- Weeks 1–2: informal introduction
 - network = path

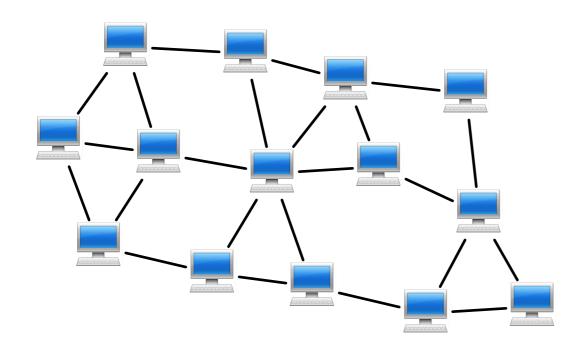


- Week 3: graph theory
- Weeks 4–7: models of computing
 - what can be computed (efficiently)?
- Weeks 8–11: lower bounds
 - what cannot be computed (efficiently)?
- Week 12: recap

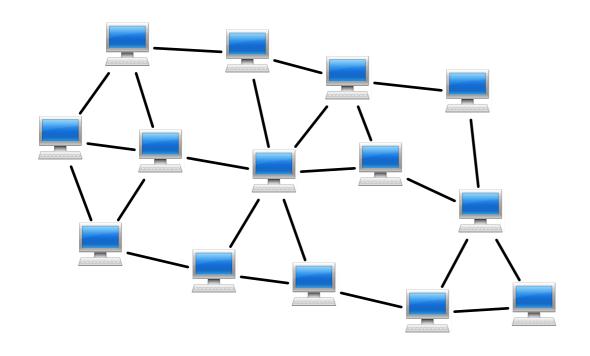
Week 12

Conclusions

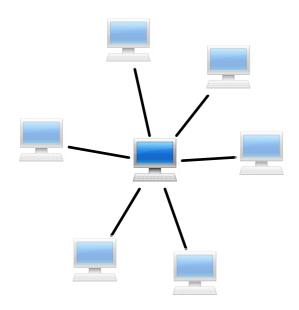
Algorithms for computer networks



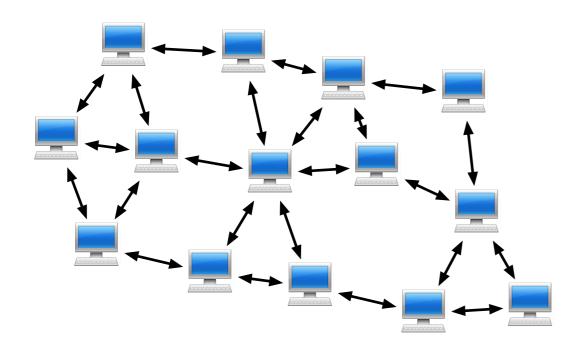
Identical computers in an unknown network, all running the same algorithm



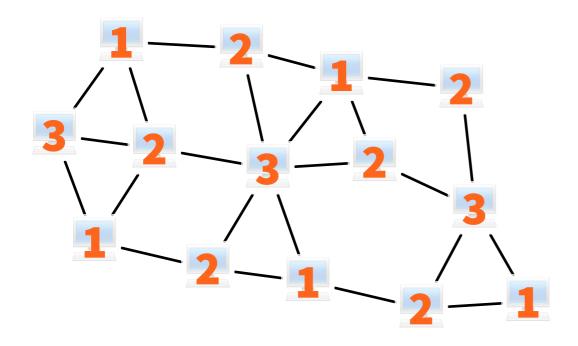
Initially each computer only aware of its immediate neighbourhood



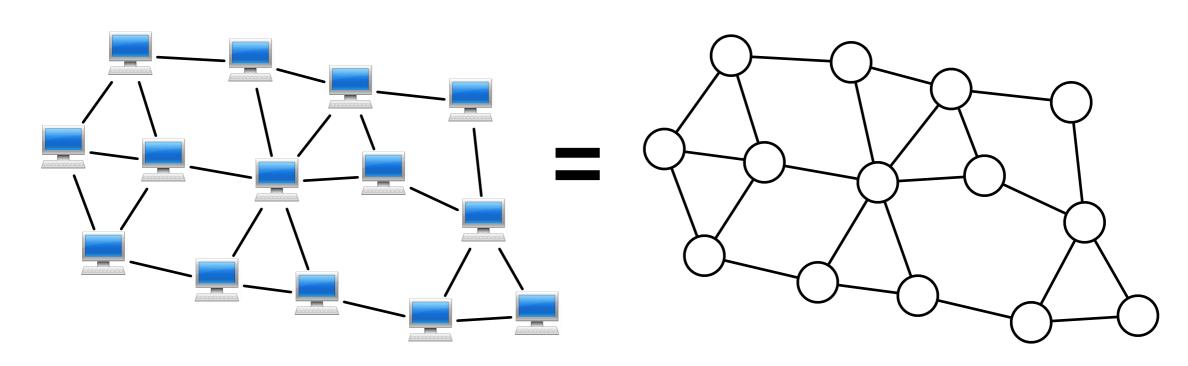
Nodes can exchange messages with their neighbours to learn more...



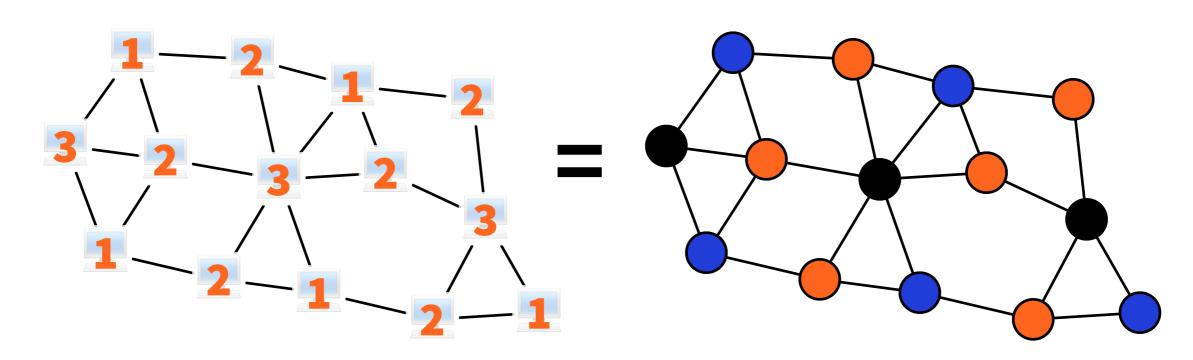
Finally, each computer has to stop and produce its own local output



Focus on graph problems: network topology = input graph



Focus on graph problems: local outputs = solution (here: graph colouring)



Typical research question:

"How fast can we solve graph problem X?"

Time = number of communication rounds

What have we learned?

- Dealing with unknown systems
- Dealing with partial information
- Dealing with parallelism
- Applications beyond distributed computing: fault tolerance, online, streaming, multicore...

Learning objectives

- Models
- Algorithms
- Lower bounds
- Graph theory

Objective 1: Models of computing

- Precisely what is a "distributed algorithm"
- In each of these models:
 - PN, LOCAL, CONGEST
 - deterministic, randomised

Objective 2: Algorithms

- Colouring paths: LOCAL, $O(\log^* n)$
- Colouring graphs: LOCAL, O(log n) w.h.p.
- Gather everything: LOCAL, O(diam(G))
- Bipartite maximal matching: PN, $O(\Delta)$
- All-pairs shortest paths: CONGEST, O(n)

Algorithm P3CBit:

Fast colour reduction

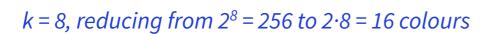
```
c_0 = 123 = 01111011_2 (my colour)

c_1 = 47 = 00101111_2 (successor's colour)

i = 2 (bits numbered 0, 1, 2, ... from right)

b = 0 (in my colour bit number i was 0)

c = 2 \cdot 2 + 0 = 4 (my new colour)
```



Week 1

Week 7

Algarithm P3CRite

Fas

$$c_0 = 12$$
:
 $c_1 = 4$:
 $i = 2$ (
 $b = 0$ (

$$c = 2 \cdot 2$$

Algorithm idea 3

- Colour palette: $\{1, 2, ..., \Delta + 1\}$
- Active with probability 1/2
- If active, pick a random free colour
 - not used by any neighbour that has stopped
- Try again if conflicts...

Fas

$$c_0 = 12$$

$$c_1 = 4$$

$$i = 2$$

$$b = 0$$

$$c = 2 \cdot 2$$

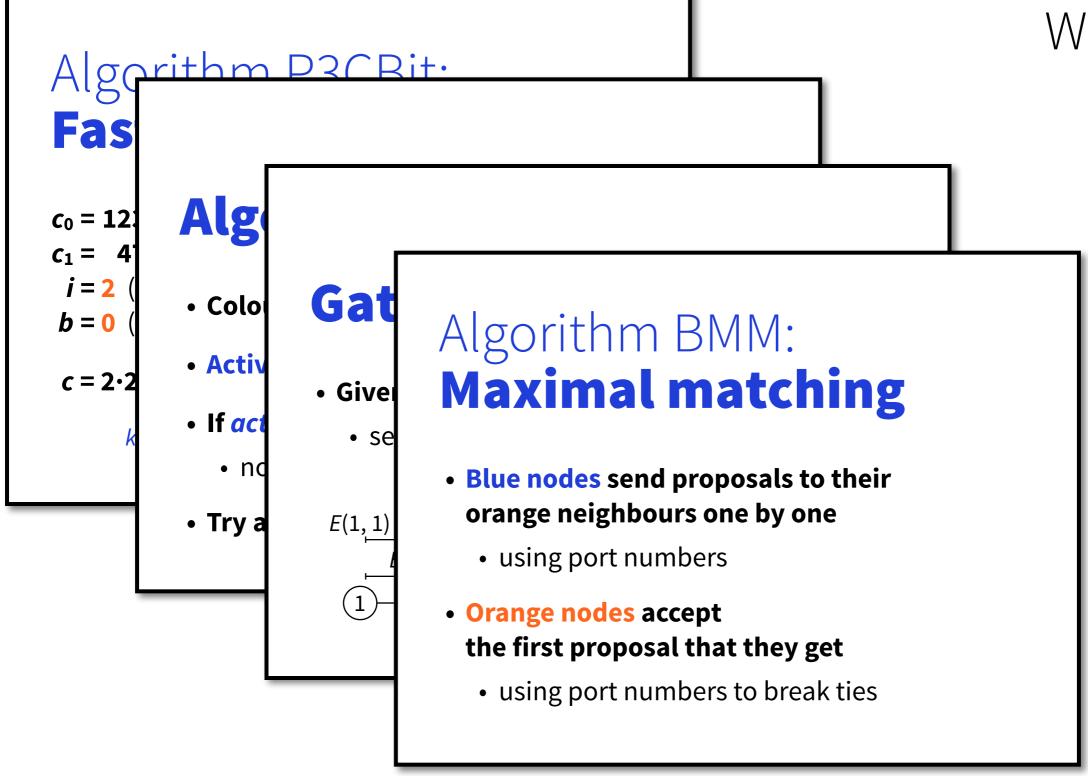
Alg

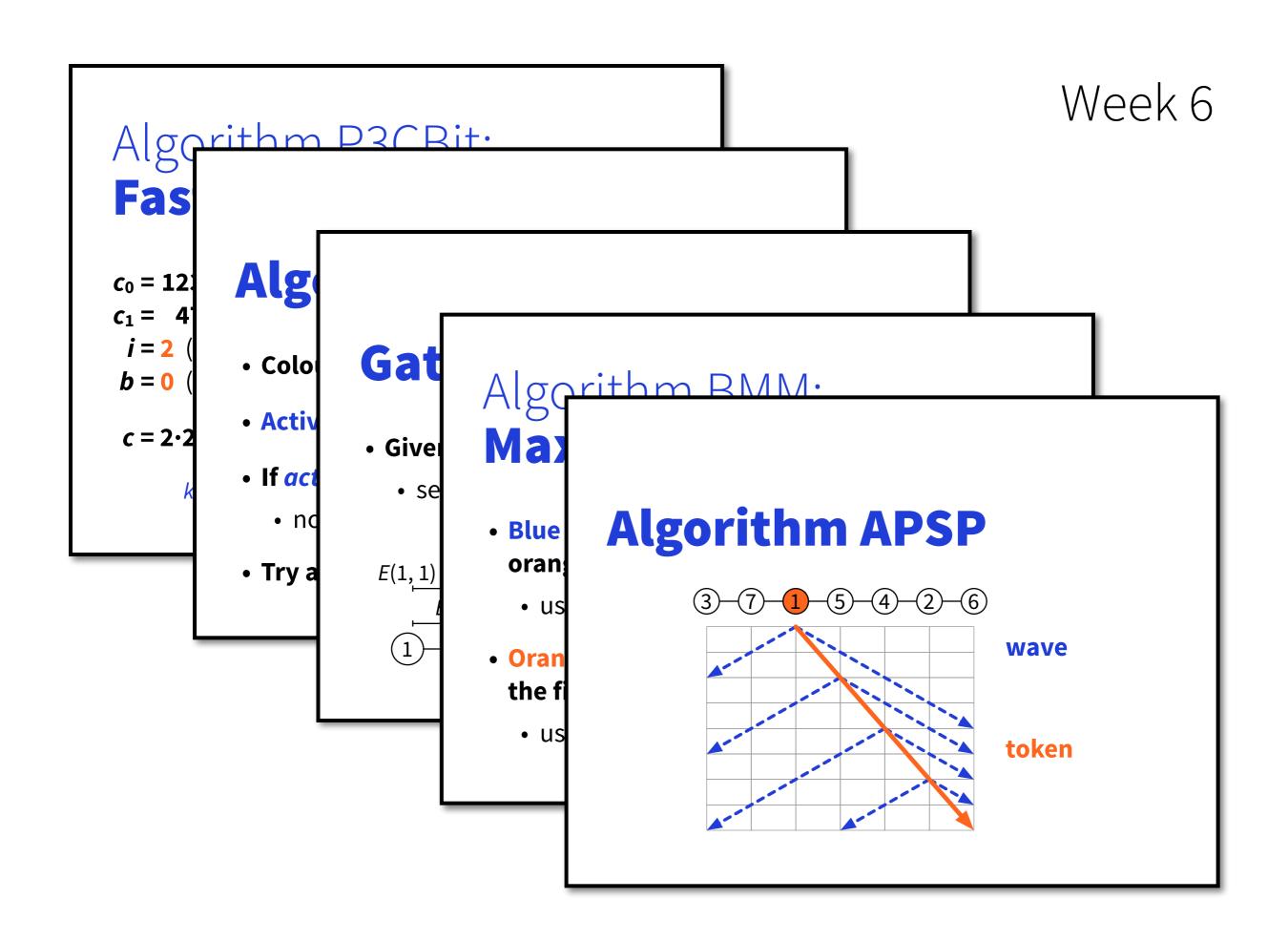
- Colo
- Activ
- If act
 - nd
- Try a

Gathering everything

- Given E(v, r), we can learn E(v, r + 1) in 1 round
 - send E(v, r) to all neighbours, take union

$$E(5, 2)$$
 $E(1,1)$
 $E(3,1)$
 $E(5,1)$
 $E(7,1)$
 $E(9,1)$
 $E(2,1)$
 $E(4,1)$
 $E(6,1)$
 $E(8,1)$
 $E(8,1)$





Objective 2: Algorithms

- Reductions!
- Graph colouring is a very useful subroutine

Objective 3: Lower bounds

- Covering maps:
 what cannot be solved at all in PN model
- Local neighbourhoods:
 what cannot be solved fast in any model
- Ramsey's theorem:
 what cannot be solved in O(1) time

Objective 4: Graph theory

- Basic definitions
- Connections between graph problems
 - e.g. maximal matching → small vertex covers
- Ramsey's theorem
 - at least for c = 2, k = 2

What else is studied in distributed computing?

- Fault-tolerance
- Asynchrony
- Shared memory
- Physical models
- Robot navigation

- Nondeterminism
- Complexity measures
- High-performance computing
- Practical aspects of networking ...

What next?

- CS-E4000 Seminar in Computer Science:
 Algorithms
 - 3rd–4th period, 5 credits
 - reading seminar
 - algorithms and theory of computation

What next?

CS-E4580 Programming Parallel Computers

- 5th period, 5 credits, intensive course
- programming modern parallel computers: multicore, GPU, memory hierarchies ...
- hands-on programming exercises
- main goal: make it as fast as you can!

What next?

- Just ask if you want to do more!
 - master's thesis topics?
 - summer internships?
 - doctoral studies?

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