

Basic Data Structures

Stacks

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Outline

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Stacks

- What is a Stack?
- The Stack Abstract Data Type
- Implementing a Stack in Python
- Simple Balanced Parentheses
- Balanced Symbols (A General Case)
- Converting Decimal Numbers to Binary Numbers
- Infix, Prefix and Postfix Expressions

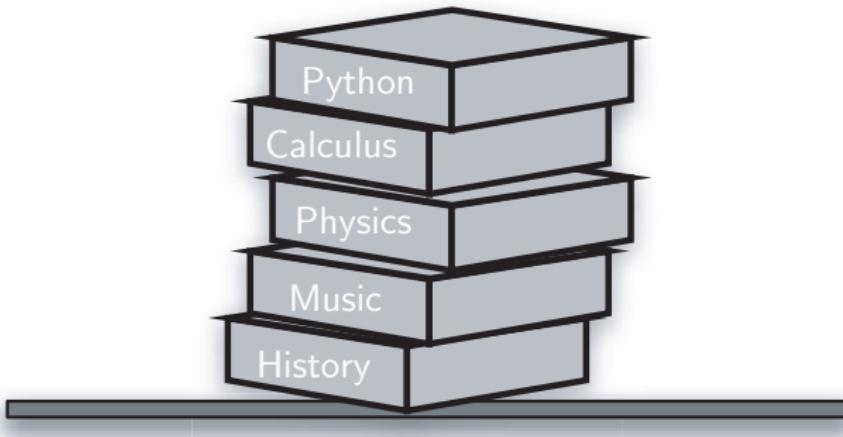
Outline

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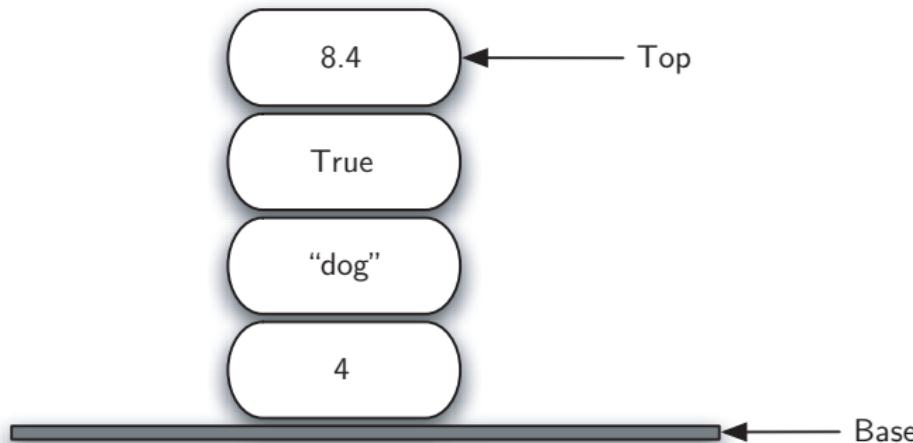
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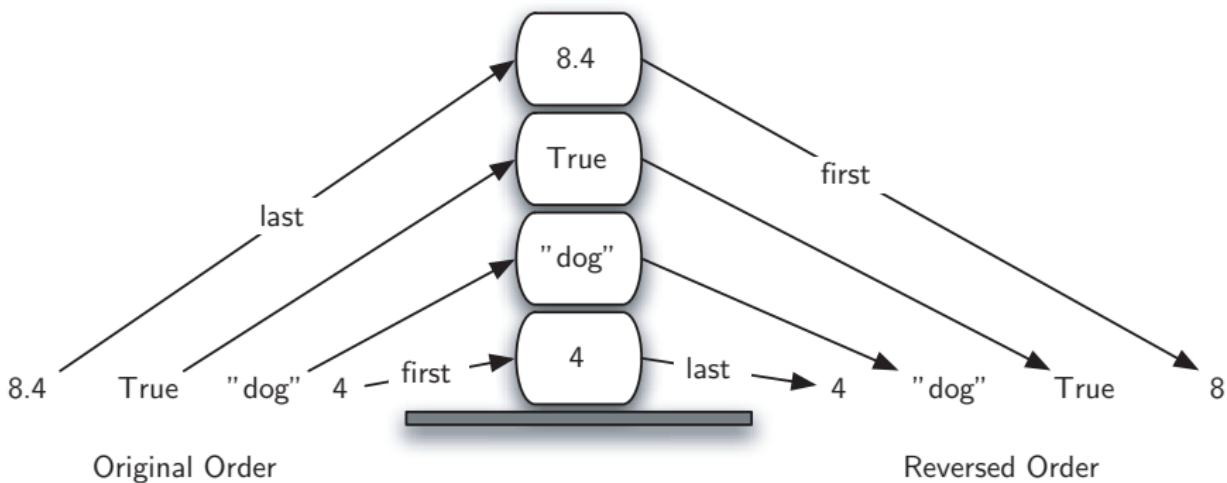
A Stack of Books



A Stack of Primitive Python Objects



The Reversal Property of Stacks



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- `Stack ()` creates a new stack that is empty. It needs no parameters and returns an empty stack.
- `push (item)` adds a new item to the top of the stack. It needs the item and returns nothing.
- `pop ()` removes the top item from the stack. It needs no parameters and returns the item. The stack is modified.
- `peek ()` returns the top item from the stack but does not remove it. It needs no parameters. The stack is not modified.
- `isEmpty ()` tests to see whether the stack is empty. It needs no parameters and returns a boolean value.
- `size ()` returns the number of items on the stack. It needs no parameters and returns an integer.

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Stack Implementation in Python I

```
1 class Stack:  
2     def __init__(self):  
3         self.items = []  
4  
5     def isEmpty(self):  
6         return self.items == []  
7  
8     def push(self, item):  
9         self.items.append(item)  
10  
11    def pop(self):  
12        return self.items.pop()  
13  
14
```

Stack Implementation in Python II

```
15     def peek(self):  
16         return self.items[len(self.items)-1]  
17  
18     def size(self):  
19         return len(self.items)
```

Alternative ADT Stack Implementation in Python I

```
1 class Stack:  
2     def __init__(self):  
3         self.items = []  
4  
5     def isEmpty(self):  
6         return self.items == []  
7  
8     def push(self, item):  
9         self.items.insert(0,item)  
10  
11    def pop(self):  
12        return self.items.pop(0)  
13  
14
```

Alternative ADT Stack Implementation in Python II

```
15     def peek(self):  
16         return self.items[0]  
17  
18     def size(self):  
19         return len(self.items)
```

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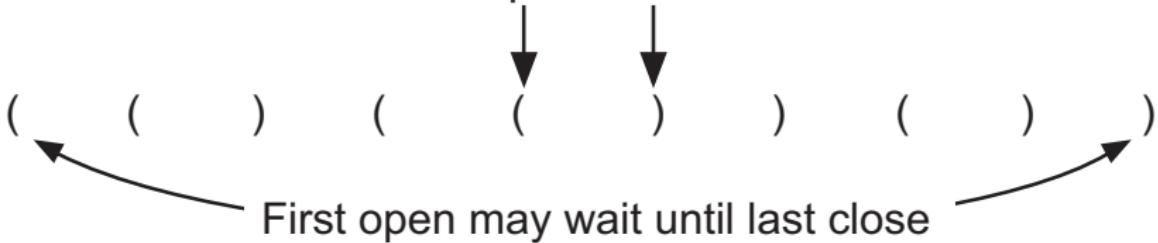
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Matching Parentheses

Most recent open matches first close



Simple Balanced Parentheses I

```
1 def parChecker(symbolString):
2     s = Stack()
3
4     balanced = True
5     index = 0
6
7     while index < len(symbolString) and balanced:
8         symbol = symbolString[index]
9         if symbol == "(":
10             s.push(symbol)
11         else:
12
13
14
```

Simple Balanced Parentheses II

```
15         if s.isEmpty():
16             balanced = False
17         else:
18             s.pop()
19
20         index = index + 1
21
22         if balanced and s.isEmpty():
23             return True
24         else:
25             return False
```

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Balanced Symbols–A General Case I

```
1 def parChecker(symbolString):
2
3     s = Stack()
4
5     balanced = True
6     index = 0
7
8     while index < len(symbolString) and balanced:
9         symbol = symbolString[index]
10        if symbol in "([{":
11            s.push(symbol)
12        else:
13
14
```

Balanced Symbols–A General Case II

```
15
16     if s.isEmpty():
17         balanced = False
18     else:
19         top = s.pop()
20         if not matches(top, symbol):
21             balanced = False
22
23         index = index + 1
24
25     if balanced and s.isEmpty():
26         return True
27     else:
28         return False
29
```

Balanced Symbols–A General Case III

```
30 def matches(open, close):  
31     opens = "[{(";  
32     closers = ")]}"  
33  
34     return opens.index(open) == closers.index(close)
```

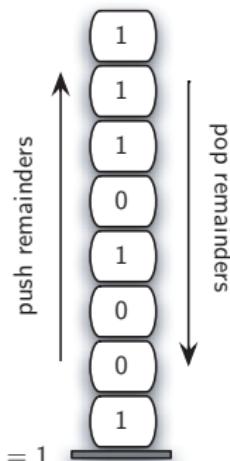
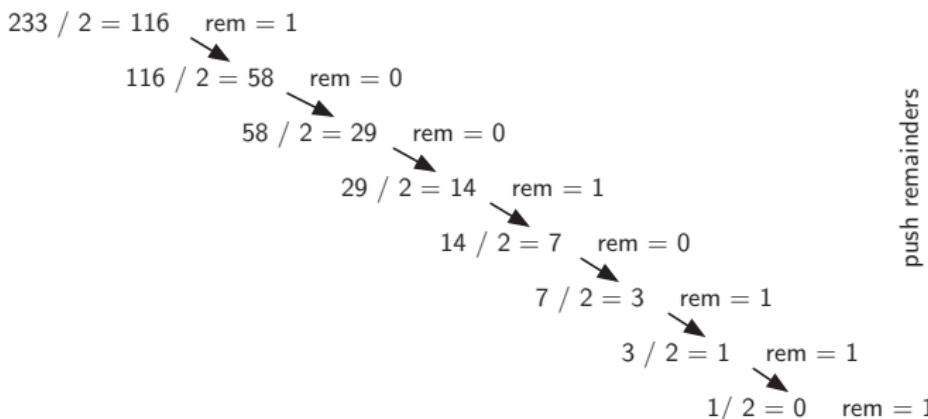
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Decimal-to-Binary Conversion



Decimal to Binary Conversion

```
1 def divideBy2(decNumber):  
2  
3     remstack = Stack()  
4  
5     while decNumber > 0:  
6         rem = decNumber % 2  
7         remstack.push(rem)  
8         decNumber = decNumber / 2  
9  
10    binString = ""  
11    while not remstack.isEmpty():  
12        binString = binString + str(remstack.pop())  
13  
14    return binString
```

Conversion to Any Base I

```
1 def baseConverter(decNumber,base):  
2  
3     digits = "0123456789ABCDEF"  
4  
5     remstack = Stack()  
6  
7     while decNumber > 0:  
8         rem = decNumber % base  
9         remstack.push(rem)  
10        decNumber = decNumber / base  
11  
12  
13  
14
```

Conversion to Any Base II

```
15     newString = ""
16     while not remstack.isEmpty():
17         newString = newString + digits[remstack.pop()]
18
19     return newString
```

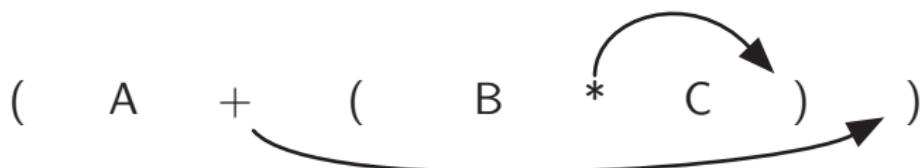
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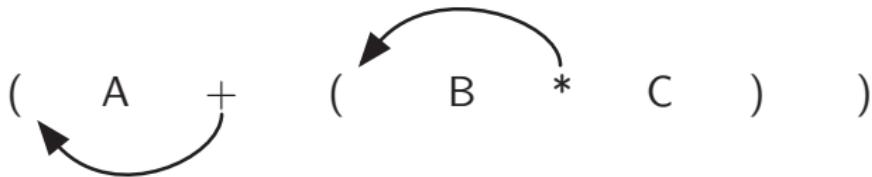
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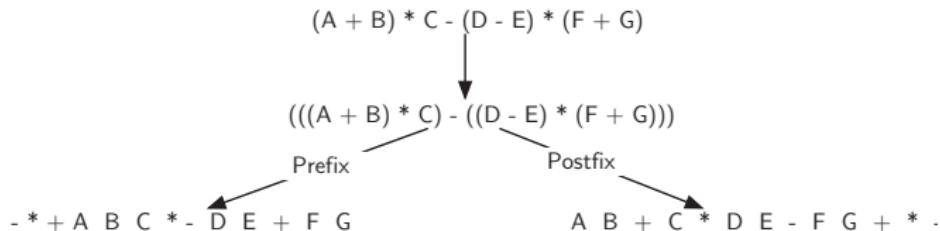
Moving Operators to the Right for Postfix Notation



Moving Operators to the Left for Prefix Notation



Converting a Complex Expression to Prefix and Postfix Notations



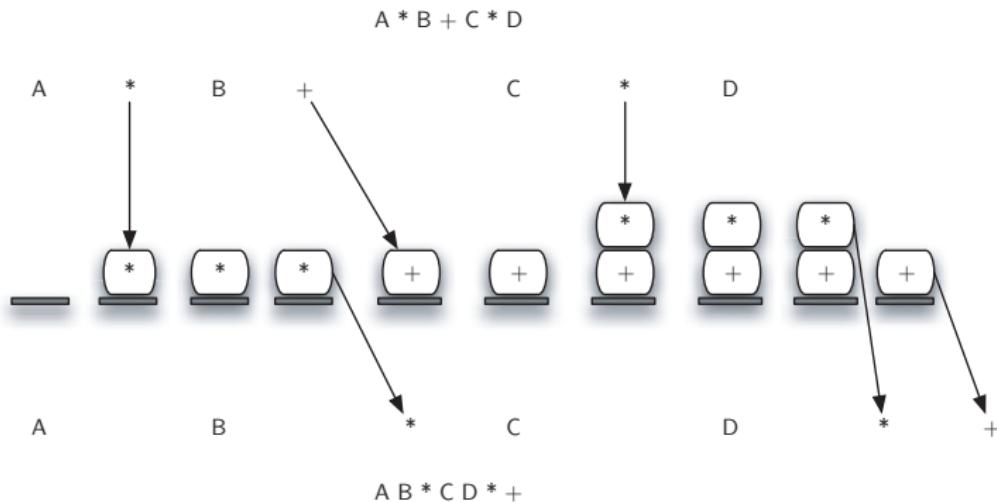
- ① Create an empty stack called `opstack` for keeping operators. Create an empty list for output.
- ② Convert the input infix string to a list by using the string method `split`.

③ Scan the token list from left to right.

- If the token is an operand, append it to the end of the output list.
- If the token is a left parenthesis, push it on the opstack.
- If the token is a right parenthesis, pop the opstack until the corresponding left parenthesis is removed. Append each operator to the end of the output list.
- If the token is an operator, *, /, +, or -, push it on the opstack. However, first remove any operators already on the opstack that have higher or equal precedence and append them to the output list.

④ When the input expression has been completely processed, check the opstack. Any operators still on the stack can be removed and appended to the end of the output list.

Converting A * B + C * D to Postfix Notation



Converting Infix Expressions to Postfix Expressions I

```
1 import string
2 def infixToPostfix(infixexpr):
3
4     prec = {}
5     prec["*"] = 3
6     prec["/"] = 3
7     prec["+"] = 2
8     prec["-"] = 2
9     prec["("] = 1
10
11    opStack = Stack()
12    postfixList = []
13
14    tokenList = infixexpr.split()
```

Converting Infix Expressions to Postfix Expressions II

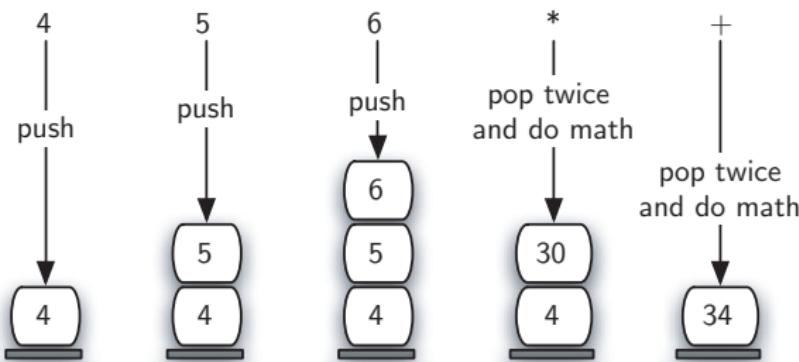
```
15
16     for token in tokenList:
17         if token in string.uppercase:
18             postfixList.append(token)
19         elif token == '(':
20             opStack.push(token)
21         elif token == ')':
22             topToken = opStack.pop()
23             while topToken != '(':
24                 postfixList.append(topToken)
25                 topToken = opStack.pop()
26
27
28
29
```

Converting Infix Expressions to Postfix Expressions III

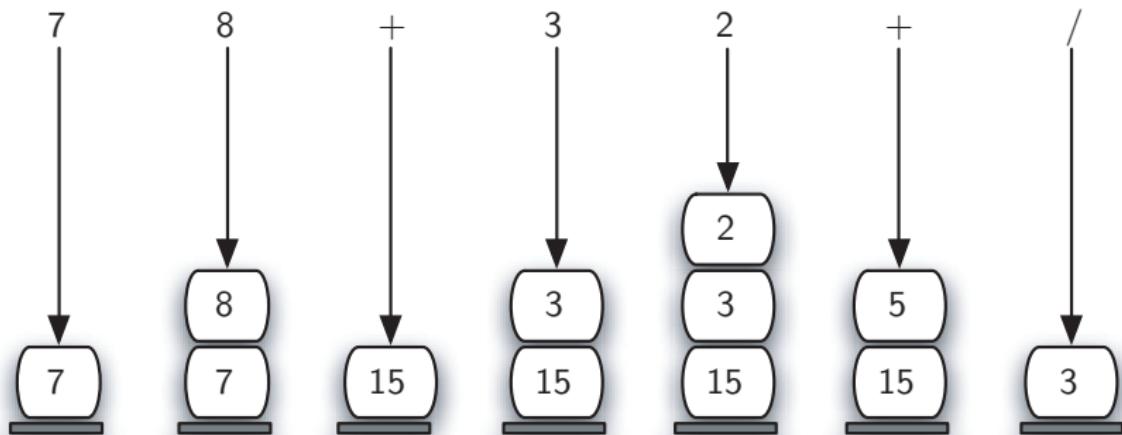
```
30     else :
31         while (not opStack.isEmpty()) and \
32             (prec[opStack.peek()] >= prec[token]):
33             postfixList.append(opStack.pop())
34
35         opStack.push(token)
36
37     while not opStack.isEmpty():
38         postfixList.append(opStack.pop())
39
40     return string.join(postfixList)
```

Stack Contents During Evaluation

Left to Right Evaluation →



A More Complex Example of Evaluation



- ➊ Create an empty stack called `operandStack`.
- ➋ Convert the string to a list by using the string method `split`.
- ➌ Scan the token list from left to right.
 - If the token is an operand, convert it from a string to an integer and push the value onto the `operandStack`.
 - If the token is an operator, `*`, `/`, `+`, or `-`, it will need two operands. Pop the `operandStack` twice. The first pop is the second operand and the second pop is the first operand. Perform the arithmetic operation. Push the result back on the `operandStack`.
- ➍ When the input expression has been completely processed, the result is on the stack. Pop the `operandStack` and return the value.

Postfix Evaluation I

```
1  def postfixEval(postfixExpr):  
2      operandStack = Stack()  
3      tokenList = postfixExpr.split()  
4  
5      for token in tokenList:  
6          if token in "0123456789":  
7              operandStack.push(int(token))  
8          else:  
9              operand2 = operandStack.pop()  
10             operand1 = operandStack.pop()  
11             result = doMath(token,operand1,operand2)  
12             operandStack.push(result)  
13  
14     return operandStack.pop()
```

Postfix Evaluation II

```
15
16 def doMath(op, op1, op2):
17     if op == "*":
18         return op1 * op2
19     else:
20         if op == "/":
21             return op1 / op2
22         else:
23             if op == "+":
24                 return op1 + op2
25             else:
26                 return op1 - op2
```