

Supporting Information for

**A Numerical Study of Lithospheric Deformation and Strain Partitioning Across the Longmen Shan Orogenic Belt, Eastern Tibetan Plateau**

Yujun Sun<sup>\*</sup>, Hailong Li, Taoyuan Fan

Chinese Academy of Geological Sciences, Beijing, 100037, China

<sup>\*</sup> Corresponding author: Yujun Sun (sunyujunabc@163.com)

**Contents of this file**

This supporting information contains supply figures and tables presented and discussed in the text, and the numerical modeling data. Table S1 shows the rheological parameters of all cases. Figure S1 to S11 show the supply figures discussed in the text. Tables R1-R14 show the cumulative strain (the second invariant of the deviatoric strain tensor), strain rate (the second invariant of the deviatoric strain rate tensor), stress (the second invariant of the deviatoric stress tensor), temperature, and vertical heat flow for different cases in the text.

**Additional supporting information**

Table S1

Figures S1 to S11

**Modeling data**

Table R1-R14

**Introduction**

**Description for Table S1**

(1) Rheological parameters for two groups of models (Table S1).

29

30 **Description for Figures S1 to S11:**

- 31 (1) Distribution of the effective viscosity at different depth in the eastern Tibetan  
32 Plateau (Figure. S1);
- 33 (2) Distribution of the strength at different depth in the eastern Tibetan Plateau  
34 (Figure. S2);
- 35 (3) Distribution of the calculated stress (the second invariant of the deviatoric stress)  
36 for the different cases A (a), A1 (b), and A2 (c) (Figure. S3);
- 37 (4) Distribution of the calculated stress (the second invariant of the deviatoric stress)  
38 for the different cases B (a), B1 (b), and B2 (c) (Figure. S4);
- 39 (5) Predicted cumulative strain and strain rate for the different cases B2, B2-1, and  
40 B2-2. This figure shows the effects of the crustal strength of the Longmen Shan on  
41 lithospheric deformation and strain partitioning (Figure. S5);
- 42 (6) Comparison of the calculated topography (a), surface heat flow (b) with the  
43 observations for cases B2, B2-1, and B2-2 (Figure. S6);
- 44 (7) Predicted cumulative strain and strain rate for the different cases B3, B3-1, and  
45 B3-2. This figure shows the effects of the initial width of the Longmen Shan on  
46 lithospheric deformation and strain partitioning (Figure. S7).
- 47 (8) Comparison of the calculated topography (a), surface heat flow (b) with the  
48 observations for cases B3, B3-1, and B3-2 (Figure. S8).
- 49 (9) Predicted cumulative strain and strain rate for the different cases A1, A1-1, and  
50 A1-2. This figure shows the effects of the convergence velocity on lithospheric  
51 deformation and strain partitioning (Figure. S9).
- 52 (10) Predicted cumulative strain and strain rate for the different cases A3, A3-1, and  
53 A3-2. This figure shows the effects of the lower crustal viscosity in the  
54 Songpan-Ganzi terrane and Longmen Shan on lithospheric deformation and strain  
55 partitioning (Figure. S10).
- 56 (11) Comparison of the calculated topography (a), surface heat flow (b) with the  
57 observations for cases A3, A3-1, and A3-2 (Figure. S11).

58

## **Description for Table R1-R14**

There are 150,000 markers used in the numerical model. Thus, we show the cumulative strain, strain rate, stress, temperature and vertical heat flow for every marker at different time steps. For each table at specific time, there are 150,000 rows and 5 columns. 150,000 rows present 150,000 markers at present time step.

The column 1 to column 7 follows:

Column 1: the x axis position (unit: meter. horizontal direction) for each marker at present time step.

Column 2: the y axis position (unit: meter. vertical direction) for each marker at present time step.

Column 3: the cumulative strain (the second invariant of the deviatoric strain  $\epsilon_{II}$ ) for each marker from 0 to present time step.

Column 4: the strain rate (the second invariant of the deviatoric strain rate  $\dot{\epsilon}_{II}$ , unit:  $s^{-1}$ ) for each marker at present time step.

Column 5: the stress (the second invariant of the deviatoric stress  $\sigma_{II}$ , unit: Pa) for each marker at present time step.

Column 6: the temperature (unit:  $^{\circ}C$ ) for each marker at present time step.

Column 7: the vertical heat flow (unit:  $mW/m^2$ ) for each marker at present time step.

Table R1: "caseA1\_20Myr.csv" contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case A1.

Table R2: "caseA2\_20Myr.csv" contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case A2.

Table R3: "caseA3\_20Myr.csv" contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case A3.

Table R4: "caseB1\_20Myr.csv" contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case B1.

Table R5: "caseB2\_20Myr.csv" contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case B2.

Table R6: "caseB3\_20Myr.csv" contains the cumulative strain, strain rate, stress,

temperature and vertical heat flow after 20 Million years of convergence in case B3.

Table R7: " caseB21\_ 20Myr. csv " contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case B2-1. The upper and middle crustal strength of the Longmen Shan in this case is 50 MPa.

Table R8: " caseB22\_ 20Myr. csv " contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case B2-2. The upper and middle crustal strength of the Longmen Shan in this case is 10 MPa.

Table R9: " caseB31\_ 20Myr. csv " contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence based on case B3-1. The initial width of the Longmen Shan in this case is 100 km.

Table R10: " caseB32\_ 20Myr. csv " contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence based on case B3-2. The initial width of the Longmen Shan in this case is 50 km.

Table R11: " caseA11\_ 26.7Myr.csv" contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 26.7 Million years of convergence in case A1-1. The velocity boundary imposed on the left boundary of the model in this case was 30 mm/yr.

Table R12: " caseA12\_ 40Myr.csv" contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 40 Million years of convergence in case A1-2. The velocity boundary imposed on the left boundary of the model in this case was 40 mm/yr.

Table R13: " caseA31\_ 20Myr. csv " contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case A3-1. The viscosity imposed on the lower crust of the Songpan-Ganzi terrane and Longmen Shan was  $1.0 \times 10^{20} \text{ Pa} \cdot \text{s}$  in this case.

Table R14: " caseA32\_ 20Myr. csv " contains the cumulative strain, strain rate, stress, temperature and vertical heat flow after 20 Million years of convergence in case A3-2. The viscosity imposed on the lower crust of the Songpan-Ganzi terrane and Longmen Shan was  $5.0 \times 10^{19} \text{ Pa} \cdot \text{s}$  in this case.

119 **Table S1** Rheological parameters in two groups of models \*.

Group A models							
Models	Layers	Songpan-Ganzi		Longmen Shan		Sichuan Basin	
		Viscosity (Pa • s)	Yield strength	Viscosity (Pa • s)	Yield strength	Viscosity	Yield strength
Case A1	Upper crust	$1 \times 10^{23}$	10	$1 \times 10^{23}$	10	$5 \times 10^{23}$	100
	Middle crust	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
	Lower crust	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
	Mantle lithosphere	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
Case A2	Upper crust	$1 \times 10^{23}$	10	$1 \times 10^{23}$	10	$5 \times 10^{23}$	20
	Middle crust	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
	Lower crust	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
	Mantle lithosphere	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
Case A3	Upper crust	$1 \times 10^{23}$	10	$1 \times 10^{23}$	10	$5 \times 10^{23}$	20
	Middle crust	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
	Lower crust	$1 \times 10^{21}$	50	$1 \times 10^{21}$	50	$5 \times 10^{23}$	100
	Mantle lithosphere	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100

120

121

Group B models							
Models	Layers	Songpan-Ganzi		Longmen Shan		Sichuan Basin	
		Viscosity	Yield	Viscosity	Yield	Viscosity	Yield
		(Pa.s)	strength	(Pa.s)	strength	(Pa.s)	strength
Case B1	Upper crust	$1 \times 10^{23}$	10	$1 \times 10^{23}$	100	$5 \times 10^{23}$	100
	Middle crust	$5 \times 10^{22}$	50	$1 \times 10^{23}$	100	$5 \times 10^{23}$	100
	Lower crust	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
	Mantle lithosphere	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
Case B2	Upper crust	$1 \times 10^{23}$	10	$1 \times 10^{23}$	100	$5 \times 10^{23}$	100
	Middle crust	$5 \times 10^{22}$	50	$1 \times 10^{23}$	100	$5 \times 10^{23}$	100
	Lower crust	$1 \times 10^{21}$	50	$1 \times 10^{21}$	50	$5 \times 10^{23}$	100
	Mantle lithosphere	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100
Case B3	Upper crust	$1 \times 10^{23}$	10	$1 \times 10^{23}$	100	$5 \times 10^{23}$	10
	Middle crust	$5 \times 10^{22}$	50	$1 \times 10^{23}$	100	$5 \times 10^{23}$	100
	Lower crust	$1 \times 10^{21}$	50	$1 \times 10^{21}$	50	$5 \times 10^{23}$	100
	Mantle lithosphere	$5 \times 10^{22}$	50	$5 \times 10^{22}$	50	$5 \times 10^{23}$	100

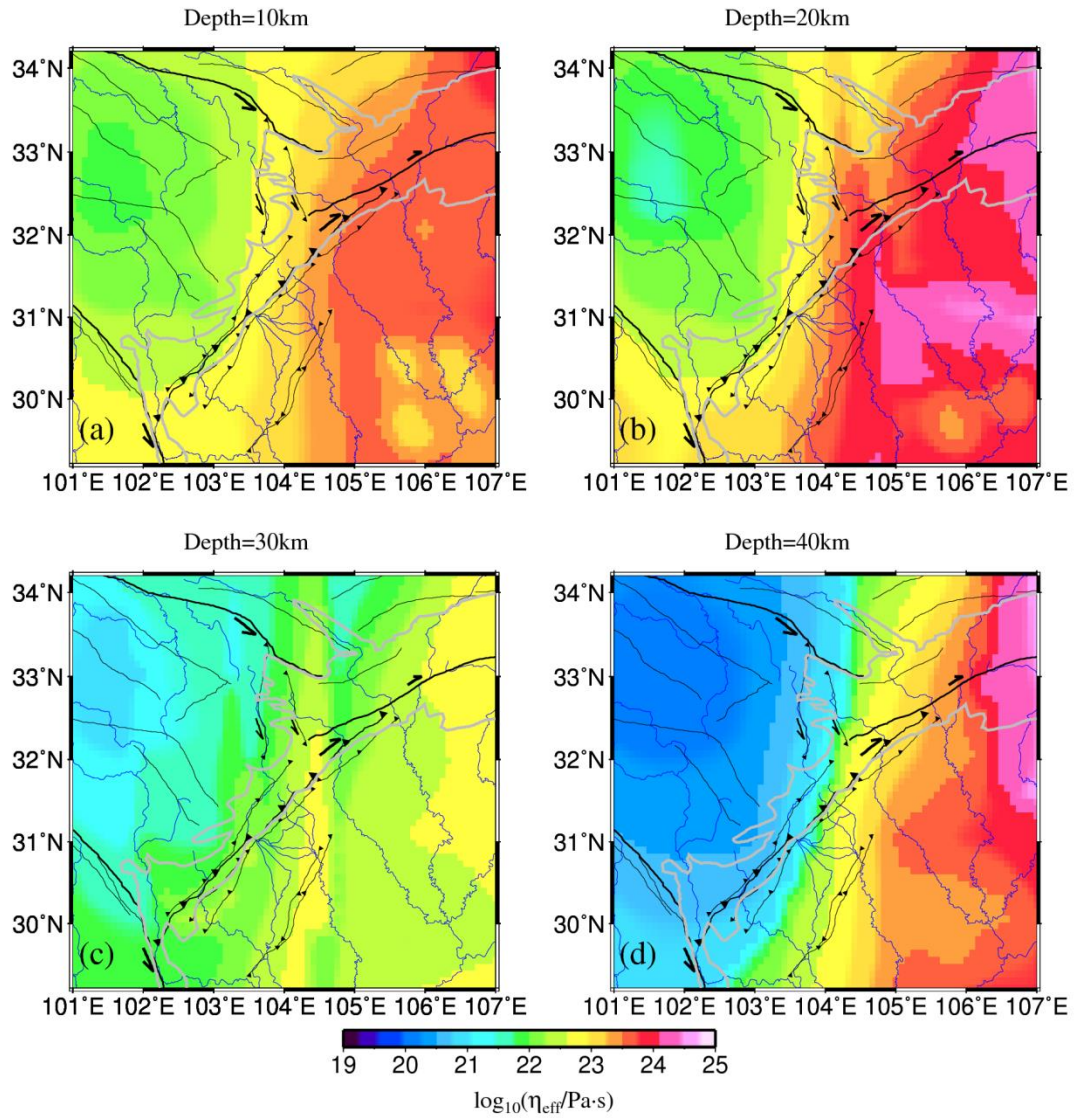
122

123 \* Constant density was used in the model:  $2600 \text{ kg/m}^3$  for the upper crust,  $2800 \text{ kg/m}^3$   
124 for the middle crust,  $3000 \text{ kg/m}^3$  for the lower crust, and  $3300 \text{ kg/m}^3$  for the mantle.

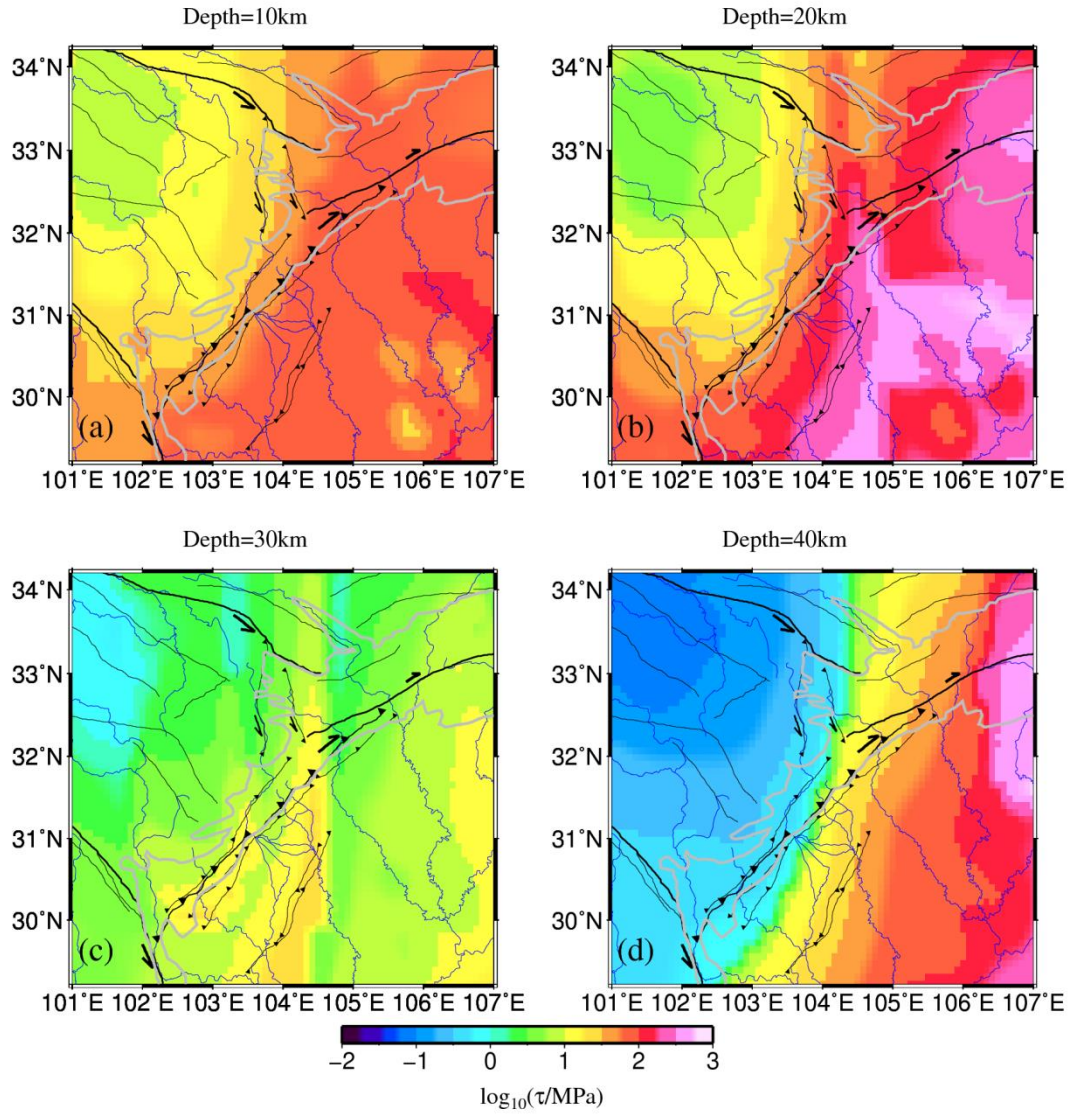
125 Radioactive heat production of  $Q_r^{upper \text{ crust}} = 1.28 \times 10^{-6} \text{ W/m}^3$ ,  $Q_r^{middle \text{ crust}} =$   
126  $1.0 \times 10^{-6} \text{ W/m}^3$  and  $Q_r^{lower \text{ crust}} = 0.8 \times 10^{-6} \text{ W/m}^3$  were imposed on the  
127 upper crust, middle crust, and lower crust, respectively. Radioactive heat production  
128 for the mantle is 0. Thermal conductivities of

129  $k^{upper \text{ crust}} = 3.0 \text{ W/(m} \cdot \text{K)}$ ,  $k^{middle \text{ crust}} = 3.0 \text{ W/(m} \cdot \text{K)}$ ,  $k^{lower \text{ crust}} =$   
130  $3.2 \text{ W/(m} \cdot \text{K)}$ ,  $k^{mantle \text{ lithosphere}} = 3.4 \text{ W/(m} \cdot \text{K)}$ ,  $k^{asthenosphere} = 3.8 \text{ W/(m} \cdot$   
131  $\text{K})$  were imposed. Heat capacity  $c = 1300 \text{ J/(kg} \cdot \text{K)}$  was used for all layers. The  
132 crust and mantle lithosphere have a visco-plastic rheology. The asthenosphere has  
133 viscous rheology, which does not include plastic deformation. The viscosity of the  
134 asthenosphere is  $1 \times 10^{21} \text{ Pa} \cdot \text{s}$  in all cases.

135

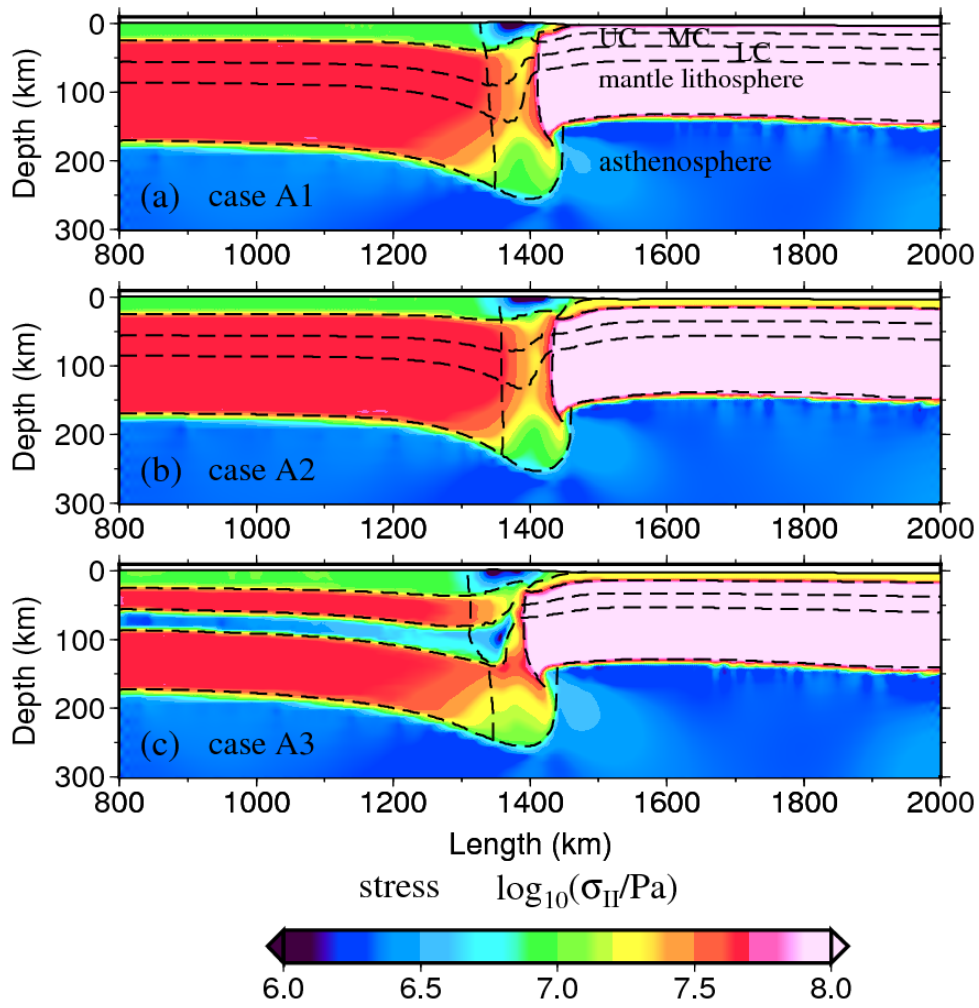


**Figure S1.** The calculated effective viscosity in this area (Sun et.al 2013a). Gray lines indicate the Paleozoic/Proterozoic stratum (Figure 2), which are generally consistent with the Longmen Shan orogenic belt. Black lines indicate the main faults in the study area. Blue lines indicate the main rivers in this area.

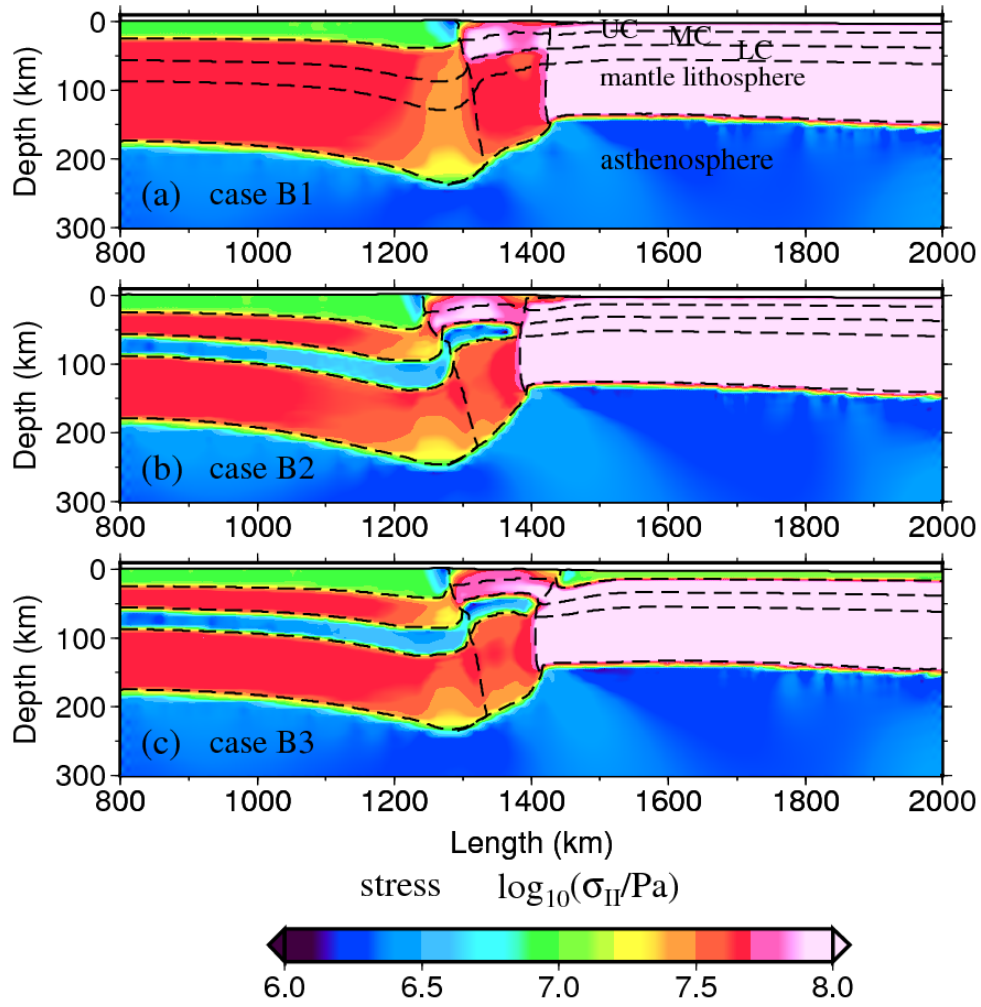


**Figure S2.** The calculated strength in this area (Sun et.al 2013a). Gray lines indicate the Paleozoic/Proterozoic stratum (Figure 2), which are generally consistent with the Longmen Shan orogenic belt. Black lines indicate the main faults in the study area. Blue lines indicate the main rivers in this area.

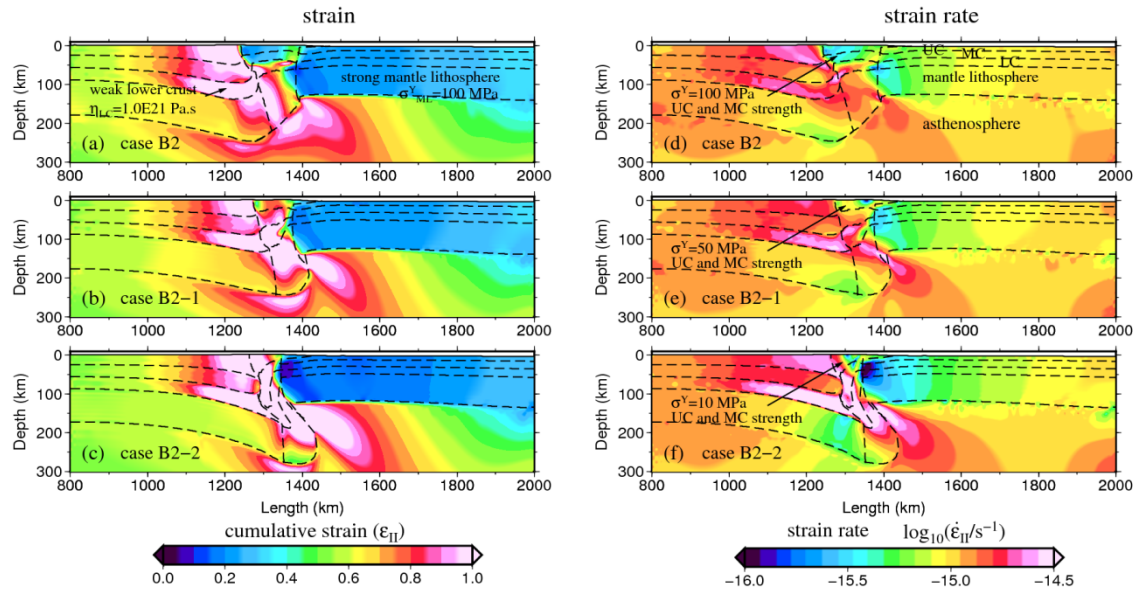




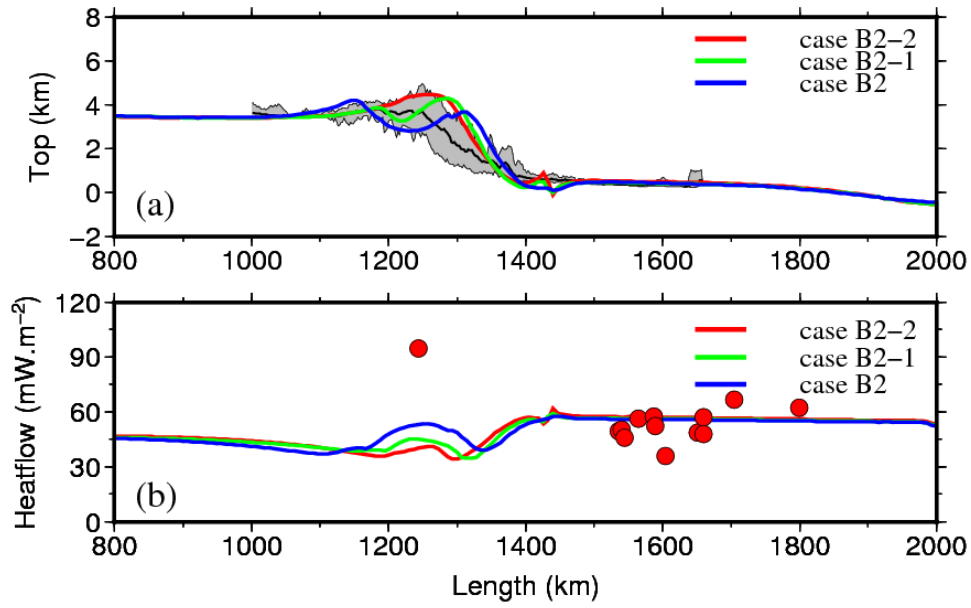
**Figure S3.** Distribution of the stress (the second invariant of the deviatoric stress tensor) in the different cases (A1, A2, and A3) after 20 Myr of compression. Dashed lines show the general boundaries of the different layers and blocks.



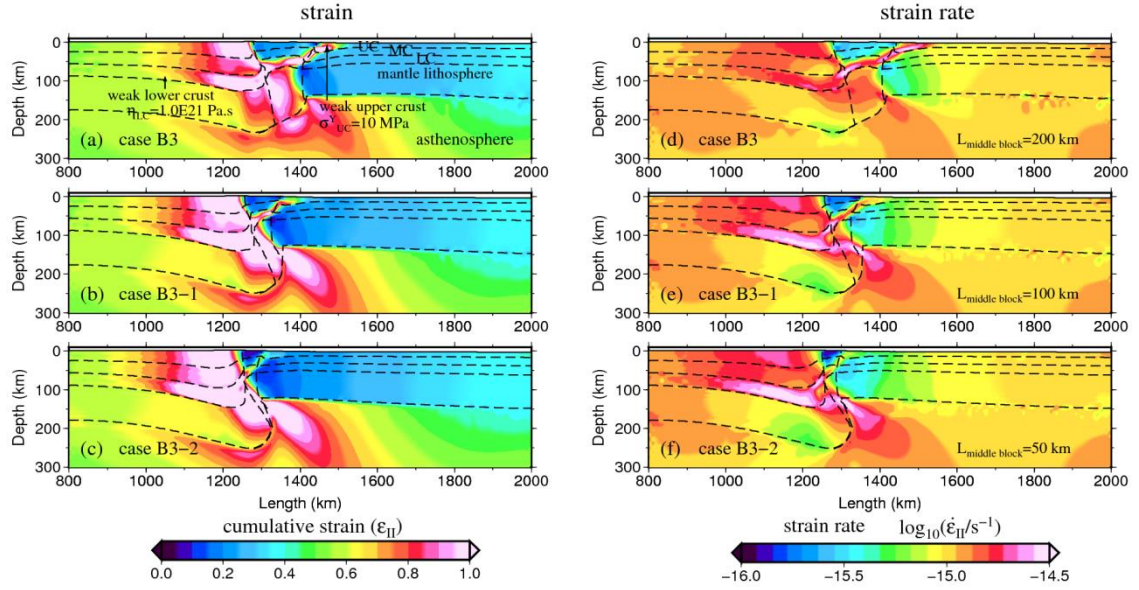
**Figure S4.** Distribution of the stress (the second invariant of the deviatoric stress tensor) for the different cases (B1, B2, and B3) after 20 Myr of compression.



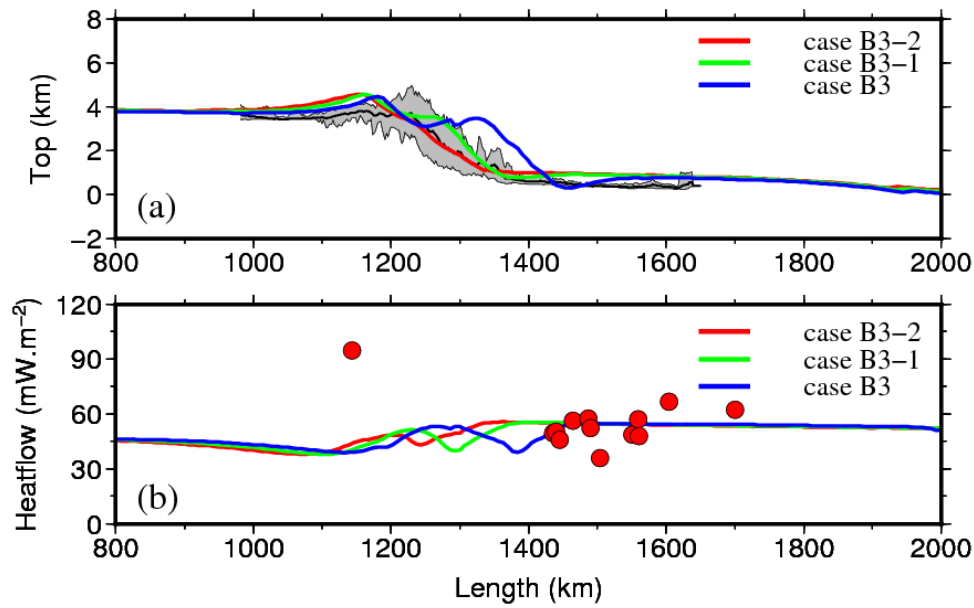
**Figure S5.** Effects of the crustal strength of the Longmen Shan on lithospheric deformation and strain partitioning. Distribution of the cumulative strain (a-c) and strain rate (d-f) in the different cases. The yield strength of the upper and middle crust of the Longmen Shan is 100 MPa, 50 MPa, and 10 MPa in cases B2, B2-1, and B2-2, respectively. The results of these cases are after 20 Myr of compression.



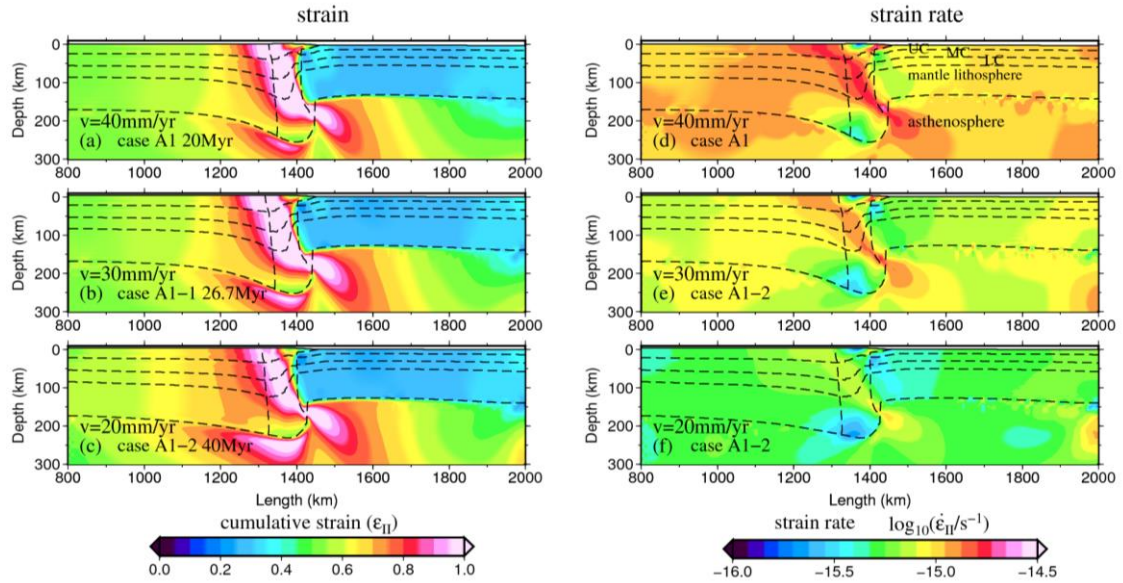
**Figure S6.** Comparisons of the predicted topography (a), and surface heat flow (b) of the different cases (B2, B2-1, and B2-2) with the observations. Gray area (a) indicates the topographic profile across the northern segment of the Longmen Shan. Red dots (b) show the surface heat flow across this profile. These results are derived from different cases after 15 Myr of compression.



**Figure S7.** Effect of the scale of the Longmen Shan on lithospheric deformation and strain partitioning. Distribution of the cumulative strain (a-c) and strain rate (d-f) in the different cases. The initial length of the Longmen Shan is 200 km, 100 km and 50 km in cases B3, B3-1, and B3-2, respectively. The results of these cases are after 20 Myr of compression.

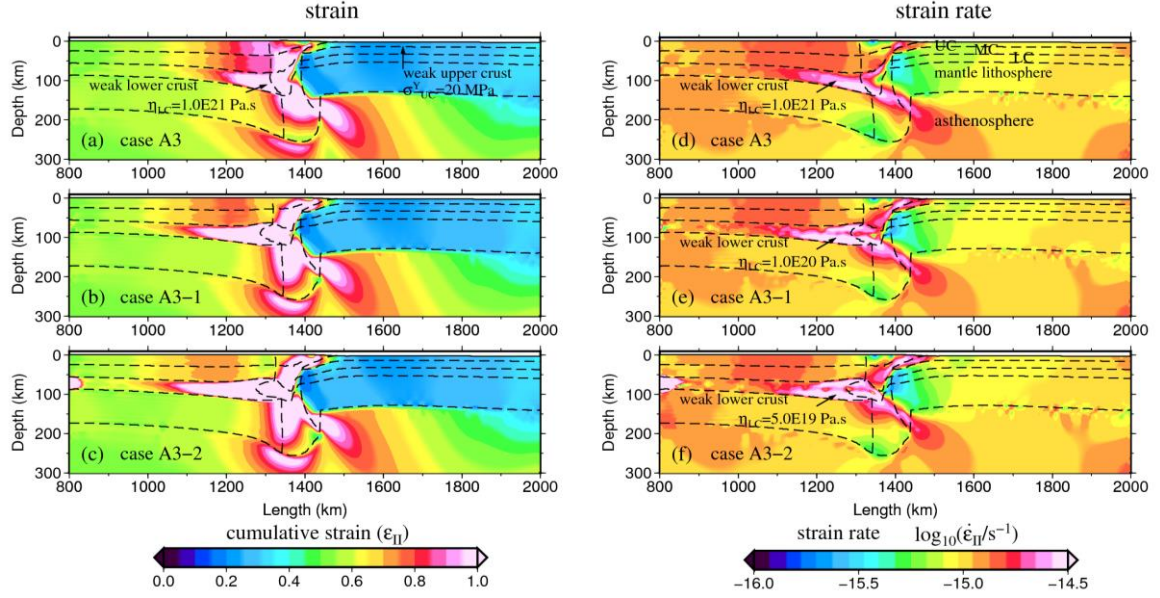


**Figure S8.** Comparison of the predicted topography (a), and surface heat flow (b) in the different cases (B3, B3-1, and B3-2) with the observations. Gray area (a) indicates the topographic profile across the northern segment of the Longmen Shan. Red dots (b) show the surface heat flow across this profile. These results are derived from different cases after 15 Myr of compression.



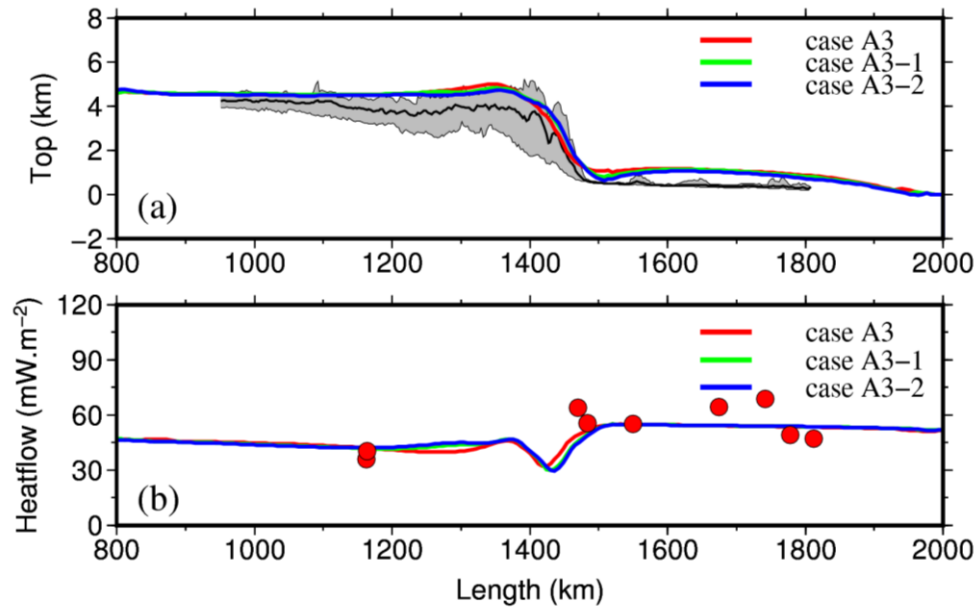
**Figure S9.** Effect of the velocity boundary condition on lithospheric deformation and strain partitioning. Distribution of the cumulative strain (a-c) and strain rate (d-f) in different cases. The velocities imposed on the left side of the model were 40 mm/yr, 30 mm/yr, and 20 mm/yr in cases A1, A1-1, and A1-2, respectively. The results shown in this figure are 20 Myr (a, d), 26.7Myr (b, e), and 40 Myr (c, f) of compression, respectively. So the same amount of convergence (800 km) was imposed.





**Figure S10.** Effect of the lower crustal viscosity of the Songpan-Ganzi terrane on lithospheric deformation and strain partitioning. Distribution of the cumulative strain (a-c) and strain rate (d-f) for different cases. The viscosities imposed on the lower crust of the Songpan-Ganzi terrane and Longmen Shan were  $1.0 \times 10^{21} \text{ Pa} \cdot \text{s}$ ,  $1.0 \times 10^{20} \text{ Pa} \cdot \text{s}$ , and  $5.0 \times 10^{19} \text{ Pa} \cdot \text{s}$  in cases A3, A3-1, and A3-2, respectively. The results shown in this figure are 20 Myr of compression.





**Figure S11.** Effect of the lower crustal viscosity of the Songpan-Ganzi terrane on the topography and surface heat flow in the different cases after 20 Myr of compression.