# TikZ Figures

# Sunny Pradhan

This file is a collection of most of the TikZ figures I made

# Contents

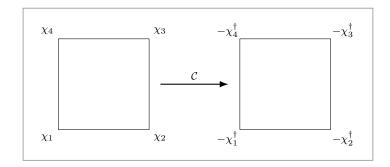
TikZ preamble	2
Figures	3
Charge conjugation of a plaquette	. 3
Closed loops on a square lattice	. 4
Gauge invariant configurations	. 5
Duality map on a ladder	. 7
Ladder geometry	. 9
Ladder operators	. 10
Lattice links labels	. 11
Non contractible loops	. 12
Non local operators	. 13
Order parameters on a ladder	
Orientation of a 2d lattice	. 15
Orientation of link operators	
Operators of a quantum double model	
Action of a ribbon operator	
Examples of ribbons	
Staggered spinor components	. 21
Toric code operators	
Gauss and plaquette operators	
Triangles on a lattice	
$\mathbb{Z}_2$ duality map	
$\mathbb{Z}_2$ vacuum states	

## TikZ preamble

```
\usepackage{tikz}
\usepackage{xcolor}
% TikZ
\usetikzlibrary{
    arrows.meta,
    decorations.markings,
    patterns,
    fit,
    positioning
\tikzset{
    % Main settings
    font=\footnotesize,
    >={Latex},
    % Ribbons styles
    direct vertex/.style={circle, inner sep=opt, minimum size=3pt, draw=black, fill=black
    dual vertex/.style={circle, inner sep=opt, minimum size=3pt, draw=black, fill=white},
    ribbon site/.style={very thick, dashed, black},
direct edge/.style={very thick, black},
    dual edge/.style={very thick, dotted, black},
    ribbon/.style={green, opacity=0.3},
    direct ribbon/.style={red, opacity=0.3},
    dual ribbon/.style={blue, opacity=0.3}
}
% Colors
\colorlet{Red}{red!70!black}
\colorlet{Blue}{blue!70!black}
\colorlet{Gray}{gray!70!black}
\colorlet{Green}{green!70!black}
```

plus maybe some macros for math commands

#### Charge conjugation of a plaquette

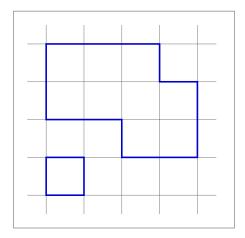


```
\begin{tikzpicture}[scale=0.6]
  \draw[step=4, black] (0,0) grid (4,4);
  \node[below left] at (0,0) {$\chi_1$};
  \node[below right] at (4,0) {$\chi_2$};
  \node[above right] at (4,4) {$\chi_3$};
  \node[above left] at (0,4) {$\chi_4$};

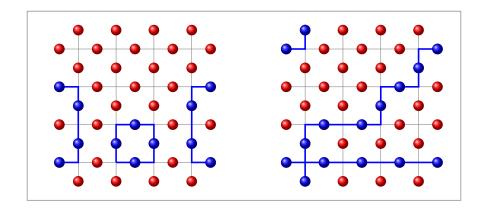
\begin{scope}[xshift=8cm, inner sep=1pt]
  \draw[step=4, black] (0,0) grid (4,4);
  \node[below left] at (0,0) {$-\chi_1^{\dagger}$};
  \node[below right] at (4,0) {$-\chi_2^{\dagger}$};
  \node[above right] at (4,4) {$-\chi_3^{\dagger}$};
  \node[above left] at (0,4) {$-\chi_4^{\dagger}$};
  \end{scope}

\draw[thick, ->] (4.5,2) -- +(3,0) node[pos=0.5, above] {$\mathcal{C}$};
  \end{tikzpicture}
```

### Closed loops on a square lattice

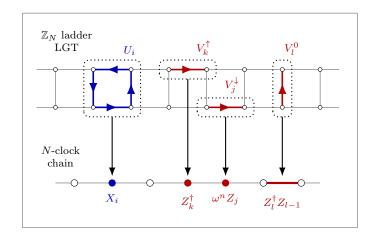


#### Gauge invariant configurations



```
% Draw horizonal line of nodes
\newcommand{\DrawHoriz}[2]{
    \draw[gray, thin] (-0.5, #1)
    -- ++(0.5, 0) node [pos=0.0, #2] {}
    -- ++(1.0, 0) node [pos=0.5, #2] {}
    -- ++(1.0, 0) node [pos=0.5, #2] {}
    -- ++(1.0, 0) node [pos=0.5, #2] {}
    -- ++(0.5, 0) node [pos=1.0, #2] {};
% Draw vertical line of nodes
\newcommand{\DrawVert}[2]{
    \draw[gray, thin] (#1, -0.5)
    -- ++(0, 0.5) node [pos=0.0, #2] {}
    -- ++(0, 1.0) node [pos=0.5, #2] {}
    -- ++(0, 1.0) node [pos=0.5, #2] {}
    -- ++(0, 1.0) node [pos=0.5, #2] {}
    -- ++(0, 0.5) node [pos=1.0, #2] {};
% Draw grid
\newcommand{\DrawGrid}[1]{
    \foreach \x in \{0,...,3\} \DrawHoriz\{\x\}{#1};
    \foreach \y in \{0,...,3\} \DrawVert\{\y\}\{\#1\};
\begin{tikzpicture}[
        ball/.style={shade, shading=ball, circle, minimum size=8pt, inner sep=opt},
        zero/.style={ball, ball color=red},
        one/.style={ball, ball color=blue},
        loopline/.style={blue, very thick},
        loopdot/.style={pos=0.5, one},
        loopstart/.style={pos=0, one},
        loopend/.style={pos=1, one}
    ]
  %%% First grid
  % Draw a grid of red dots
  \DrawGrid{zero};
  % Draw over loops of blue dots
  \draw[loopline]
  (1,0) foreach \x / \y in \{1/0, 0/1, -1/0, 0/-1\} \{ -- ++(\x, \y) node [loopdot] \{ \} \};
  \draw[loopline]
    (-0.5,0) -- (0,0) node [loopstart] {}
    foreach y in \{1, 1\} \{--++(0, y) \text{ node [loopdot] } \{\}
    -- ++(-0.5, 0) node [loopend] {};
  \draw[loopline]
  (3.5,0) -- (3,0) node [loopstart] {}
  foreach y in \{1, 1\} \{--++(0, y) \text{ node [loopdot] } \{\}
  -- ++(0.5, 0) node [loopend] {};
  %%% Second grid, shifted
```

#### Duality map on a ladder



```
\begin{tikzpicture}[
    scale=1,
    site/.style = {circle, inner sep=0 pt, minimum size=3pt, draw=black, fill=white},
    site2/.style = {circle, inner sep=0 pt, minimum size=5pt, draw=black, fill=white},
    decoration={
        markings,
        mark=at position 0.65 with {\arrow{>}}
    },
    plaq/.style={Blue, very thick, postaction={decorate}},
    elec/.style={Red, very thick, postaction={decorate}},
    arr/.style={->, thick, shorten >=5pt},
    box/.style={dotted, rounded corners, thick}
    % ladder
    \draw[Gray, thin] (-0.5,0) grid (7.5,1);
    % plaquette operator
    \draw[plaq] (1,0) -- (2,0);
    \draw[plaq] (2,0) -- (2,1);
    \draw[plaq] (2,1) -- (1,1);
    \draw[plaq] (1,1) -- (1,0);
    \draw[box] (0.75,-0.25) rectangle (2.25, 1.25) node [above left, Blue] {$U_{i}};
    % horizontal electric operators
    \draw[elec] (4,0) -- (5,0);
    \draw[elec] (3,1) -- (4,1);
    \displaystyle \frac{1}{3.75,-0.25} rectangle (5.25, 0.25) +(-0.25,0) node [above left, Red] {$\
   Vdown_{j}$};;
    \displaystyle \frac{(2.75, 0.75)}{(2.75, 0.75)} rectangle (4.25, 1.25) node [above left, Red] {\vert {k}};
    % vertical electric operator
    \draw[elec] (6,0) -- (6,1);
    \draw[box] (5.75,-0.25) rectangle (6.25, 1.25) node [above, Red] {$V^0_{{l}}};
    % ladder sites
    \foreach \y in \{0,1\} \foreach \x in \{0,...,7\} \draw (\x,\y) node [site] \{\};
    % chain
    \draw[Gray, thin] (-0,-2) -- (7,-2);
    % clock operators
    \draw (1.5,-2) node [site2, draw=Blue, fill=Blue] {} node [text=Blue, below=5pt] {$X
    _{i}$};
    \displaystyle (3.5,-2) \ node \ [site2, draw=Red, fill=Red] \ \{\} \ node \ [text=Red, below=5pt] \ \{$Z^\ ]
   dagger_{k}$;
    \displaystyle (4.5,-2) \bmod [site2, draw=Red, fill=Red] {} \bmod [text=Red, below=5pt] {}
   omega^n Z_{j}$;
```

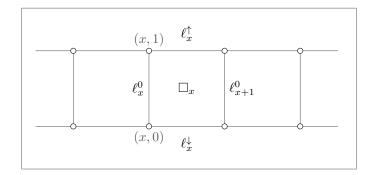
```
\draw [ultra thick, Red] (5.5,-2) -- (6.5,-2) node [pos=0.5, below=5pt] {$Z^\dagger_{ l} Z_{l-1}$};

% chain sites
\foreach \x in {0,2,5,6} \draw (\x+0.5,-2) node [site2] {};

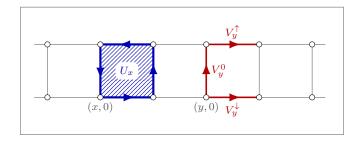
% arrows
\draw[arr] (1.5,-0.25) -- (1.5, -2);
\draw[arr] (3.5, 0.75) -- (3.5, -2);
\draw[arr] (4.5,-0.25) -- (4.5, -2);
\draw[arr] (6.0,-0.25) -- (6.0, -2);

% labels
\draw (-0.5,1.75) node [right, align=center] {$\Z_N$ ladder \\ LGT};
\draw (-0.5,-1.3) node [right, align=center] {$N$-clock \\ chain};
\end{tikzpicture}
```

#### Ladder geometry

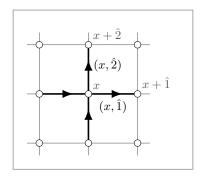


#### Ladder operators



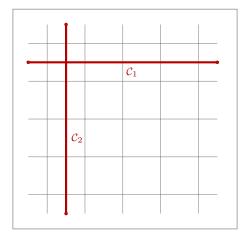
```
\begin{tikzpicture}[
    scale=0.7,
    site/.style = {circle, inner sep=0 pt, minimum size=4pt, draw=black, fill=white},
    decoration={
         markings,
         mark=at position 0.65 with {\arrow{>}}
    plaq/.style={Blue, very thick, postaction={decorate}},
    elec/.style={Red, very thick, postaction={decorate}}
    % ladder
    \draw[Gray, step=2, thin] (-0.5,0) grid (10.5,2);
    % Plaquette operator
    \draw[Gray] (2,0) node [below] {(x,0)$};
    \draw[Blue, ultra thick, pattern=north east lines, pattern color=Blue] (2,0)
    rectangle +(2,2);
    \draw[plaq] (2,0) -- (4,0);
    \draw[plaq] (4,0) -- (4,2);
    \draw[plaq] (4,2) -- (2,2);
    \draw[plaq] (2,2) -- (2,0);
    \node at (3,1) [fill=white, rounded corners, text=Blue] {$U_x$};
    % Electric field operators
    \draw[Gray] (6,0) node [below] {(y,0)$};
    \draw[elec] (6,0) -- (6,2) node [pos=0.5, right] {$V^o_y$};
\draw[elec] (6,2) -- (8,2) node [pos=0.5, above] {$\Vup_y$};
\draw[elec] (6,0) -- (8,0) node [pos=0.5, below] {$\Vdown_y$};
    \foreach \y in \{0,2\} \foreach \x in \{0,2,...,10\} \draw (\x,\y) node [site] \{\};
\end{tikzpicture}
```

#### Lattice links labels



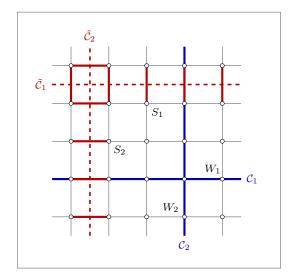
```
\begin{tikzpicture}[
        font=\small,
        scale=1.3,
        site/.style = {circle, inner sep=0 pt, minimum size=5pt, draw=black, fill=white},
        decoration={
            markings,
            mark=at position 0.35 with {\arrow{>}},
            mark=at position 0.85 with {\arrow{>}}
        }
   % Lattice
    \draw[Gray, thin] (-1.25, -1.25) grid (1.25, 1.25);
   % links
    \draw[very thick, postaction={decorate}]
        (-1, 0) -- (1, 0)
        node [pos=0.75, below] \{\$(x, \hat{1})\}
        % node [pos=0.25, below] \{(x, -\hat{1})\}
    \draw[very thick, postaction={decorate}]
        (0, -1) -- (0, 1)
        node [pos=0.8, right] \{ (x, \hat{2}) \}
        % node [pos=0.15, right] \{(x, -\hat{2})\}
   % sites
    \foreach \x in \{-1, ..., 1\}
        \foreach \y in \{-1, \ldots, 1\}
            \draw(x, y) node [site] {};
    \draw (0, 0) node [Gray, above right] {$x$};
    \draw (1, 0) \node [Gray, above right] {$x + \hat{1}};
    \downarrow (0, 1) \node [Gray, above right] {$x + \hat{2}};
\end{tikzpicture}
```

### Non contractible loops



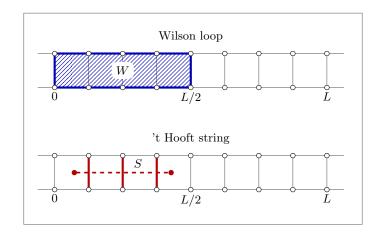
```
\begin{tikzpicture}
  \draw[step=1.0,gray,thin] (-0.5,-0.5) grid (4.5,4.5);
  \draw[black!30!red, ultra thick] (0.5,-0.5) circle (0.5 pt) -- (0.5,4.5) node[pos=0.4, right] {$\mathcal{C}_2$} circle (0.5pt);
  \draw[black!30!red, ultra thick] (-0.5,3.5) circle (0.5 pt) -- (4.5,3.5) node[pos=0.55, below] {$\mathcal{C}_1$} circle (0.5pt);
  \end{tikzpicture}
```

#### Non local operators



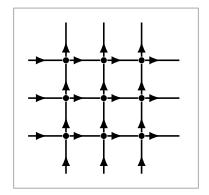
```
\begin{tikzpicture}[
        site/.style = {circle, inner sep=0 pt, minimum size=3pt, draw=black, fill=white},
    % lattice grid
    \draw[Gray,thin] (-0.5,-0.5) grid (4.5,4.5);
    % Wilson loops
    \draw[Blue, ultra thick]
        (-0.5, 1) -- (4.5, 1)
node [pos=1, right] {$\mathcal{C}_1$}
        node [pos=0.85, above, black] {$W_1$}
    \draw[Blue, ultra thick]
        (3, -0.5) -- (3, 4.5)
        node [pos=0, below] {$\mathcal{C}_2$}
        node [pos=0.15, left, black] {$W_2$}
    % 't Hooft strings
    \draw[Red, very thick, dashed]
        (-0.5,3.5) -- (4.5,3.5)
        node[pos=0, left] {$\tilde{\mathcal{C}}_1$}
    \foreach \x in \{0,...,4\} { \draw[Red, ultra thick] (\x, 3) -- +(0, 1); }
    \draw (2,3) node [below right] {$S_1$};
    \draw[Red, very thick, dashed]
        (0.5,-0.5) -- (0.5,4.5)
node[pos=1, above] {$\tilde{\mathcal{C}}_2$}
    \foreach \y in \{0,...,4\} { \draw[Red, ultra thick] (0, y) -- +(1, 0); }
    \draw (1,2) node [below right] {$S_2$};
    \foreach \y in \{0,...,4\} \foreach \x in \{0,...,4\} \draw (\x,\y) node [site] \{\};
\end{tikzpicture}
```

#### Order parameters on a ladder



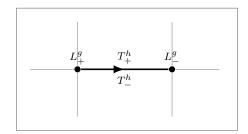
```
\begin{tikzpicture}[
    scale=0.9,
    font=\small,
    site/.style = {circle, inner sep=0 pt, minimum size=3.5pt, draw=black, fill=white},
    string/.style={{Circle[length=4pt, width=4pt]}-{Circle[length=4pt, width=4pt]}, very
   thick, dashed, Red}
    %%% Wilson loop
    % Lattice
    \draw[Gray, thin] (-0.5,0) grid (8.5,1);
    % Loop interior
    \draw[Blue, ultra thick, pattern=north east lines, pattern color=Blue] (0,0)
   rectangle (4,1);
    % Labels
    \draw (2,0.5) node [fill=white, rounded corners] {$W$};
    \forall o,o  node [below] {$o$};
    \draw (4,0) node [below] {$L/2$};
    \draw (8,0) node [below] {$L$};
    \draw (4,1.5) node {Wilson loop};
    \foreach \y in \{0,1\} \foreach \x in \{0,...,8\} \draw (\x,\y) node [site] \{\};
    %%% 't Hooft string
    \begin{scope}[yshift=-3cm]
        % Lattice
        \draw[Gray, thin] (-0.5,0) grid (8.5,1);
        \frac{1}{3} (0.5,0.5) -- (3.5,0.5) node [black, above, pos=0.65] {$S$};
        \foreach \x in \{1,2,3\} \draw [Red, ultra thick] (\x,0) -- (\x,1);
        % Labels
        \draw (0,0) node [below] {$0$};
        \draw (4,0) \node [below] {$L/2$};
        \draw (8,0) node [below] {$L$};
        \draw (4,1.5) node {'t Hooft string};
        \foreach \y in \{0,1\} \foreach \x in \{0,...,8\} \draw (\x,\y) node [site] \{\};
    \end{scope}
\end{tikzpicture}
```

#### Orientation of a 2d lattice

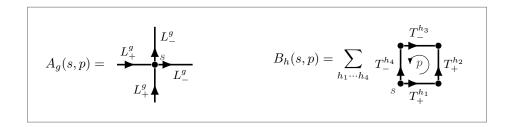


```
%
Picture of the orientation of the 2d square lattice
%
\textbf{begin}{tikzpicture}[
    decoration={
        markings,
        mark=at position 0.5 with {\arrow{>}}
    },
    link/.style={postaction={decorate}, very thick},
    site/.style={circle, inner sep=opt, minimum size=5pt, draw=white, fill=black}
    |
        | \foreach \x in {0,...,2} \draw [link] (\x, -1) -- +(0, 1);
        | \foreach \x in {0,...,2} \draw [link] (-1, \y) -- +(1, 0);
        | \foreach \x in {0,...,2}
        | \draw[link] (\x, \y) -- +(1, 0);
        | \draw[link] (\x, \y) -- +(0, 1);
        | \draw[link] (\x, \y) node[site] {};
}
\end{tikzpicture}
```

#### Orientation of link operators

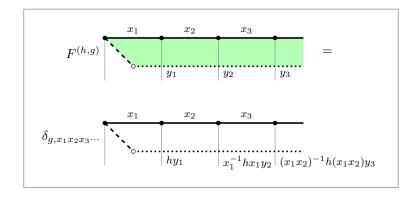


#### Operators of a quantum double model



```
% Pictorial representations of the operators A_g and B_h
\begin{tikzpicture}[
       decoration={
           markings,
           mark=at position 0.5 with {\arrow{>}}
       link/.style={postaction={decorate}, very thick},
       site/.style={circle, inner sep=opt, minimum size=5pt, draw=white, fill=black},
        font=\small
        ]
        \frac{-1.2, 0}{node[font=\frac{size}{anchor=east}]} {$A_g(s,p) = $};
       \draw[link] (-1, 0) -- (0, 0) node [pos=0.3, above] {$L^g_+$};
       \draw (0, 0) node [site] {};
       \draw (0, 0) node [above right, black!70] {\$s$};
       \begin{scope}[xshift=7cm]
           \frac{-1.2, 0}{node[font=\frac{size}{anchor=east}]} {B_h(s,p) = \frac{1.2}{anchor}}
   displaystyle\sum_{h_1 \cdots h_4} $};
           \draw[link] (-0.5, -0.5) -- (+0.5, -0.5) node [pos=0.5, below] {$T^{h}$}
           \draw[link] (+0.5, -0.5) -- (+0.5, +0.5) node [pos=0.5, right] {$T^{h}}
   _2}_+$};
\draw[link] (-0.5, +0.5) -- (+0.5, +0.5) node [pos=0.5, above] {$T^{h}}
   _3}_-$};
\draw[link] (-0.5, -0.5) -- (-0.5, +0.5) node [pos=0.5, left ] {$T^{h}
           \draw[->] (0, -0.25) arc (-90:180:0.25);
           \draw[black!70] (0,0) node {$p$};
           \draw[black!70] (-0.5, -0.5) node [below left] {$s$};
           foreach \x in {-0.5,0.5} \foreach \y in {-0.5,0.5} \draw (\x,\y) node [site]
        \end{scope}
\end{tikzpicture}
```

#### Action of a ribbon operator

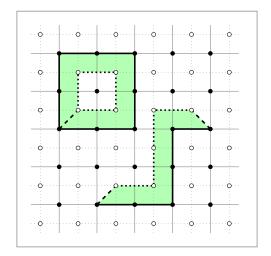


```
\begin{tikzpicture}[scale=1.5, font=\footnotesize]
    % ribbon fill
    \fill [ribbon] (0, 0) -- ++ (3.5, 0) -- ++(0, -0.5) -- ++(-3, 0) -- cycle;
    % lattice grid
    \draw[thin, gray] (0,0) grid (3.5, -0.75);
    % ribbon edges
    \draw[ribbon site] (0, 0) -- ++(0.5, -0.5);
    \draw[direct edge] (0, 0) -- ++(3.5, 0);
    \draw[dual edge] (0.5, -0.5) -- ++(3, 0);
    % lattice vertices
    \foreach \x in \{0,...,3\} \node at (\x, 0) [direct vertex] \{\};
    \node at (0.5, -0.5) [dual vertex] {};
    % labels
    \node at (0.5, 0) [above] {$x_1$};
\node at (1.5, 0) [above] {$x_2$};
\node at (2.5, 0) [above] {$x_3$};
    \node at (1, -0.5) [below right] \{y_1\};
    \node at (2, -0.5) [below right] \{ y_2 \};
    \node at (3, -0.5) [below right] \{\$y_3\$\};
    \node at (0, -0.25) [left, font=\normalsize] \{F^{(h,g)}\};
    \node at (3.75, -0.25) [right, font=\normalsize] {\$ = \$};
    % transformed grid
    \begin{scope}[yshift=-1.5cm]
        % lattice grid
        \draw[thin, gray] (0,0) grid (3.5, -0.75);
        % ribbon edges
        \draw[ribbon site] (0, 0) -- ++(0.5, -0.5);
        \draw[direct edge] (0, 0) -- ++(3.5, 0);
        \draw[dual edge] (0.5, -0.5) -- ++(3, 0);
        % lattice vertices
        \foreach \x in \{0,...,3\} \node at (\x, 0) [direct vertex] \{\};
        \node at (0.5, -0.5) [dual vertex] {};
        % labels
        \node at (0.5, 0) [above] \{x_1\};
        \node at (1.5, 0) [above] \{x_2\};
        \node at (2.5, 0) [above] \{x_3\};
        \node at (1, -0.5) [below right] {\$hy_1\$};
        \node at (2, -0.5) [below right] {$x_1^{-1} h x_1 y_2$};
```

```
\node at (3, -0.5) [below right] {$(x_1 x_2)^{-1} h (x_1 x_2) y_3$};

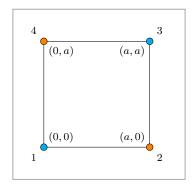
\node at (0, -0.25) [left, font=\normalsize] {$\delta_{g, x_1 x_2 x_3 \cdots}$};
\end{scope}
\end{tikzpicture}
```

#### Examples of ribbons



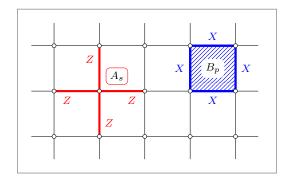
```
\begin{tikzpicture}
    % first ribbon fill
    \fill[ribbon]
    (1,0) -- ++(2,0) -- ++(0,2) -- ++(1,0) -- ++(-0.5,0.5)
    -- ++(-1, 0) -- ++(0, -2) -- ++(-1, 0) -- cycle;
   % second ribbon fill
    \fill[ribbon] (0,2) rectangle ++(2, 2);
    \fill[white] (0.5, 2.5) rectangle ++(1, 1);
    % lattice grid
    \draw[gray, thin] (-0.75, -0.75) grid (4.75, 4.75);
    % dual lattice grid
    \draw[gray, dotted, xshift=-0.5cm, yshift=-0.5cm] (-0.25, -0.25) grid (5.25, 5.25);
    % first ribbon draw
    \draw[ribbon site] (1, 0) -- ++(0.5, 0.5); % starting ribbon site
    \draw[direct edge] (1,0) -- ++(2, 0) -- ++(0, 2) -- ++(1,0);
    \draw[ribbon site] (4, 2) -- ++(-0.5, 0.5); % ending ribbon site
    \draw[dual edge] (3.5, 2.5) -- ++(-1, 0) -- ++(0, -2) -- ++(-1, 0);
    % second ribbon draw
    \draw[ribbon site] (0, 2) -- ++ (0.5, 0.5);
    \draw[direct edge] (0, 2) rectangle ++(2, 2);
    \draw[dual edge] (0.5, 2.5) rectangle ++(1, 1);
    % lattice sites
    \foreach \x in \{0,...,4\} \foreach \y in \{0,...,4\} \node at (\x, \y) [direct vertex]
   {};
    % dual lattice sites
    \begin{scope}[xshift=-0.5cm, yshift=-0.5cm] \\ for each \xin {0,...,5} \for each \yin {0,...,5} \node at (\x, \y) [dual vertex] \end{scope}
    \end{scope}
\end{tikzpicture}
```

#### Staggered spinor components



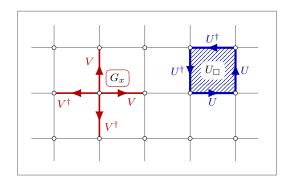
```
begin{tikzpicture}[scale=0.7,
  dot/.style = {circle, minimum size=5pt, inner sep=0pt, draw=black},
  even/.style = {dot, fill=cyan},
  odd/.style = {dot, fill=orange}
  ]
  \draw[step=4.0,black,thin] (0,0) grid (4,4);
  \draw (0,0) node [even, label=below left:{$1$}] {} node [black, above right] {$(0,0) $};
  \draw (4,0) node [odd, label=below right:{$2$}] {} node [black, above left] {$(a,0) $};
  \draw (4,4) node [even, label=above right:{$3$}] {} node [black, below left] {$(a,a) $};
  \draw (0,4) node [odd, label=above left:{$4$}] {} node [black, below right] {$(0,a) $};
  \end{tikzpicture}
```

#### Toric code operators



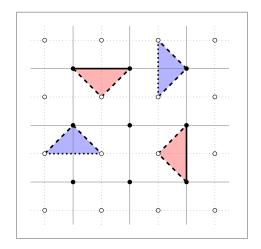
```
\begin{tikzpicture}[
         scale=1.2,
         site/.style = {circle, inner sep=0 pt, minimum size=3pt, draw=black, fill=white},
         plaq/.style={blue, ultra thick},
         gauss/.style={red, ultra thick}
    % Lattice
    \draw[thin] (-0.5,-0.5) grid (4.5,2.5);
    % Plaquette operator
    \displaystyle \frac{1}{3,1} -- (4,1) \text{ node [pos=0.5, below] {} $X$};
    \displaystyle \frac{(4,1) -- (4,2) \text{ node [pos=0.5, right] {}x$};}
    \draw[plaq] (4,2) -- (3,2) node [pos=0.5, above] {$X$};
    \draw[plaq] (3,2) -- (3,1) node [pos=0.5, left] {$X$};
    \draw[blue, ultra thick, pattern=north east lines, pattern color=blue] (3,1)
    rectangle (4,2);
    \draw (3.5,1.5) node [fill=white, rounded corners] {$B_p$};
    % Gauss operator
    \draw[gauss] (1, 1) -- (2, 1) node [pos=0.5, below right] {$Z$};
    \draw[gauss] (1, 1) -- (1, 2) node [pos=0.5, above left] \$Z\$\; \draw[gauss] (1, 1) -- (0, 1) node [pos=0.5, below left] \$Z\$\; \draw[gauss] (1, 1) -- (1, 0) node [pos=0.5, below right] \$Z\$\;
    \foreach \y in \{0,1,2\} \foreach \x in \{0,1,...,4\} \draw (\x,\y) node [site] \{\};
    \draw (1,1) node [above right, outer sep=5pt, inner sep=3pt, draw=red, rounded
    corners=3pt] {$A_s$};
\end{tikzpicture}
```

#### Gauss and plaquette operators



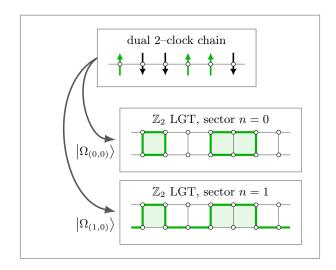
```
\begin{tikzpicture}[
                                 scale=1.2,
                                 site/.style = {circle, inner sep=0 pt, minimum size=3pt, draw=black, fill=white},
                                 decoration={
                                                  markings,
                                                  mark=at position 0.65 with {\arrow{>}}
                                 plaq/.style={Blue, very thick, postaction={decorate}},
                                 gauss/.style={Red, very thick, postaction={decorate}}
                % Lattice
                \draw[Gray,thin] (-0.5,-0.5) grid (4.5,2.5);
                % Plaquette operator
                \draw[plaq] (3,1) -- (4,1) node [pos=0.5, below] {$U$};
                 \draw[plaq] (4,1) -- (4,2) node [pos=0.5, right] {$U$};
                \draw[plaq] (4,2) -- (3,2) node [pos=0.5, above] {$U^\dagger$}; \draw[plaq] (3,2) -- (3,1) node [pos=0.5, left] {$U^\dagger$};
                \draw[Blue, ultra thick, pattern=north east lines, pattern color=Blue] (3,1)
               rectangle (4,2);
                \draw (3.5,1.5) \ node [fill=white, rounded corners] {$U_{\square}};
                % Gauss operator
                \label{lem:continuous} $$ \draw[gauss] (1, 1) -- (2, 1) \ node [pos=0.5, below right] {$V$}; $$ \draw[gauss] (1, 1) -- (1, 2) \ node [pos=0.5, above left] {$V$};
                 \draw[gauss] (1, 1) -- (0, 1) node [pos=0.5, below left] {$V^\dagger$};
                \displaystyle \frac{1}{2} = \frac{1}{2} \left( \frac{1}{2} \right) - \frac{1}{2} = \frac{1}{2} \left( \frac{1}{2} \right) - \frac{1}{2} \left( \frac{1}{2} \right) - \frac{1}{2} \left( \frac{1}{2} \right) + \frac{1}{2
                \foreach \y in \{0,1,2\} \foreach \x in \{0,1,\ldots,4\} \draw (\x,\y) node [site] \{\};
                \draw (1,1) node [above right, outer sep=5pt, inner sep=3pt, draw=Red, rounded
               corners=3pt] \{ G_x \};
\end{tikzpicture}
```

#### Triangles on a lattice



```
\begin{tikzpicture}[scale=1.5]
   % direct ribbons fill
   \fill [direct ribbon] (0, 2) -- ++(1, 0) -- ++(-0.5, -0.5) -- cycle;
   \fill [direct ribbon] (2, 0) -- ++(0, 1) -- ++(-0.5, -0.5) -- cycle;
   % dual ribbons fill
    \fill [dual ribbon] (-0.5, 0.5) -- ++(1, 0) -- ++(-0.5, 0.5) -- cycle;
    \fill [dual ribbon] (1.5, 1.5) -- ++(0, 1) -- ++(0.5, -0.5) -- cycle;
   % lattice grid
   \draw[gray, thin] (-0.75, -0.75) grid (2.75, 2.75);
   % dual lattice grid
   \draw[gray, dotted, xshift=-0.5cm, yshift=-0.5cm] (-0.25, -0.25) grid (3.25, 3.25);
   % direct ribbon draw
    \draw [direct edge] (0, 2) -- ++(1, 0);
    \draw [direct edge] (2,0) -- ++(0, 1);
    \draw [ribbon site] (0, 2) -- ++(0.5, -0.5) -- ++(0.5, 0.5);
   \draw [ribbon site] (2, 0) -- ++(-0.5, 0.5) -- ++(0.5, 0.5);
   % dual ribbon draw
   \draw [dual edge] (-0.5, 0.5) -- ++(1, 0);
    \draw [dual edge] (1.5, 1.5) -- ++(0, 1);
    \draw [ribbon site] (-0.5, 0.5) -- ++(0.5, 0.5) -- ++(0.5, -0.5);
   \draw [ribbon site] (1.5, 1.5) -- ++(0.5, 0.5) -- ++(-0.5, 0.5);
   % lattice sites
   \foreach \x in \{0,...,2\} \foreach \y in \{0,...,2\} \node at (\x, \y) [direct vertex]
   {};
   % dual lattice sites
   \begin{scope}[xshift=-0.5cm, yshift=-0.5cm]
        \foreach \x in \{0,...,3\} \foreach \y in \{0,...,3\} \node at (\x, \y) [dual vertex]
    {};
    \end{scope}
\end{tikzpicture}
```

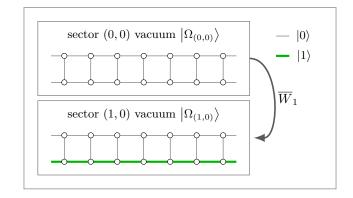
#### $\mathbb{Z}_2$ duality map



```
\newcommand{\UpArrow}[2]{\draw[up] (#1,#2) ++(0,-0.5) -- ++(0,1);}
\mbox{newcommand} \DownArrow [2] \draw[down] (#1,#2) ++(0,-0.5) -- ++(0,1);
\begin{tikzpicture}[
    font=\small,
    scale=0.6,
    site/.style = {circle, inner sep=0 pt, minimum size=3pt, draw=black, fill=white},
    on/.style = {ultra thick, Green},
    flux/.style = {fill=Green, fill opacity=0.1},
    up/.style = {-{Latex[length=5pt, width=5pt]}, very thick, Green},
    down/.style = {{Latex[length=5pt, width=5pt]}-, very thick}
    % Clock chain
    \begin{scope}[xshift=-1cm, yshift=4cm, local bounding box=chain]
        \draw[Gray, thin] (-0.5, 0) -- (5.5,0) node [pos=0.5, above=10pt, inner sep=5pt,
   black] {dual 2--clock chain};
        \foreach \x/\arr in {o/\UpArrow, 1/\DownArrow, 2/\DownArrow, 3/\UpArrow, 4/\
   UpArrow, 5/\DownArrow} {
            \arr{\x}{0};
            \d (\x, o) \ node [site] {};
        \useasboundingbox (-1, 0) -- (6,0) -- +(0,-1);
    \end{scope}
    % LGT sector (0,0)
    \begin{scope}[local bounding box=trivial]
        \node at (3,1) [above, inner sep=5pt] \{X_2\ LGT, sector n=0\;
        \draw[Gray, thin] (-0.5,0) grid (6.5,1);
        \draw[on, flux] (0,0) rectangle (1,1);
        \draw[on, flux] (3,0) rectangle (5,1);
        \foreach \y in \{0,1\} \foreach \x in \{0,1,...,6\} \draw (\x,\y) node [site] \{\};
        \useasboundingbox (-1, 0) -- (7,0) -- +(0,-0.75);
    \end{scope}
    % LGT sector (1,0)
    \begin{scope}[yshift=-3.2cm, local bounding box=topological]
        \node at (3,1) [above, inner sep=5pt] \{ \Z_2 \ LGT, \ sector \ n=1 \} \};
        \draw[Gray, thin] (-0.5,0) grid (6.5,1);
\draw[on] (-0.5, 0) -- (0,0) -- (0,1) -- (1,1) -- (1,0) -- (3,0) -- (3,1) --
   (5,1) -- (5,0) -- (6.5,0);
        fill[flux] (0,0) rectangle (1,1);
        \fill[flux] (3,0) rectangle (5,1);
        % sites
        \foreach \y in \{0,1\} \foreach \x in \{0,1,...,6\} \draw (\x,\y) node [site] \{\};
```

```
\useasboundingbox (-1, 0) -- (7,0) -- +(0,-0.75);
   \end{scope}
   % Bounding boxes
   \draw [thin, Gray] (chain.north west) rectangle (chain.south east);
   \draw [thin, Gray] (trivial.north west) rectangle (trivial.south east);
   \draw [thin, Gray] (topological.north west) rectangle (topological.south east);
   % Arrows between the bounding boxes
   \draw [thick, Gray, shorten >= 3pt] (chain.west)
       edge [bend right=70, -{Latex}, Gray, very thick]
       % node [pos=0.8, below=6pt, text=black] \{ \text{Omega}_{(0,0)} \} 
       (trivial.west);
   \draw [thick, Gray, shorten >= 3pt] (chain.west)
       edge [bend right=70, -{Latex}, Gray, very thick]
       % node [pos=0.85, below=10pt, text=black] \{ \text{Omega}_{(1,0)} \}
       (topological.west);
   \draw (trivial.west) node [below left] {\\cdot\\Omega_{(0,0)}}\\;
   \end{tikzpicture}
```

#### $\mathbb{Z}_2$ vacuum states



```
\begin{tikzpicture}[
   font=\small,
    scale=0.7,
    site/.style = {circle, inner sep=0 pt, minimum size=4pt, draw=black, fill=white},
    up/.style = {ultra thick, green!70!black},
   legend/.style = {text=black, inner sep=5pt}
]
%%% Sector (0,0) vacuum
\begin{scope}[local bounding box=trivial]
    \node at (3,1) [above=5pt, legend] {sector (0,0)$ vacuum \\kappa \
   \draw[Gray, thin] (-0.5,0) grid (6.5,1);
   % sites
   \foreach \y in \{0,1\} \foreach \x in \{0,1,...,6\} \draw (\x,\y) node [site] \{\};
    \useasboundingbox (-1,0) -- (7,0) -- +(0,-0.5);
\end{scope}
%%% Sector (1,0) vacuum
\begin{scope}[yshift=-3cm, local bounding box=topol]
    \node at (3,1) [above=5pt, legend] {sector (1,0) vacuum \left(\frac{0}{0},\frac{1}{0}\right)}
   % ladder
   \draw[Gray, thin] (-0.5,0) grid (6.5,1);
   % Wilson loop
    \draw[up] (-0.5, 0) -- (6.5, 0);
   % sites
   \foreach \y in \{0,1\} \foreach \x in \{0,1,...,6\} \draw (\x,\y) node [site] \{\};
    \useasboundingbox (-1,0) -- (7,0) -- +(0,-0.5);
\end{scope}
legend
\begin{scope}[xshift=8cm, yshift=1cm, local bounding box=legend]
    \draw [Gray, thin] (0,0.75) -- +(0.5,0) node [right, legend] {$\ket{0}$};
                     -- +(0.5,0) node [right, legend] {$\ket{1}$};
    \draw [up] (0.0)
    \useasboundingbox (-0.25,0);
\end{scope}
\draw[thin, Gray] (trivial.south west) rectangle (trivial.north east);
\draw[thin, Gray] (topol.south west) rectangle (topol.north east);
% \draw[thin, Gray] (legend.south west) rectangle (legend.north east);
    \draw [shorten >= 3pt] (trivial.east)
    edge [-{Latex}, Gray, very thick, out=0, in=0]
    node [font=\normalsize, right, text=black] {$\overline{W}_1$}
    (topol.east);
\end{tikzpicture}
```