

FALL 20/20

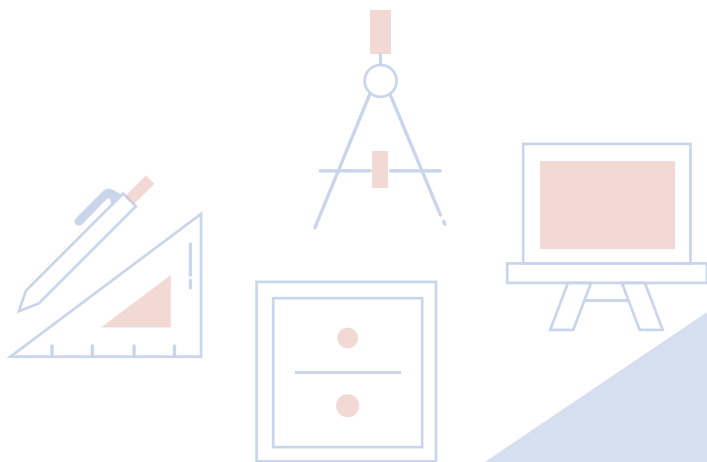


Data Structure

CS 240

Week 1

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SavvyUni CS 240 FAQ by 豌豆射手



关于我？

- UW 4A CS AI Option 在读
- 连续三个学期没学期上（等效）7 门课
- CS 341 Algorithm: 99
- 上个 Coop Term 在一家保险公司担任 Full Stack Developer

为什么要上 CS 240 ？

- 为了学习更多解决问题的方法
- 为了面试
- 为了毕业

来参加这节课的目的是什么？

- 为了分！
- 学知识！
- 用尽可能少的时间拿尽可能高的分！
- 用尽可能少的时间拿尽可能高的分的同时还把知识学会！

CS 240 Overview

Data Structures and Data Management

Course Description

Introduction to widely used and effective methods of data organization, focusing on data structures, their algorithms, and the performance of these algorithms.

Prerequisite: CS 245, CS 246, Stat 230

- CS 136: Tree, Stack, Queue, Dictionary, Sorting, and Big-O Notation
- CS 245: Loop Invariant (并不会直接用到，但是会帮助你理解)
- CS 246: 用 C++ 写代码
- Math 137: Limit, l'Hôpital (洛必达)
- Stat 230: Probability, Expectation, and Binomial Distribution

Topic

- Asymptotic Analysis (Formal Definition of Big-O Notation)

除了 Asymptotic Analysis, 其他章节相互独立

Data Structure (Extended from CS 136)

- Queue → Priority Queue and Heap
- Sorting → Selection, Radix Sort, and Interpolation Search
- BST → AVL-Tree and B-Tree
- Dictionary(map) → Tries, Skip Lists, Ordering, and Hashing

Algorithm

- Range Search
- String Matching
- Data Compression

Marks Breakdown

- | | | |
|----------------------|-----|-----------------|
| • Written Assignment | 40% | |
| • Programming | 5% | |
| • Mini Test | 20% | |
| • Midterm Assessment | 10% | Oct 26 - Oct 27 |
| • Final Assessment | 25% | TBD |

Terminology

Problem Desired _____/ _____ relationship

- Example: Sorting Problem 排序问题
- Input: A sequence of _____
- Output: A reordering _____

Instance of a Problem An _____ satisfy all _____

Solution of a Problem _____ for specified _____

Size of an instance A _____ that measure of the size of the instance

- Example:
- For sorting problem, the size is defined to be the _____ of the input array
- For some numerical computation(Fibonacci Number), the size is defined to be _____

Algorithm A _____ of _____ that transform _____ to _____

Correctness An algorithm is said to be correct if for _____, it halts correct output.

- An incorrect algorithm may _____ on some input, or
- halt with _____ output

Program An _____ of an algorithm using a special programming language

Data Structure A way to _____ and _____ data

- No single Data Structure is _____
- It is important to know their _____ and _____

Pseudocode An method of _____ an _____ to _____

Pseudocode

Use most clear and concise to specify an algorithm

- Sometime _____ Clear
- Sometime _____ Clear
- Avoid _____ Concise
- Avoid _____ Concise

伪代码是给人看的，所以每个人写的伪代码可能不太一样，会有自己的特点

Some Conventions

while, if-else has the same meaning in C, C++

for has different meaning in C, C++. It is flexible, for example

- for $i = 0$ to $n - 1$: print(i)
- for x in A . (Similar to for (auto x : vector))

Indentation indicates block structure

// 你看不见这一行，因为 // 后面跟的是注释

Array indexing is similar in C, C++

-
-

Variable refers array or object are passed by reference

- If an variable refer to _____, we give it special value _____

其他习惯问题

- 有的人用 \leftarrow 当 assignment，本讲义里用 $=$
- 有的人用 $=$ 做 equality testing，本讲义里用 $==$

Example: Binary Search in Array

Iterative version Binary Search in C Language

```
1.  int binary_search(const int arr[], int start, int end,
2.                          int key) {
3.      int ret = -1;
4.      int mid;
5.      while (start <= end) {
6.          mid = (start + end) / 2;
7.          if (arr[mid] < key) {
8.              start = mid + 1;
9.          } else if (arr[mid] > key) {
10.             end = mid - 1;
11.          } else {
12.              ret = mid;
13.              break;
14.          }
15.      }
16.      return ret
17. }
```

Iterative version Binary Search Pseudocode

BinarySearch(A, start, end, key)

```
1.
2.
3.
4.
5.
6.
7.
8.
9.
10.
11.
12.
13.
14.
```

Analyze an algorithm

In CS 240, Analyze an algorithm means

- Analyze the _____ of given algorithm
- Analyze the _____ of given algorithm

Step to Analyze Running time of Algorithm

1. Express algorithm in _____
2. Identify _____ in pseudocode
3. Express running time as a _____ that _____ primitive operations where ____ is the input size.
4. Determine _____ of _____ with _____

Example of Primitive Operations

Arithmetic

- Addition
- Subtraction
- Multiplication
- Division
- Remainder
- Floor
- Ceiling

Assignment

Control Flow

- If-else
- For, while
- Function Call
- Return

Array Indexing

Example:

Category A - For loop (Easy)

Sum(A)

A: array of size n

1. *i = 0*
2. *acc = 0*
3. *for i = 0 to n - 1*
4. *acc += A[i]*
5. *return acc*

Category B: Recursion (Easy)

BinarySearch(A, start, end, key)

1. *if (start > end)*
2. *return "Did not found"*
3. *mid = (start + end) / 2*
4. *if (A[mid] > key)*
5. *return BinarySearch(A, start, mid - 1, key)*
6. *else if (A[mid] < key)*
7. *return BinarySearch(arr, mid + 1, end, key)*
8. *else:*
9. *return mid*

Category C: While - loop (Hard)

BinarySearch(A, start, end, key)

1. *while (start < end)*
 2. *mid = (start + end) / 2*
 3. *if (A[mid] > key)*
 4. *start = mid + 1*
 5. *else if (A[mid] < key)*
 6. *end = mid - 1*
 7. *else*
 8. *return mid*
 9. *return "Did not found"*
-

Exercise

For loop 1

1. $m = 0$
2. for $i = 1$ to $3n$
3. $m = m * 4$
4. for $j = 1025$ to 2048
5. for $k = 4i + 1$ to $6i$
6. $m = m + 4 * k$

For loop 2 (give an upper bound)

1. $x = 0$
2. for $i = 1$ to $\text{floor}(\log n)$
3. for $j = 1$ to 2^i
4. $x = x + i * j$

Exercise

while loop 1

```
1.   $i = 0$ 
2.   $j = 0$ 
3.   $k = 1$ 
4.   $\text{while}(2*j + k \leq n)$ 
5.       $i = i + 1$ 
6.       $j = j + i$ 
7.       $k = k + 1$ 
```

iter	t	i	j	k	2j+k

Nested loop (give an upper bound)

```
1.   $x = 0$ 
2.   $\text{for } i = 1 \text{ to } n$ 
3.       $j = i$ 
4.       $\text{while } (i > 0)$ 
5.           $i = i / 2$ 
```

Asymptotic Notation

Big-O Notation

Meaning

- $O(g(n))$ is a ____
- It is a set of function whose growth rate is ____ or ____ than g
- If ____, we say ____ is an ____ of ____

Formal Definition ____ if ____ constants ____ and ____ such that ____ for all ____

Example

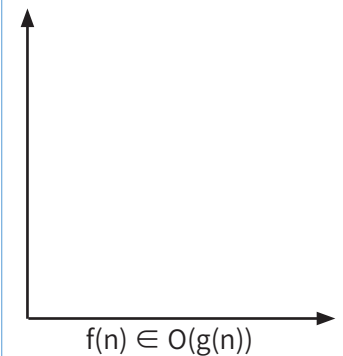
Proof ____ from first principle

Proof ____ from first principle

Proof ____ from first principle

当输入规模无限增加时，算法的运行时间如何随着输入规模的变大而增加？

有时候我们也会用 $f(n) = O(g(n))$ 代替 $f(n) \in O(g(n))$ 来方便递归计算



Definition 有时也叫 First Principle

Big-Ω Notation

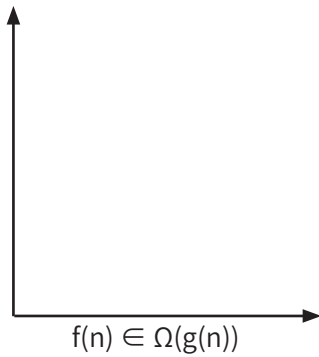
Meaning

- $\Omega(g(n))$ is a set of function whose growth rate is _____ or _____ than g
- If _____, we say _____ is an _____ of _____

Formal Definition _____ if _____ constants _____ and _____ such that _____ for all _____

Example

Proof _____ from first principle



Big-Θ Notation

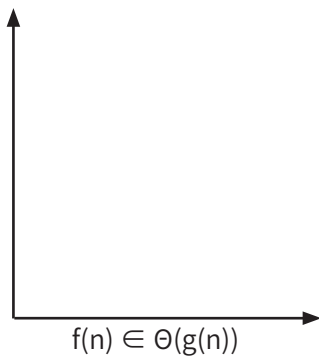
Meaning

- $\Theta(g(n))$ is a set of function whose growth rate is _____ to g
- If _____, we say _____ is an _____ of _____

Formal Definition _____ if _____ constants _____ and _____ such that _____ for all _____.

Example

Proof _____ from first principle



Example

Proof _____ from first principle

Proof _____ from first principle

Example

Proof _____ from first principle

Proof _____ from first principle

Summary

- Basic Concept about Data Structure & Algorithm
- Pseudocode
- How to analyze an algorithm
- Asymptotic Notation (O , Ω , Θ)

Three level in Mastering CS 240

- Known basic concept and able to directly apply algorithm.
 - Find property of DS/Algorithm with given input, or find specific input that satisfy some requirement.
 - Analyze variation of DS/Algorithm and design new DS/Algorithm.
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/// **有你有未来**