

Swarm and Evolutionary Based Algorithms used for Optimization

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Abstract—In this paper, a study of evolution and swarm based algorithms is presented, using two classical engineering problems: *Spring Tension* and *Pressure Vessel Designs*. The test code for the problems was made using the *Python Language*, version 3.10 and uses *MealPy* package, version 2.5.1, to provide the algorithms. The algorithms were randomly chosen from a vast list from *MealPy*'s algorithms: *Evolutionary Programming (LevyEP)*, *Evolution Strategies (OriginalES)* and *Genetic Algorithm (BaseGA)* from *evolutionary_based* subpackage; *Bees Algorithm (OriginalBeesA)*, *Firefly Algorithm (OriginalFFA)* and *Particle Swarm Optimization (OriginalPSO)* from *swarm_based* subpackage. Each problem was modeled using *SciPy* package, with constraints implemented as *penalty functions*. Each algorithm were optimized separately to extract the best solutions from each problem using the *MealPy*'s *Tuner* utility. The results, however, are dependant of algorithm and/or problem solved and the Friedman's chi squared test for similarity make it noticeable because, although the values for best fits are similar, running the same algorithm with different initial conditions does not converge to similar values.

Index Terms—Optimization Methods, Evolutionary Programming, Evolutionary and Swarm Based Strategies.

I. DEFINITIONS

The main objective of this paper is study evolutionary and swarm intelligence algorithms. We present the main concepts of these two algorithm's classes, along with the chosen algorithms definitions in this section. All citations made in this document are due to Swarm Intelligence classes and to *MealPy*'s documentation, which points out the theoretical documentation for each implemented algorithm.

Evolution: From Jason Brownlee's "*Clever Algorithms*" - Evolutionary Algorithms belong to the Evolutionary Computation field of study concerned with computational methods inspired by the process and mechanisms of biological evolution. The process of evolution by means of natural selection (descent with modification) was proposed by Darwin to account for the variety of life and its suitability (adaptive fit) for its environment. The mechanisms of evolution describe how evolution actually takes place through the modification and propagation of genetic material (proteins). Evolutionary Algorithms are concerned with investigating computational systems that resemble simplified versions of the processes and mechanisms of evolution toward achieving the effects of these processes and mechanisms, namely the development of adaptive systems. Additional subject areas that fall within the realm of Evolutionary Computation are algorithms that seek to exploit the properties from the

related fields of Population Genetics, Population Ecology, Coevolutionary Biology, and Developmental Biology.

Swarm Intelligence: From Jason Brownlee's "*Clever Algorithms*" - Swarm intelligence is the study of computational systems inspired by the 'collective intelligence'. Collective Intelligence emerges through the cooperation of large numbers of homogeneous agents in the environment. Examples include schools of fish, flocks of birds, and colonies of ants. Such intelligence is decentralized, self-organizing and distributed through out an environment. In nature such systems are commonly used to solve problems such as effective foraging for food, prey evading, or colony re-location. The information is typically stored throughout the participating homogeneous agents, or is stored or communicated in the environment itself such as through the use of pheromones in ants, dancing in bees, and proximity in fish and birds.

Evolutionary Programming: From Jason Brownlee's "*Clever Algorithms*" - Evolutionary Programming is a Global Optimization algorithm and is an instance of an Evolutionary Algorithm from the field of Evolutionary Computation. The approach is a sibling of other Evolutionary Algorithms such as the Genetic Algorithm, and Learning Classifier Systems. It is sometimes confused with Genetic Programming given the similarity in name, and more recently it shows a strong functional similarity to Evolution Strategies. Evolutionary Programming is inspired by the theory of evolution by means of natural selection. Specifically, the technique is inspired by macro-level or the species-level process of evolution (phenotype, hereditary, variation) and is not concerned with the genetic mechanisms of evolution (genome, chromosomes, genes, alleles).

Evolutionary Strategies: From Jason Brownlee's "*Clever Algorithms*" - Evolution Strategies is a global optimization algorithm and is an instance of an Evolutionary Algorithm from the field of Evolutionary Computation. Evolution Strategies is a sibling technique to other Evolutionary Algorithms such as Genetic Algorithms (Section 3.2), Genetic Programming (Section 3.3), Learning Classifier Systems, and Evolutionary Programming. A popular descendant of the Evolution Strategies algorithm is the Covariance Matrix Adaptation Evolution Strategies (CMA-ES).

Genetic Algorithms: From Jason Brownlee's "*Clever Algorithms*" - The Genetic Algorithm is an Adaptive Strategy and a Global Optimization technique. It is an Evolutionary Algorithm

and belongs to the broader study of Evolutionary Computation. The Genetic Algorithm is a sibling of other Evolutionary Algorithms such as Genetic Programming, Evolution Strategies, Evolutionary Programming, and Learning Classifier Systems. The Genetic Algorithm is a parent of a large number of variant techniques and sub-fields too numerous to list. The Genetic Algorithm is inspired by population genetics (including heredity and gene frequencies), and evolution at the population level, as well as the Mendelian understanding of the structure (such as chromosomes, genes, alleles) and mechanisms (such as recombination and mutation). This is the so-called new or modern synthesis of evolutionary biology.

Particle Swarm Optimization: From Jason Brownlee's "Clever Algorithms" - Particle Swarm Optimization belongs to the field of Swarm Intelligence and Collective Intelligence and is a sub-field of Computational Intelligence. Particle Swarm Optimization is related to other Swarm Intelligence algorithms such as Ant Colony Optimization and it is a baseline algorithm for many variations, too numerous to list. It is inspired by the social foraging behavior of some animals such as flocking behavior of birds and the schooling behavior of fish.

Firefly Algorithm: From Xin-She Yang "Nature-Inspired Metaheuristic Algorithms" - The flashing light of fireflies is an amazing sight in the summer sky in the tropical and temperate regions. There are about two thousand firefly species, and most fireflies produce short and rhythmic flashes. The pattern of flashes is often unique for a particular species. The flashing light is produced by a process of bioluminescence, and the true functions of such signaling systems are still being debated. However, two fundamental functions of such flashes are to attract mating partners (communication), and to attract potential prey. In addition, flashing may also serve as a protective warning mechanism to remind potential predators of the bitter taste of fireflies. The firefly algorithm tries to mimic the attractiveness of Fireflies and has three basic rules:

- All fireflies are unisex so that one firefly will be attracted to other fireflies regardless of their sex;
- Attractiveness is proportional to the their brightness, thus for any two flashing fireflies, the less brighter one will move towards the brighter one. The attractiveness is proportional to the brightness and they both decrease as their distance increases. If there is no brighter one than a particular firefly, it will move randomly;
- The brightness of a firefly is affected or determined by the landscape of the objective function.

Bees Algorithm: From Jason Brownlee's "Clever Algorithms" - The Bees Algorithm belongs to Bee Inspired Algorithms and the field of Swarm Intelligence, and more broadly the fields of Computational Intelligence and Metaheuristics. The Bees Algorithm is related to other Bee Inspired Algorithms, such as Bee Colony Optimization, and other Swarm Intelligence algorithms such as Ant Colony Optimization and Particle Swarm Optimization. It is inspired by the foraging behavior of honey bees. Honey bees collect nectar from vast areas around their hive (more than 10 kilometers). Bee Colonies have been

observed to send bees to collect nectar from flower patches relative to the amount of food available at each patch. Bees communicate with each other at the hive via a waggle dance that informs other bees in the hive as to the direction, distance, and quality rating of food sources.

II. METHODOLOGY

A. Optimization Problem Selection

The two problems selected for this paper were *Spring Tension Design* and *Pressure Vessel Design*. Although it was simple to choose the first two problems from the computational work statements, the choice was more than justified because these problems are well known in the literature. Thus, the problem selection was driven by which has more than one source to compare results.

1) *Spring Tension Design:* From *Nature-Inspired Metaheuristic Algorithms* - Xin-She Yang - The design of a tension and compression spring is a well-known benchmark optimization problem. The main aim is to minimize the weight subject to constraints on deflection, stress, surge frequency and geometry. It involves three design variables: the wire diameter x_1 , coil diameter x_2 and number/length of the coil x_3 . This problem can be summarized as:

$$f(x) = x_1^2 x_2 (2 + x_3) \quad (1)$$

subject to

$$\begin{aligned} g_1(x) &= \frac{x_2^3 x_3}{71785 x_1^4} \leq 0 \\ g_2(x) &= \frac{4x_2^2 - x_1 x_2}{12566 (x_1^3 x_2 - x_1^4)} \\ &\quad + \frac{1}{5108 x_1^2} - 1 \leq 0 \\ g_3(x) &= 1 - \frac{140.45 x_1}{x_2^2 x_3} \leq 0 \\ g_4 &= \frac{x_1 + x_2}{1.5} - 1 \leq 0 \end{aligned} \quad (2)$$

The original bounding limits of the variables, extracted from computational work statements, are:

$$\begin{aligned} 0.05 &\leq x_1 \leq 2.0 \\ 0.25 &\leq x_2 \leq 1.3 \\ 2.0 &\leq x_3 \leq 15.0 \end{aligned} \quad (3)$$

2) *Pressure Vessel Design:* From *Solving Design of Pressure Vessel Engineering Problem Using a Fruit Fly Optimization Algorithm* - XIANTING KE et al - A pressure vessel design model involves four decision variables: x_1 is defined thickness of the pressure vessel T_s , x_2 stands for thickness of the head T_H , x_3 represents inner radius of the vessel R , and x_4 is on behalf of length of the vessel barring head L , the total variables described as (x_1, x_2, x_3, x_4) . The objective function of the problem is to minimize the total cost, including the cost

of material, forming, and welding. The general pressure vessel design optimization model is expressed as:

$$f(x) = 0.6224x_1x_3x_4 + 1.7781x_2x_3^2 + 3.1661x_1^2x_4 + 19.84x_1^2x_3 \quad (4)$$

subject to:

$$\begin{aligned} g_1(x) &= -x_1 + 0.0193x_3 \leq 0 \\ g_2(x) &= -x_2 + 0.00954x_3 \leq 0 \\ g_3(x) &= -\pi x_3^2x_4 - \frac{4}{3}\pi x_3^3 + 1296000 \leq 0 \\ g_4(x) &= x_4 - 240 \leq 0 \end{aligned} \quad (5)$$

The original bounding limits of the variables, extracted from computational work statements, are:

$$\begin{aligned} 0 &\leq x_1 \leq 99 \\ 0 &\leq x_2 \leq 99 \\ 10 &\leq x_3 \leq 200 \\ 10 &\leq x_4 \leq 200 \end{aligned} \quad (6)$$

For some reason these settings does not work at all with the selected optimizers, so some research in the literature *Solving Design of Pressure Vessel Engineering Problem Using a Fruit Fly Optimization Algorithm - XIANTING KE et al* suggest the following bounding limits:

$$\begin{aligned} 0.0625 &\leq x_1 \leq 99 \times 0.0625 \\ 0.0625 &\leq x_2 \leq 99 \times 0.0625 \\ 10 &\leq x_3 \leq 200 \\ 10 &\leq x_4 \leq 200 \end{aligned} \quad (7)$$

But these settings produce many random, bizarre and noisy results in all selected optimizers. Then a proud-and-lame-homemade set of variable boundings comes in handy, obtained by tweaking the original boundings:

$$\begin{aligned} 0.75 &\leq x_1 \leq 0.8 \\ 0.35 &\leq x_2 \leq 0.4 \\ 39.5 &\leq x_3 \leq 41.0 \\ 195.0 &\leq x_4 \leq 205.0 \end{aligned} \quad (8)$$

It is not intended here to point out modeling errors of any kind, nor point out package errors made by the authors or ours, but the homemade bounding limits was necessary to reach the literature results.

B. Constraint Implementation

The constraints that all problems are subjected were implemented as *penalty functions*, that is, it adds a high value when the constraint is not satisfied, zero otherwise. It is an optional requirement from computational work in question and is the recommended way to put constraints from *MealPy*'s Manual.

C. Programming Language

The chosen programming language for the test code was *Python Language*, version 3.10, because it is an opensource language easy to program and has a huge amount of packages regarding artificial intelligence, genetic algorithms and swarm based algorithms. From these packages it was selected *MealPy* package, version 2.5.1, because it comprises all the algorithm's classed tested in this paper.

D. Algorithm Selection

The algorithm selection was made in two steps: first, it was extracted simple version of the two classes (evolutionary and swarm based) and then it was used a simple shuffle using Python's *random.shuffle* in a terminal - no script was required.

The chosen algorithms were:

- **Evolution Based Algorithms:** LevyEP (Evolutionary Programming), OriginalES (Evolution Strategy) and BaseGA (Genetic Algorithm)
- **Swarm Based Algorithms:** OriginalBeesA (Bees Algorithm), OriginalFFA (Original Firefly Algorithm) and OriginalPSO (Particle Swarm Optimization)

E. Optimizer Tuning

The hyperparameters for each optimizer were tuned using the *MealPy*'s *Tuner* utility. It is a recommended procedure to tune hyperparameters for each optimizer and problem, according to *MealPy*'s Manual. The *Tuner* utility is a very simple grid search metaheuristic search tool that test each grid configuration for a specified optimizer runs. Although simple, it is a very expensive procedure that took 2 days to complete. It was defined 10 runs for each configuration, with the following set of hyperparameter:

- **Evolution Based Algorithms:**

LevyEP:

bout_size (float): percentage of child agents implement tournament selection.

OriginalES:

lamda (float): Percentage of child agents evolving in the next generation.

BaseGA:

pc (float): cross-over probability

pm (float): mutation probability

- **Swarm Based Algorithms:**

OriginalBeesA:

selected_site_ratio (float)

elite_site_ratio (float)

selected_site_bee_ratio (float)

elite_site_bee_ratio (float)

dance_radius (float)

dance_reduction (float)

OriginalFFA:

gamma (float): Light Absorption Coefficient

beta_base (float): Attraction Coefficient

Value

alpha (float): Mutation Coefficient

Rate *alpha_damp* (float): Mutation Coefficient Damp
delta (float): Mutation Step Size
exponent (int): Exponent
OriginalPSO:
c1 (float): local coefficient
c2 (float): global coefficient
w_min (float): Weight min of bird
w_max (float): Weight max of bird

F. Optimizer Parameters

For all optimizers and problems, were selected the following parameters:

- *Runs*: 100 runs
- *Epochs*: 100 epochs
- *Population*: 100 initial points

The initial solutions were randomly selected using the same seed for all algorithms.

III. RESULTS

A. Spring Tension Design

- 1) *Evolutionary Algorithms*:
- 2) *Swarm Based Algorithms*:

B. Pressure Vessel Design

- 1) *Evolutionary Algorithms*:
- 2) *Swarm Based Algorithms*:

IV. DISCUSSION

The main objective of this work is demonstrate the inner work of a optimization class of algorithms called *Quasi-Newton algorithms*. Four of them are presented, along with the results and analysis regarding convergence, function evaluations and function objective values.

For implementation, it was decided to put constraints on search space, because for the original search space of some functions, like Ackley and Rastrigin, there are other minimas that will confuse every algorithm tested for this paper, and there is no sense on test a local minima procedure on these conditions. To restrain the initial solution to some region in the search space was a cheap and ready solution to avoid the algorithms to stop because of stumbling upon the wrong minimum.

The *Levenberg-Marquardt Algorithm* implemented for this paper is very sensitive to hyperparameters, namely α and λ , which was not tuned to every function, so, the conspicuous performance variation is noticeable along the results. LMA is known to be fast and reliable, but in our implementation it was found a little tricky to get the hyperparameters right for all the test functions. But for Rosenbrock and Rastrigin, it is the best option, even for lame implementations like ours.

The *Broyden-Fletcher-Goldfarb-Shanno* Algorithm was the only one that we decided to use it as is from *SciPy*, because it has features desired for this work, like counting of function evaluations, gradient evaluation and iterations. It performed

very well for Ackley and Booth Functions, and reasonably well for other functions.

The *Davidon-Fletcher-Powell* Algorithm is not implemented in *SciPy* but its equations shows that it is the dual of BFGS, so, it was easy to implement using some *SciPy* code for BFGS algorithm. In the DFP procedure, there is a Hessian inversion to be evaluated every iteration, then, numerical imprecision would be taken into consideration evaluating its results. While in some cases it has a superb performance (Like Ackley Function), it has very poor performance in Rosenbrock Function and even in Beale Function. The increase of dimensions makes DFP suffer of numerical imprecision due to the Hessian inversion, except for Rastrigin, and it is the loser algorithm in other functions.

Finally, the *Limited memory BFGS* has an average performance among the functions. The original algorithm was implemented using code found in the url <https://github.com/qkolj/L-BFGS/blob/master/L-BFGS.ipynb>.

In fact, there are no Quasi-Newton algorithms that solver the minima problem for an any function. From the standpoint of performance and convergence, all the algorithms have an average performance and a reasonable convergence, although we have to restrain the search space to a small area near the optimal solution.