

Please use python3 to execute the code.

In problem 1 we are give a processed data of handwritten digits 5 and 6. The data set has 64 features and I calculate the gaussian probability density using this data set .

For classification of test data here I use bayesian decision theory in which I calculate the discriminant function for both the class and applied it to the test data set. If $g_1 > g_2$, the the given input will be classified as class1 else in class2.

The covariance matrix from the training data is find out to be as :

Cov_5:

```
[ [ 38.87878788  21.48484848  23.59343434 ..., 24.71212121  24.8510101
  25.71969697]
 [ 21.48484848  38.50568182  23.01262626 ..., 27.85248316  23.5625
  25.52504209]
 [ 23.59343434  23.01262626  44.67401286 ..., 23.97237527  19.34871442
  26.90159167]
 ...,
 [ 24.71212121  27.85248316  23.97237527 ..., 45.62679191  26.25258264
  24.49300454]
 [ 24.8510101  23.5625  19.34871442 ..., 26.25258264  39.28575528
  24.95299587]
 [ 25.71969697  25.52504209  26.90159167 ..., 24.49300454  24.95299587
  41.08393914]]
```

And cov_6:

```
[ [ 42.92450452  23.42862752  25.62609792 ..., 20.85917705  24.01364003
  28.49383099]
 [ 23.42862752  40.29649837  25.98059396 ..., 25.11684268  26.76751331
  27.75090417]
 [ 25.62609792  25.98059396  42.79041891 ..., 22.37846942  20.9158865
  29.15812098]
 ...,
 [ 20.85917705  25.11684268  22.37846942 ..., 40.86152617  26.69629584
  22.87389175]
 [ 24.01364003  26.76751331  20.9158865 ..., 26.69629584  45.98686975
  26.5309484 ]
 [ 28.49383099  27.75090417  29.15812098 ..., 22.87389175  26.5309484
  42.04373075]]
```

For the performance analysis , I use the confusion matrix which is defined as $M = \begin{bmatrix} \text{true 5} & \text{false 6} \\ \text{false 5} & \text{true 6} \end{bmatrix}$ and classification percentage.

For various cases I analyse the classification problem as follows:

Case 1: using true cov_5 and cov_6:

Confusion matrix = [[106, 27], [49, 151]]

% classification of 5 and 6 resp.: 68.38709677419355 84.8314606741573

Case 2: using true cov_5 and cov_6 but neglecting the determinant term:

Confusion matrix : [[128 44],[27 134]]

% classification of 5 and 6 resp.: 82.58064516129032 75.28089887640449

Case 3 : using cov_5 = cov_6:

Confusion matrix : [[110 11],[45 167]]

% classification of 5 and 6 resp.: 70.96774193548387 93.82022471910112

Case 4 : using cov_6 = cov_5:

Confusion matrix : [[139 50],[16 128]]

% classification of 5 and 6 resp.: 89.6774193548387 71.91011235955057

Case 5 : using cov_5 = cov_6 = cov where cov = p_5*cov_5+p_6*cov_6:

Confusion matrix : [[134 27], [21 151]]

% classification of 5 and 6 resp.: 86.45161290322581 84.8314606741573

I have tested the code for the 5 cases on test data and above findings are obtained. And it is found that case 5 is the best possible combination for classification.

