

# Step by Step Calculation of the Penman-Monteith Evapotranspiration (FAO-56 Method)<sup>1</sup>

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## Introduction

The term evapotranspiration ( $ET$ ) is commonly used to describe two processes of water loss from land surface to atmosphere, evaporation and transpiration. Evaporation is the process where liquid water is converted to water vapor (vaporization) and removed from sources such as the soil surface, wet vegetation, pavement, water bodies, etc. Transpiration consists of the vaporization of liquid water within a plant and subsequent loss of water as vapor through leaf stomata.

Evaporation and transpiration occur simultaneously and both processes depend on solar radiation, air temperature, relative humidity (i.e. vapor pressure deficit) and wind speed. Transpiration rate is also influenced by crop characteristics, environmental aspects and cultivation practices. Different kinds of plants may have different transpiration rates. Not only the type of crop, but also the crop development, environment and management should be considered when assessing transpiration. For example, when the crop is small, water is predominately lost by soil evaporation because little of the soil surface is covered by the plant, but once the crop is well developed and completely covers the soil, transpiration becomes the main process (Allen et al., 1998).

Reference evapotranspiration ( $ET_o$ ) is defined as the rate at which readily available soil water is vaporized from specified vegetated surfaces (Jensen et al., 1990). Then, reference evapotranspiration is defined as the  $ET$  rate from a uniform surface of dense, actively growing vegetation having specified height and surface resistance, not short of soil water, and representing an expanse of at least 100 m of the same or similar vegetations (Allen et al., 2005). The concept of the  $ET_o$  was introduced to study the evaporative demand of the atmosphere independent of crop type, crop development and management practices. If water is abundantly available at the reference surface, soil factors do not affect  $ET$ , however,  $ET$  may decrease overtime as soil water content decreases. Relating  $ET$  to a specific surface provides a reference to which  $ET$  from other surfaces can be related. It obviates the need to define a separate  $ET$  level for each crop and stage of growth and is referred to as crop  $ET$  ( $ET_c$ ).  $ET_o$  values measured or calculated at different locations or in different seasons are comparable as they refer to the  $ET$  from the same reference surface. The only factors affecting  $ET_o$  are climatic parameters and  $ET_c$  can be determined from  $ET_o$  using a crop specific coefficient ( $K_c$ ). The use of  $K_c$  with specific crops is the subject

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A large number of empirical methods have been developed over the last 50 years to estimate evapotranspiration from different climatic variables. Some of these derived from the now well-known Penman equation (Penman, 1948) to determine evaporation from open water, bare soil and grass (now called evapotranspiration) based on a combination of an energy balance and an aerodynamic formula, given as equation [1]:

$$\lambda E = \frac{[\Delta(R_n - G)] + (\gamma \lambda E_a)}{(\Delta + \gamma)}$$

where  $\lambda E$  = evaporative latent heat flux ( $\text{MJ m}^{-2} \text{d}^{-1}$ ),  $\Delta$  = slope of the saturated vapor pressure curve [ $\delta e^o / \delta T$ , where  $e^o$  = saturated vapor pressure (kPa) and  $T_{mean}$  = daily mean temperature ( $^{\circ}\text{C}$ )];  $R_n$  = net radiation flux ( $\text{MJ m}^{-2} \text{d}^{-1}$ ),  $G$  = sensible heat flux into the soil ( $\text{MJ m}^{-2} \text{d}^{-1}$ ),  $\gamma$  = psychrometric constant ( $\text{kPa } ^{\circ}\text{C}^{-1}$ ), and  $E_a$  = vapor transport of flux ( $\text{mm d}^{-1}$ ).

Various derivation of the Penman equation included a bulk surface resistance term (Monteith, 1965) and the resulting equation is now called the Penman-Monteith equation, which may be expressed for daily values as equation [2]:

$$\lambda ET_o = \frac{\Delta(R_n - G) + [86,400 \frac{\rho_a C_p (e_s^o - e_a)}{r_{av}}]}{\Delta + \gamma \left(1 + \frac{r_s}{r_{av}}\right)}$$

where  $\rho_a$  = air density ( $\text{kg m}^{-3}$ ),  $C_p$  = specific heat of dry air,  $e_s^o$  = mean saturated vapor pressure (kPa) computed as the mean  $e^o$  at the daily minimum and maximum air temperature ( $^{\circ}\text{C}$ ),  $r_{av}$  = bulk surface aerodynamic resistance for water vapor ( $\text{s m}^{-1}$ ),  $e_a$  = mean daily ambient vapor pressure (kPa) and  $r_s$  = the canopy surface resistance ( $\text{s m}^{-1}$ ).

An updated equation was recommended by FAO (Allen et al. 1998) with the FAO-56 Penman-Monteith Equation, simplifying equation [2] by utilizing some assumed constant parameters for a clipped grass reference crop. It was assumed that the definition for the reference crop was a hypothetical reference crop with crop height of 0.12 m, a fixed surface resistance of  $70 \text{ s m}^{-1}$  and an albedo value (i.e. portion of light reflected by the leaf surface) of 0.23 (Smith et al., 1992). The new equation is given as equation [3]:

$$ET_o = \frac{0.408 \Delta (R_n - G) + \gamma \frac{900}{T + 273} u_2 (e_s - e_a)}{\Delta + \gamma (1 + 0.34 u_2)}$$

where  $ET_o$  = reference evapotranspiration rate ( $\text{mm d}^{-1}$ ),  $T$  = mean air temperature ( $^{\circ}\text{C}$ ), and  $u_2$  = wind speed ( $\text{m s}^{-1}$ ) at 2 m above the ground. Equation 3 can be applied using hourly data if the constant value “900” is divided by 24 for the hours in a day and the  $R_n$  and  $G$  terms are expressed as  $\text{MJ m}^{-2} \text{h}^{-1}$ .

In 1999, the Irrigation Association (IA) requested the Evapotranspiration in Irrigation and Hydrology Committee – Environmental and Water Resources Institute (American Society of Civil Engineering)(ASCE-ET) to establish one standardized equation for estimating the parameters to gain consistency and wider acceptance of  $ET$  models (Howell and Evett, 2006). The principal outcome was that two

**Table 1:** Values for  $C_n$  and  $C_d$  in Eq. 4 (after Allen et al., 2005).

Calculation time step	Short reference crop $ET_{os}$		Tall reference crop, $ET_{rs}$		Units for $ET_{os}$ and $ET_{rs}$	Units for $R_n$ and $G$
	$C_n$	$C_d$	$C_n$	$C_d$		
Daily	900	0.34	1600	0.38	mm d <sup>-1</sup>	MJ m <sup>-2</sup> d <sup>-1</sup>
Hourly, daytime	37	0.24	66	0.25	mm h <sup>-1</sup>	MJ m <sup>-2</sup> h <sup>-1</sup>
Hourly, nighttime	37	0.96	66	1.7	mm h <sup>-1</sup>	MJ m <sup>-2</sup> h <sup>-1</sup>

equations, one for a short crop (similar to clipped, cool-season grass) named  $ET_{os}$  and another for a tall crop (similar to full-cover alfalfa) named  $ET_{rs}$ , were developed for daily (24 hr) and hourly time periods. The ASCE-EWRI standardized reference  $ET$  equation based on the FAO 56 Penman-Monteith equation (4) for a hypothetical crop is given as equation [4]:

$$ET_{sz} = \frac{0.408\Delta (R_n - G) + \gamma \frac{C_n}{T + 273} u_2 (e_s^o - e_a)}{\Delta + \gamma(1 + C_d u_2)}$$

where  $ET_{sz}$  = the standardized reference evapotranspiration for grass ( $ET_{os}$ ) or alfalfa ( $ET_{rs}$ ) in units based on the time step of mm d<sup>-1</sup> for a 24-h day or mm h<sup>-1</sup> for an hourly time step,  $C_n$  = the numerator constant for the reference crop type and time step and  $C_d$  = the denominator constant for the reference crop type and time step (see Table 1 for values of  $C_n$  and  $C_d$ ).

Note that  $ET_{sz}$  for a short crop ( $ET_{os}$ ) equation is identical to the FAO-56 Penman-Monteith equation previously described [Eq. 3]. FAO 56 equation has been selected because it closely approximates grass  $ET_o$  at the location evaluated, is physically based and explicitly incorporates both physiological and aerodynamic parameters. FAO-56 Penman-

Monteith equation has been widely use for Florida conditions. Moreover, procedures have been developed for estimating missing climatic parameters (Allen et al., 2005; Romero et al., 2009).

The objective of this publication is to provide a step-by-step calculation of the reference evapotranspiration (FAO-56 method) for a given location from the available weather data.

### Required parameters to calculate $ET_o$

Reference evapotranspiration estimation method is based on climatic data, which can be obtained from a local weather station or, for Florida can be obtained accessing the Florida Automated Weather Network (FAWN, <http://fawn.ifas.ufl.edu/>). The equation uses standard climatological records of solar radiation (sunshine), air temperature, humidity and wind speed. To ensure the integrity of computations, the weather measurements should be made at 2 m (or converted to that height) above an extensive surface of green grass, shading the ground and not short of water. Table 2 shows a list of parameters required to calculate  $ET_o$ .

**Table 2.** Required inputs for  $ET_o$  calculation.

Symbol	Parameter	Unit
$T_{max}^a$	maximum temperature	°C
$T_{min}^a$	minimum temperature	°C
$RH_{max}^a$	maximum relative humidity	%
$RH_{min}^a$	minimum relative humidity	%
$R_s$	average solar radiation	MJ m <sup>-2</sup> d <sup>-1</sup>
$u_2$	average wind speed	m s <sup>-1</sup> at $h^b$ m
$P$	atmospheric pressure (barometric)	kPa
$z$	site elevation above sea level	m
$J$	Julian day	-
LAT	Latitude	degree

<sup>a</sup> values obtained in the period of 24h (0:00:01 AM to 11:59:59 PM).

<sup>b</sup>  $h$  = height of measurement above ground surface in meters.

## Overall equation of Penman-Monteith

The FAO Penman-Monteith method to estimate  $ET_o$  can be derived [Eq. 3]:

$$ET_o = \frac{0.408\Delta (R_n - G) + \gamma \frac{900}{T + 273} u_2 (e_s - e_a)}{\Delta + \gamma(1 + 0.34 u_2)}$$

where,

$ET_o$  = reference evapotranspiration, mm day<sup>-1</sup>;

$R_n$  = net radiation at the crop surface, MJ m<sup>-2</sup> d<sup>-1</sup>;

$G$  = soil heat flux density, MJ m<sup>-2</sup> d<sup>-1</sup>;

$T$  = mean daily air temperature at 2 m height, °C;

$u_2$  = wind speed at 2 m height, m s<sup>-1</sup>;

$e_s$  = saturation vapor pressure, kPa;

$e_a$  = actual vapor pressure, kPa;

$e_s - e_a$  = saturation vapor pressure deficit, kPa;

$\Delta$  = slope of the vapor pressure curve, kPa °C<sup>-1</sup>;

$\gamma$  = psychrometric constant, kPa °C<sup>-1</sup>.

The reference evapotranspiration,  $ET_o$ , provides a standard to which:

- evapotranspiration at different periods of the year or in other regions can be compared;
- evapotranspiration of other crops can be related.

## $ET_o$ - Practical calculation steps

### Step 1 – Mean daily temperature

The (average) daily maximum and minimum air temperatures in degrees Celsius (°C) are required. Where only (average) mean daily temperatures are available, the calculations can still be executed but some underestimation of  $ET_o$  will probably occur due to the non-linearity of the saturation vapor pressure - temperature relationship (Allen et al., 1998). Average temperature is calculated by [Eq. 5]:

$$T_{mean} = \frac{T_{max} + T_{min}}{2}$$

where,

$T_{mean}$  = mean daily air temperature, °C;

$T_{max}$  = maximum daily air temperature, °C;

$T_{min}$  = minimum daily air temperature, °C.

**Step 2 – Mean daily solar radiation ( $R_s$ )**

The average daily net radiation expressed in megajoules per square meter per day ( $\text{MJ m}^{-2} \text{ day}^{-1}$ ) is required. A simple average of solar radiation values obtained from a weather station in the period of 24h (0:00:01 am to 11:59:59 pm) is required. The conversion of units may be required when solar radiation is expressed in watts per square meter per day ( $\text{W m}^{-2} \text{ day}^{-1}$ ). The conversion is given as equation [Eq.6]:

$$R_s (\text{MJ m}^{-2} \text{ day}^{-1}) = R_s (\text{W m}^{-2} \text{ day}^{-1}) * 0.0864$$

**Step 3 – Wind speed ( $u_2$ )**

The average daily wind speed in meters per second ( $\text{m s}^{-1}$ ) measured at 2 m above the ground level is required. It is important to verify the height at which wind speed is measured, as wind speeds measured at different heights above the soil surface differ. The wind speed measured at heights other than 2 m can be adjusted according to the follow equation [7]:

$$u_2 = u_h \frac{4.87}{\ln(67.8 h - 5.42)}$$

where,

$u_2$  = wind speed 2 m above the ground surface,  $\text{m s}^{-1}$ ;

$u_z$  = measured wind speed  $z$  m above the ground surface,  $\text{m s}^{-1}$ ;

$h$  = height of the measurement above the ground surface, m.

In case of wind speed is given in miles per hour ( $\text{mi h}^{-1}$ ) the conversion to  $\text{m s}^{-1}$  is given as equation [Eq.8]:

$$u_2 (\text{m s}^{-1}) = u_2 (\text{mi h}^{-1}) * 0.477$$

**Step 4 - Slope of saturation vapor pressure curve ( $\Delta$ )**

For the calculation of evapotranspiration, the slope of the relationship between saturation

vapor pressure and temperature,  $\Delta$ , is given as equation [Eq.9]:

$$\Delta = \frac{4098 \left[ 0.6108 \exp \left( \frac{17.27 * T_{mean}}{T_{mean} + 237.3} \right) \right]}{(T_{mean} + 273.3)^2}$$

$T_{mean}$  = mean daily air temperature,  $^{\circ}\text{C}$ , [Eq.5];

$\exp$  = 2.7183 (base of natural logarithm).

**Step 5 – Atmospheric Pressure ( $P$ )**

The atmospheric pressure,  $P$ , is the pressure exerted by the weight of the earth's atmosphere. Evaporation at high altitudes is promoted due to low atmospheric pressure. This effect is, however, small and in the calculation procedures, the average value for a location is sufficient. A simplification of the ideal gas law, assuming  $20^{\circ}\text{C}$  for a standard atmosphere, can be employed to calculate  $P$  in kPa at a particular elevation [Eq. 10]:

$$P = 101.3 \left[ \frac{293 - 0.0065z}{293} \right]^{5.26}$$

where,

$z$  = elevation above sea level, m.

$P$  = atmospheric pressure, kPa.

**Step 6 – Psychrometric constant ( $\gamma$ )**

The psychrometric constant relates the partial pressure of water in air to the air temperature so that vapor pressure can be estimated using paired dry and wet thermometer bulb temperature readings. Another way to describe the psychrometric constant is the ratio of specific heat of moist air at constant pressure ( $C_p$ ) to latent heat of vaporization. The specific heat at constant pressure is the amount of energy required to increase the temperature of a unit mass of air by one degree at constant pressure. Its value depends on the composition of the air, i.e., on its humidity. For average atmospheric conditions a  $C_p$  value of  $1.013 \times 10^{-3} \text{ MJ kg}^{-1} ^{\circ}\text{C}^{-1}$  can be used. As an average atmospheric



pressure is used for each location, the psychrometric constant is kept constant for each location depending of the altitude [see Eq. 10]. Psychrometric constant is given as [Eq. 11]:

$$\gamma = \frac{C_p P}{\varepsilon \lambda} = 0.000665 P$$

$\gamma$  = psychrometric constant, kPa °C<sup>-1</sup>;

$P$  = atmospheric pressure, kPa, [Eq. 10];

$\lambda$  = latent heat of vaporization, 2.45, MJ kg<sup>-1</sup>;

$c_p$  = specific heat at constant pressure, 1.013 10<sup>-3</sup>, MJ kg<sup>-1</sup> °C<sup>-1</sup>;

$\varepsilon$  = ratio molecular weight of water vapour/dry air = 0.622.

#### Step 7 – Delta Term (DT) (auxiliary calculation for Radiation Term)

In order to simplify the  $ET_o$  calculation, several terms are calculated separated. The delta term is used to calculate the “Radiation Term” of the overall  $ET_o$  equation [see Eq. 33]. DT term is given as [Eq.12]:

$$DT = \frac{\Delta}{\Delta + \gamma(1 + 0.34 u_2)}$$

where,

$\Delta$  = slope of saturation vapor curve [Eq.9];

$\gamma$  = psychrometric constant, kPa °C<sup>-1</sup>, [Eq.11];

$u_2$  = wind speed 2 m above the ground surface, m s<sup>-1</sup>, [Eq.7].

#### Step 8 – Psi Term (PT) (auxiliary calculation for Wind Term)

The psi term is used to calculate the “Wind Term” of the overall  $ET_o$  equation [see Eq. 34]. PT term is given as [Eq. 13]:

$$PT = \frac{\gamma}{\Delta + \gamma(1 + 0.34 u_2)}$$

where,

$\Delta$  = slope of saturation vapor curve [Eq.9];

$\gamma$  = psychrometric constant, kPa °C<sup>-1</sup>, [Eq.11];

$u_2$  = wind speed 2 m above the ground surface, m s<sup>-1</sup>, [Eq.9].

#### Step 9 – Temperature Term (TT) (auxiliary calculation for Wind Term)

The temperature term is used to calculate the “Wind Term” of the overall  $ET_o$  equation [see Eq. 34]. Temperature term is given as [Eq.14]:

$$TT = \left[ \frac{900}{T_{mean} + 273} \right] * u_2$$

where,

$T_{mean}$  = mean daily air temperature, °C, [Eq.5].

#### Step 10 – Mean saturation vapor pressure derived from air temperature ( $e_s$ )

As saturation vapor pressure is related to air temperature, it can be calculated from the air temperature. The relationship is expressed by [Eq. 15]:

$$e_{(T)} = 0.6108 \exp \left[ \frac{17.27T}{T + 237.3} \right]$$

where,

$e_{(T)}$  = saturation vapor pressure at the air temperature  $T$ , kPa

$T$  = air temperature, °C.

Therefore, the mean saturation vapor pressure is calculated as the mean between the

saturation vapor pressure at both the daily maximum [Eq. 16]:

$$e_{(T_{max})} = 0.6108 \exp \left[ \frac{17.27 T_{max}}{T_{max} + 237.3} \right]$$

and minimum air temperatures [Eq.17]:

$$e_{(T_{min})} = 0.6108 \exp \left[ \frac{17.27 T_{min}}{T_{min} + 237.3} \right]$$

where,

$T_{max}$  = maximum daily air temperature, °C;

$T_{min}$  = minimum daily air temperature, °C.

The mean saturation vapor pressure for a day, week, decade or month should be computed as the mean between the saturation vapor pressure at the mean daily maximum and minimum air temperatures for that period [Eq. 18]:

$$e_s = \frac{e_{(T_{max})} + e_{(T_{min})}}{2}$$

### Step 11 – Actual vapor pressure ( $e_a$ ) derived from relative humidity

The actual vapor pressure can also be calculated from the relative humidity. Depending on the availability of the humidity data, different equations should be used [Eq. 19]:

$$e_a = \frac{e_{(T_{min})} \left[ \frac{RH_{max}}{100} \right] + e_{(T_{max})} \left[ \frac{RH_{min}}{100} \right]}{2}$$

where,

$e_a$  = actual vapour pressure, kPa;

$e_{(T_{min})}$  = saturation vapour pressure at daily minimum temperature, kPa, [Eq. 17];

$e_{(T_{max})}$  = saturation vapour pressure at daily maximum temperature, kPa, [Eq. 16];

$RH_{max}$  = maximum relative humidity, %;

$RH_{min}$  = minimum relative humidity, %.

Note I: When using equipment where errors in estimating  $RH_{min}$  can be large, or when  $RH$  data integrity are in doubt, use only  $RH_{max}$  [Eq. 20]:

$$e_a = e_{(T_{min})} \left[ \frac{RH_{max}}{100} \right]$$

In the absence of  $RH_{max}$  and  $RH_{min}$  [Eq.21]:

$$e_a = \frac{RH_{mean}}{100} \left[ \frac{e_{(T_{min})} + e_{(T_{max})}}{2} \right]$$

Note II: For missing or questionable quality of humidity data, the  $e_a$  can be obtained by assuming when the air temperature is close to  $T_{min}$ , the air is nearly saturated with water vapor and the relative humidity is near 100%, in other words, dewpoint temperature ( $T_{dew}$ ) is near the daily minimum temperature ( $T_{min}$ ). If  $T_{min}$  is used to represent  $T_{dew}$  then [Eq. 22]:

$$e_a = e_{(T_{min})} = 0.6108 \exp \left[ \frac{17.27 T_{min}}{T_{min} + 237.3} \right]$$

### Step 12 – The inverse relative distance Earth-Sun ( $d_r$ ) and solar declination ( $\bullet$ )

The inverse relative distance Earth-Sun,  $d_r$ , and the solar declination,  $\bullet$ , are given by equation [Eq. 23]:

$$d_r = 1 + 0.033 \cos \left[ \frac{2\pi}{365} J \right]$$

and [Eq. 24]:

$$\delta = 0.409 \sin \left[ \frac{2\pi}{365} J - 1.39 \right]$$

where,

$J$  = number of the day in the year between 1 (1 January) and 365 or 366 (31 December).

Note: to convert date ( $MM/DD/YYYY$ ) to Julian in Microsoft Excel the following command can be used:

= (( $MM/DD/YYYY$ )-DATE(YEAR(( $MM/DD/YYYY$ )), "01", "01")+1)

### Step 13 – Conversion of latitude ( $\bullet$ ) in degrees to radians

The latitude,  $\bullet$ , expressed in radians is positive for the northern hemisphere and negative for the southern hemisphere (see example below). The conversion from decimal degrees to radians is given by [Eq. 25]:

$$\varphi[\text{Radians}] = \frac{\pi}{180} \varphi[\text{decimal degrees}]$$

e.g.1. to convert  $13^{\circ}44'N$  to decimal degrees  
=  $13+44/60 = 13.73$

e.g.2. to convert  $22^{\circ}54'S$  to decimal degrees  
=  $(-22)+(-54/60) = -22.90$

### Step 14 - Sunset hour angle ( $\bullet_s$ )

The sunset hour angle ( $\bullet_s$ ) is given by [Eq. 26]:

$$\omega_s = \arccos[-\tan(\varphi)\tan(\delta)]$$

where,

- $\bullet$  = latitude expressed in radians, [Eq. 25];
- $\bullet$  = solar declination, [Eq. 24];

### Step 15 – Extraterrestrial radiation ( $R_a$ )

The extraterrestrial radiation,  $R_a$ , for each day of the year and for different latitudes can be estimated from the solar constant, the solar declination and the time of the year by [Eq. 27]:

$$R_a = \frac{24(60)}{\pi} G_{sc} d_r [(\omega_s \sin \varphi \sin \delta) + (\cos \varphi \cos \delta \sin \omega_s)]$$

where,

$R_a$  = extraterrestrial radiation,  $\text{MJ m}^{-2} \text{ day}^{-1}$ ;

$G_{sc}$  = solar constant =  $0.0820 \text{ MJ m}^{-2} \text{ min}^{-1}$ ;

$d_r$  = inverse relative distance Earth-Sun [Eq.23];

$\bullet_s$  = sunset hour angle, rad, [Eq. 26];

$\bullet$  = latitude, rad, [Eq.25];

$\delta$  = solar declination, rad, [Eq. 24].

### Step 16 – Clear sky solar radiation ( $R_{so}$ )

The calculation of the clear-sky radiation is given by [Eq. 28]:

$$R_{so} = (0.75 + 2E10^{-5}z)R_a$$

where,

$z$  = elevation above sea level, m;

$R_a$  = extraterrestrial radiation,  $\text{MJ m}^{-2} \text{ day}^{-1}$ , [Eq.27];

### Step 17 – Net solar or net shortwave radiation ( $R_{ns}$ )

The net shortwave radiation resulting from the balance between incoming and reflected solar radiation is given by [Eq. 29]:



$$R_{ns} = (1 - \alpha)R_s$$

where,

$R_{ns}$  = net solar or shortwave radiation, MJ m<sup>-2</sup> day<sup>-1</sup>;

$\alpha$  = albedo or canopy reflection coefficient, which is 0.23 for the hypothetical grass reference crop, dimensionless;

$R_s$  = the incoming solar radiation, MJ m<sup>-2</sup> day<sup>-1</sup>, [Step 2, Eq.6];

### Step 18 – Net outgoing long wave solar radiation ( $R_{nl}$ )

The rate of longwave energy emission is proportional to the absolute temperature of the surface raised to the fourth power. This relation is expressed quantitatively by the Stefan-Boltzmann law. The net energy flux leaving the earth's surface is, however, less than that emitted and given by the Stefan-Boltzmann law due to the absorption and downward radiation from the sky. Water vapor, clouds, carbon dioxide and dust are absorbers and emitters of longwave radiation. It is thereby assumed that the concentrations of the other absorbers are constant. The net outgoing longwave radiation is given by [Eq. 30]:

$$R_{nl} = \sigma \left[ \frac{(T_{max} + 273.16)^4 + (T_{min} + 273.16)^4}{2} \right] (0.34 - 0.14\sqrt{e_a}) \left[ 1.35 \frac{R_s}{R_{so}} - 0.35 \right]$$

where,

$R_{nl}$  = net outgoing longwave radiation, MJ m<sup>-2</sup> day<sup>-1</sup>,

$\sigma$  = Stefan-Boltzmann constant [4.903 10<sup>-9</sup> MJ K<sup>-4</sup> m<sup>-2</sup> day<sup>-1</sup>],

$T_{max}$  = K maximum absolute temperature during the 24-hour period [K = °C + 273.16],

$T_{min}$  = K minimum absolute temperature during the 24-hour period [K = °C + 273.16],

$e_a$  = actual vapor pressure, kPa,

$R_s$  = the incoming solar radiation, MJ m<sup>-2</sup> day<sup>-1</sup>, [Step 2, Eq.6];

$R_{so}$  = clear sky solar radiation, MJ m<sup>-2</sup> day<sup>-1</sup>, [Step 16, Eq.28];

### Step 19 – Net radiation ( $R_n$ )

The net radiation ( $R_n$ ) is the difference between the incoming net shortwave radiation ( $R_{ns}$ ) and the outgoing net longwave radiation ( $R_{nl}$ ), [Eq. 31]:

$$R_n = R_{ns} - R_{nl}$$

where,

$R_{ns}$  = net solar or shortwave radiation, MJ m<sup>-2</sup> day<sup>-1</sup>, [Step 17, Eq. 29];

$R_{nl}$  = net outgoing longwave radiation, MJ m<sup>-2</sup> day<sup>-1</sup>, [Step 18, Eq. 30].

To express the net radiation ( $R_n$ ) in equivalent of evaporation (mm) ( $R_{ng}$ ), [Eq. 32]:

$$R_{ng} = 0.408 \times R_n$$

where,

$R_n$  = net radiation, MJ m<sup>-2</sup> day<sup>-1</sup>, [Eq. 31];

### Final Step – Overall $ET_o$ equation

#### FS1. Radiation term ( $ET_{rad}$ )

Radiation term is given by [Eq. 33]:

$$ET_{rad} = DT \times R_{ng}$$

where,

$ET_{rad}$  = radiation term, mm d<sup>-1</sup>;

$DT$  = Delta term, [Step 7, Eq. 12];

$R_{ng}$  = net radiation, mm, [Eq. 32]

### FS2. Wind term ( $ET_{wind}$ )

Wind term is given by [Eq. 34]:

$$ET_{wind} = PT \times TT(e_s - e_a)$$

where,

$ET_{wind}$  = wind term, mm d<sup>-1</sup>;

$PT$  = Psi term, [Step 8, Eq. 13];

$TT$  = Temperature term, [Step 9, Eq. 14];

$e_a$  = actual vapor pressure, kPa, [Step 11, Eq. 19];

$e_s$  = mean saturation vapor pressure derived from air temperature, kPa, [Step 10, Eq. 15];

### Final Reference Evapotranspiration Value ( $ET_o$ )

The final reference evapotranspiration value is the sum of wind and radiation terms,  $ET_o$  is given by [Eq. 35]:

$$ET_o = ET_{wind} + ET_{rad}$$

where,

$ET_o$  = reference evapotranspiration, mm d<sup>-1</sup>;

$ET_{wind}$  = wind term, mm d<sup>-1</sup>;

$ET_{rad}$  = radiation term, mm d<sup>-1</sup>;

## Summary

The step by step process of reference evapotranspiration calculation was given in this document. Values of evapotranspiration are largely determined by climatic conditions which are available in the FAWN system (<http://fawn.ifas.ufl.edu/>). The Penman-Monteith  $ET$  estimation detailed has been shown to be the most accurate for Florida conditions, and it can be applied on a daily basis for better irrigation management or other water resources applications.

## Useful conversions

1 mm	=	0.003937 in
1 mm d <sup>-1</sup>	=	2.45 MJ m <sup>-2</sup> d <sup>-1</sup>
1 J cm <sup>-2</sup> d <sup>-1</sup>	=	0.01 MJ m <sup>-2</sup> d <sup>-1</sup>
1 calorie	=	4.1868 J
1 cal cm <sup>-2</sup> d <sup>-1</sup>	=	4.1868 * 10 <sup>-2</sup> MJ
m <sup>-2</sup> d <sup>-1</sup> 1 W	=	1 J s <sup>-1</sup>
1 W m <sup>-2</sup>	=	0.0864 MJ m <sup>-2</sup>
°C	=	(°F - 32) 5/9
Kelvin (°K)	=	(°C) + 273.16
1 millibar (mbar)	=	0.1 kPa
1 bar	=	100 kPa
1 cm of water	=	0.09807 kPa
1 mm of mercury (mmHg)	=	0.1333 kPa
1 atmosphere (atm)	=	101.325 kPa
1 lb/in <sup>-2</sup> (psi)	=	6.896 kPa
1 kilometer day <sup>-1</sup> (km d <sup>-1</sup> )	=	0.01157 m s <sup>-1</sup>
1 ft s <sup>-1</sup>	=	0.3048 m s <sup>-1</sup>

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