

# Recitation.

## Probabilities (Review)

- Independence.
- Chain Rule & Bayes Rule

## Bayes Net

D-separation.

Explain Away.

## Application.

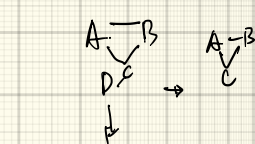
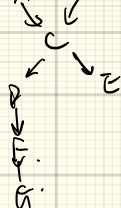
- Naive Bayes.
- Model.

## Bayes Net.

assumption a var is condi indep.  
of its non-desc given parent

## D-separation.

Ex.  $A \perp\!\!\!\perp B \mid D, E?$



①  $A \perp\!\!\!\perp B?$   
A, B. indep.  
 $A \perp\!\!\!\perp B \mid C?$

$A \perp\!\!\!\perp B$  structurally dependent.

## Probabilities.

Independence.

① marginal indep.

$A \perp\!\!\!\perp B.$

$$P(A|B) = P(A)$$

$$P(A|B) = P(A) P(B).$$

② conditional indep.

$A \perp\!\!\!\perp B \mid C$

$$P(A|B, C) = P(A|C).$$

$$P(A|B, C) = P(A|C) \cdot P(B|C)$$

Chain Rule.

① joint prob.  $P(A, B, C, D) = P(A|B, C, D) \cdot P(B|C, D) \cdot P(C|D) \cdot P(D)$

② condi prob.  $P(A, B, C, D) = \frac{P(A, B, C, D)}{P(C, D)} = P(A|B, C, D) \cdot P(B|C, D) \cdot P(C, D)$

③ Bayes Rule.

$$\begin{aligned} P(A|B) &= P(A|B) \cdot P(B) \\ P(B|A) &= P(B|A) \cdot P(A) \end{aligned} \quad \text{④}$$

$$P(A|B) = \frac{P(B|A) \cdot P(A)}{P(B)}$$

## Explain Away.

two vars that were marginally indep.  
becomes conditionally dep given child  
- Berkson's Fallacy / Paradox.  
(counterintuitive).  
: when prob. for each is low.