

Course ID: CS 501

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Description:

http://npu85.npu.edu/~henry/npu/classes/algorithm/geeksforgeeks/slide/exercise_geeksforgeeks.html

Q4 ==> Prove that the Big-O of the following loop is $O(N)$

Q5 ==> Find the Big-O of the following loops

4. Prove that the Big-O of the following loop is $O(N)$

```
for (int i = 1; i <= n; i += c) {  
    // some  $O(1)$  expressions  
}
```

Answer: $O = n / c * O(1) = 1 / c * n * O(1) = n * O(1) = O(n)$;

5. Find the Big-O of the following loops

```
// c is constant  
for (int i = 1; i <= n; i += c) {  
    for (int j = 1; j <= n; j = pow(i, c)) {  
        // some  $O(1)$  expressions  
    }  
}  
  
for (int i = n; i > 0; i += c) {  
    for (int j = i+1; j <= n; j *= c) {  
        // some  $O(1)$  expressions  
    }  
}
```

Answer:

Part 1: $O = O(n) * O(\log \log n) = n O(\log \log n)$;

Part 2: $O = O(n) * O(\log n) = n O(\log n)$;

$O = n O(\log \log n) + n O(\log n) = n O(\log n)$;