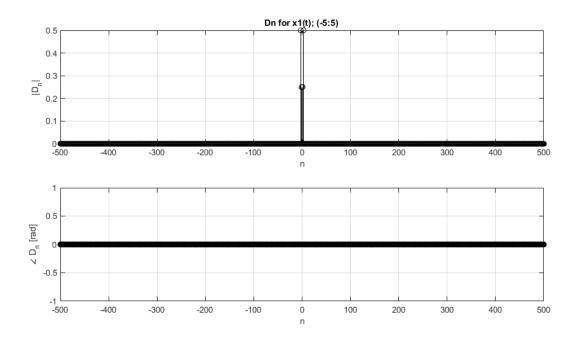
## A.4 (x1c)

```
n = (-50:50);
D_n = (n==1).*(1/4)+(n==-1).*(1/4)+(n==3).*(1/2)+(n==-3).*(1/2);
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x1(t); (-5:5) ');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



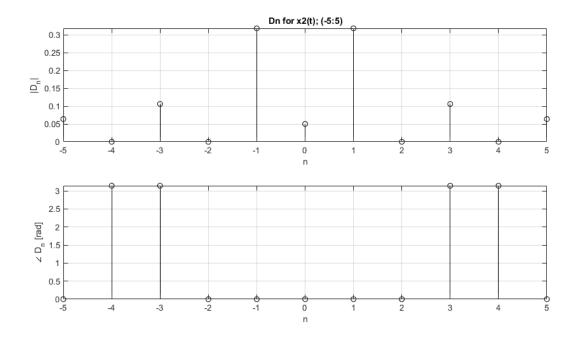
## A.4 (x1d)

```
n = (-500:500);
D_n = (n==1).*(1/4)+(n==-1).*(1/4)+(n==3).*(1/2)+(n==-3).*(1/2);
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x1(t); (-5:5) ');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



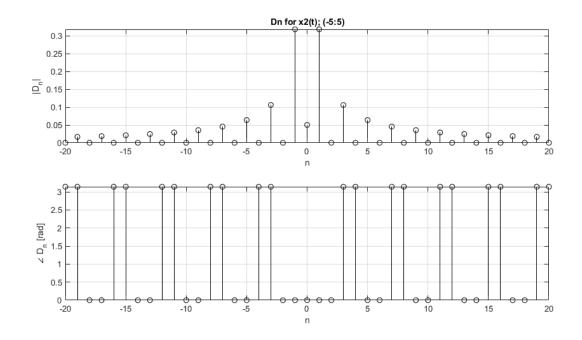
## A.4 (x2a)

```
n=(-5:5);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.05;
D_n((i+abs(min(n))+1))=(sin((i*pi)/2))./(i*pi);
end
end
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x2(t); (-5:5)');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



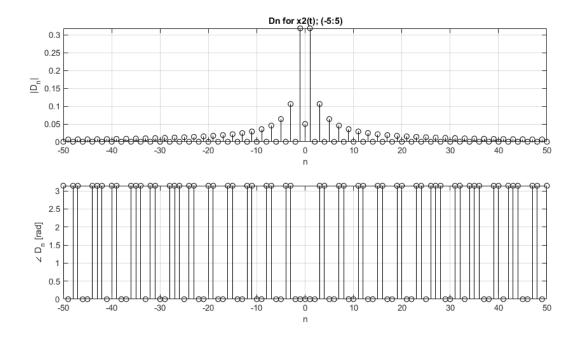
## A.4 (x2b)

```
n=(-20:20);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.05;
D_n((i+abs(min(n))+1))=(sin((i*pi)/2))./(i*pi);
end
end
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x2(t); (-5:5)');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



## A.4 (x2c)

```
n=(-50:50);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.05;
D_n((i+abs(min(n))+1))=(sin((i*pi)/2))./(i*pi);
end
end
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x2(t); (-5:5)');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```

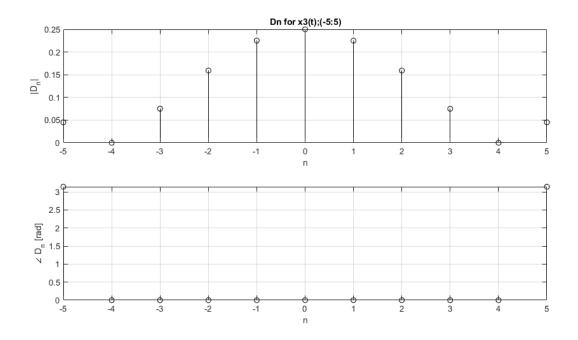


## A.4 (x2d)

```
n=(-500:500);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.05;
D_n((i+abs(min(n))+1))=(sin((i*pi)/2))./(i*pi);
end
end
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x2(t); (-5:5)');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
clf;
```

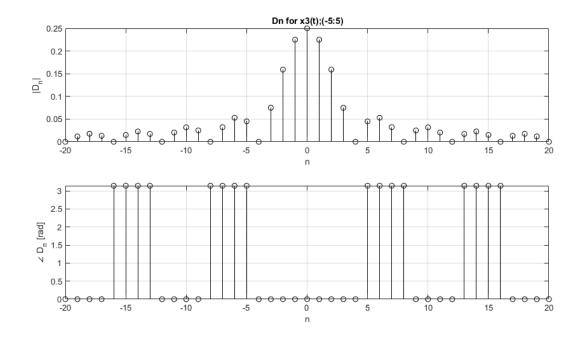
## A.4 (x3a)

```
n=(-5:5);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.25;
D_n((i+abs(min(n))+1))=(sin((i*pi)/4))./(i*pi);
end
end
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x3(t);(-5:5)');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



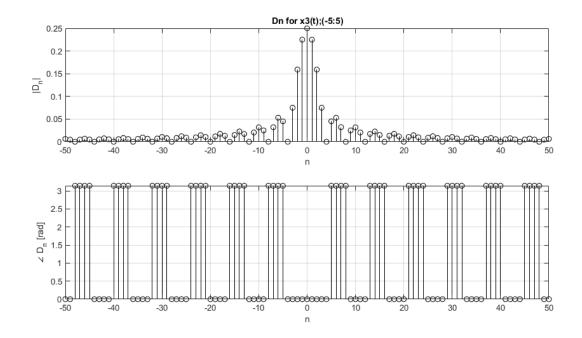
## A.4 (x3b)

```
n=(-20:20);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.25;
D_n((i+abs(min(n))+1))=(sin((i*pi)/4))./(i*pi);
end
end
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x3(t);(-5:5)');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



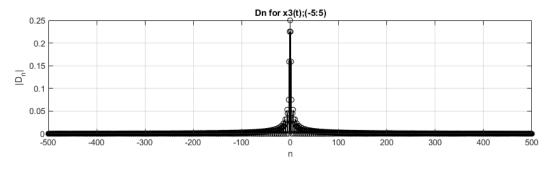
## A.4 (x3c)

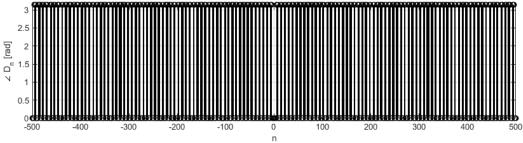
```
n=(-50:50);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.25;
D_n((i+abs(min(n))+1))=(sin((i*pi)/4))./(i*pi);
end
end
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x3(t);(-5:5)');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```



## A.4 (x3d)

```
n=(-500:500);
D_n = n;
for i=min(n):1:max(n)
if i==0
D_n((i+abs(min(n))+1))=0.25;
D_n((i+abs(min(n))+1))=(sin((i*pi)/4))./(i*pi);
end
end
subplot(2,1,1);
stem(n,abs(D_n), 'k');
xlabel('n');
ylabel('|D_n|');
title('Dn for x3(t);(-5:5)');
grid;
subplot(2,1,2);
stem(n,angle(D_n),'k');
xlabel('n');
ylabel('\angle D_n [rad]');
grid;
```





## A5 (x1)

```
t = -300:1:300;
x = 0;
for n = -5:5
D_n = 0;
if (n==3 || n==-3)
D_n=(1/2);
end
if (n==1||n==-1)
D_n=(1/4);
end
x=x+D_n.*(exp(sqrt(-1)*n*(pi/10)*t));
end
```

## A5 (x2)

```
D_n=[-50:50];
nleftlim = -50;
nrightlim = 50;
x = 50+1;
if n == 0,
D_n(x) = 0.5;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.5)./(n.*pi));
end
n = [nleftlim:nrightlim];
W0 = pi/10; t = -300:300;
s = 300+1;
b=length(t);
```

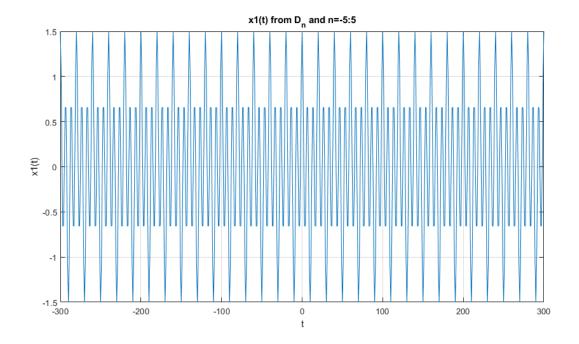
```
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*li*W0*t));
end
end
```

### A5 (x3)

```
D_n = [-500:500];
nleftlim = -500; nrightlim = 500; x = 500+1;
if n == 0,
D_n(x) = 0.5;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.25)./(n.*pi));
n = [nleftlim:nrightlim];
W0 = pi/20; t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
```

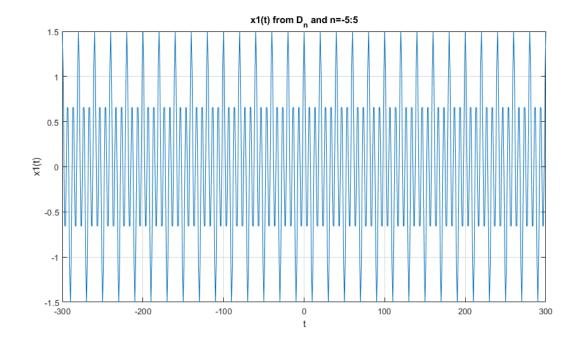
### A6 (x1a)

```
clf;
t = -300:1:300;
x = 0;
for n = -5:5
D_n = 0;
if (n==3 | n==-3)
D_n = (1/2);
end
if (n==1 | n==-1)
D_n = (1/4);
x=x+D_n.*(exp(sqrt(-1)*n*(pi/10)*t));
end
plot(t,x);
xlabel('t');
ylabel('x1(t)');
title('x1(t) from D_n and n=-5:5');
grid;
```



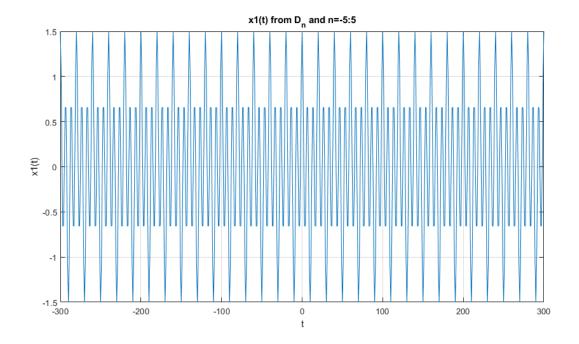
## A6 (x1b)

```
t = -300:1:300;
x = 0;
for n = -20:20
D_n = 0;
if (n==3 || n==-3)
D_n=(1/2);
end
if (n==1||n==-1)
D_n=(1/4);
end
x=x+D_n.*(exp(sqrt(-1)*n*(pi/10)*t));
end
plot(t,x);
xlabel('t');
ylabel('x1(t)');
title('x1(t) from D_n and n=-5:5');
grid;
```



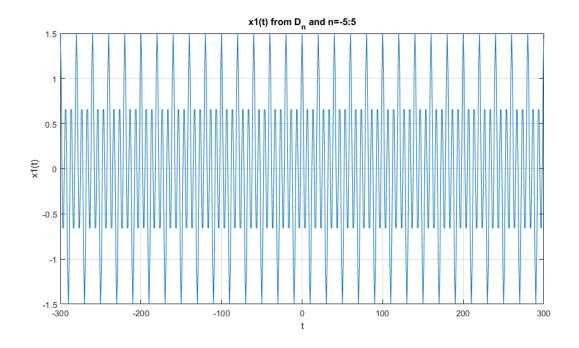
## A6 (x1c)

```
t = -300:1:300;
x = 0;
for n = -50:50
D_n = 0;
if (n==3 || n==-3)
D_n=(1/2);
end
if (n==1||n==-1)
D_n=(1/4);
end
x=x+D_n.*(exp(sqrt(-1)*n*(pi/10)*t));
end
plot(t,x);
xlabel('t');
ylabel('x1(t)');
title('x1(t) from D_n and n=-5:5');
grid;
```



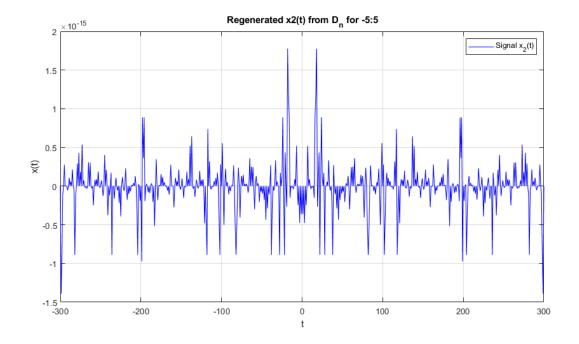
## A6 (x1d)

```
t = -300:1:300;
x = 0;
for n = -500:500
D_n = 0;
if (n==3 || n==-3)
D_n=(1/2);
end
if (n==1||n==-1)
D_n=(1/4);
end
x=x+D_n.*(exp(sqrt(-1)*n*(pi/10)*t));
end
plot(t,x);
xlabel('t');
ylabel('x1(t)');
title('x1(t) from D_n and n=-5:5');
grid;
```



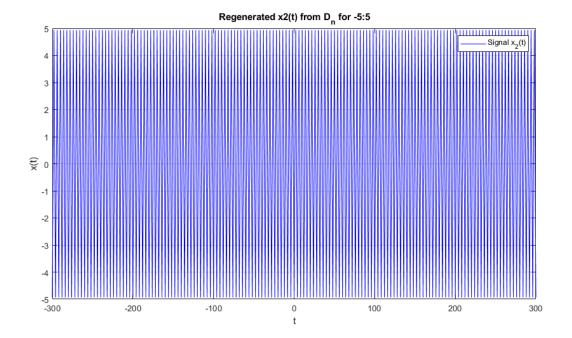
## A6 (x2a)

```
D_n=[-5:5]; nleftlim = -5;
nrightlim = 5;
x = 5+1;
if n == 0,
D_n(x) = 0.05;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.5)./(n.*pi));
end
n = [nleftlim:nrightlim];
W0 = pi/10;
t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
t=-300:300;
plot(t,real(x),'b');
ylabel('x(t)');
xlabel('t');
title('Regenerated x2(t) from D_n for -5:5');
legend('Signal x_2(t)');
grid;
```



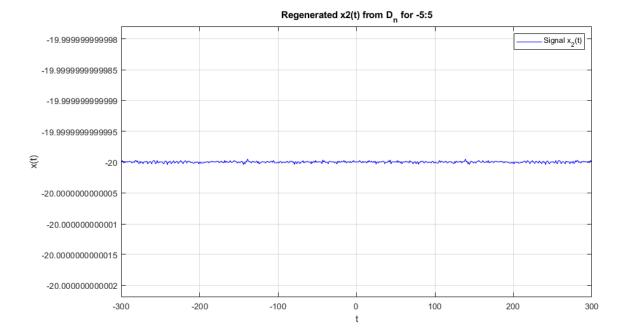
## A6 (x2b)

```
D_n=[-20:20]; nleftlim = -20;
nrightlim = 20;
x = 20+1;
if n == 0,
D_n(x) = 0.05;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.5)./(n.*pi));
end
n = [nleftlim:nrightlim];
W0 = pi/10;
t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
t=-300:300;
plot(t,real(x),'b');
ylabel('x(t)');
xlabel('t');
title('Regenerated x2(t) from D_n for -5:5');
legend('Signal x_2(t)');
grid;
```



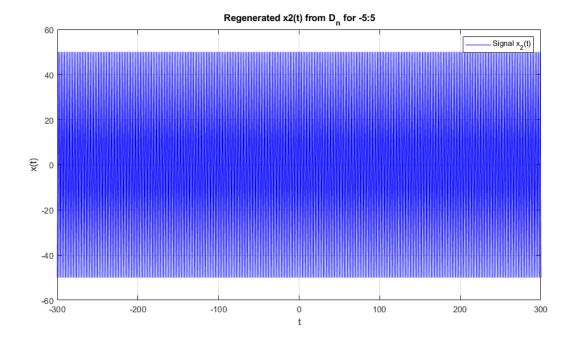
## A6 (x2c)

```
D_n=[-50:50]; nleftlim = -50;
nrightlim = 50;
x = 50+1;
if n == 0,
D_n(x) = 0.05;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.5)./(n.*pi));
end
n = [nleftlim:nrightlim];
W0 = pi/10;
t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
t=-300:300;
plot(t,real(x),'b');
ylabel('x(t)');
xlabel('t');
title('Regenerated x2(t) from D_n for -5:5');
legend('Signal x_2(t)');
grid;
```



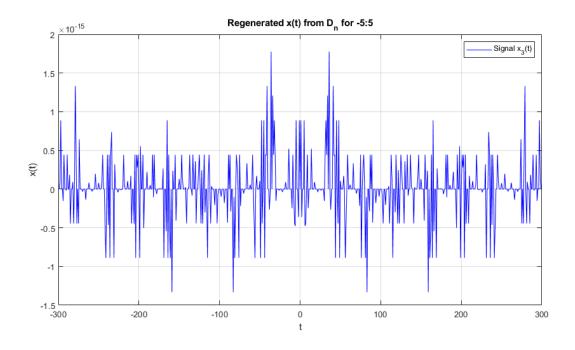
### A6 (x2d)

```
D_n=[-500:500]; nleftlim = -500;
nrightlim = 500;
x = 500+1;
if n == 0,
D_n(x) = 0.05;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.5)./(n.*pi));
end
n = [nleftlim:nrightlim];
W0 = pi/10;
t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
t=-300:300;
plot(t,real(x),'b');
ylabel('x(t)');
xlabel('t');
title('Regenerated x2(t) from D_n for -5:5');
legend('Signal x_2(t)');
grid;
```



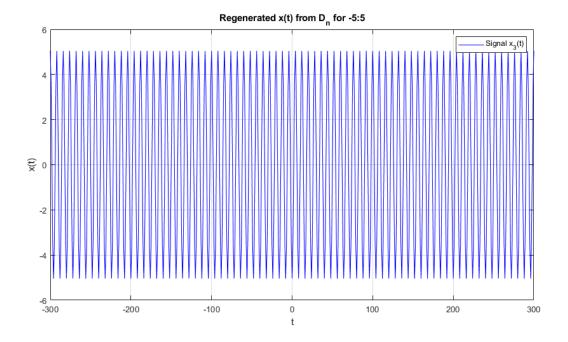
### A6 (x3a)

```
D_n=[-5:5];
nleftlim = -5;
nrightlim = 5;
x = 5+1;
if n == 0,
D_n(x) = 0.025;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.25)./(n.*pi));
end
n = [nleftlim:nrightlim];
W0 = pi/20;
t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
t=-300:300;
plot(t,real(x),'b');
ylabel('x(t)');
xlabel('t');
title('Regenerated x(t) from D_n for -5:5');
legend('Signal x_3(t)');
grid;
```



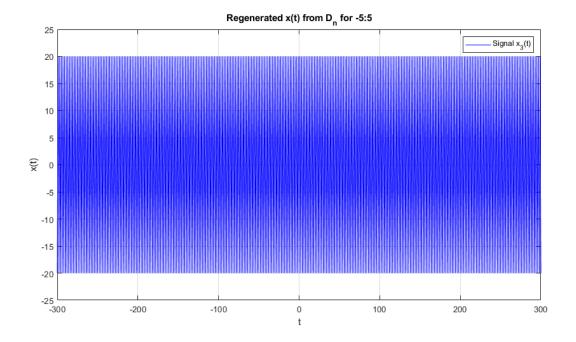
## A6 (x3b)

```
D_n = [-20:20];
nleftlim = -20;
nrightlim = 20;
x = 20+1;
if n == 0,
D_n(x) = 0.025;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.25)./(n.*pi));
end
n = [nleftlim:nrightlim];
W0 = pi/20;
t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
t=-300:300;
plot(t,real(x),'b');
ylabel('x(t)');
xlabel('t');
title('Regenerated x(t) from D_n for -5:5');
legend('Signal x_3(t)');
grid;
```



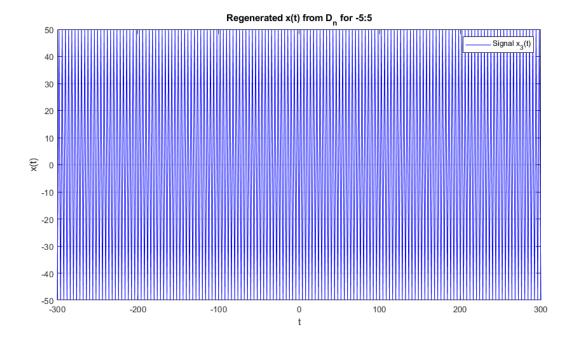
## A6 (x3c)

```
D_n=[-50:50];
nleftlim = -50;
nrightlim = 50;
x = 50+1;
if n == 0,
D_n(x) = 0.025;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.25)./(n.*pi));
end
n = [nleftlim:nrightlim];
W0 = pi/20;
t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
t=-300:300;
plot(t,real(x),'b');
ylabel('x(t)');
xlabel('t');
title('Regenerated x(t) from D_n for -5:5');
legend('Signal x_3(t)');
grid;
```



### A6 (x3d)

```
D_n = [-500:500];
nleftlim = -500;
nrightlim = 500;
x = 500+1;
if n == 0,
D_n(x) = 0.025;
else
D_n(n-nleftlim+1) = (sin(n.*pi*0.25)./(n.*pi));
n = [nleftlim:nrightlim];
W0 = pi/20;
t = -300:300;
s = 300+1;
b=length(t);
x = zeros(1,b);
for t=-300:300
for n=nleftlim:nrightlim
x(t+s) = x(t+s) + real(D_n(n-nleftlim+1).*exp(n.*1i*W0*t));
end
end
t=-300:300;
plot(t,real(x),'b');
ylabel('x(t)');
xlabel('t');
title('Regenerated x(t) from D_n for -5:5');
legend('Signal x_3(t)');
grid;
```



#### **B1**

```
% From A.1 and A.2;
% wo for x1(t) : pi/10
% wo for x2(t) : pi/10
% wo for x3(t) : pi/20
```

#### **B2**

% The difference between the fourier coefficients of x1 and x2 is % that from n = (-inf:inf), for x2, there are infinite coefficients and % for x1, there will always be only 4 coefficients.

#### **B3**

% The fourier coefficients are similar except for x3, the sin function % is dilated by 4pi and for x2 the sine function is dilated by pi/2

#### **B4**

 $\mbox{\$ For x2, D0 is 1/2 and since x4 is just x2 shifted down by 1/2, D0 for <math display="inline">\mbox{\$ x4 is 0}$ 

#### **B5**

% x1 would not change since there are distinct number % for x2 and x3 the higher the value of n, the more accurate % the functions become

### **B6**

 $\mbox{\%}$  for x2 and x3, you would need n to be from (-inf:inf) to reconstruct the  $\mbox{\%}$  functions properly

#### **B7**

\$ storing the coeffecients would not work as x(t) is arbritary, so we don't \$ know how many coeffecients are there

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