

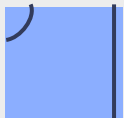
Function, List, Sort, Recursion

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Data eXperience Lab(Instructor: Eunil Park),
Winter Seminar

2018312824 Ryu Chaeun

OUTLINE



1. LIST



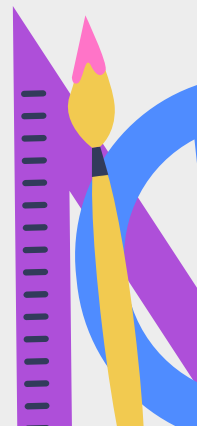
3. RECURSION



2. FUNCTION



4. SORT



LIST

```
>>> my_list = ["a","b","c"]
```

```
>>> my_number_list = [1,3,5,7]
```

Lists are used to store multiple items in a single variable.

Lists are one of 4 built-in data types in Python used to store collections of data, along with Tuple, Set, and Dictionary.

LIST: CREATION

Creation

Brackets [] are used to create a list.

“list()” can be used to make an empty list

Comma(,) is used to separate items in the list.

Lists can be inside lists.

```
>>> my_list = ["a","b","c"]
>>> my_list
['a', 'b', 'c']
>>> my_number_list = [1,3,5,7]
>>> my_number_list
[1, 3, 5, 7]
>>> type(my_list)
<class 'list'>
>>> type(my_number_list)
<class 'list'>
```

```
>>> a = list()
>>> a
[]
>>> type(a)
<class 'list'>
```

```
>>> dimensions = [1,2,3,["a","b","c"]]
>>> dimensions
[1, 2, 3, ['a', 'b', 'c']]
>>> type(dimensions)
<class 'list'>
```

LIST: INDEXING

Indexing

To retrieve an element of the list, we use the *index operator* (`[]`)

- Index of a list starts from 0 to (number of items in a list -1)
- Indexing a list more than one dimension

```
>>> my_numbers_list = [1,2,3,4,5]
>>> my_numbers_list[0]#get the first item
1
>>> my_numbers_list[2]#get third item
3
>>> my_numbers_list[4]#get fifth item
5
>>> my_numbers_list[-1]#get last item
5
```

```
>>> dimensions = [1,2,3,["a","b","c"]]
>>> dimensions[0]#first item in a list
1
>>> dimensions[3]#fourth item
['a', 'b', 'c']
>>> dimensions[3][0]#first item of fourth item in a list
'a'
```

LIST : SLICING

Slicing

Use colon(:) to slice lists.

If you want to slice a list consisting of item with index of “beginning index” to item with index of “end index”,:

List[beginning index : end index +1]

```
>>> my_numbers_list
[1, 2, 3, 4, 5]
>>> my_numbers_list[0:2]#0th index item ~ (2-1)th index item
[1, 2]
>>> my_numbers_list[:3]#get beginning ~ (3-1)th index item
[1, 2, 3]
>>> my_numbers_list[-2:]#get two last items
[4, 5]
```

```
def function(param1, param2):  
    print("hello")  
    return param1 + param2
```

FUNCTION

A function is a block of code which only runs when it is called.

FUNCTION : DEFINITION

Definition

A function is a block of code which only runs when it is called.

Types of function:

1. Built-in Functions:
 - a. Functions that are built into Python.
 - b. print, input, etc.

2. User-defined Functions: Functions defined by the users themselves.

FUNCTION : USER-DEFINED

User-defined function

Why we use:

- our program -> smaller and modular chunks.
- functions make it more organized and manageable.

When to use:

- repeatedly used codes -> functions

Features:

- Function names can be generated the same way as defining variable names
- Formal parameters: names of variables that are called when function is called and used inside the function.
- The result of function will be returned with “return” at the end of function. (Procedure: A function without “return”)

```
def add_function(param1, param2):  
    result = param1+param2  
    return result  
  
print(add_function(1,2))
```

Formal parameters

3
>>>

```
def procedure():  
    print("Hello, I return nothing")  
  
a = procedure()  
print("returned:",a)
```

Hello, I return nothing
returned: None
>>>

FUNCTION : CALLING FUNCTION

Function call

- Only predefined function can be called.
- **Actual Parameter(argument)**: The actual value that is passed into the method by a caller.
- Number of actual parameters = number of formal parameters

```
def add_function(param1, param2):  
    result = param1+param2  
    return result
```

Actual parameter

```
print(add_function(1,2))
```



```
3  
>>>
```

```
def func(): <--  
    |  
    | (recursive call)  
    |  
func() ----
```

RECURSION

Recursion is the process of defining something in terms of itself.

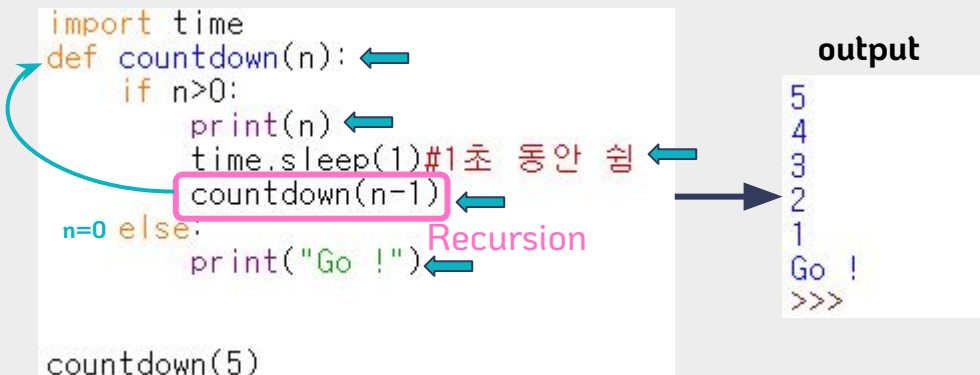
RECURSION : CALLING FUNCTION

How it works:

Top-down method that can be used instead of iteration

Example 1

```
import time
def countdown(n): ←
    if n>0:
        print(n) ←
        time.sleep(1) #1초 동안 쉼 ←
        countdown(n-1) ←
    n=0 else:
        print("Go !") ← Recursion
countdown(5)
```



output

```
5
4
3
2
1
Go !
>>>
```

sequence

```
countdown(5)
print(5)
time.sleep(1)
countdown(4)
print(4)
time.sleep(1)
countdown(3)
print(3)
time.sleep(1)
countdown(2)
print(2)
time.sleep(1)
countdown(1)
print(1)
time.sleep(1)
countdown(0)
Go !
```

RECURSION : CALLING FUNCTION

Example 2

```
def sigma(n):  
    if n>0:  
        return n+sigma(n-1)  
    else:  
        return 0  
  
print(sigma(5))
```

Recursion

15
>>>

sequence

```
sigma(5)  
→ if 5 > 0 : return 5 + sigma(5-1) else: return 0 실행 (1)  
→ 5 + sigma(4) 실행 (2)  
→ 5 + if 4 > 0 : return 4 + sigma(4-1) else: return 0 실행 (3)  
→ 5 + 4 + sigma(3) 실행 (4)  
→ 5 + 4 + if 3 > 0 : return 3 + sigma(3-1) else: return 0 실행 (5)  
→ 5 + 4 + 3 + sigma(2) 실행 (6)  
→ 5 + 4 + 3 + if 2 > 0 : return 2 + sigma(2-1) else: return 0 실행 (7)  
→ 5 + 4 + 3 + 2 + sigma(1) 실행 (8)  
→ 5 + 4 + 3 + 2 + if 1 > 0 : return 1 + sigma(1-1) else: return 0 실행 (9)  
→ 5 + 4 + 3 + 2 + 1 + sigma(0) 실행 (10)  
→ 5 + 4 + 3 + 2 + 1 + if 0 > 0 : return 0 + sigma(0-1) else: return 0 실행 (11)  
→ 5 + 4 + 3 + 2 + 1 + 0 실행 (12)  
→ 5 + 4 + 3 + 2 + 1 실행 (13)  
→ 5 + 4 + 3 + 3 실행 (14)  
→ 5 + 4 + 6 실행 (15)  
→ 5 + 10 실행 (16)  
→ 15
```

RECURSION: ANALYSIS

TIME EFFICIENCY

- In proportion to the number of function recursively called
- If function(n) \rightarrow recursively called for n times \rightarrow in proportion to argument 'n'

SPACE EFFICIENCY

- In proportion to the number of function recursively called

(function must remember what to do with the recursively returned value(ex. addition))
- If function(n) \rightarrow recursively called for n times \rightarrow in proportion to argument 'n'

RECURSION: TAIL RECURSION

WHAT IS "TAIL RECURSION"

- Nothing to remember when recursion is occurred.
- -> No additional memory space

CREATION OF TAIL RECURSION

- Pre-calculate the necessary calculation and take the result of calculation as the additional argument.

```
#tail recursion    Additional argument
def loop(n, summation):
    if n>0:
        return loop(n-1, n+summation)
    else:
        return summation

def signal(n):
    return loop(n,0)

print(signal(5))
```



Encapsulation →

Local function →

```
def signal(n):
    def loop(n, summation):
        if n>0:
            return loop(n-1, n+summation)
        else:
            return summation
    return loop(n,0)
```

RECURSION : TAIL RECURSION

code

```
#tail recursion
def loop(n, summation):
    if n>0:
        return loop(n-1, n+summation)
    else:
        return summation

def sigma1(n):
    return loop(n,0)

print(sigma1(5))
```

Additional argument

output

15
>>>

sequence

sigma1(5)

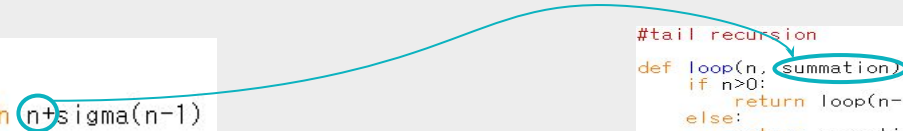
- loop(5,0) 실행 (1)
- if 5 > 0 : return loop(5-1, 5+0) else : return 0
- loop(4,5) 실행 (2)
- if 4 > 0 : return loop(4-1, 4+5) else : return 5
- loop(3,9) 실행 (4)
- if 3 > 0 : return loop(3-1, 3+9) else : return 9
- loop(2,12) 실행 (6)
- if 2 > 0 : return loop(2-1, 2+12) else : return 12
- loop(1,14) 실행 (8)
- if 1 > 0 : return loop(1-1, 1+14) else : return 14
- loop(0,15) 실행 (10)
- if 0 > 0 : return loop(0-1, 1+15) else : return 15
- 15

TAIL RECURSION : ANALYSIS

TIME EFFICIENCY

- In proportion to the number of function recursively called
- If function(n) -> recursively called for n+1 times-> in proportion to argument 'n'

```
def sigma(n):  
    if n>0:  
        return n+sigma(n-1)  
    else:  
        return 0  
  
print(sigma(5))
```



NORMAL RECURSION

SPACE EFFICIENCY

- Consistent regardless of the number of recursion

```
#tail recursion  
def loop(n, summation):  
    if n>0:  
        return loop(n-1, n+summation)  
    else:  
        return summation  
  
def sigma1(n):  
    return loop(n,0)  
  
print(sigma1(5))
```

TAIL RECURSION

VS

- Space efficiency enhanced in tail recursion.

- 
1. **SELECTION SORT**
 2. **INSERTION SORT**
 3. **MERGE SORT**
 4. **QUICK SORT**
 5. **BUBBLE SORT**

SORT

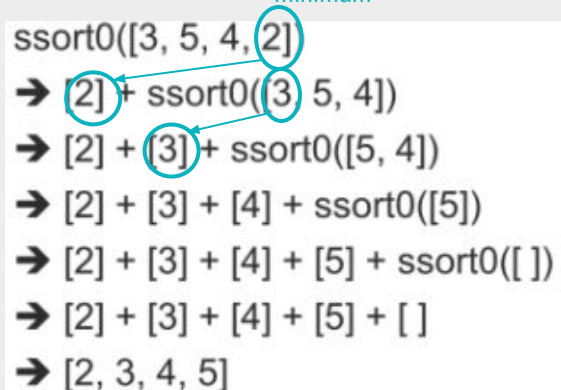
the arrangement of data in a prescribed sequence.

SORT : SELECTION SORT

Definition

Selection Sort sorts an array by repeatedly finding the minimum element from unsorted part and putting it at the beginning.

Sequence


ssort0([3, 5, 4, 2])
→ [2] + ssort0([3, 5, 4])
→ [2] + [3] + ssort0([5, 4])
→ [2] + [3] + [4] + ssort0([5])
→ [2] + [3] + [4] + [5] + ssort0([])
→ [2] + [3] + [4] + [5] + []
→ [2, 3, 4, 5]

Implementation

```
def ssort0(s):#selection sort (s:list)

    if s != []:#if list(s) is not empty
        smallest = min(s)#find the minimum value in s
        s.remove(smallest)#remove the minimum value
        return [smallest]+ssort0(s)#put at the beginning
    else:#when it is empty
        return []
```

```
print(ssort0([3,5,4,2]))
```


[2, 3, 4, 5]

SORT: INSERTION SORT

Definition

Insertion sort is a sorting algorithm that places an element at its suitable place in each iteration.

How it works

The array is virtually split into a sorted and an unsorted part. Values from the unsorted part are picked and placed at the correct position in the sorted part

Code

Insert(x,ss):

Put 'x' into the sorted list 'ss' in right order.

insert(6, [2, 4, 5, 7, 8]) → [2, 4, 5, 6, 7, 8]

```
def isort0(s):#insertion sort
    if s!=[]:#if list to sort is not empty
        return insert(s[0], isort0(s[1:]))
    else:#if there is nothing to sort
        return []
```

sequence

isort0([3, 5, 4, 2]) S: [3,5,4,2]
→ insert(3, isort0([5, 4, 2]))
→ insert(3, insert(5, isort0([4, 2])))
→ insert(3, insert(5, insert(4, isort0([2])))
→ insert(3, insert(5, insert(4, insert(2, isort0([])))))
→ insert(3, insert(5, insert(4, insert(2, []))))
→ insert(3, insert(5, insert(4, [2])))
→ insert(3, insert(5, [2, 4]))
→ insert(3, [2, 4, 5])
→ [2, 3, 4, 5]

SORT: INSERTION SORT

Implementation

```
def insert(x,ss):
    if ss != []:
        if x <= ss[0]:#put at the beginning
            ss = [x]+ss
            return ss
        if x>ss[-1]:#put at the end
            ss = ss + [x]
            return ss
        for idx in range(len(ss)-1):#find where to put x
            left = ss[idx]
            right = ss[idx+1]
            if left <= x and x<= right:#x should be put in the middle of left and right
                left_ss = ss[:idx+1]
                right_ss = ss[idx+1:]
                ss = left_ss + [x]+right_ss
                return ss
    else:
        return [x]

def isort0(s):#insertion sort
    if s!=[]:#if list to sort is not empty
        return insert(s[0], isort0(s[1:]))
    else:#if there is nothing to sort
        return []
```

```
print(isort0([3,5,4,2])) → [2, 3, 4, 5]
>>>
```

Returned ss from insert function in order

```
initial ss: [3, 5, 4, 2]
[]
[2, 4]
[2, 4, 5]
[2, 3, 4, 5]
```

SORT: MERGE SORT

How it works

In merge sort, the array is virtually split into a sorted and an unsorted part. Values from the unsorted part are picked and placed at the correct position in the sorted part.

Algorithm

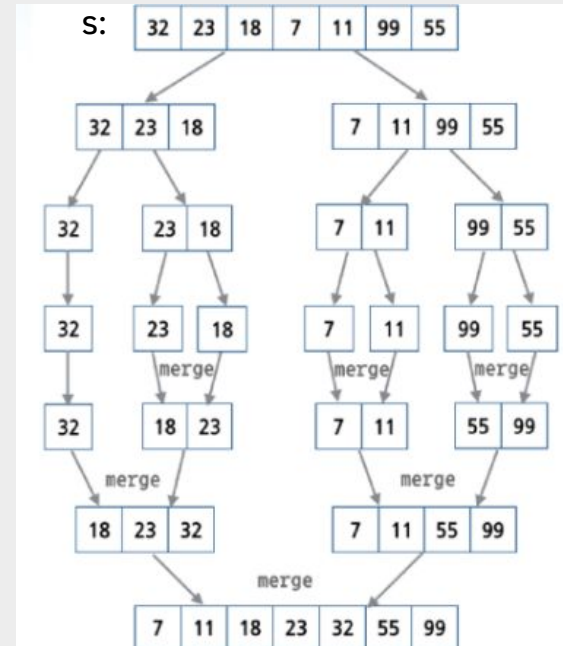
s: unsorted list

if $\text{len}(s) > 1$:

- split s in half and finish sorting through recursion respectively.
- Merge the splitted pieces by traversing from the front and selecting the minimum value

else:

- when $\text{len}(s) \leq 1$
- no need for sorting, so leave it be.



SORT: QUICK SORT

How it works

Quicksort works by selecting an element called a pivot and splitting the array around that pivot

Algorithm

s: unsorted list

if len(s)>1:

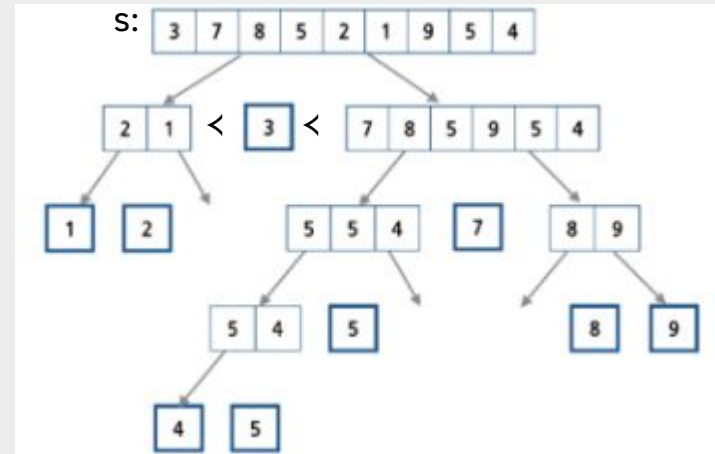
- Select a value to use as pivot. (For convenience, first value)
- Move the values in list based on pivot value.
 - pivot<value: move left to pivot
 - pivot>=value: move right to pivot
- sort left list and right rest by recursion, and place pivot in the middle

else:

- when len(s)<=1
- no need for sorting, so leave it be.

Sequence

Pivot is in darker blue colored square



SORT : QUICK SORT

Implementation

```
def partition(pivot, s):#partitions list based on pivot value
    left, right = [], []
    for x in s:#for value in list
        if x<= pivot:# if value <= pivot
            left.append(x)#save the value in left
        else:#if value > pivot
            right.append(x)#save the value in right
    return left, right

def qsort(s):#quick sort
    if len(s)>1:
        pivot = s[0]#set pivot as the first value
        (left, right) = partition(pivot, s[1:])
        return qsort(left)+[pivot]+qsort(right)#put pivot in the middle
    else:
        return s
```

The more the left, the smaller the value, the more the right, the bigger the value

```
s = [3,7,8,5,2,1,9,5,4]
print(qsort(s))
```



```
[1, 2, 3, 4, 5, 5, 7, 8, 9]
>>>
```

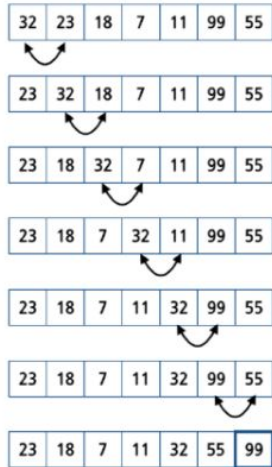
SORT: BUBBLE SORT

How it works

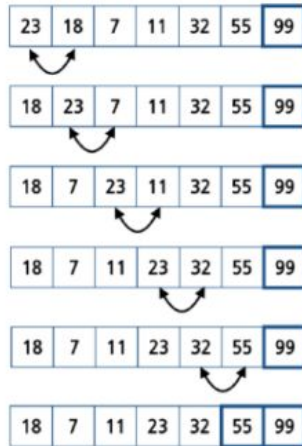
Bubble Sort compares two adjacent values in list, and swap their places, if the order is not right. It is an in-place sort that does not take up additional space, unlike the previous four sorting algorithms.

Sequence $n-1$ loops

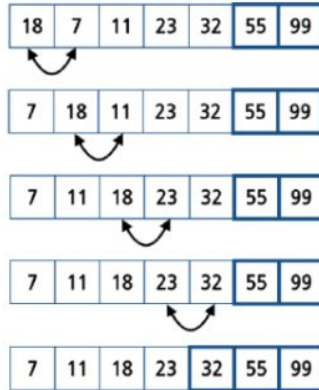
1st loop



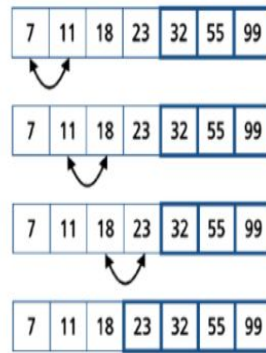
2nd loop



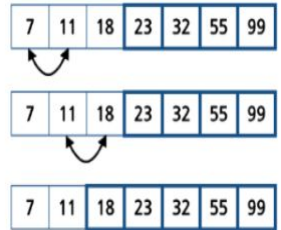
3rd loop



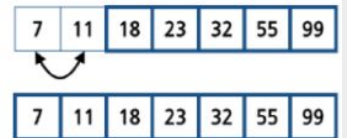
4th loop



5th loop



6th loop




SORT: BUBBLE SORT

Implementation

```
def bubblesort(arr):  
    n = len(arr) #number of values in list  
    for i in range(n-1): loop  
        for j in range(0,n-i-1):  
            #swap  
            if arr[j]>arr[j+1]:  
                arr[j], arr[j + 1] = arr[j + 1], arr[j]  
    return arr
```

```
arr = [32,23,18,7,11,99,55]  
print(bubblesort(arr))
```



```
[7, 11, 18, 23, 32, 55, 99]  
>>>
```

7	11	18	23	32	55	99
---	----	----	----	----	----	----