

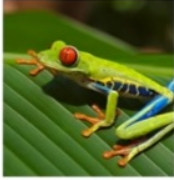


Suppose: 3 training examples, 3 classes.

With some  $W$  the scores  $f(x, W) = Wx$  are:

			
cat	<b>3.2</b>	1.3	2.2
car	5.1	<b>4.9</b>	2.5
frog	-1.7	2.0	<b>-3.1</b>

$\mathcal{L}_0 = 2.9$     $\mathcal{L}_1 = 0$     $\mathcal{L}_2 = 12.9$

Compute Multiclass SVM loss

$$\begin{aligned}\mathcal{L} &= \frac{1}{N} \sum_{i=1}^N \mathcal{L}_i \\ &= \frac{1}{3} (2.9 + 0 + 12.9) \\ &= 5.27\end{aligned}$$

$s_{y_0} = 3.2$

$$\mathcal{L}_i = \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + 1)$$

choice of the safety margin doesn't really matter

$$\begin{aligned}\mathcal{L}_0 &= \max(0, s_1 - s_{y_0} + 1) + \max(0, s_2 - s_{y_0} + 1) \\ &= \max(0, 5.1 - 3.2 + 1) + \max(0, -1.7 - 3.2 + 1) \\ &= \max(0, 2.9) + \max(0, -3.9) \\ &= 2.9\end{aligned}$$

$$\begin{aligned}\mathcal{L}_1 &= \max(0, s_0 - s_{y_1} + 1) + \max(0, s_2 - s_{y_1} + 1) \quad s_{y_1} = 4.9 \\ &= \max(0, 1.3 - 4.9 + 1) + \max(0, 2.0 - 4.9 + 1) \\ &= 0\end{aligned}$$

$$\begin{aligned}\mathcal{L}_2 &= \max(0, s_0 - s_{y_2} + 1) + \max(0, s_1 - s_{y_2} + 1) \quad s_{y_2} = -3.1 \\ &= \max(0, 2.2 + 3.1 + 1) + \max(0, 2.5 + 3.1 + 1) \\ &= 6.3 + 6.6 \\ &= 12.9\end{aligned}$$