

ELEC207 - Instrumentation & Control

Part-A: Instrumentation

Problem Class 2

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Lecture schedule:

Monday 1700-1800 (CHAD-CHAD)

Thursday 1400-1500 (CTH-LTA)

Office Location: Room 513, Electrical Engineering

Lecture covers

- Exam questions on:
 - Temperature measurement devices
 - Thermocouples
 - Resistance Temperature Device (RTD)
 - Thermistor
 - Error Analysis
- Feedback on:
 - HW-2
 - Online Survey

Feedback on HW-2

Resistance Temperature Device (RTD)

a) A platinum resistive temperature detector (RTD) is used to measure the temperature of a jet engine wall. Assuming that the temperature is never below 0° C. Write the (quadratic) Callender-van Dusen equation which relates the RTD resistance to its temperature. **(7 Marks)**

Solution:

$$R(T) = R_0(1 + a_1T + a_2T^2 + \dots + a_nT^n)$$

$$R(T) = R_0(1 + a_1T + a_2T^2)$$

Quadratic form (Callender-van Dusen equation)

Where, R_0 is resistance at 0°C, a_1 and a_2 are metal specific coefficients.

Feedback on HW-2

Resistance Temperature Device (RTD)

b) Given the Callender-van Dusen coefficients for platinum $A=3.9 \times 10^{-3} \text{ }^{\circ}\text{C}^{-1}$, $B=-5.8 \times 10^{-7} \text{ }^{\circ}\text{C}^{-2}$, the RTD resistance $R_0=100 \text{ } \Omega$ at 0°C , and the range of measurements (full scale deflection - FSD) from 0°C to 850°C calculate:

i) The RTD resistance R_T at 800°C . **(5 Marks)**

Solution:

$$R(T) = R_0(1 + a_1T + a_2T^2) \quad a_1 \rightarrow A; a_2 \rightarrow B$$

$$R(800) = 100. [1 + (3.9 \times 10^{-3}). (800) + (-5.8 \times 10^{-7}). (800)^2]$$

$$R(800) = 100. [1 + 3.12 - 0.3712]$$

$$R(800) = 374.88 \text{ } \Omega$$

Feedback on HW-2

Error Analysis

- b) Given the Callender-van Dusen coefficients for platinum $A=3.9 \times 10^{-3} \text{ }^{\circ}\text{C}^{-1}$, $B=-5.8 \times 10^{-7} \text{ }^{\circ}\text{C}^{-2}$, the RTD resistance $R_0=100 \text{ } \Omega$ at 0°C , and the range of measurements (full scale deflection - FSD) from 0°C to 850°C calculate:
- ii) Assuming endpoint linearity calculate the RTD sensitivity for the given FSD. **(5 Marks)**

Solution:

$$\text{Sensitivity} = \frac{R(850) - R(0)}{\Delta T}$$

$$R(850) = 100. [1 + (3.9 \times 10^{-3}). (850) + (-5.8 \times 10^{-7}). (850)^2]$$

$$R(850) = 100. [1 + 3.315 - 0.41905]$$

$$R(850) = 389.595 \text{ } \Omega$$

Feedback on HW-2

Error Analysis

- b) Given the Callender-van Dusen coefficients for platinum $A=3.9 \times 10^{-3} \text{ }^{\circ}\text{C}^{-1}$, $B=-5.8 \times 10^{-7} \text{ }^{\circ}\text{C}^{-2}$, the RTD resistance $R_0=100 \text{ } \Omega$ at 0°C , and the range of measurements (full scale deflection - FSD) from 0°C to 850°C calculate:
- ii) Assuming endpoint linearity calculate the RTD sensitivity for the given FSD. **(5 Marks)**

Solution:

$$\text{Sensitivity} = \frac{R(850) - R(0)}{\Delta T}$$

$$R(850) = 389.595 \text{ } \Omega$$

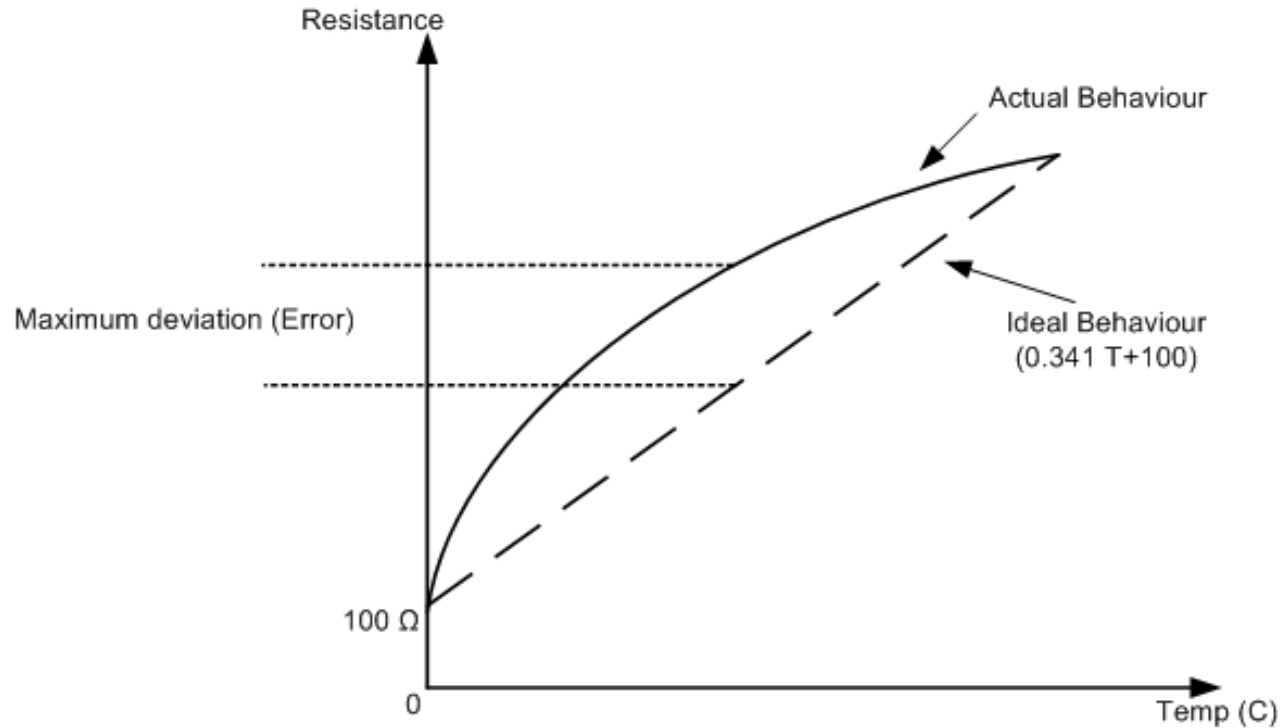
$$\text{Sensitivity} = \frac{389.595 - 100}{850} = \frac{289.585}{850} = 0.3407 \text{ } \Omega \text{ }^{\circ}\text{C}^{-1}$$

Error Analysis

- b) Given the Callender-van Dusen coefficients for platinum $A=3.9 \times 10^{-3} \text{ }^{\circ}\text{C}^{-1}$, $B=-5.8 \times 10^{-7} \text{ }^{\circ}\text{C}^{-2}$, the RTD resistance $R_0=100 \text{ } \Omega$ at 0°C , and the range of measurements (full scale deflection - FSD) from 0°C to 850°C calculate:
- iii) The maximum endpoint linearity error in % FSD.
- (8 Marks)**

See Bentley, Chapter 2, pages 9-11 for more details.

Error Analysis



$$\varepsilon(T) = R(T) - R(Ideal)$$

$$\varepsilon(T) = [R_0(1 + a_1T + a_2T^2)] - (0.341T + 100)$$

Error Analysis

$$\varepsilon(T) = [R_0(1 + a_1T + a_2T^2)] - (0.341T + 100)$$

$$\varepsilon(T) = [100. [1 + (3.9 \times 10^{-3})T + (-5.8 \times 10^{-7})T^2] - (0.341T + 100)]$$

$$\varepsilon(T) = [100. [(3.9 \times 10^{-3})T - (5.8 \times 10^{-7})T^2] - (0.341T)]$$

$$\varepsilon(T) = (3.9 \times 10^{-1})T - (5.8 \times 10^{-5})T^2 - (0.341T)]$$

$$\varepsilon(T) = 0.049 T - 5.8 \times 10^{-5} T^2 \quad \dots (1)$$

Error Analysis

$$\varepsilon(T) = 0.049 T - 5.8 \times 10^{-5} T^2 \quad \dots (1)$$

Differentiate w.r.t “T” and equate to 0, for maximum deviation

$$\frac{d \varepsilon(T)}{dT} = 0.049 - (2) \cdot (5.8 \times 10^{-5}) T = 0$$

$$\frac{d \varepsilon(T)}{dT} = 0.049 - 1.16 \times 10^{-4} T = 0$$

$$T = \frac{0.049}{1.16 \times 10^{-4}}$$

$$T = 422.41 \text{ }^{\circ}\text{C}$$

Error Analysis

$$T = 422.41 \text{ }^{\circ}\text{C}$$

Substituting the value in Eq. 1

$$\varepsilon(T) = 0.049 T - 5.8 \times 10^{-5} T^2 \quad \dots (1)$$

$$\varepsilon(T_{Max}) = 0.049 (422.41) - 5.8 \times 10^{-5} (422.41)^2$$

$$\varepsilon(T_{Max}) = 20.6981 - 10.3489$$

$$\varepsilon(T_{Max}) = 10.35 \text{ } \Omega$$

Error Analysis

$$\varepsilon(T_{Max}) = 10.35 \, \Omega$$

In terms of % of FSD

$$\varepsilon (\%FSD) = \frac{10.35}{389.595 - 100} * 100$$

$$\varepsilon (\%FSD) = 3.57\%$$

Thermocouples

The output voltage of a thermocouple with its reference junction at 40°C is 3.562 mV. Using Table Q1 determine the temperature measured by the thermocouple. **(8 Marks)**

Similar Questions in 2012-2015 exams

| °C | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 0 | 0.000 | 0.059 | 0.118 | 0.176 | 0.235 | 0.294 | 0.354 | 0.413 | 0.472 | 0.532 | 0.591 |
| 10 | 0.591 | 0.651 | 0.711 | 0.770 | 0.830 | 0.890 | 0.950 | 1.010 | 1.071 | 1.131 | 1.192 |
| 20 | 1.192 | 1.252 | 1.313 | 1.373 | 1.434 | 1.495 | 1.556 | 1.617 | 1.678 | 1.740 | 1.801 |
| 30 | 1.801 | 1.862 | 1.924 | 1.986 | 2.047 | 2.109 | 2.171 | 2.233 | 2.295 | 2.357 | 2.420 |
| 40 | 2.420 | 2.482 | 2.545 | 2.607 | 2.670 | 2.733 | 2.795 | 2.858 | 2.921 | 2.984 | 3.048 |
| 50 | 3.048 | 3.111 | 3.174 | 3.238 | 3.301 | 3.365 | 3.429 | 3.492 | 3.556 | 3.620 | 3.685 |
| 60 | 3.685 | 3.749 | 3.813 | 3.877 | 3.942 | 4.006 | 4.071 | 4.136 | 4.200 | 4.265 | 4.330 |
| 70 | 4.330 | 4.395 | 4.460 | 4.526 | 4.591 | 4.656 | 4.722 | 4.788 | 4.853 | 4.919 | 4.985 |
| 80 | 4.985 | 5.051 | 5.117 | 5.183 | 5.249 | 5.315 | 5.382 | 5.448 | 5.514 | 5.581 | 5.648 |
| 90 | 5.648 | 5.714 | 5.781 | 5.848 | 5.915 | 5.982 | 6.049 | 6.117 | 6.184 | 6.251 | 6.319 |

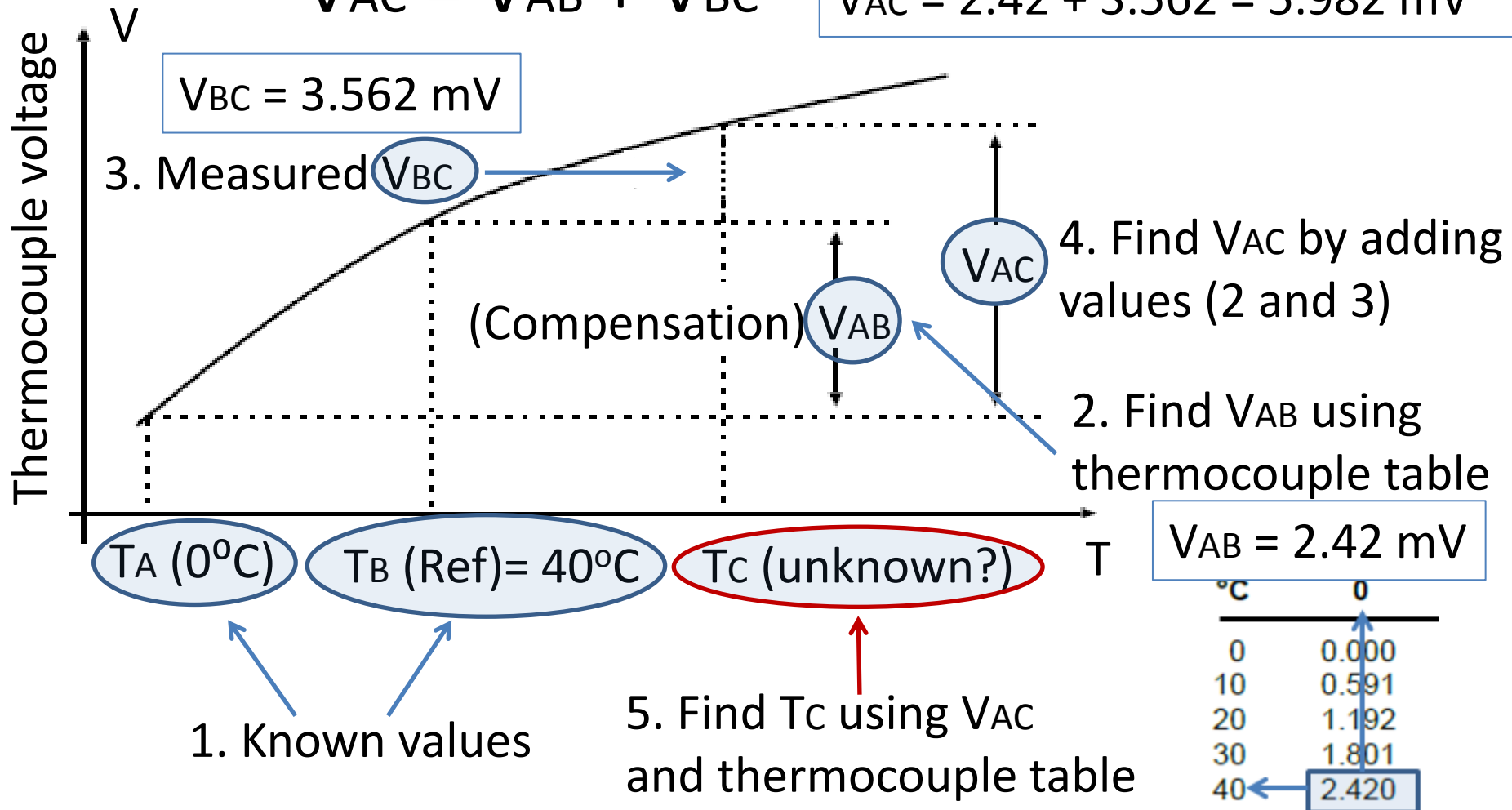

mV



Thermocouples

$$V_{AC} = V_{AB} + V_{BC}$$

$$V_{AC} = 2.42 + 3.562 = 5.982 \text{ mV}$$





Thermocouples

| °C | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 0 | 0.000 | 0.059 | 0.118 | 0.176 | 0.235 | 0.294 | 0.354 | 0.413 | 0.472 | 0.532 | 0.591 |
| 10 | 0.591 | 0.651 | 0.711 | 0.770 | 0.830 | 0.890 | 0.950 | 1.010 | 1.071 | 1.131 | 1.192 |
| 20 | 1.192 | 1.252 | 1.313 | 1.373 | 1.434 | 1.495 | 1.556 | 1.617 | 1.678 | 1.740 | 1.801 |
| 30 | 1.801 | 1.862 | 1.924 | 1.986 | 2.047 | 2.109 | 2.171 | 2.233 | 2.295 | 2.357 | 2.420 |
| 40 | 2.420 | 2.482 | 2.545 | 2.607 | 2.670 | 2.733 | 2.795 | 2.858 | 2.921 | 2.984 | 3.048 |
| 50 | 3.048 | 3.111 | 3.174 | 3.238 | 3.301 | 3.365 | 3.429 | 3.492 | 3.556 | 3.620 | 3.685 |
| 60 | 3.685 | 3.749 | 3.813 | 3.877 | 3.942 | 4.006 | 4.071 | 4.136 | 4.200 | 4.265 | 4.330 |
| 70 | 4.330 | 4.395 | 4.460 | 4.526 | 4.591 | 4.656 | 4.722 | 4.788 | 4.853 | 4.919 | 4.985 |
| 80 | 4.985 | 5.051 | 5.117 | 5.183 | 5.249 | 5.315 | 5.382 | 5.448 | 5.514 | 5.581 | 5.648 |
| 90 | 5.648 | 5.714 | 5.781 | 5.848 | 5.915 | 5.982 | 6.049 | 6.117 | 6.184 | 6.251 | 6.319 |

mV

Oil temperature is 95° C

Thermistor

d) Determine the temperature measured by a thermistor if it has a resistance of 50 kΩ at 25°C, the characteristic temperature of 2000 K, and the measured resistance 150 kΩ. **(8 Marks)**

Lecture 5.pdf

$$R = R_0 e^{\left[\beta \left(\frac{1}{T} - \frac{1}{T_0}\right)\right]}$$

R is the resistance at temperature T,
R₀ is the resistance at temperature T₀,
β is a material constant
β, T and T₀ are expressed in 'K'

Thermistor

$$R = R_0 e^{\left[\beta \left(\frac{1}{T} - \frac{1}{T_0}\right)\right]}$$

$$\beta = 2000 \text{ K}$$

$$R_0 = 50 \text{ K}\Omega \quad T_0 = 25 \text{ }^\circ\text{C} = 25 + 273 = 298 \text{ K}$$

$$R = 150 \text{ K}\Omega \quad T = ?$$

$$150 \text{ K} = 50 \text{ K} e^{\left[2000 \left(\frac{1}{T} - \frac{1}{298}\right)\right]}$$

Thermistor



$$3 \quad \cancel{150 \text{ K}} = \cancel{50 \text{ K}} e^{[2000(\frac{1}{T} - \frac{1}{298})]}$$

$$3 = e^{[2000(\frac{1}{T} - \frac{1}{298})]}$$

$$3 = e^{[2000(\frac{298-T}{298.T})]}$$

$$\ln(3) = 2000 \left(\frac{298 - T}{298.T} \right)$$

$$\ln(3) = 2000 \left(\frac{298 - T}{298.T} \right)$$

$$1.0986 = 2000 \left(\frac{298 - T}{298.T} \right)$$

$$0.0005493 = \frac{298 - T}{298.T}$$

$$0.1637T = 298 - T$$

$$1.1637T = 298$$

Thermistor

$$1.1637T = 298$$

$$T = \frac{298}{1.1637}$$

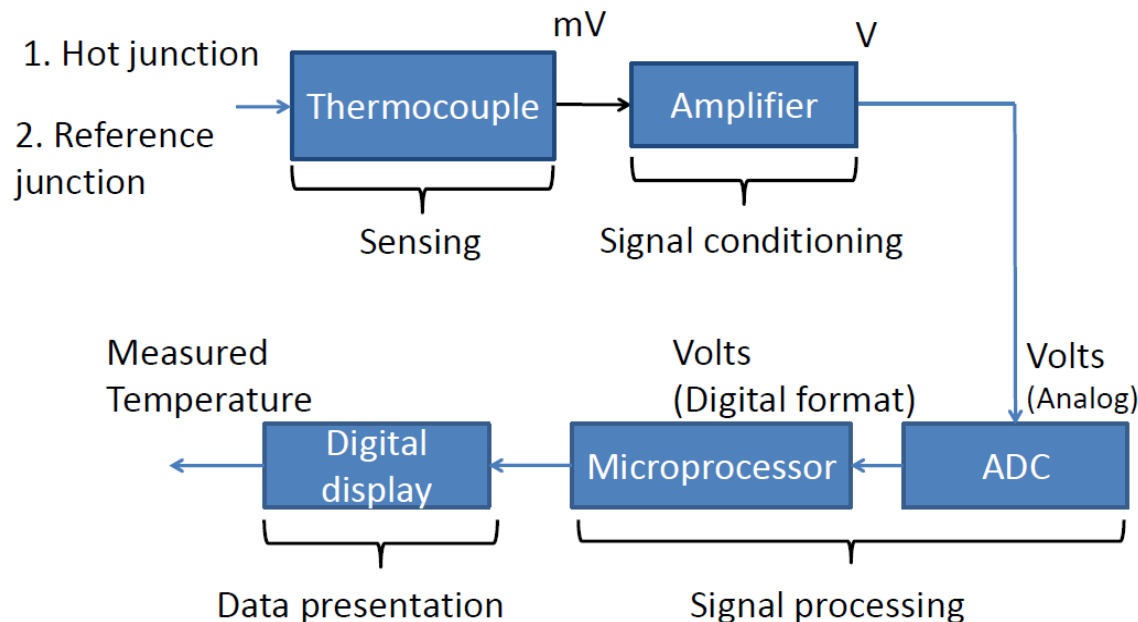
$$T = 256.1 \text{ K}$$

$$T = 256.1 - 273 = -16.9 \text{ }^{\circ}\text{C}$$

$$T = -16.9 \text{ }^{\circ}\text{C}$$

Measurement System (2014-15)

Q. With the aid of a block diagram, show how a thermocouple is used in a temperature measurement system. The block diagram should clearly show the sensing element, the required signal conditioning and signal processing elements. (5 Marks)



Slide 4, Lecture 5.pdf

Summary

Topics covered:

- ✓ Exam questions on:
 - ✓ Temperature measurement devices.
 - ✓ Thermocouples
 - ✓ RTDs
 - ✓ Thermistors
 - ✓ Error Analysis
- ✓ Feedback on:
 - ✓ HW-2
 - ✓ Online Survey

Next Lecture:

- Monday, 9th Nov 2015 (CHAD-CHAD) 1700-1800