The Allocation of Teaching Talent and Human Capital Accumulation

Simeon Alder¹ Yulia Dudareva¹ Ananth Seshadri¹

¹University of Wisconsin-Madison

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- Public education in U.S. has gone through major (positive) changes since end of WW II, e.g.
 - ► Real expenditures per student per year: \$2,100 (1950s) to \$12,000 (2010s)
 - Student-teacher ratio: 27 (1955) to 16 (2010s)
- However, evolution of educational outcomes doesn't compare favorably with other developed countries (e.g. PISA assessments)
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 - ▶ Local funding for public education (e.g. property taxes)



3 Stylized Facts

Model ► OLG

- Non-linear version of canonical occupational choice model
- ► Educational barriers / labor market discrimination as in Hsieh et al. (2019)

Data ► Project TALENT

- ► NLSY79
- ► NLSY97

Stylized Fact #1

Majority of (Public) School Teachers is Female

% Female	Time Period
61.1	early 70s
77.7	1986-1993
77.1	2009-2013
75	2003-4
	61.1 77.7 77.1

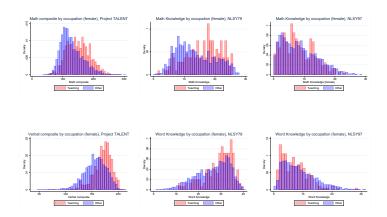
Stylized Fact #2

Educational Barriers / Labor Market Discrimination

- ► Females face low barriers / discrimination in teaching
- Barriers / discrimination in non-teaching occupations falling over time

Stylized Fact #3

Ability Distribution of Females by Occupation



Model

Endowments, Preferences

- ▶ Each period, a measure M of agents is born and lives for two periods ("young" and "old")
- Individuals born with occupation-specific abilities drawn from a joint bivariate distribution with c.d.f. $F(a^T,a^O)$
- ► Individuals have log preferences over leisure and consumption (no discounting):

$$\ln c_{t+1} + \ln \left(1 - s_t\right)$$

Model

Technologies

- Children ("young") make occupation-specific educational investments (in units of time and output)
- Adults work as teachers or production workers.

Human capital production (teaching) depends on teacher's h^T , child's ability a, and child's educational investments (time s and goods e) according to:

$$\begin{split} \boldsymbol{h}'(a) &= \left(\boldsymbol{h}^T\right)^{\beta} a^{\alpha} s\left(a\right)^{\phi} e(a)^{\eta} N(\boldsymbol{h}^T, \widetilde{\boldsymbol{H}}^T)^{-\sigma} \\ \text{where } \widetilde{\boldsymbol{H}}^T &= \int_0^{\infty} \left(\boldsymbol{h}^T\left(a\right)\right)^{\frac{\beta}{\sigma}} f^T(a) da \end{split}$$

Final output production depends on adult worker's human capital h^O and exogenous productivity A^O :

$$y = A^O h^O$$

Values

$$V^g(a^T, a^O, \widetilde{H}^T) = \max_{\{s^O, s^T, e^O, e^T\}} \left\{ V^{O,g}(a^O, \widetilde{H}^T), V^{T,g}(a^T, \widetilde{H}^T) \right\}$$

where

$$V^{O,g}(a^{O}, \widetilde{H}^{T}) = \ln\left(1 - s^{O}\left(a^{O}, \widetilde{H}^{T}\right)\right) + \mu \ln\left[h'^{O}A'^{O}(1 - \tau'^{O,g,w})(1 - t)\right) - e^{O}(a^{O}, \widetilde{H}^{T})(1 + \tau^{O,g,e}),$$
$$V^{T,g}(a^{T}, \widetilde{H}^{T}) = \ln\left(1 - s^{T}\left(a^{T}, \widetilde{H}^{T}\right)\right) + \mu \ln\left[\omega'(h'^{T}, \widetilde{H'}^{T})(1 - \tau'^{T,g,w})(1 - t)\right) - e^{T}(a^{T}, \widetilde{H}^{T})(1 + \tau^{T,g,e}),$$

Model (cont'd)

Constraints, Laws of Motion

$$\begin{split} \mathbf{t} \int_0^\infty \left(\omega \left(h^T \left(a \right) \right) f^T (a) + A^O h^O (a) f^O (a) \right) da &= \int_0^\infty \omega \left(h^T (a) \right) f^T (a) da \\ f^T (a) &= \int_0^{\bar{a}^{-1} (a)} f \left(a, b \right) db \\ f^O (b) &= \int_0^{\bar{a} (b)} f \left(a, b \right) da \end{split}$$

Aggregate laws of motion for \widetilde{H}^T and H^O :

$$\widetilde{H'}^{T} = \int_{0}^{\infty} \left(\left(\frac{2\widetilde{H}^{T}}{M} \right)^{\sigma} a^{\alpha} s^{T} \left(a, \widetilde{H}^{T} \right)^{\phi} e^{T} (a, \widetilde{H}^{T})^{\eta} \right)^{\frac{\beta}{\sigma}} f^{T}(a) da$$

$$H'^{O} = \int_{0}^{\infty} \left(\frac{2\widetilde{H}^{T}}{M} \right)^{\sigma} a^{\alpha} s^{O} \left(a, \widetilde{H}^{T} \right)^{\phi} e^{O} (a, \widetilde{H}^{T})^{\eta} f^{O}(a) da$$

Model (cont'd)

Occupational Threshold

$$a^{T*}(a^O) = \bar{a} \left(a^O, \widetilde{H}^T \right)$$

such that

$$V^O(a^O, \widetilde{H}^T) = V^T\left(a^{T*}(a^O), \widetilde{H}^T\right)$$
 , for all $a^O \in (0, \infty)$

Model (cont'd)

- Assignment of students to teachers is random
 ⇒ distribution of students' skill identical across classrooms
- lacktriangle Teachers with different h^T vary with respect to class size
- \blacktriangleright $\omega(\cdot,\cdot)$ is proportional to the *number of students* in a teacher's class and to :

$$\begin{split} \omega(h^T, \tilde{H}^T) &= \lambda N(h^T, \tilde{H}^T) \\ &= \underbrace{\frac{H'^O A'^O}{\frac{M}{2} \int_o^\infty f^O(a) da}}_{=N(h^T, \tilde{H}^T)} \underbrace{\frac{\frac{M}{2} \frac{1}{\tilde{H}^T}}{N(1, \tilde{H}^T)} \left(h^T\right)^{\frac{\beta}{\sigma}}}_{=N(h^T, \tilde{H}^T)} \\ &= \frac{H'^O A'^O}{\int_o^\infty f^O(a) da} \frac{\left(h^T\right)^{\frac{\beta}{\sigma}}}{\tilde{H}^T} \end{split}$$

Optimal Investments for Prospective Teachers (I)

$$\begin{split} s^T &= \frac{\mu \phi}{\mu \phi + \frac{\beta}{\sigma} - \eta} \\ e^T &= \left(\frac{(1 - t)(1 - {\tau'}^{T,w}) \left(\frac{2}{M}\right)^{\beta} A'^O(s^T) \frac{\phi \beta}{\sigma} \left(\frac{\eta \beta}{\sigma}\right) \left(\widetilde{H}^T\right)^{\beta} \left(a^T\right)^{\frac{\alpha \beta}{\sigma}}}{1 + {\tau}^{T,e}} \right)^{\frac{1}{1 - \frac{\eta \beta}{\sigma}}} \\ &\times \left(\frac{H'^O}{\int_{o}^{\infty} f^O(a) da} \left(\widetilde{H'}^T\right)^{-1} \right)^{\frac{1}{1 - \frac{\eta \beta}{\sigma}}} \end{split}$$

Aggregate Laws of Motion

$$\begin{split} \widetilde{H'}^T &= \left[\left(\frac{(1 - {\tau'}^{T,w}) \left(\frac{\eta \beta}{\sigma} \right)}{1 + {\tau}^{T,e}} \right)^{\eta} \left(\frac{(1 - {\tau'}^{O,w}) \eta}{1 + {\tau}^{O,e}} \right)^{\frac{\eta}{1 - \eta} \eta} \left((1 - t) A'^O \right)^{\frac{\eta}{1 - \eta}} \\ &\times \left(\frac{2}{M} \right)^{\frac{\sigma}{1 - \eta}} (s^T)^{\phi} (s^O)^{\frac{\eta}{1 - \eta} \phi} \left(\frac{\int_0^{\infty} a^{\frac{\alpha}{1 - \eta}} f^O(a) da}{\int_0^{\infty} f^O(a) da} \right)^{\eta} \\ &\times \left(\int_0^{\infty} a^{\frac{\alpha \beta}{\sigma - \eta \beta}} f^T(a) da \right)^{\frac{\sigma - \eta \beta}{\beta}} \left(\widetilde{H}^T \right)^{\frac{\sigma}{1 - \eta}} \right]^{\frac{\beta}{\sigma}} \\ &H'^O &= \left(\frac{(1 - t)(1 - {\tau'}^{O,w}) A'^O \eta}{1 + {\tau}^{O,e}} \right)^{\frac{\eta}{1 - \eta}} \left(\frac{2}{M} \right)^{\frac{\sigma}{1 - \eta}} (s^O)^{\frac{\phi}{1 - \eta}} \\ &\times \left(\int_0^{\infty} a^{\frac{\alpha}{1 - \eta}} f^O(a) da \right) \left(\widetilde{H}^T \right)^{\frac{\sigma}{1 - \eta}} \end{split}$$

Optimal Investments for Prospective Teachers (II)

$$\begin{split} s^T &= \frac{\mu \phi}{\mu \phi + \frac{\beta}{\sigma} - \eta} \\ e^T &= \left((1 - t) \left(\frac{2}{M} \right)^{\sigma} A'^O \eta(s^O)^{\phi} \left(\widetilde{H}^T \right)^{\sigma} \left(a^T \right)^{\alpha} \right)^{\frac{1}{1 - \eta}} \\ &\times \frac{(1 - \tau'^{T,w}) (1 - \tau'^{O,w})^{\frac{\eta}{1 - \eta}}}{(1 + \tau^{T,e}) (1 + \tau^{O,e})^{\frac{\eta}{1 - \eta}}} \cdot \frac{\beta}{\sigma} \\ &\times \left(\frac{\int_0^\infty a^{\frac{\alpha}{1 - \eta}} f^O(a) da}{\int_0^\infty f^O(a) da} \right) \left(\int_0^\infty a^{\frac{\alpha}{\beta - \eta}} f^T(a) da \right)^{-1} \end{split}$$

Optimal Investments for Prospective "Other" Workers

$$s^{O} = \frac{\mu\phi}{\mu\phi + 1 - \eta}$$

$$e^{O} = \left(\frac{(1 - t)(1 - \tau'^{O,w})\left(\frac{2}{M}\right)^{\sigma} A'^{O}(s^{O})^{\phi} \eta\left(\widetilde{H}^{T}\right)^{\sigma} \left(a^{O}\right)^{\alpha}}{1 + \tau^{O,e}}\right)^{\frac{1}{1 - \eta}}$$

Some Parameter Restrictions

- $\blacktriangleright \ \beta < 1 \eta$ to guarantee existence of stable $\widetilde{H^T} = \widetilde{H^T}' > 0$
- $\frac{\sigma}{\beta} > \eta$ and $\mu \phi > 0$ for $s^{T*} \in (0,1)$
- $1>\eta$ and $\mu\phi>0$ for $s^{O*}\in(0,1)$

Occupational Choice Boundary...

 \ldots does not depend on aggregate state $\widetilde{H^T}$

$$\left(\frac{1-\tau'^{O,w}}{1-\tau'^{T,w}}\right) \left(\frac{1-\eta}{1-\frac{\eta\beta}{\sigma}}\right) \left(\frac{1-s^O}{1-s^T}\right)^{\frac{1}{\mu}} \left(\frac{(a^O)^{\frac{\alpha}{1-\eta}}}{\left(\bar{a}^T(a^O)\right)^{\frac{\alpha}{\beta}-\eta}}\right) \\
= \left(\frac{\int_0^\infty a^{\frac{\alpha}{1-\eta}} f^O(a) da}{\int_0^\infty f^O(a) da}\right) \left(\int_0^\infty a^{\frac{\alpha}{\beta}-\eta} f^T(a) da\right)^{-1}$$

Equilibrium

The equilibrium is characterized by:

- 1. the optimal investment for prospective teachers
- 2. the optimal investment for prospective "other" workers
- 3. the aggregate laws of motion
- 4. the occupational choice boundary and the corresponding densities f^T and f^O

Data for Quantitative Exercise

- Micro-data on abilities and occupational choice:
 - 1. Project TALENT (1960-1975):
 - representative 5% sample of high school population in 1960
 - ▶ follow-up surveys at 1, 5, and 11-year post graduation
 - 2. NLSY 79
 - NLSY 97
- Cognitive abilities in math, verbal,... based on standardized assessments (e.g. ASVAB in NLSY)
- Occupational choice 11 years after (likely) high school graduation in all surveys

Occupational Skills from Cognitive Scores

- ► Harmonized cognitive scores from NLSY79 and NLSY97 for:
 - 1. Mathematics knowledge
 - 2. Arithmetic reasoning
 - 3. Word knowledge
 - 4. Paragraph comprehension
- "Crosswalk" from composite math and verbal scores in Project TALENT to AFQT equivalents (Air Force)
- Skill requirements by occupation from O*NET
- Occupation-specific skills based on "translation" of cognitive scores (work in progress)
- In contrast to standard Roy model, occupational choice depends on comparative and absolute advantage here!



Ongoing and Future Work

- Decentralized equilibrium vs. planner's solution (human capital externality in teaching)
- Calibrated reduction in discrimination & barriers: static gains (as in Hsieh et al., 2019) vs. dynamic effects (human capital accumulation)
- Multiple locations differentiated by amenities and/or local tax rates (implicit school segregation by income)