

**INDIVIDUAL WORK: Deadline: 09/02/2023**

Sent the pdf file with answers by email to

[leandro.coelho@ufpr.br](mailto:leandro.coelho@ufpr.br) **SUBJECT:** List of exercises 02

# List of exercises 02

## Metaheuristics

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Google Scholar: <https://scholar.google.com/citations?user=0X7VkC4AAAAJ&hl=pt-PT>

# Question 01 (a)

1 **Complete the following tables** with the steps of a genetic algorithm (GA) during an evolutionary cycle.

a) Generation of the **initial population** of solutions and **evaluation of objective function**

Set the initial generations counter: ***generation = 0***

Member of population	Genotype (binary representation) Base 2			Phenotype (floating point representation) Base 10			(maximization) objective function, $f$
	$g_1$	$g_2$	$g_3$	$x_1$	$x_2$	$x_3$	$f = x_1 + x_2 + x_3$
1	001.110	001.100	011.100	1.750	1.500	3.500	6.750
2		000.010		0.125		1.875	
3	101.010	110.011	100.110				
4	010.011	010.110	000.000			0.000	
Best member							

# Question 01 (b), (c)

**Example:** In the member 1,  $g_1$  with 001.11 has cut in 00 | 1.11

**b)** Apply the **crossover operation** after selection using roulette selection

Selected the same cut point in the 3<sup>rd</sup> position (left to right)

Selected members to match (parents)	Genotype (binary representation) Base 2			Phenotype (floating point representation) Base 10		
	$g_1'$	$g_2'$	$g_3'$	$x_1'$	$x_2'$	$x_3'$
1': 1 and 2						
2': 1 and 2						
3': 2 and 3						
4': 2 and 3						

**c)** Apply the **mutation operation**

Members to apply the mutation (offspring)	Genotype (binary representation) Base 2			Phenotype (floating point representation) Base 10		
	$g_1''$	$g_2''$	$g_3''$	$x_1''$	$x_2''$	$x_3''$
1': yes						
2': no						
3': yes						
4': no						

# Question 01 (d)

d) New **population** of solutions and **evaluation of objective function**

Update the generation counter i.e. **generation = generation + 1** and return to Step b

Member of population	<b>Genotype</b> of the current population (binary representation)			<b>Phenotype</b> of the current population (floating point representation)			(maximization) objective function, f
	Base 2			Base 10			New
	$g_1''$	$g_2''$	$g_3''$	$x_1''$	$x_2''$	$x_3''$	$f = x_1 + x_2 + x_3$
1''							
2''							
3''							
4''							
Current best member							

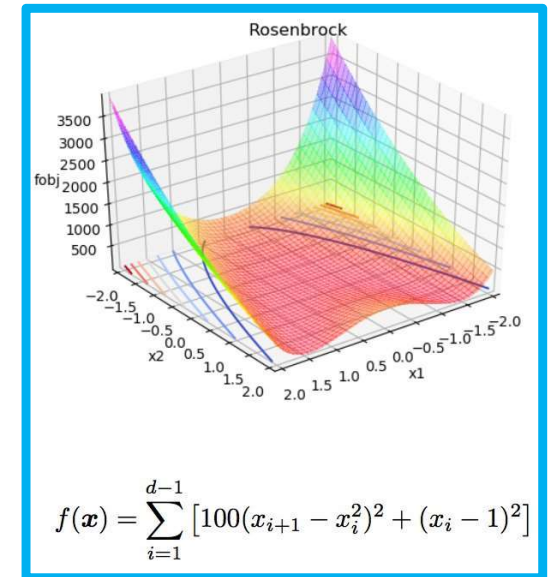
# Question 02

What are the **differences** between heuristics, metaheuristics, and hyperheuristics?

# Question 03

Considering the optimization problem  $\min f(x)$  illustrated in figure.

- a) What are the **independent variables** of  $f(x)$ ?
- b) What are the **decision variables** of  $f(x)$ ?
- c) Rewrite this problem as a **maximization** problem.



# Question 04

- a) What is the **difference** between exploration and exploitation?
- b) What is the **difference** between intensification and diversification?
- c) What is the **difference** between global search and local search?

# Question 05

How the **exploration and exploitation** strategies are designed in a **standard particle swarm optimization** approach?

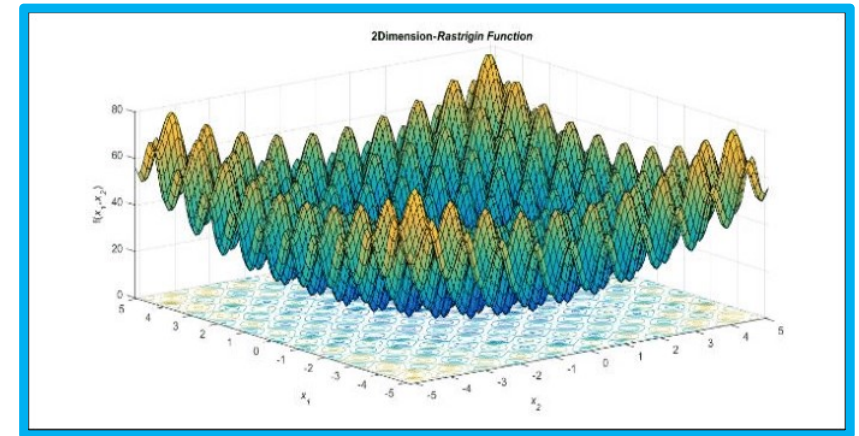


# Question 06

We want to a binary GA (Genetic Algorithm) to find  $x$  to a **resolution of 0.1** to minimize the two-dimensional Rastrigin function ( $n=2$ ) on the domain  $[-5,5]$ .

$$f(x_1 \cdots x_n) = 10n + \sum_{i=1}^n (x_i^2 - 10\cos(2\pi x_i))$$
$$-5 \leq x_i \leq 5$$

minimum at  $f(0, \cdots, 0) = 0$



- a) How many **genes** do we need for each chromosome:
- b) How many **bits** do we need in each gene?
- c) Given your answer to part (b), what is the **resolution** of each element of  $x$ ?

# Question 07

How could you **change** the **differential evolution** algorithm to be **non-elitist**?

# Question 08

What are the **differences** between standard (classical) **evolutionary programming** and **evolution strategy** when applied to continuous optimization?

# Question 09

Present **step-by-step** the approach named **harmony search algorithm** (Geem et al., 2001) applied to a general continuous optimization problem?

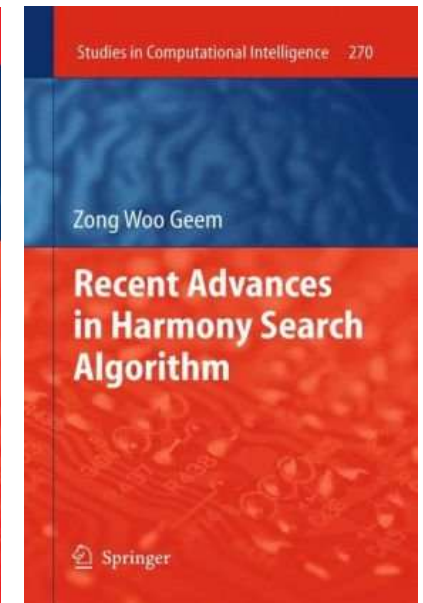
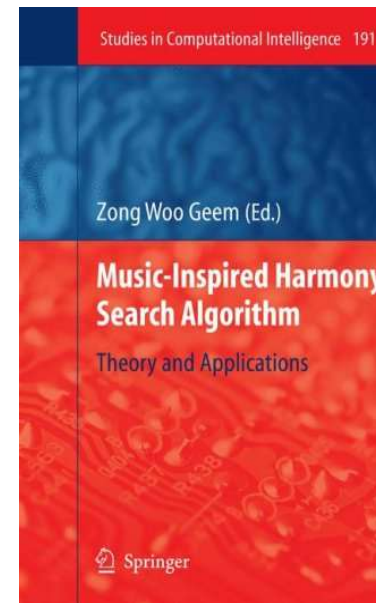
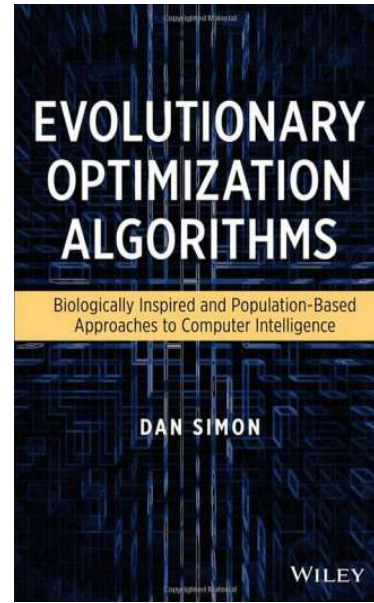
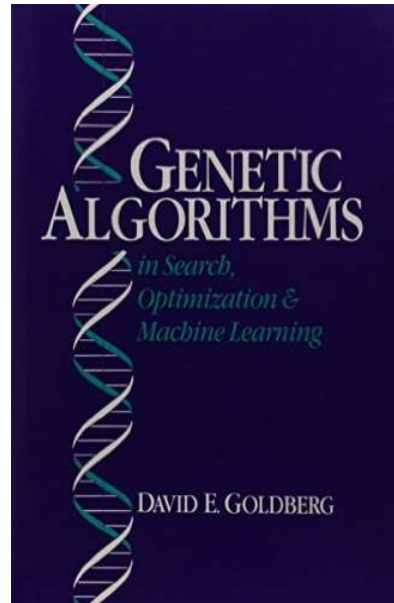
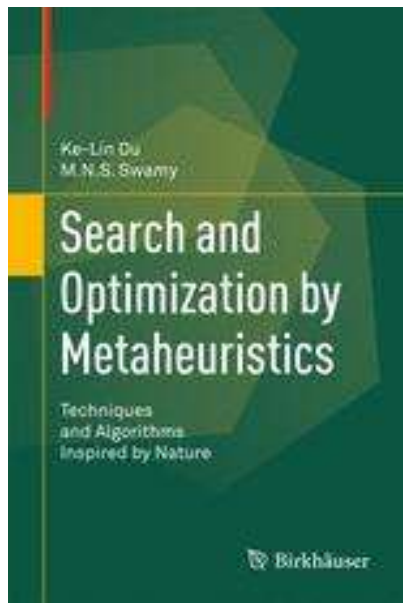
See

<https://sites.google.com/a/hydroteq.com/www/>

<https://www.sciencedirect.com/science/article/abs/pii/S2210650218303791>

Geem, Z. W., Kim, J. H., Loganathan, G. V., 2001. A new heuristic optimization algorithm: Harmony search. Simulation. 76(2), pp. 60–68. 10.1177/003754970107600201

# Support materials



# Quote

It is during our darkest moments that we must focus to see the light.

Aristotle (384-322 BC)

Greek philosopher and polymath during the Classical period in Ancient Greece.

