

# Recitation.

## Independence.

→ Can simplify some cond. probs.

① marginal indep.  $A \perp\!\!\!\perp B$ . # vars

$$P(A|B) = P(A).$$

$$P(A, B) = P(A) \cdot P(B).$$

② cond. indep.  $A \perp\!\!\!\perp B | C$ .

$$P(A|B, C) = P(A|C).$$

$$P(A, B|C) = P(A|C) \cdot P(B|C)$$

→ reduce #Params. needed to compute joint prob.

1  
bowl  
vars.

③ w/o independence.

A B	P(A, B)
T T	$P_1$
T F	$P_2$
F T	$P_3$
F F	$1 - (P_1 + P_2 + P_3)$

$2^k - 1$   
= exhaustive.

④ with marginal indep.

$$P(A, B) = P(A) \cdot P(B).$$

$$P(\bar{A}, B) = (1 - P(A)) \cdot P(B).$$

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## □ BAYES NET.

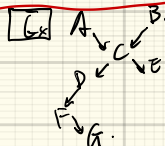
- representation of independence assumption.

- DAG: no loop.

- may be disconnected.

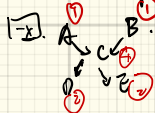
### Assumption

A variable is cond. indep. of its non-descendants given its parent.



$$\begin{aligned} P(F | \text{parent}(F)) &= P(F | \text{parent}(F)) \\ &= P(F | A, B, C, D, E) \\ &= P(F | D, E) \end{aligned}$$

③ with cond. indep.



$$\begin{aligned} P(A, B, C, D, E, F, G) &\leftarrow \text{reverse topo.} \leftarrow \text{given parent.} \\ &= P(A, B, C, D, E, F, G) \\ &= P(E | \bar{D}, \bar{C}, \bar{B}, \bar{A}) \cdot P(D | \bar{C}, \bar{B}, \bar{A}) \\ &= P(E | \bar{D}, \bar{C}, \bar{B}, \bar{A}) \cdot P(D | \bar{C}, \bar{B}, \bar{A}) \cdot P(C | \bar{B}, \bar{A}) \cdot P(B | \bar{A}) \cdot P(A) \\ &= P(E | \bar{D}, \bar{C}) \cdot P(D | \bar{C}) \cdot P(C | \bar{B}) \cdot P(B | \bar{A}) \cdot P(A) \end{aligned}$$

all encoded in Bayes Net

④ with conditional prob

$$P(C | A=a, B=b).$$

exhaustive all prob

$$(\# \text{Val} - 1) \cdot \# \text{parent}$$

(ex)

A B	P(C   A, B)
T T	$P_1$
T F	$P_2$
F T	$P_3$
F F	$P_4$

infer  $P(C | A, B)$   
 $P(A, B, C)$ .