#### Recreation

What is the sum of the coefficients of

$$(1 - 3x + 3x^2)^{743}(1 + 3x - 3x^2)^{744}$$

after expanding and collecting terms?

### CS61B Lecture #6: Arrays

- An array is a structured container whose components are
  - length, a fixed integer.
  - a sequence of length simple containers of the same type, numbered from 0.
  - (.length field usually implicit in diagrams.)
- Arrays are anonymous, like other structured containers.
- Always referred to with pointers.
- For array pointed to by A,
  - Length is A.length
  - Numbered component i is A[i] (i is the index)
  - Important feature: index can be any integer expression.

## A Few Samples

Java

#### Results

```
int[] x, y, z;
                                                                3
                                     x:
String[] a;
                                     y:
x = new int[3];
y = x;
                                     z:
a = new String[3];
                                     a:
x[1] = 2;
y[1] = 3;
a[1] = "Hello";
                                                             Hello
int[] q;
q = new int[] { 1, 2, 3 };
                                     q:
                                                                     3
                                                                2
// Short form for declarations:
int[] r = { 7, 8, 9 };
                                                                     9
                                     r:
```

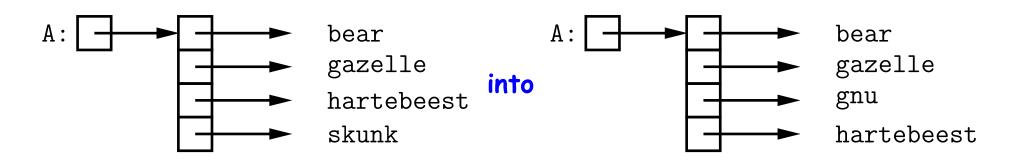
### Example: Accumulate Values

**Problem:** Sum up the elements of array A.

```
static int sum(int[] A) {
  int N;
                                                   // New (1.5) syntax
  N = 0;
  for (int i = 0; i < A.length; i += 1)
                                                    for (int x : A)
    N += A[i];
                                                       \mathbb{N} += x;
  return N;
// For the hard-core: could have written
int N, i;
for (i=0, N=0; i<A.length; N += A[i], i += 1)</pre>
  { } // or just ;
// But please don't: it's obscure.
```

## Example: Insert into an Array

**Problem:** Want a call like insert(A, 2, "gnu") to convert (destructively)



### (Aside) Java Shortcut

• Useful tip: Can write just 'arraycopy' by including at the top of the source file:

```
import static java.lang.System.arraycopy;
```

- This means "define the simple name arraycopy to be the equivalent of java.lang.System.arraycopy in the current source file."
- Can do the same for out so that you can write

```
out.println(...);
in place of
System.out.println(...);
```

• Finally, a declaration like

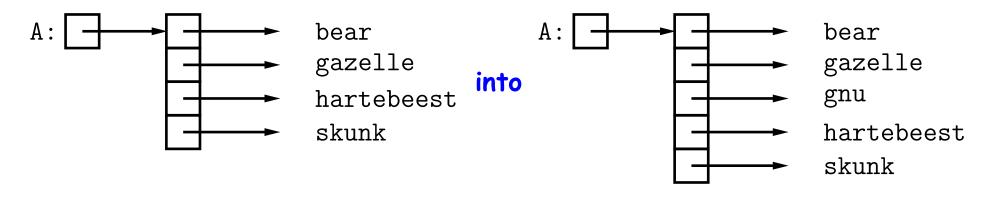
```
import static java.lang.Math.*;
```

means "take all the (public) static definitions in java.lang.Math and make them available in this source file by their simple names (the name after the last dot)."

Useful for functions like sin, sqrt, etc.

### Growing an Array

**Problem:** Suppose that we want to change the description above, so that A = insert2 (A, 2, "gnu") does not shove "skunk" off the end, but instead "grows" the array.

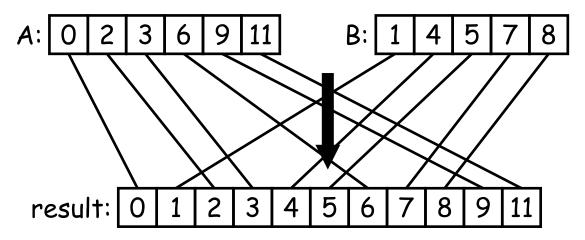


```
/** Return array, r, where r.length = ARR.length+1; r[0..K-1]
  * the same as ARR[0..K-1], r[k] = x, r[K+1..] same as ARR[K..]. */
static String[] insert2(String[] arr, int k, String x) {
  String[] result = new String[arr.length + 1];
  arraycopy(arr, 0, result, 0, k);
  arraycopy(arr, k, result, k+1, arr.length-k);
  result[k] = x;
  return result;
}
```

Why do we need a different return type from insert2??

# Example: Merging

**Problem:** Given two sorted arrays of ints, A and B, produce their merge: a sorted array containing all items from A and B.



### Example: Merging Program

**Problem:** Given two sorted arrays of ints, A and B, produce their merge: a sorted array containing all from A and B.

**Remark:** In order to solve this recursively, it is useful to *generalize* the original function to allow merging *portions* of the arrays.

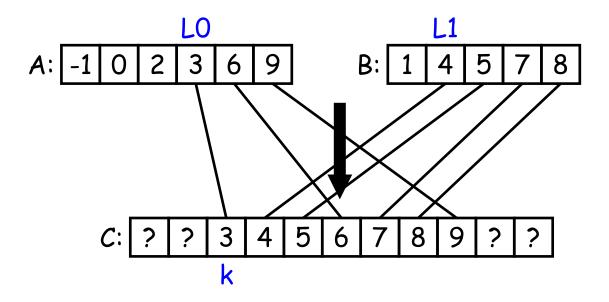
```
/** Assuming A and B are sorted, returns their merge. */
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, 0, B, 0);
/** The merge of A[LO..] and B[L1..] assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1) {
   int N = A.length - LO + B.length - L1; int[] C = new int[N];
   if (L0 >= A.length) arraycopy(B, L1, C, 0, N);
                                                           What is wrong with
   else if (L1 >= B.length) arraycopy(A, L0, C, 0, N);
                                                           this implementation?
   else if (A[L0] <= B[L1]) {</pre>
      C[0] = A[L0]; arraycopy(mergeTo(A, L0+1, B, L1), 0, C, 1, N-1);
   } else {
      C[0] = B[L1]; arraycopy(mergeTo(A, L0, B, L1+1), 0, C, 1, N-1);
   return C;
```

### A Tail-Recursive Strategy

```
public static int[] merge(int[] A, int[] B) {
    return mergeTo(A, 0, B, 0, new int[A.length+B.length], 0);
}

/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int L0, int[] B, int L1, int[] C, int k){
    ...
}
```

This last method merges part of A with part of B into part of C. For example, consider a possible call mergeTo(A, 3, B, 1, C, 2)



```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (??) {
     return C;
   } else if (??) {
     C[k] = A[LO];
      return mergeTo(A, ??, B, ??, C, ??)
   } else {
      C[k] = B[L1];
     return mergeTo(A, ??, B, ??, C, ??)
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (L0 \ge A.length \&\& L1 \ge B.length) {
      return C;
   } else if (??) {
     C[k] = A[LO];
      return mergeTo(A, ??, B, ??, C, ??)
   } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (L0 \ge A.length \&\& L1 \ge B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {</pre>
      C[k] = A[LO]:
      return mergeTo(A, ??, B, ??, C, ??)
  } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (L0 \ge A.length \&\& L1 \ge B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {</pre>
      C[k] = A[LO]:
      return mergeTo(A, L0 + 1, B, L1, C, k + 1);
   } else {
      C[k] = B[L1];
      return mergeTo(A, ??, B, ??, C, ??)
```

```
public static int[] merge(int[] A, int[] B) {
   return mergeTo(A, O, B, O, new int[A.length+B.length], O);
/** Merge A[LO..] and B[L1..] into C[K..], assuming A and B sorted. */
static int[] mergeTo(int[] A, int LO, int[] B, int L1, int[] C, int k){
   if (L0 \ge A.length \&\& L1 \ge B.length) {
      return C;
   } else if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {</pre>
      C[k] = A[LO]:
      return mergeTo(A, L0 + 1, B, L1, C, k + 1);
   } else {
      C[k] = B[L1];
      return mergeTo(A, LO, B, L1 + 1, C, k + 1);
```

#### Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int LO, L1, k;
   L0 = L1 = k = 0:
   while (??) {
       if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
           C[k] = A[LO];
           ??
       } else {
           C[k] = B[L1];
           ??
   return C;
```

#### Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, O, B, O, C, O)
   int LO, L1, k;
   L0 = L1 = k = 0;
   while (LO < A.length | L1 < B.length) {
       if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
           C[k] = A[LO];
           ??
       } else {
           C[k] = B[L1];
           ??
  return C;
```

#### Iterative Solution

In general, we don't use either of the previous approaches in languages like C and Java. Array manipulation is most often iterative:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   // mergeTo(A, 0, B, 0, C, 0)
   int LO, L1, k;
   L0 = L1 = k = 0;
   while (LO < A.length | L1 < B.length) {
       if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
           C[k] = A[LO];
           L0 += 1; k += 1;
       } else {
          C[k] = B[L1];
          L1 += 1; k += 1;
   return C;
```

#### Iterative Solution II

#### The same, with a for loop:

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int LO, L1;
   LO = L1 = 0;
   for (int k = 0; k < C.length; k += 1) {
      if (L1 >= B.length || (L0 < A.length && A[L0] <= B[L1])) {
         C[k] = A[L0]; L0 += 1;
      } else {
         C[k] = B[L1]; L1 += 1;
      }
   }
   return C;
}</pre>
```

### Alternative Solution: Removing k

Claim: An invariant of the loop is that k=L0+L1.

```
public static int[] merge(int[] A, int[] B) {
   int[] C = new int[A.length + B.length];
   int LO, L1;
   LO = L1 = 0;
   while (L0 + L1 < C.length) {
      if (L1 >= B.length || (L0 < A.length && A[L0] < B[L1])) {
         C[L0 + L1] = A[L0]; L0 += 1;
      } else {
         C[L0 + L1] = B[L1]; L1 += 1;
      }
   }
   return C;
}</pre>
```

# Multidimensional Arrays

What about two- or higher-dimensional layouts, such as

# Multidimensional Arrays in Java

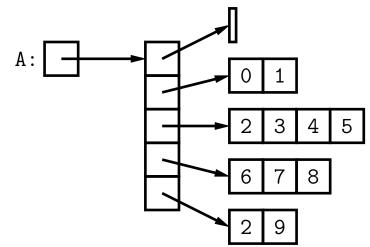
These are not primitive in Java, but we can build them as arrays of arrays:

```
int[][] A = new int[3][]:
  A[0] = new int[] \{2, 3, 4, 5\};
  A[1] = new int[] \{4, 9, 16, 25\};
  A[2] = new int[] \{8, 27, 64, 125\};
// or
  int[][] A;
  A = \text{new int}[][] \{ \{2, 3, 4, 5\}, \}
                     {4, 9, 16, 25},
                     { 8, 27, 64, 125} };
                                                                       16 25
// or
  int[][] A = { {2, 3, 4, 5},}
                {4, 9, 16, 25},
                 {8, 27, 64, 125} };
// or
  int[][] A = new A[3][4];
  for (int i = 0; i < 3; i += 1)
      for (int j = 0; j < 4; j += 1)
          A[i][j] = (int) Math.pow(j + 2, i + 1);
```

## Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single "width" in general:

```
int[][] A = new int[5][]:
A[0] = new int[] \{\};
A[1] = new int[] \{0, 1\};
A[2] = new int[] \{2, 3, 4, 5\};
A[3] = \text{new int}[] \{6, 7, 8\};
A[4] = new int[] \{9\};
```



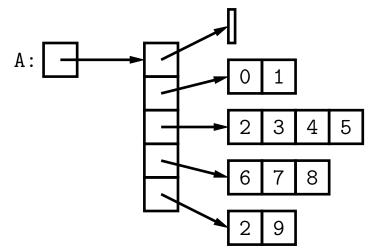
What does this print?

```
int[][] ZERO = new int[3][];
ZERO[0] = ZERO[1] = ZERO[2] =
    new int[] {0, 0, 0};
ZERO[0][1] = 1;
System.out.println(ZERO[2][1]);
```

### Exotic Multidimensional Arrays

• Since every element of an array is independent, there is no single "width" in general:

```
int[][] A = new int[5][]:
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A[3] = \text{new int}[] \{6, 7, 8\};
A[4] = new int[] \{9\};
```



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