

Introduction 簡介

Does not cover microcontroller 不包含微控制器

Demo 展示

Body design Physics 機構設計原理

Sensor & Alignment 感測器與電腦鼠姿態和位置的校正

PID control 比例-積分-微分控制

Speed Profile 速度命令曲線

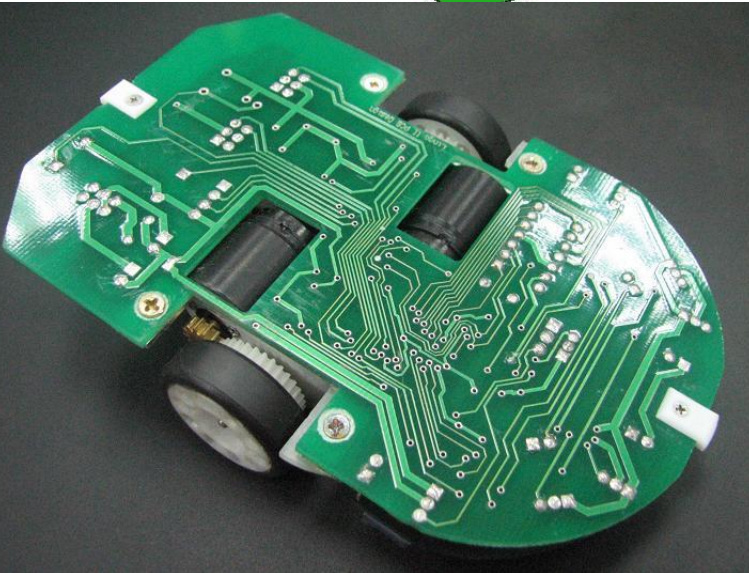
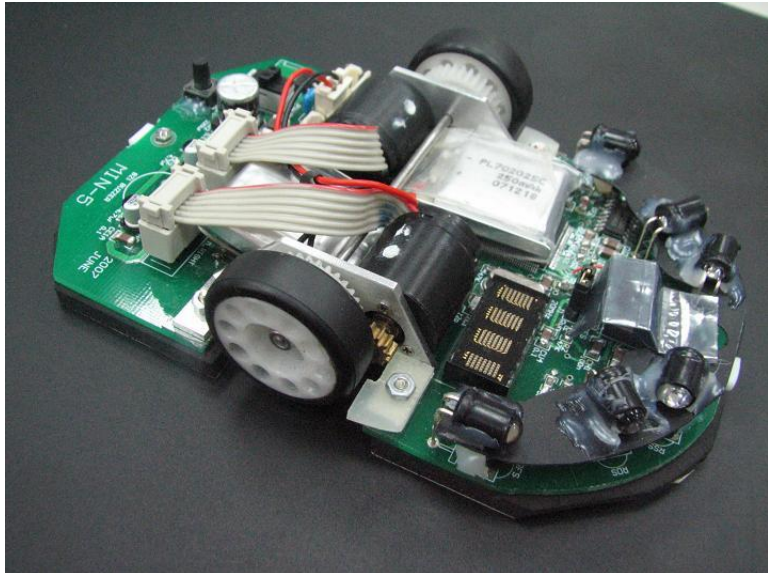
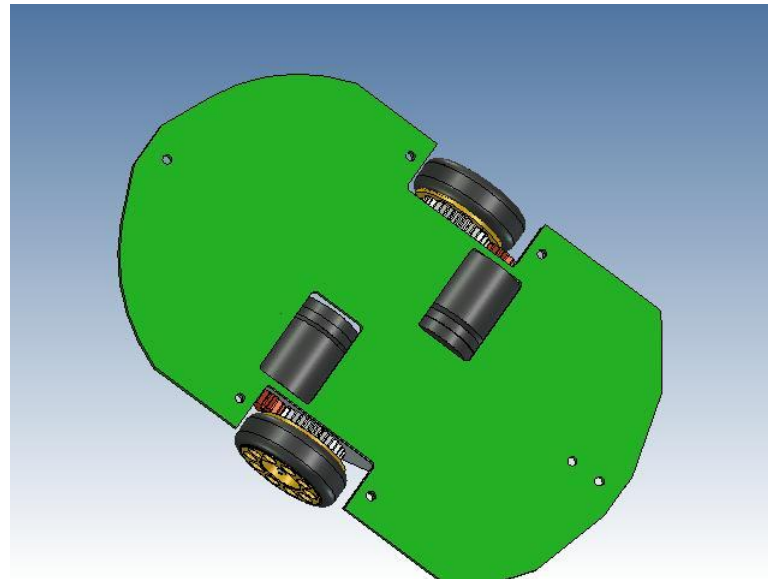
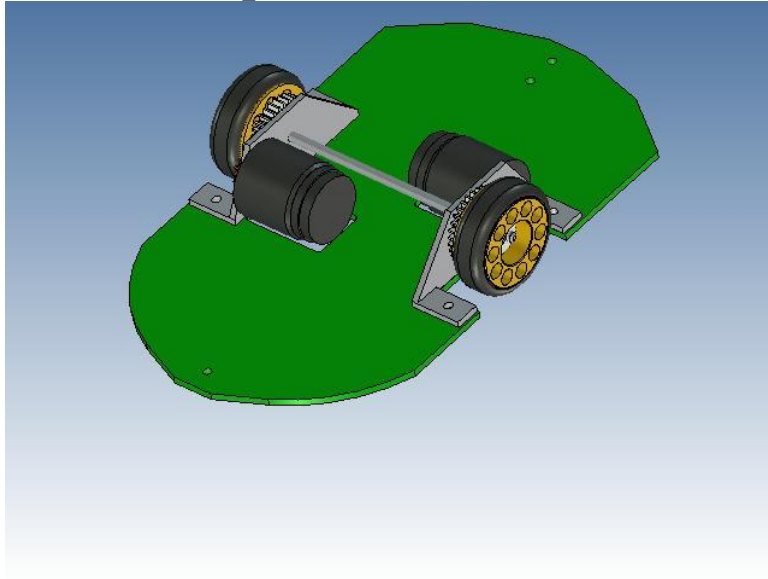
DC Motor sizing 直流馬達的選擇

DC Motor driver 直流馬達驅動電路

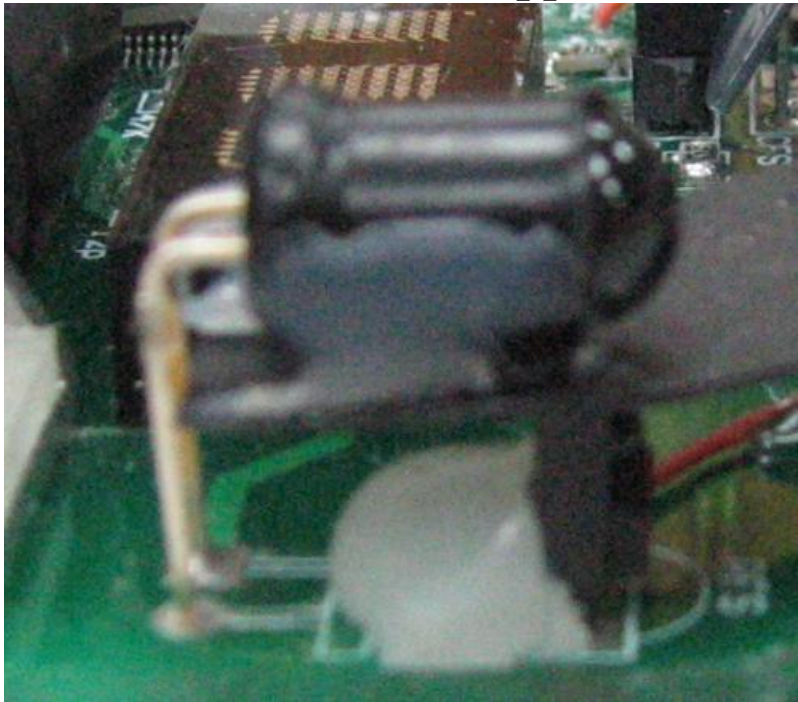
Battery 電池

~~Search Algorithm??? 迷宮搜尋演算法則~~

Photo of top and bottom of Min5



- Minimum 最低 mechanical 機械 design 設計& construction 建造
- PCB 電路板 used as robot body (玻璃纖維)
- PCB is tough 堅韌 and strong
- Good soldering 焊接 to withstand crash 撞擊
- Sensors must be well supported (hot glue 熱膠)

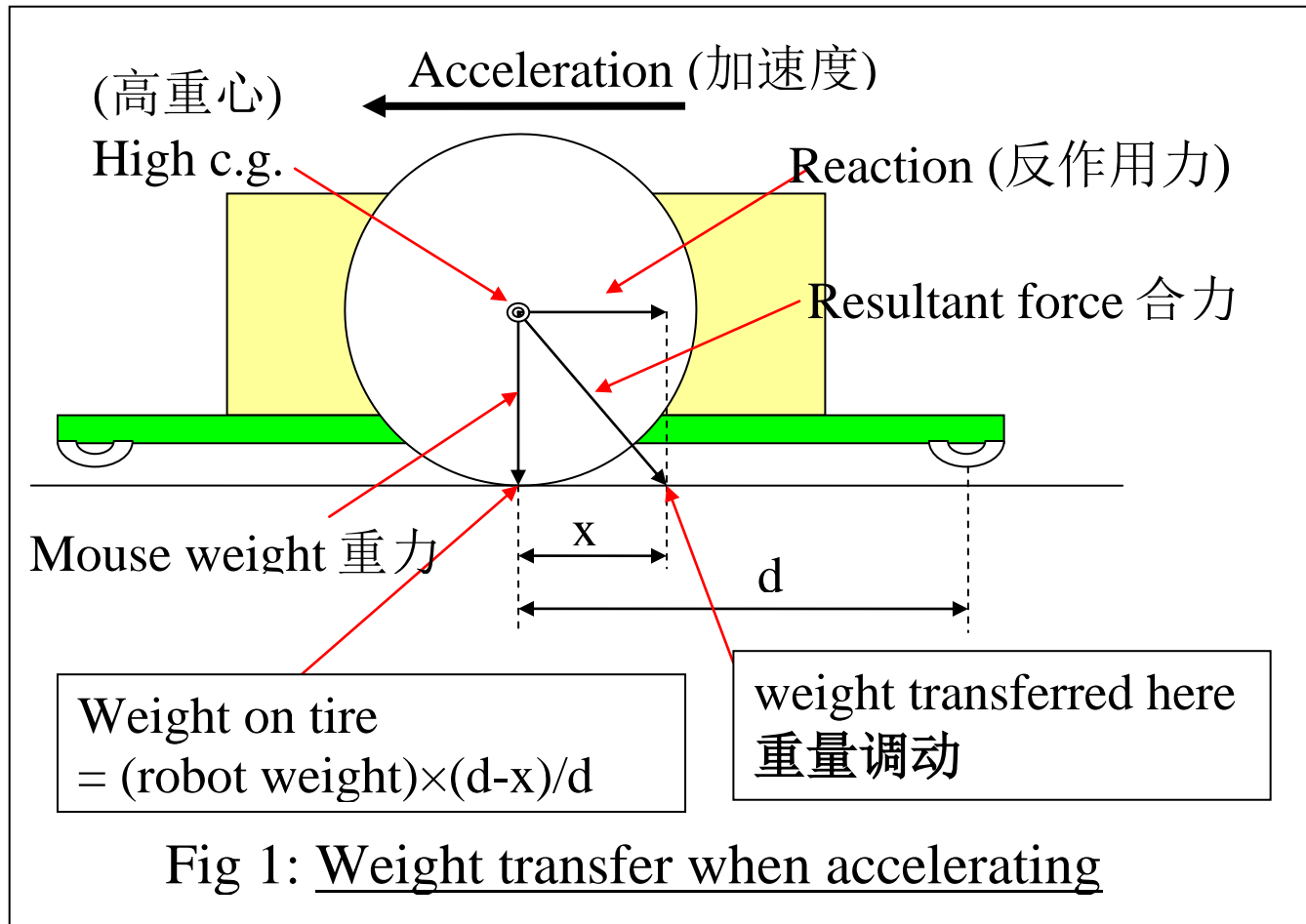


# DEMO

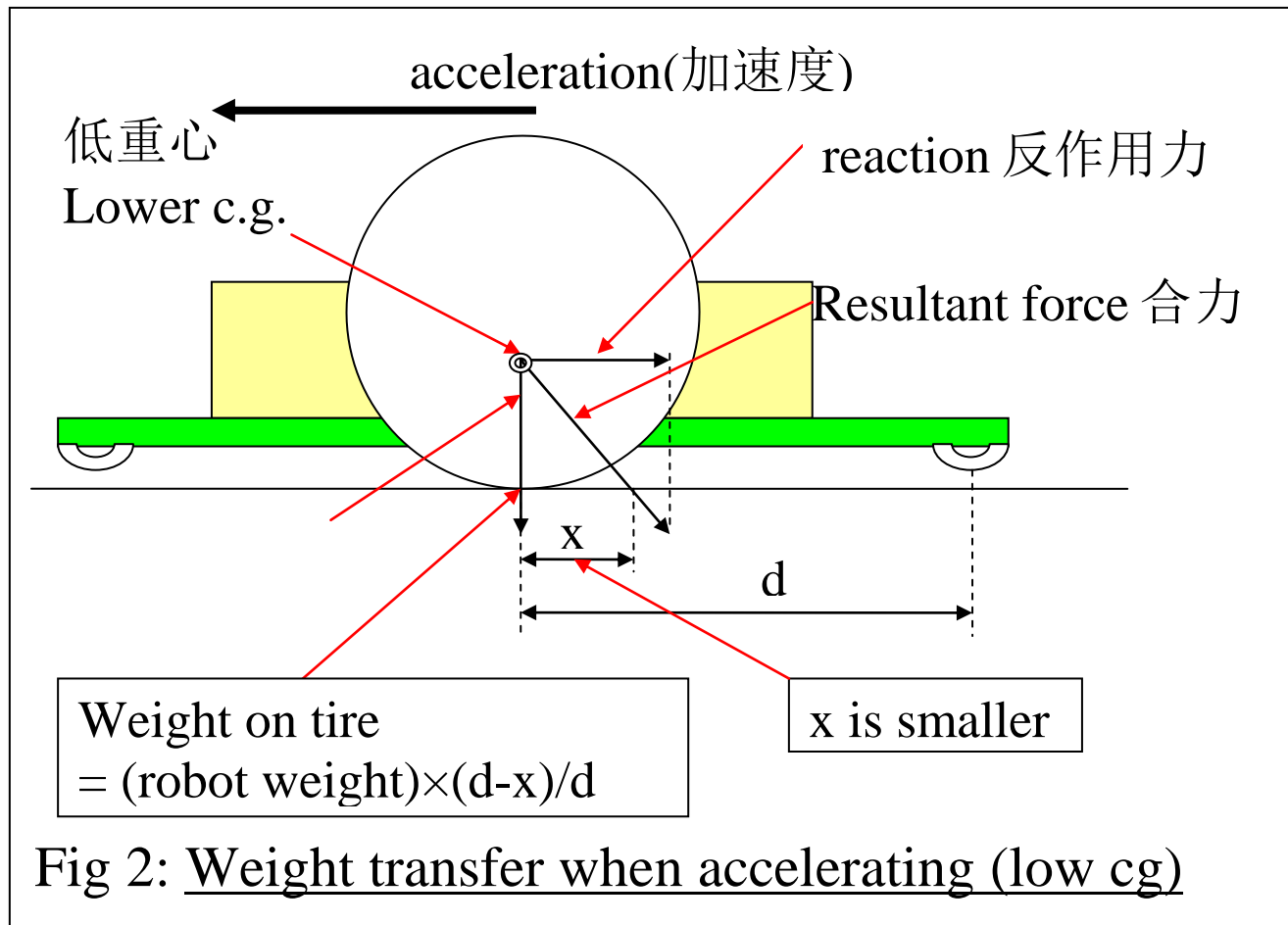
# 1.0 Body Design Physics (物理)(機構設計原理)

- Centre of gravity 重心& weight transfer 重量调动
- Moment of inertia (转动惯量)
- Robot weight (重量) – heavier or lighter?
- Robot wheel (輪子) – bigger or smaller?

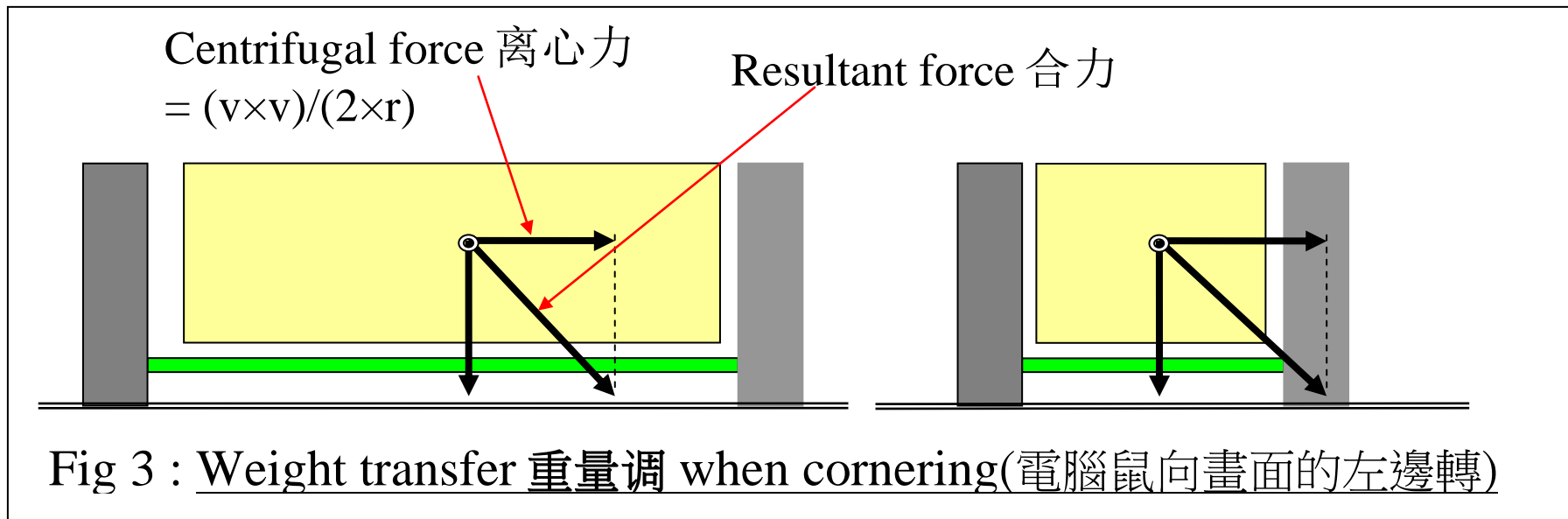
## 1.1 Centre of gravity & weight transfer (重心&重量轉移)



- When Robot is not accelerating/decelerating, all weight is on tires
- If there is no weight on tires -> no grip



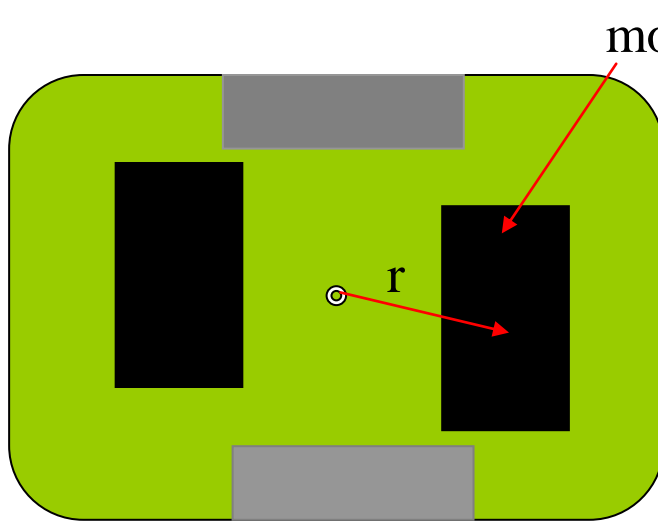
- Lighter or slimmer motors to lower c.g.
- More weight on tires, hence more grip for acceleration
- Resultant force acts through c.g.



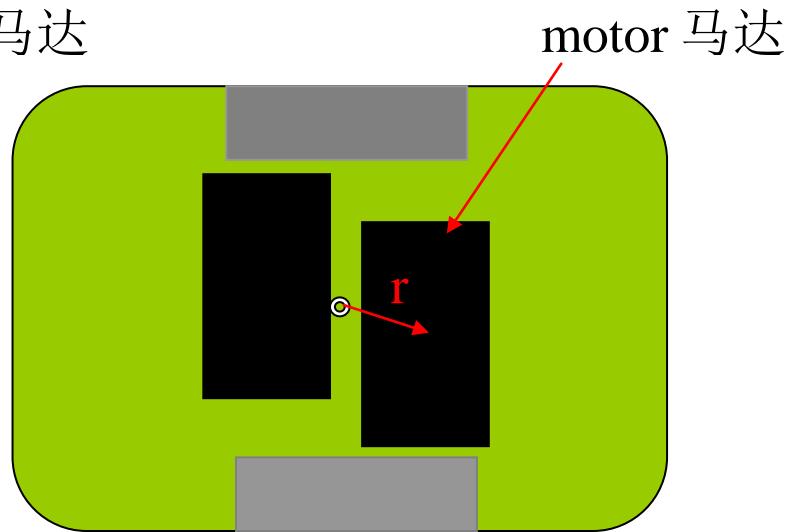
- Stepper motor 步進馬達 based micromouse has high c.g.
- Has a higher tendency to roll over 翻轉 if cornering at high speed.  
 由於離心力與轉彎速度的平方成正比，倘使迴轉半徑沒有改變的情況下，容易因上圖”車重轉移(重力與離心力的合力)”效應的影響而翻車。
- Always keep the robot c.g. as low as possible  
 電腦鼠的重心設計，越低越好。
- Make robot as wide 宽 as possible (愈寬愈不會翻車)
- Make your robot like F1 car



## 1.2 Moment of inertia (转动惯量)



High moment of inertia



Low moment of inertia

$$I = m \times r^2$$

m = motor weight

- When moment of inertia is high, rotational acceleration (旋转的加速度) is reduced for the same torque 扭矩.

$$\text{Torque} = I \times \alpha \quad (F = m \times a)$$

當轉動慣量大時，由於馬達的出力固定，因此在不考慮阻力 而且轉動慣量×旋轉加速度(角加速度) = 馬達輸出力矩 的情形下，電腦鼠的旋轉加速度(角加速度)會降低，轉彎因此會花更多的時間。

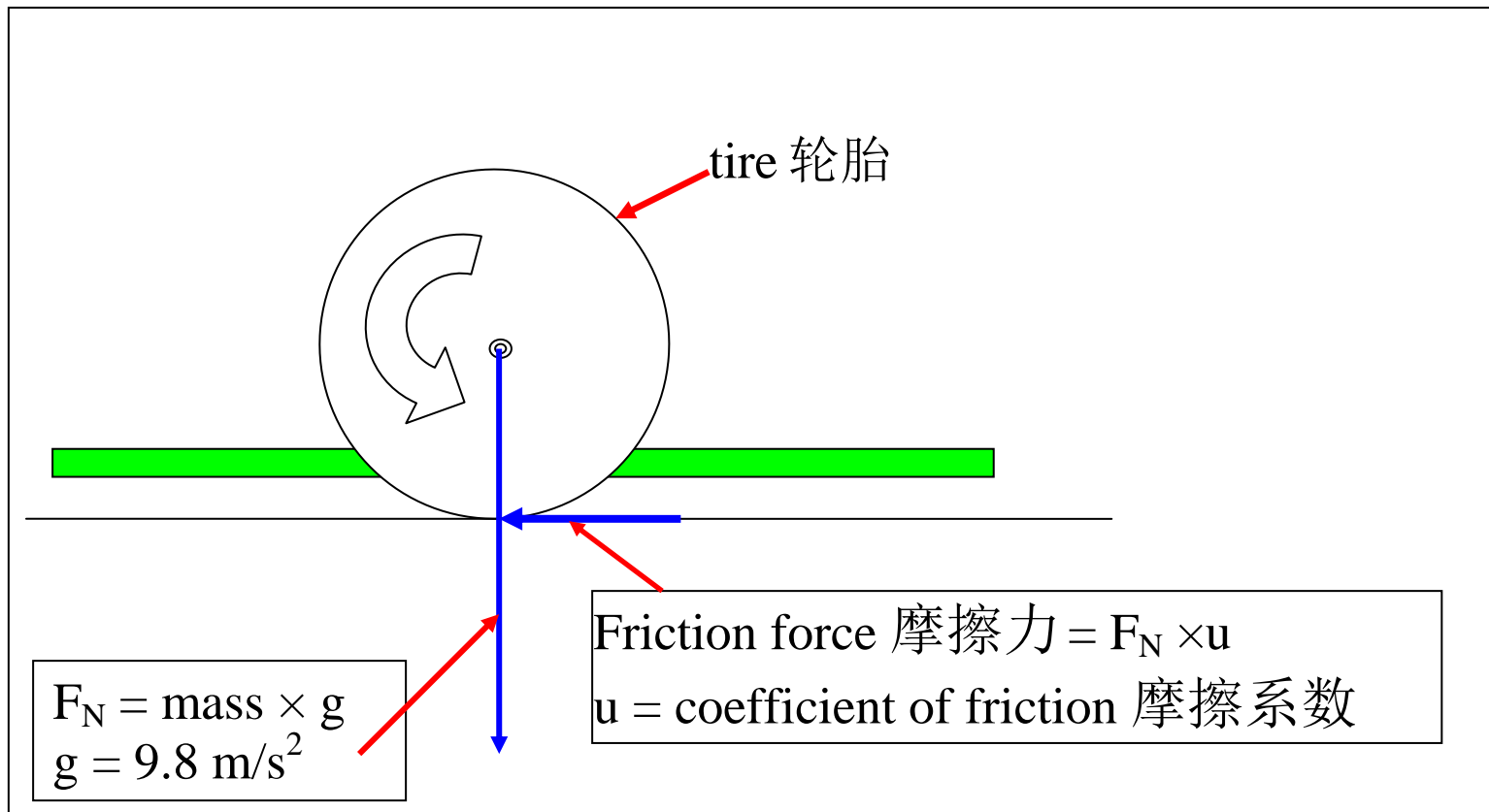
- Keep heavy parts like motors, battery etc as close to robot centre as possible  
因此電腦鼠上較重的元件(如馬達、電池等)，愈靠近旋轉中心(重心)擺放愈好。
- If moment of inertia is high, stronger motor is required, -> bigger battery too!

## 1.3 Robot weight (重量)

Question : Does a heavier mouse provides more acceleration (has more grip 抓地力)?

Question: 重量較重的電腦鼠可以提供較大的加速度嗎(提供較大的抓地力)?

$$\text{Force (Newton)} = \text{mass(kg)} \times \text{acceleration(m/s}^2\text{)}$$



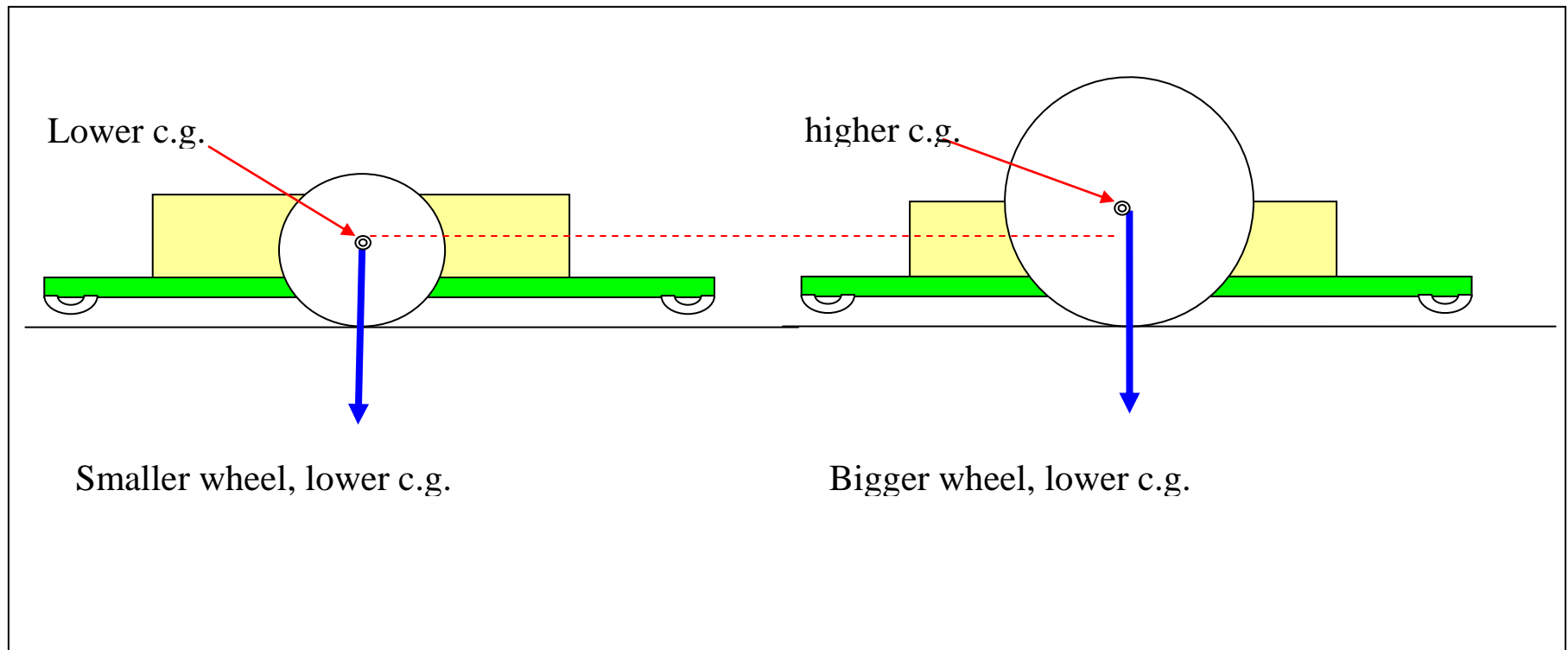
- Force available to propel the robot forward depends on motor power 功率 and friction force 摩擦力.
- If motor is powerful enough, then friction is the limiting factor (限制因素) 如果馬達夠力的話，地面的摩擦力便是主要的限制因素。

- If motor exerts a force greater than friction force, tires will skid (滑行).
- To prevent skidding, driving force < friction force  
 為了避免滑動，馬達出力必須小於地面所能提供的摩擦力
  - Friction  $= F_N \times u$   
 $= \text{mass} \times g \times u$
  - Therefore acceleration limit  $= g \times u$   
 因此加速度的限制就是 重力加速度×摩擦係數
  - If  $u=0.7$ , then acceleration limit is about  $7\text{m/s}^2$ .  
 假如摩擦係數  $u = 0.7$ ，那麼電腦鼠加速度的上限就是  $7\text{m/s}^2$ 。
- Acceleration is independent of mass. Limited by tires.  
 電腦鼠加速度的上限與重量無關
- Keep robot weight low -> reduce motor size -> reduce battery capacity.

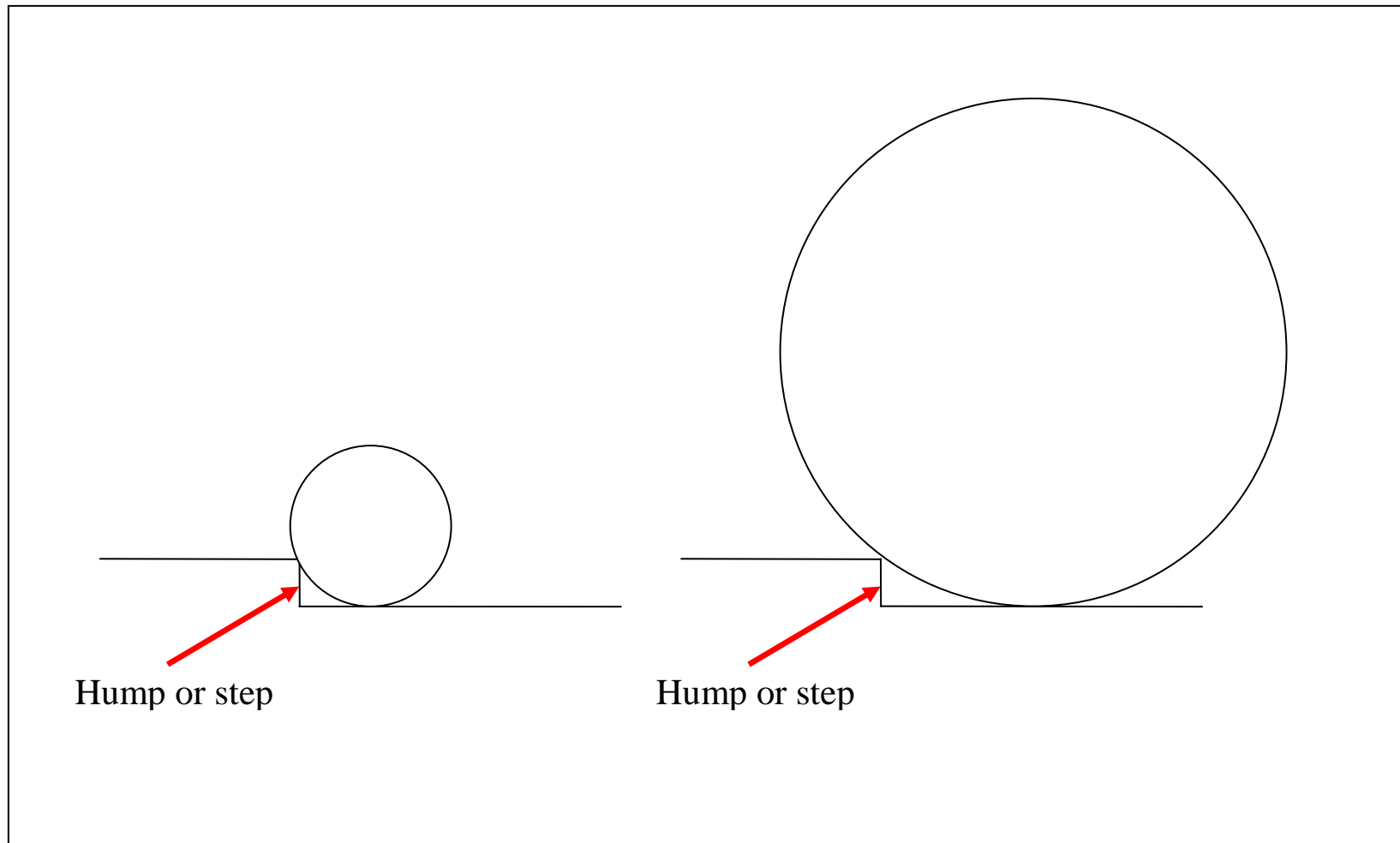
## 1.4 Robot wheel

Question : A bigger wheel or a smaller wheel?

- Tire friction is reduced by dirt (灰塵)
- Clean tires before run
- A smaller wheel would need to rotate more times for the same distance
  - Pick up more dirt(容易積聚較多的灰塵)
  - If maze is dirty, performance will be affected
- Bigger wheels raise the c.g. (大車輪會提高電腦鼠的重心)

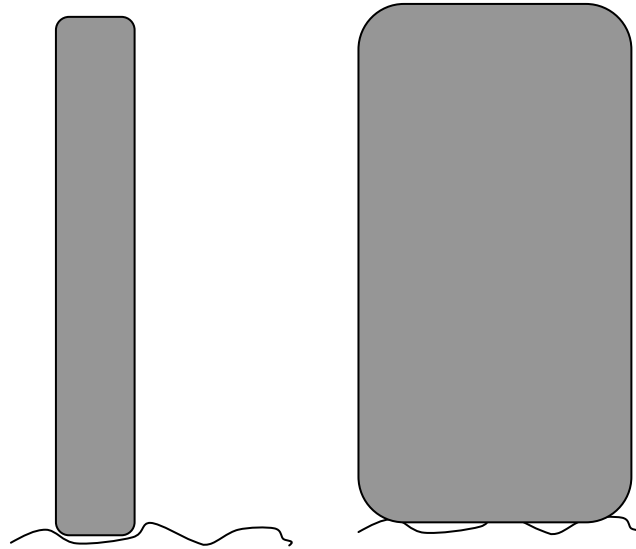


- Weight of wheels and shaft 軸 affect the robot's c.g.
- Keep wheels & shaft as light as possible
- Use light and thin material if possible



- Big wheel will roll easily over steps or humps(大車輪比起小車輪更容易越過地面的突起處)

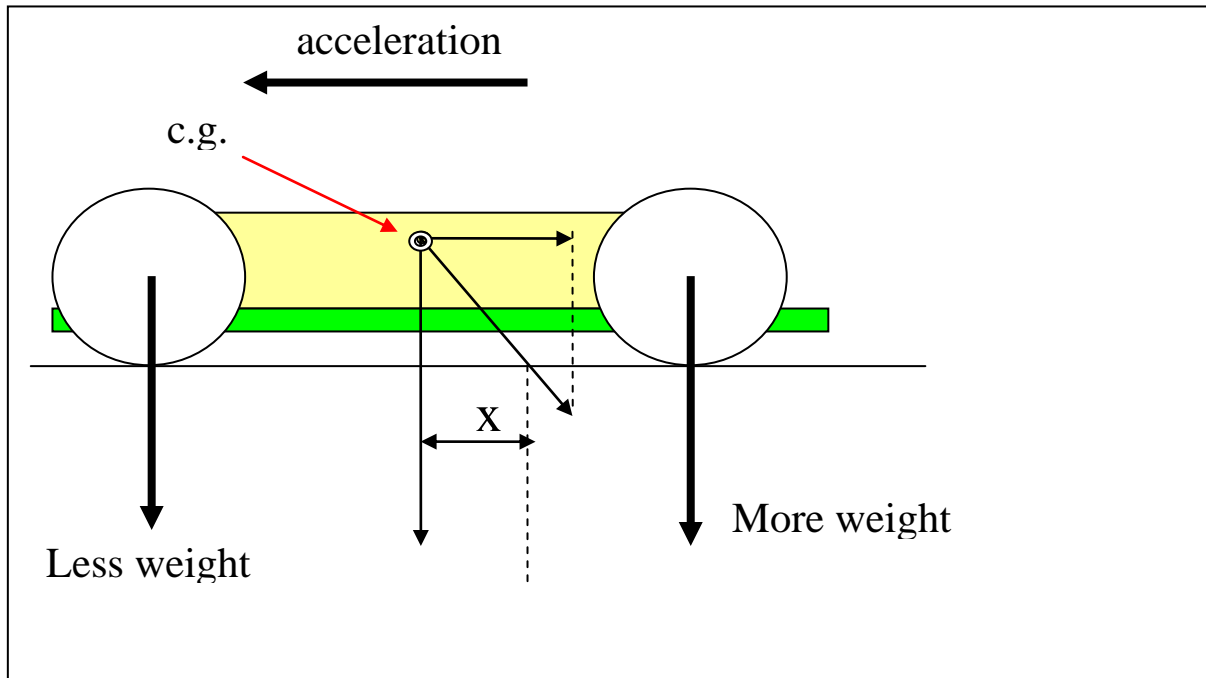




A bigger surface allows the wheel to ride over unevenness

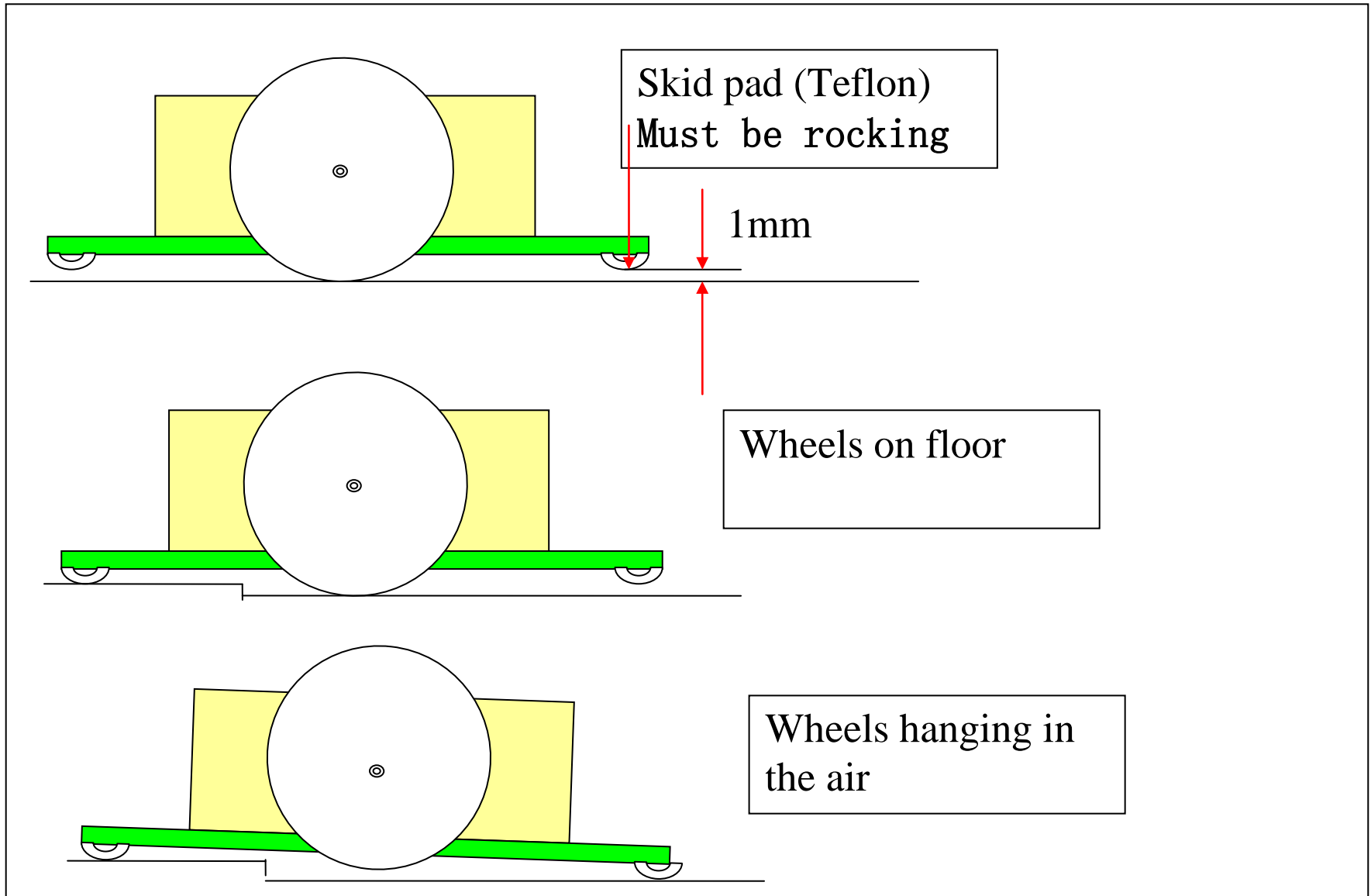
- Wider wheel will also be less affected by unevenness. (寬車輪比起窄車輪較不受地面不平的影響)
- On a flat and clean surface, tire diameter and width has negligible impact on performance. (但在平坦而乾淨的地面上，車輪的寬度與大小對性能的影響很小)
- Too wide and it's hard to turn

## 1.5 Four wheel drive ?

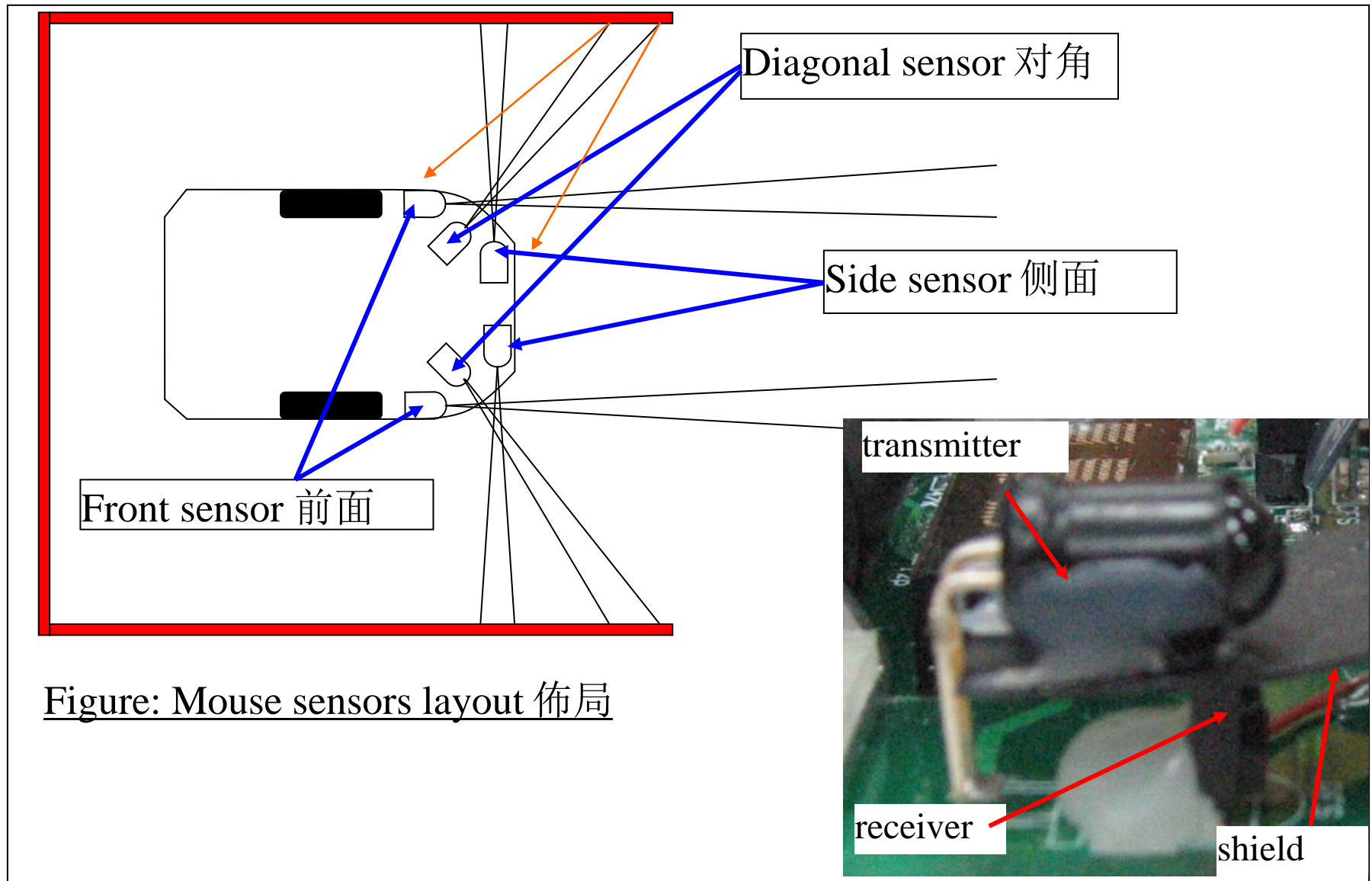


- During acceleration, weight is transferred to back wheels (加速時，重量移轉至後輪)
- During deceleration, weight is transferred to front wheels
- Good for straight acceleration/deceleration (對直線加減速不錯)
- Complex and hard to build (但複雜而不好做)
- My dream mouse !!!

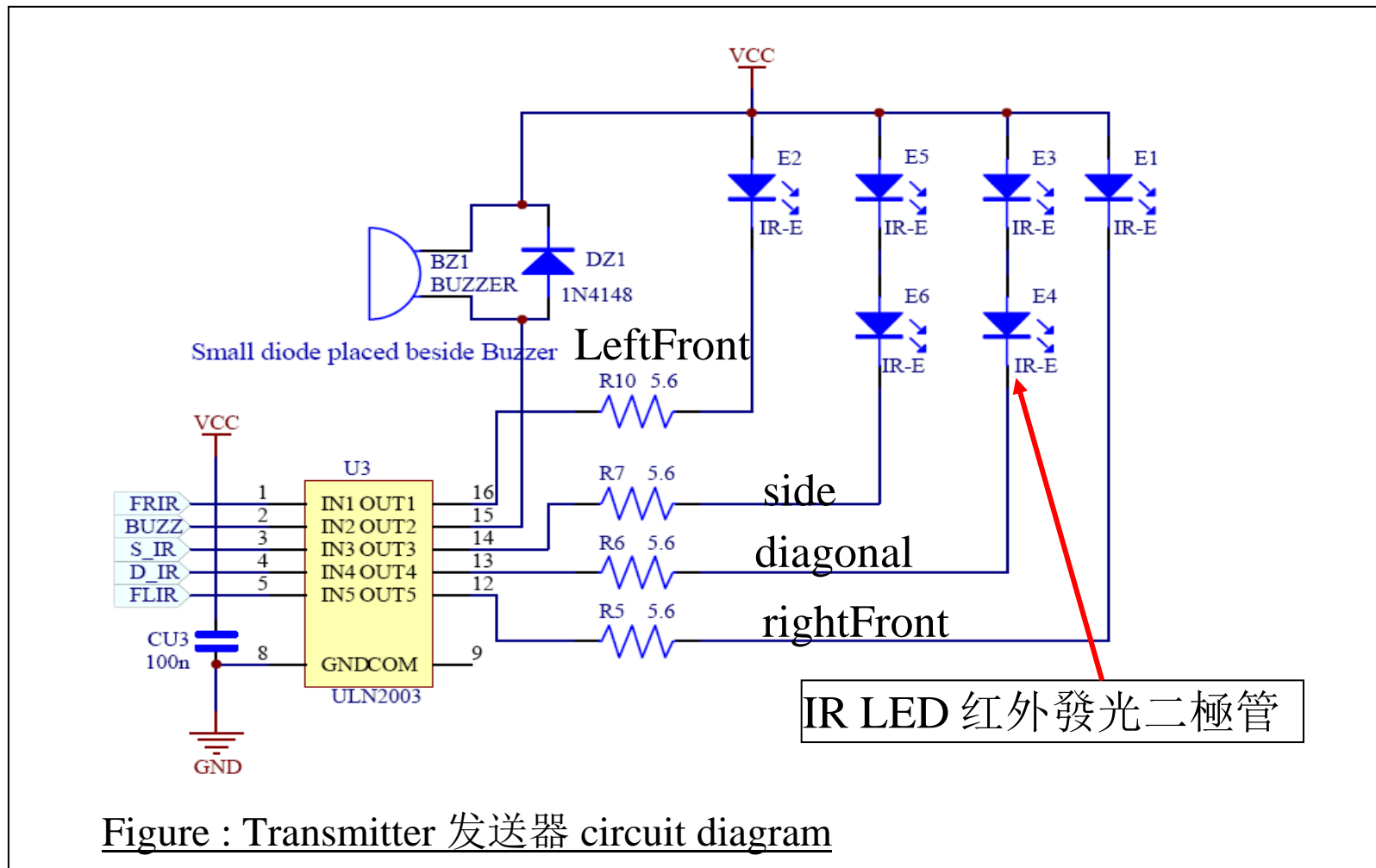
## 1.6 Skid Pads



## 2.0 Sensors 感測器 & Alignment 位置的校正



## 2.1 Sensor circuit and operation



- Left and right front sensors pulsed separately to avoid interference 干擾

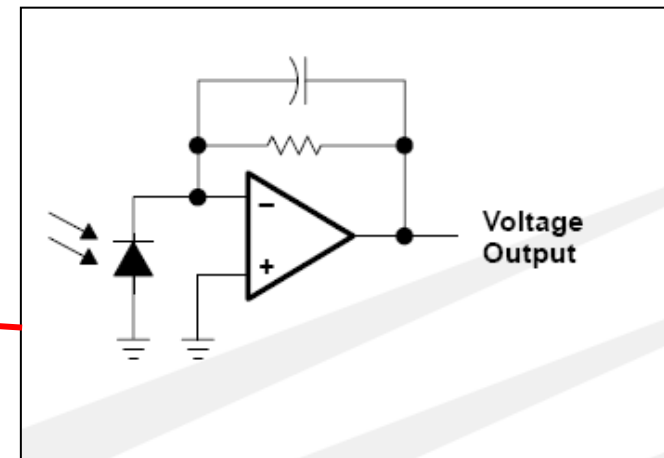
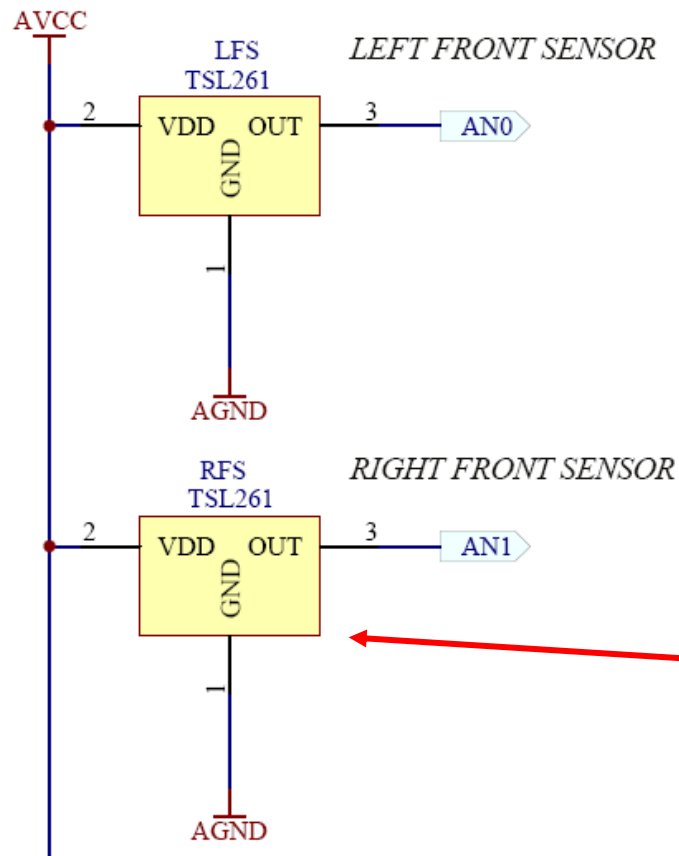


Figure : Receiver 接收器 circuit

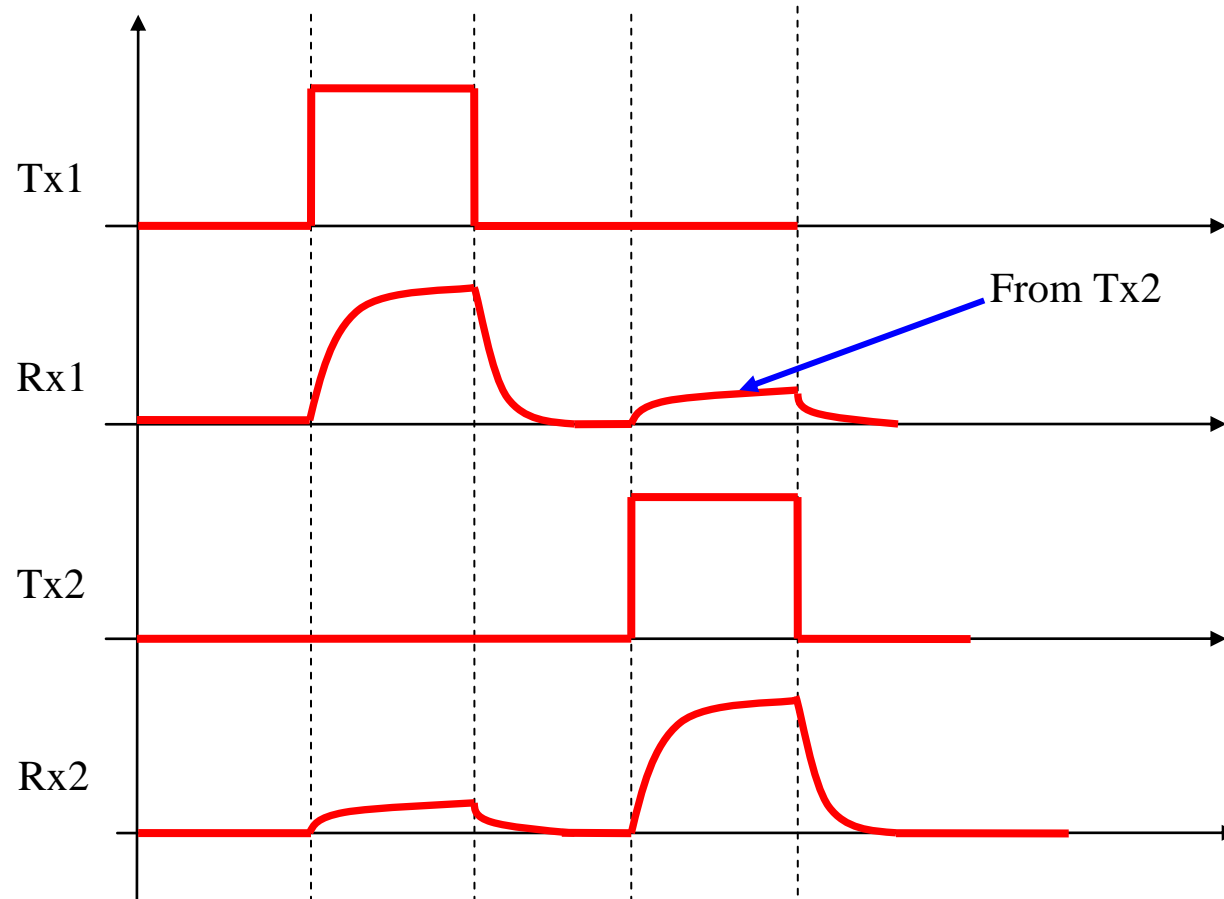
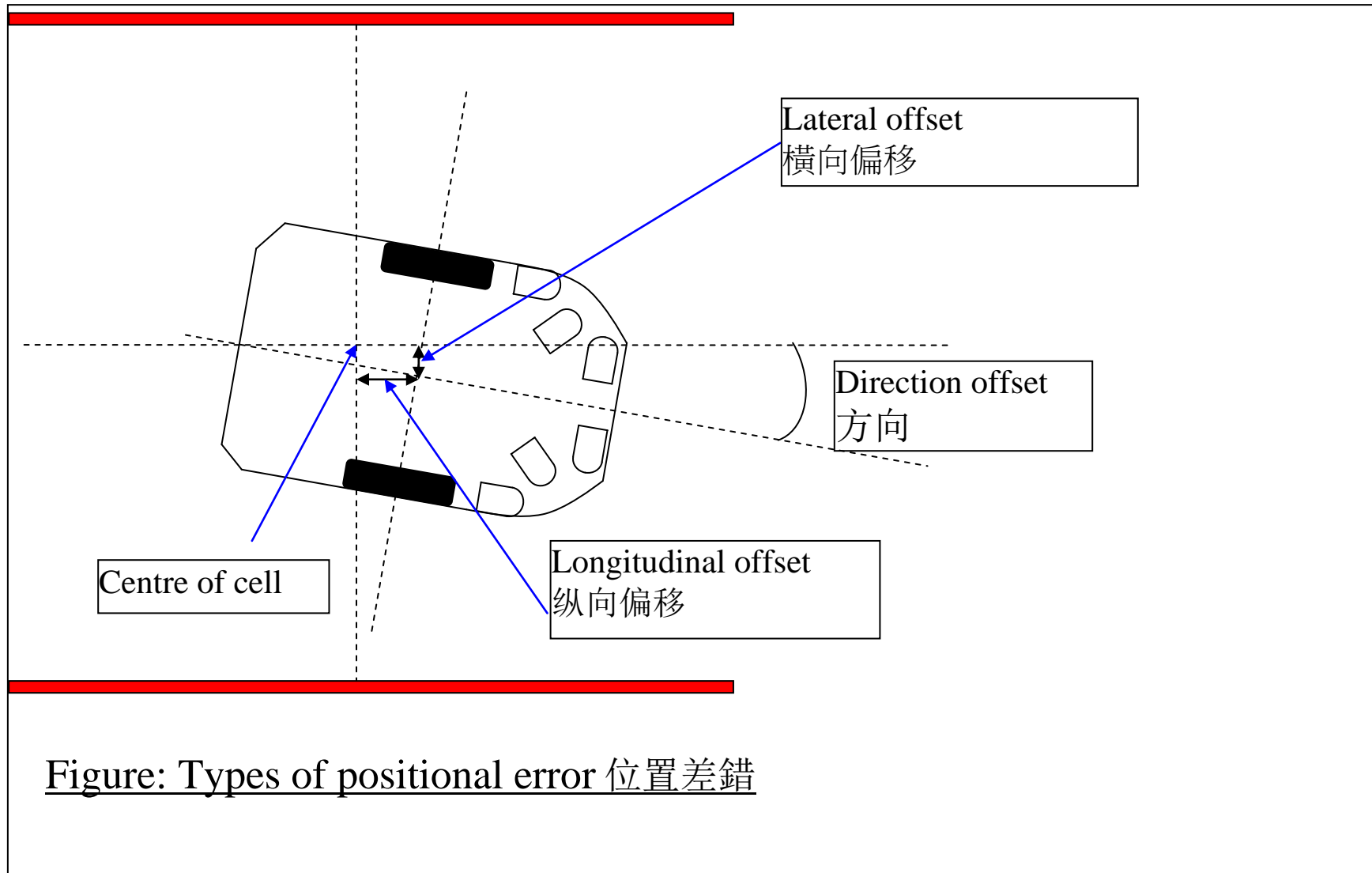


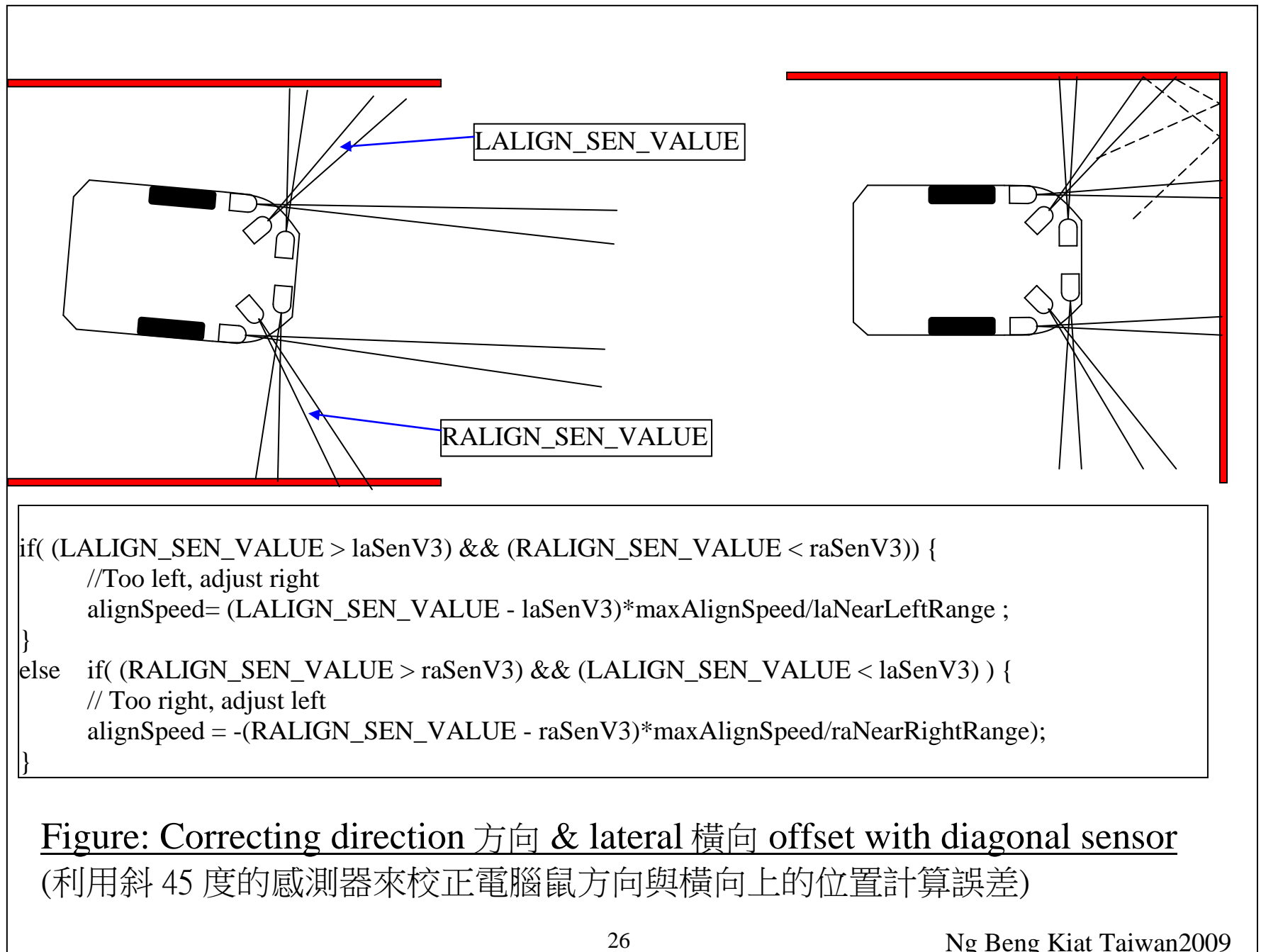
Figure : Timing diagram of sensors' signals(感測器信號的時序圖)

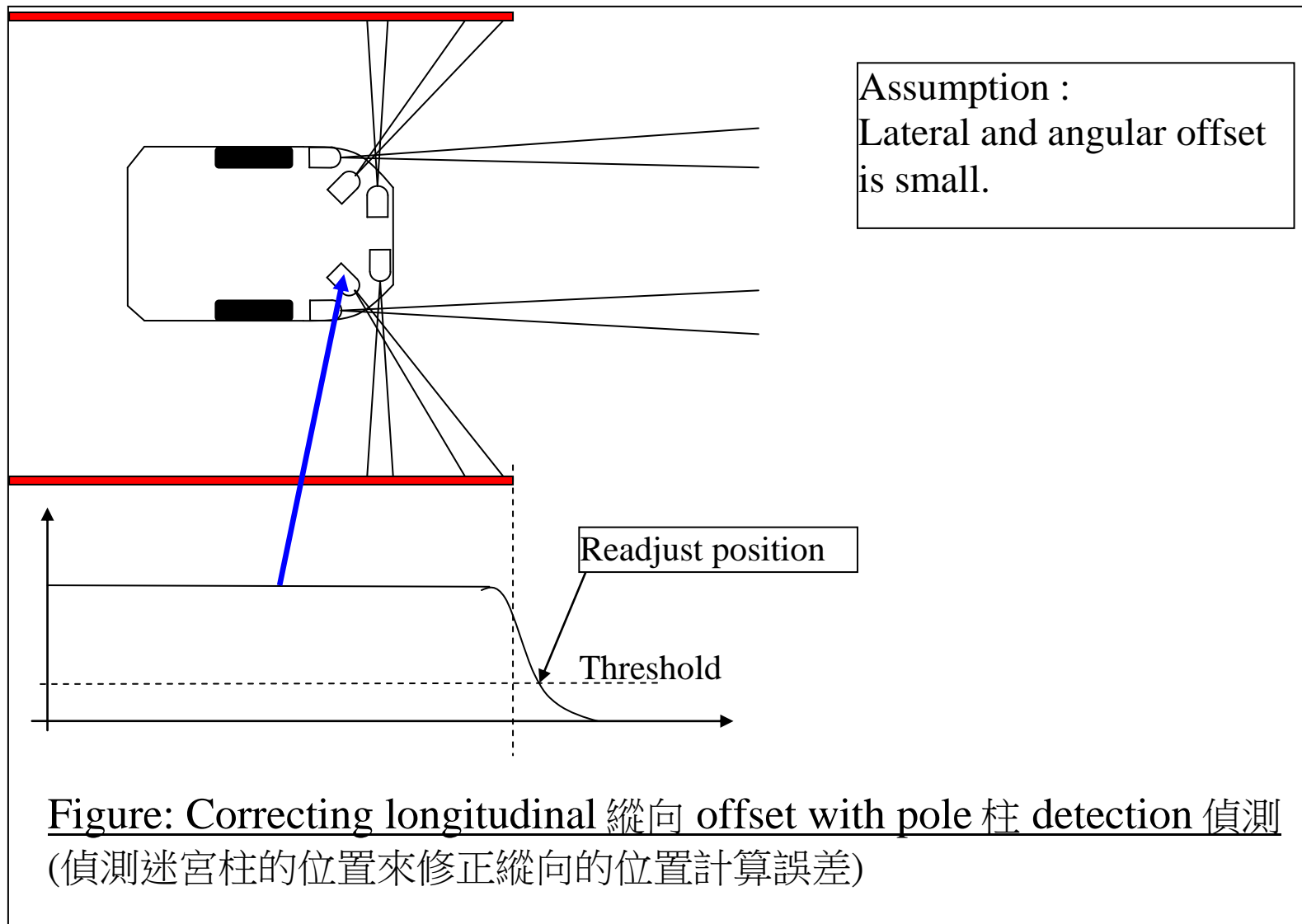
- IR LED 红外發光二極管
- Pulsing allows higher current to swarm interference 干扰  
(脈衝式的信號可以提高電流大小以對抗環境的干擾)  
LED on < 10% of time only -> can stand higher current
- Pulsing minimize interference from neighbouring sensors
- Receiver should be less sensitive 敏感 -> allows high transmitter output  
(接收器不需要太敏感)
- Improve signal noise ratio 信号噪声比率



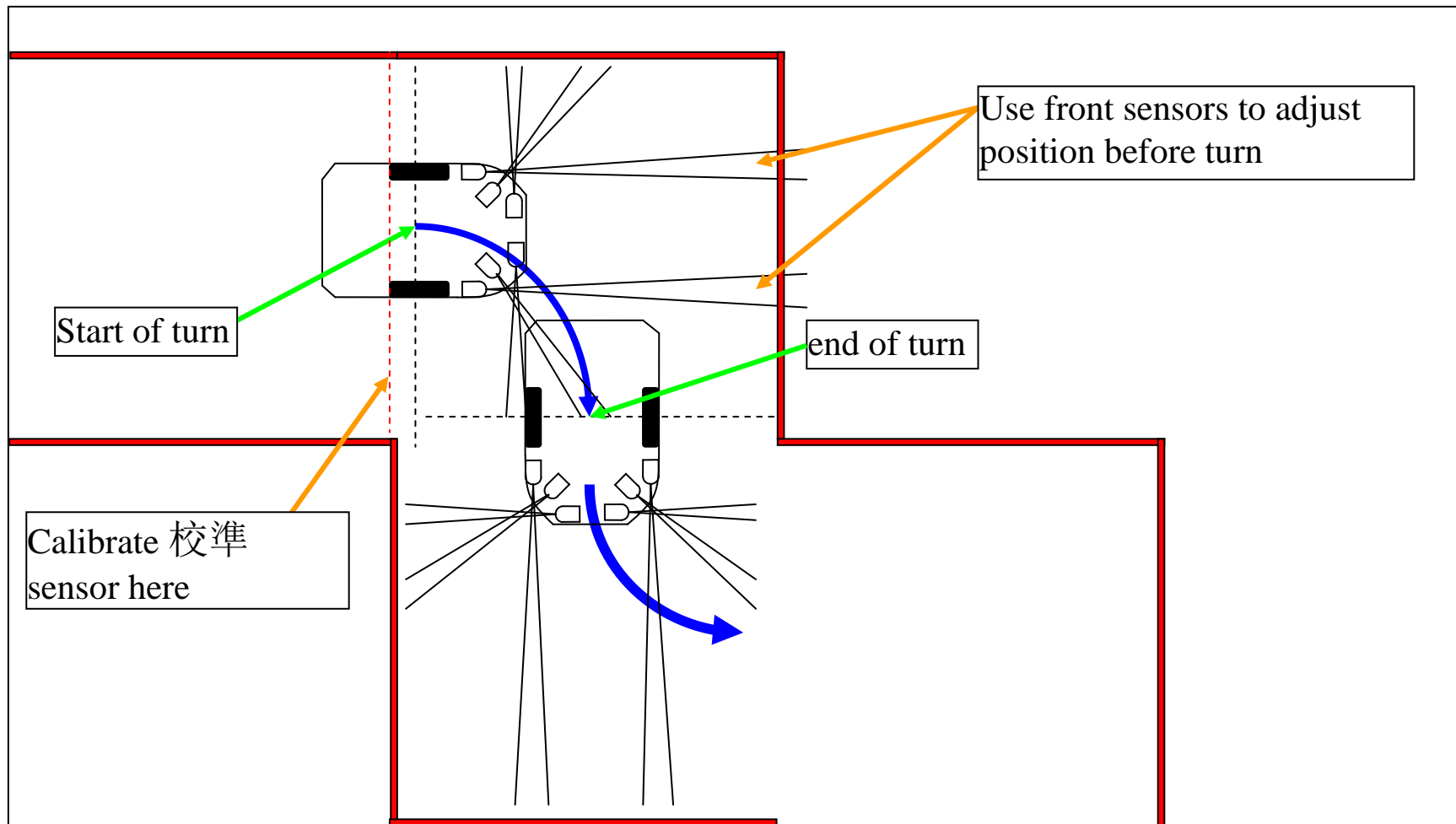
## 2.2 Alignment 位置校正







\*Almost all turns are preceded by a pole to no-pole transisition



**Figure: Correcting longitudinal offset with front wall (exploration)**  
(轉彎前如果前方有牆，可以利用往前的光感測器來修正縱向的位置計算誤差)

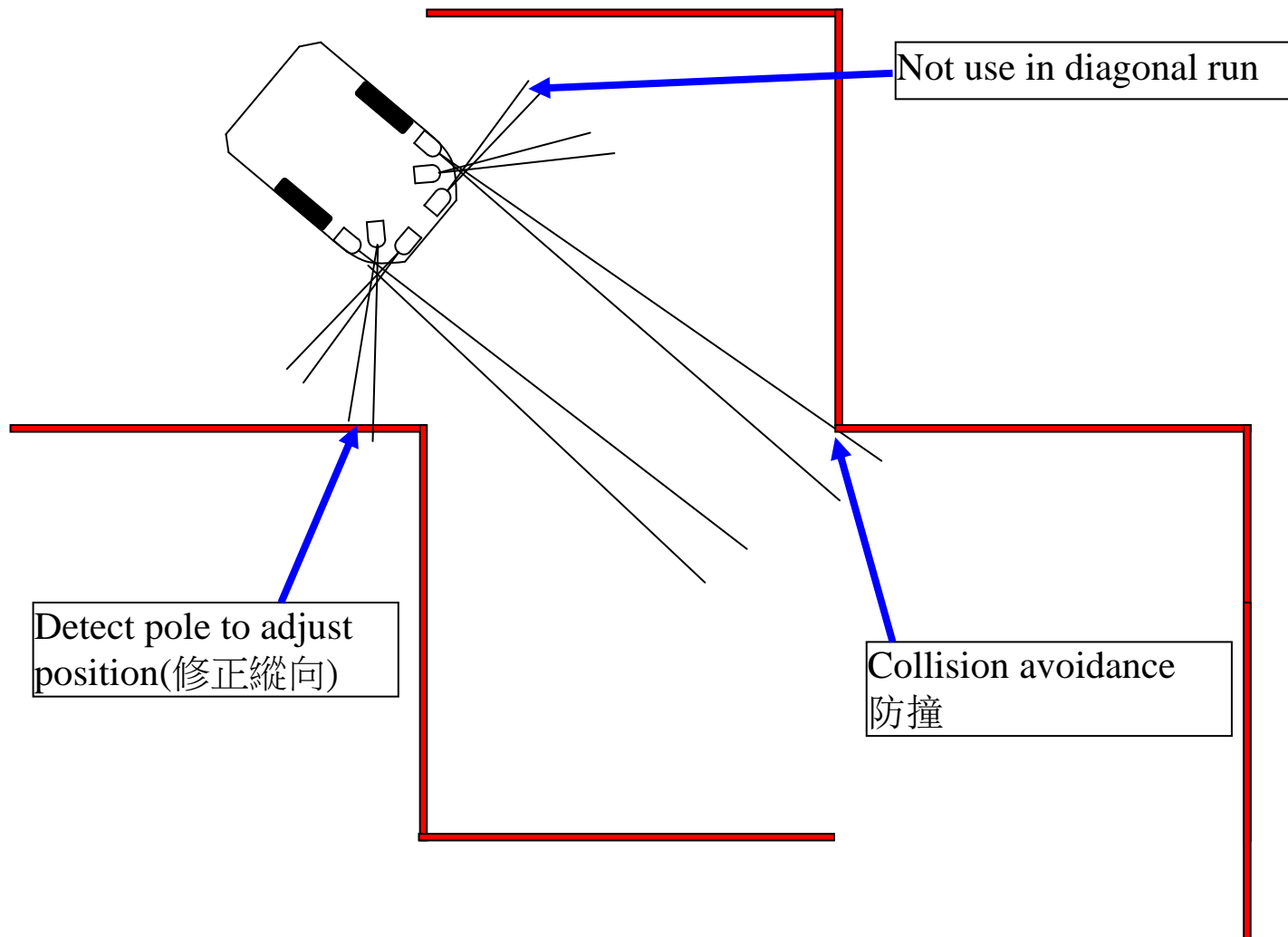
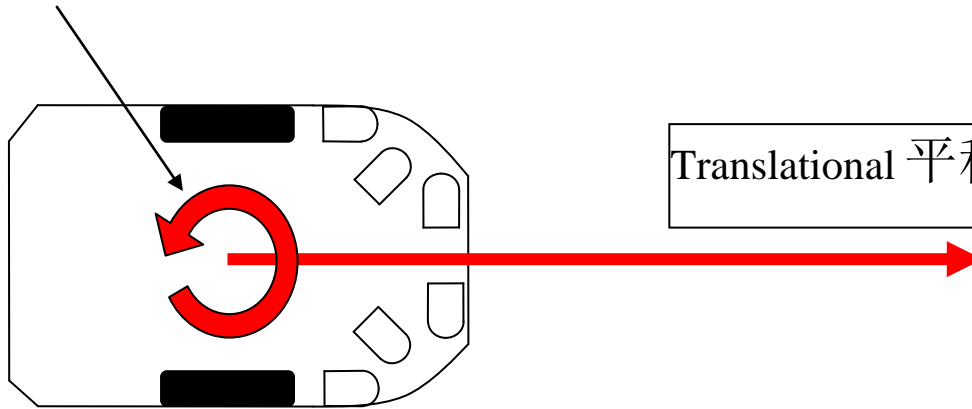


Figure: Diagonal 斜线 run. Collision avoidance and position adjustment

### 3.0 Speed Profile 速度命令曲線

Rotational 旋转 speed(wSpeed)



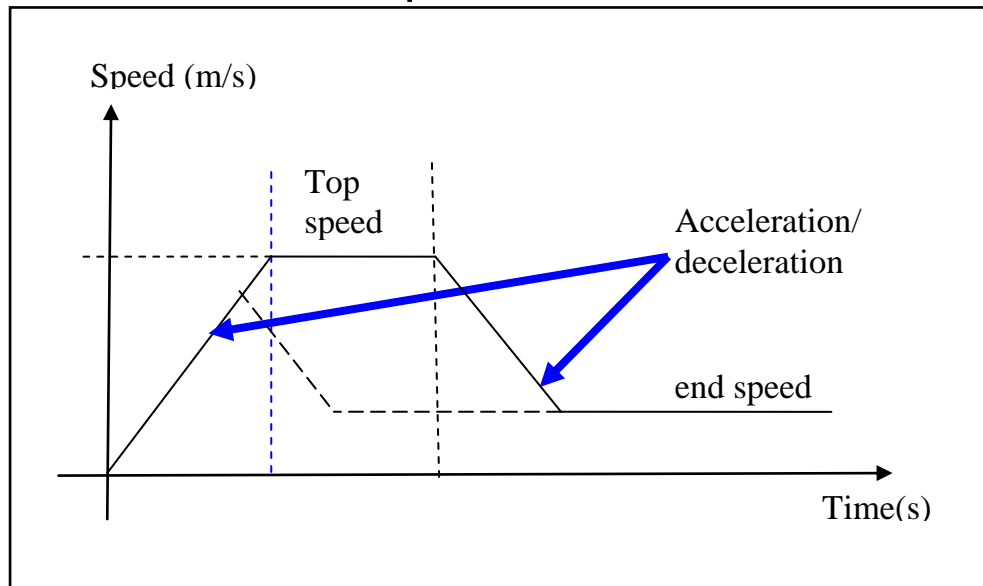
Translational 平移 speed (xSpeed)

```
leftWheelSpeed = xSpeed - wSpeed;  
rightWheelSpeed = xSpeed + wSpeed;
```

Figure : Speed components of a 2 wheels robot

### 3.1 Two basic speed profiles

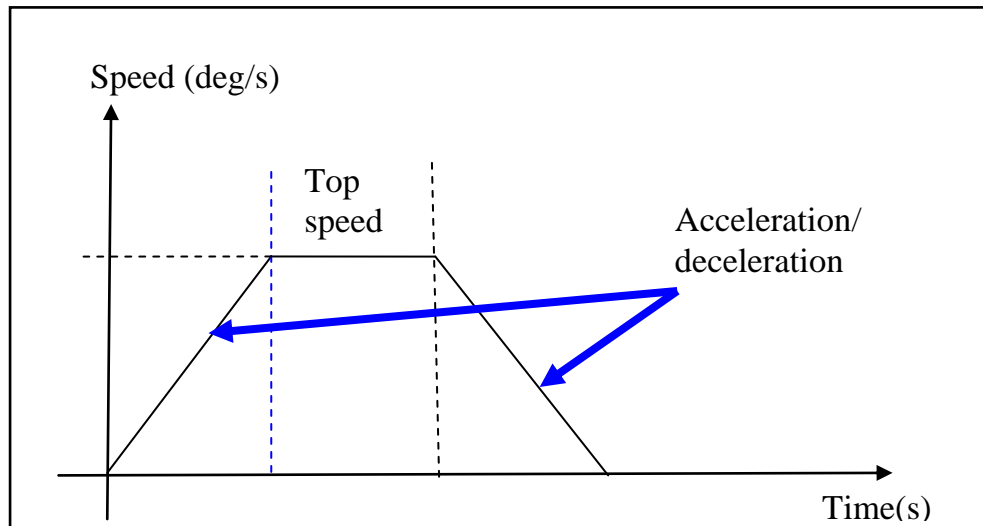
Translational speed 平移



Parameters 參數

- Top speed
- Acceleration/deceleration
- End speed (= curve turn speed)
- Distance 距離

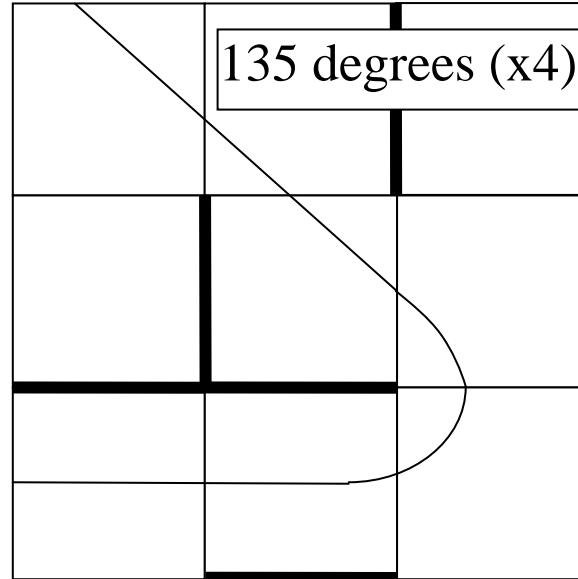
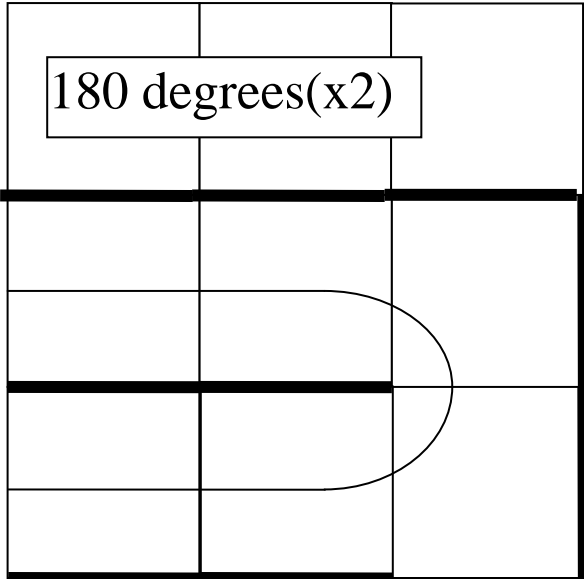
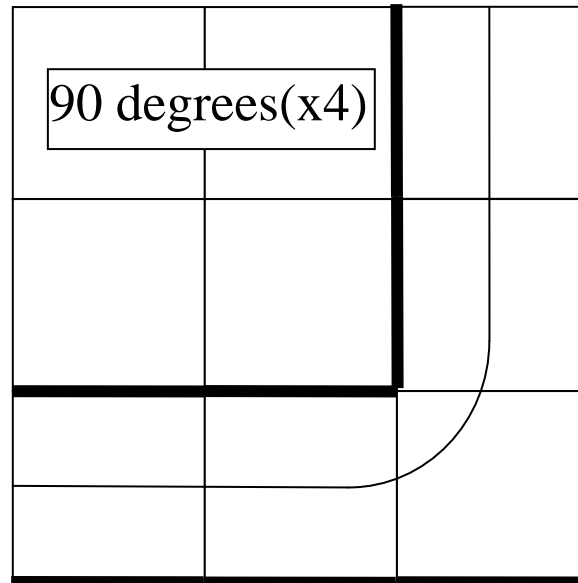
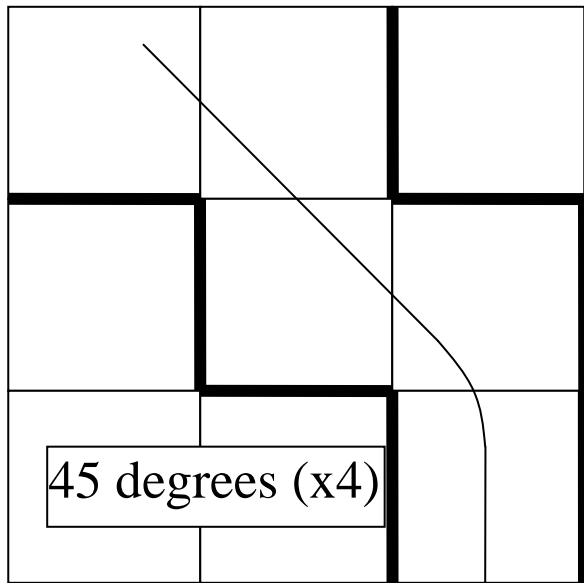
## Rotational speed (旋轉速度)

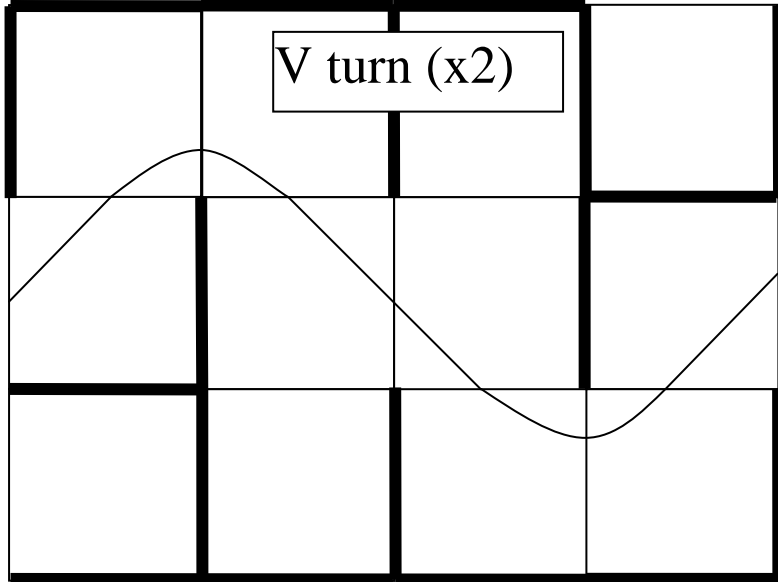


### 3.2 Basic movements

- Diagonal & non-diagonal straight runs ( $w\text{Speed}=0$ ) 對角或非對角的直線運動
- Pivot turns ( $x\text{Speed}=0$ ) (原地旋轉)
- Curve turns 90, 180(U), 135(J), 45,V( $x\text{Speed}=\text{constant}$ , +  $w\text{Speed}$ )







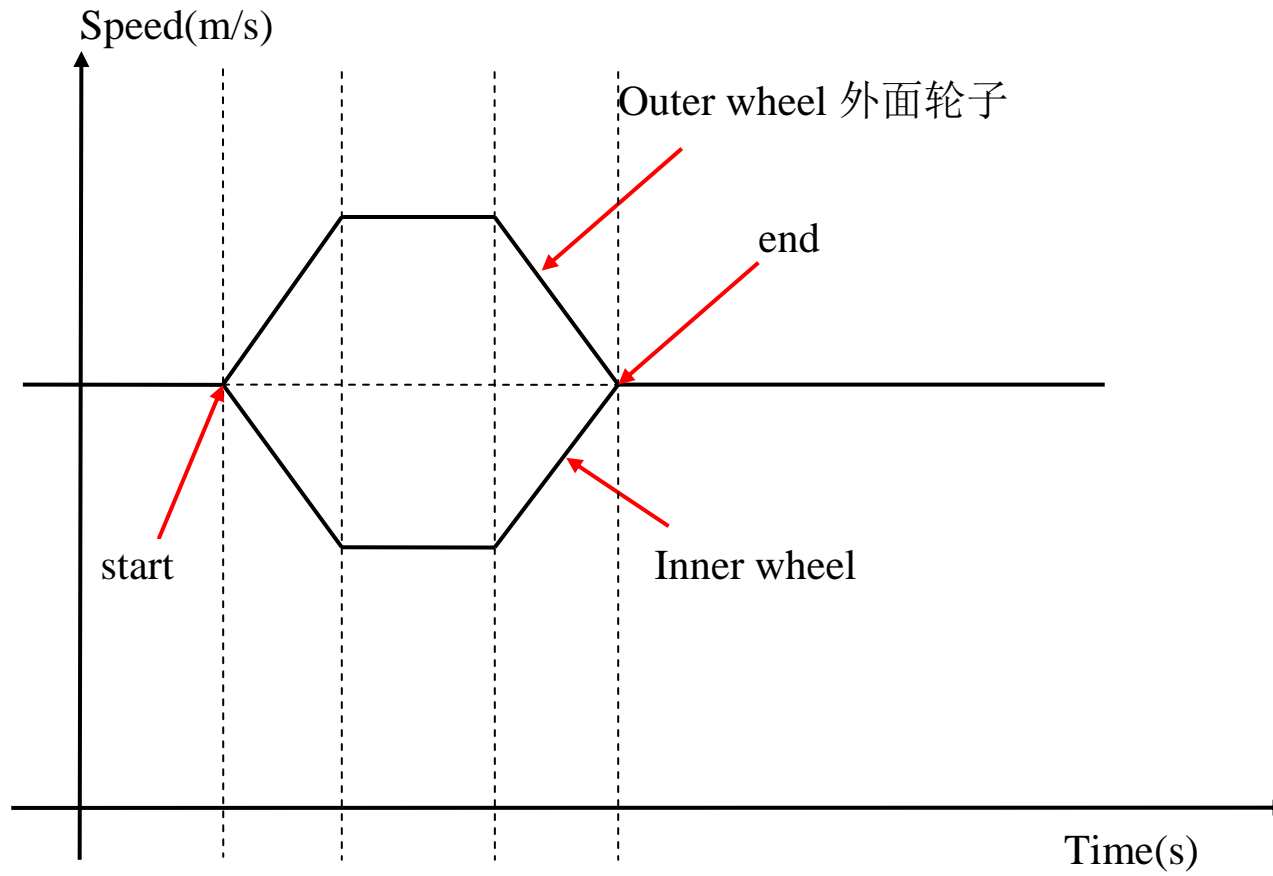
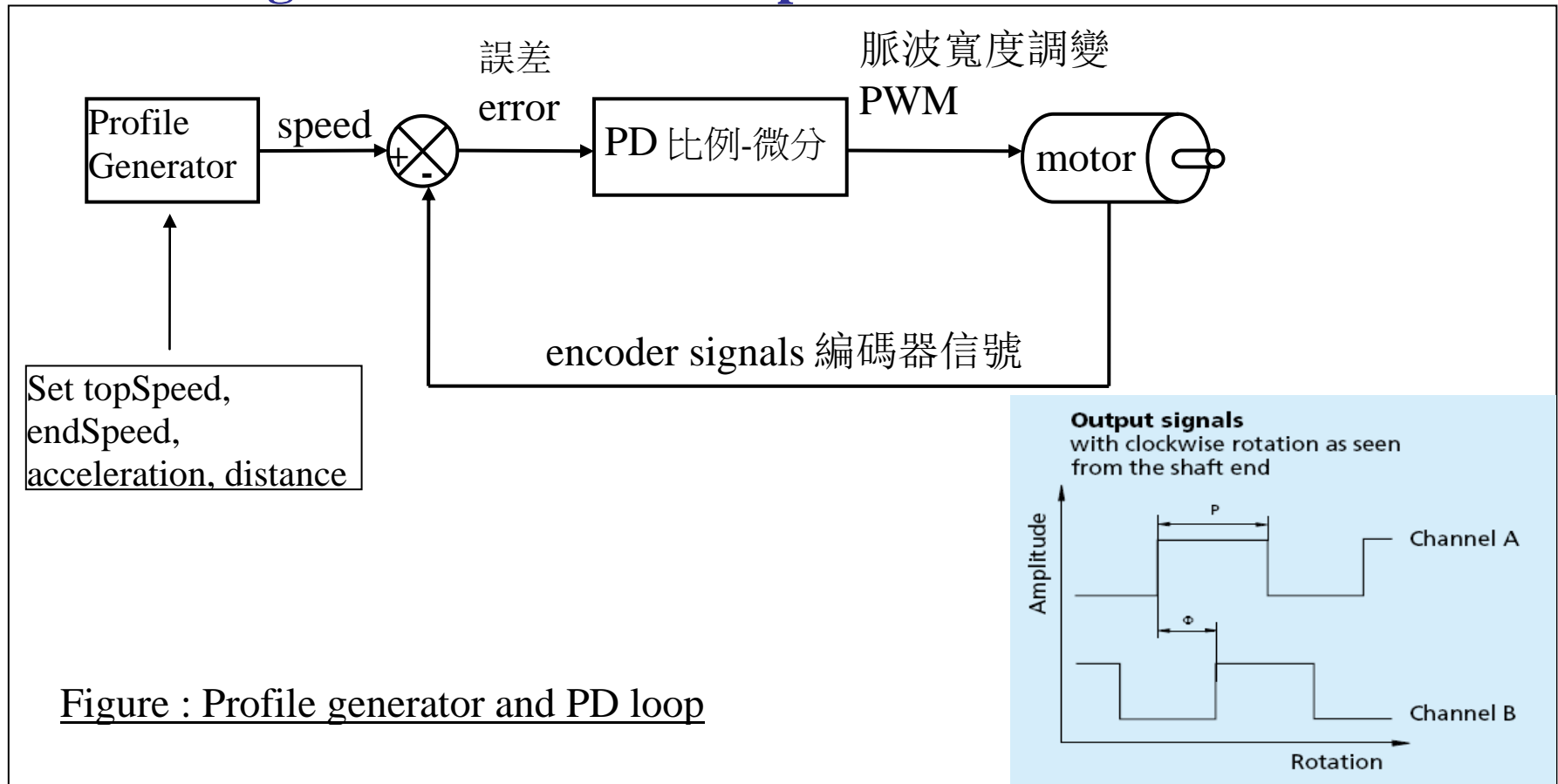


Figure : Curve turn speed profile

### 3.3 Profile generator and PD loop



- No integral 積分 term
- PD control & Profile generator is executed every msec 毫秒
- PWM frequency 頻率 is 10kHz 千赫
- PWM duty cycle =  $k_p \times \text{error}_n + k_d \times (\text{error}_n - \text{error}_{n-1})$

### 3.4 Straight speed profile C code

*// At the beginning of profile, targetSpeed = topSpeed;*

*// Keep checking for deceleration condition*

```
void SpeedProfile() {
```

```
    decelerationRequired = (curSpeed2 - endSpeed2) / (2 × distance);
```

```
    if (decelerationRequired > deceleration) targetSpeed = endSpeed;
```

```
    if (curSpeed < targetSpeed) curSpeed += acceleration;
```

```
    if (curSpeed > targetSpeed) curSpeed -= deceleration;
```

```
    distance += curSpeed;
```

```
}
```

distance - 距離; curSpeed - 目前的速度; endSpeed - 終點速度;

acceleration - 加速度; deceleration - 減速度

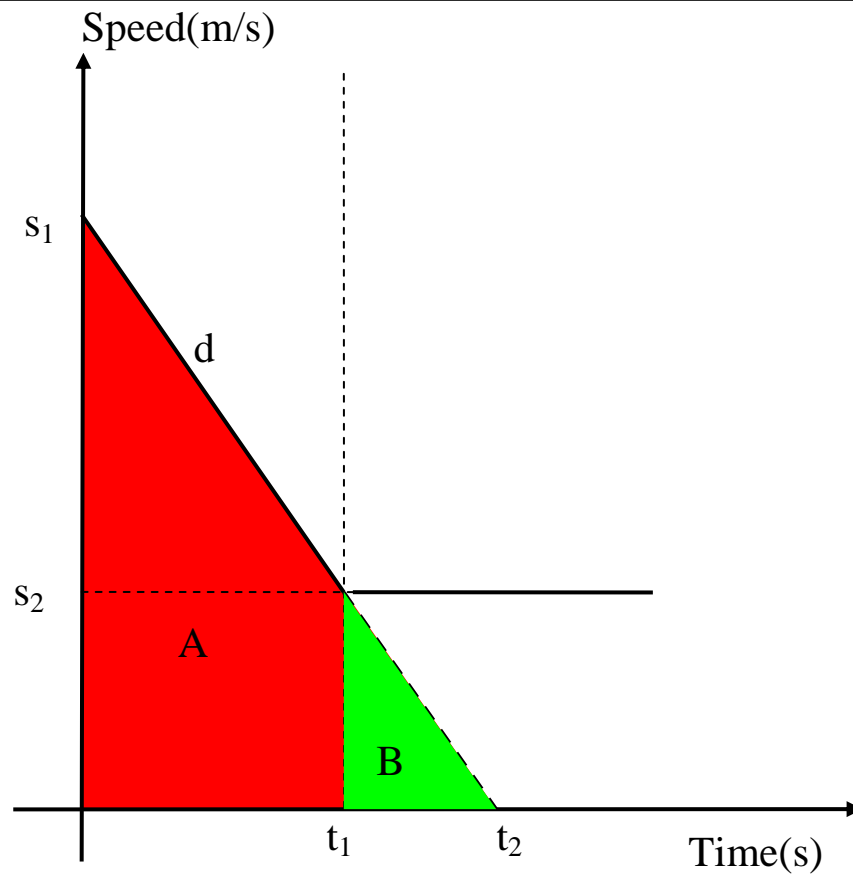


Figure : Speed profile

Calculating deceleration:

$$A+B = (S_1 t_2)/2$$

$$B = S_2(t_2 - t_1)/2$$

$$d = S_1/t_2 = S_2/(t_2 - t_1)$$

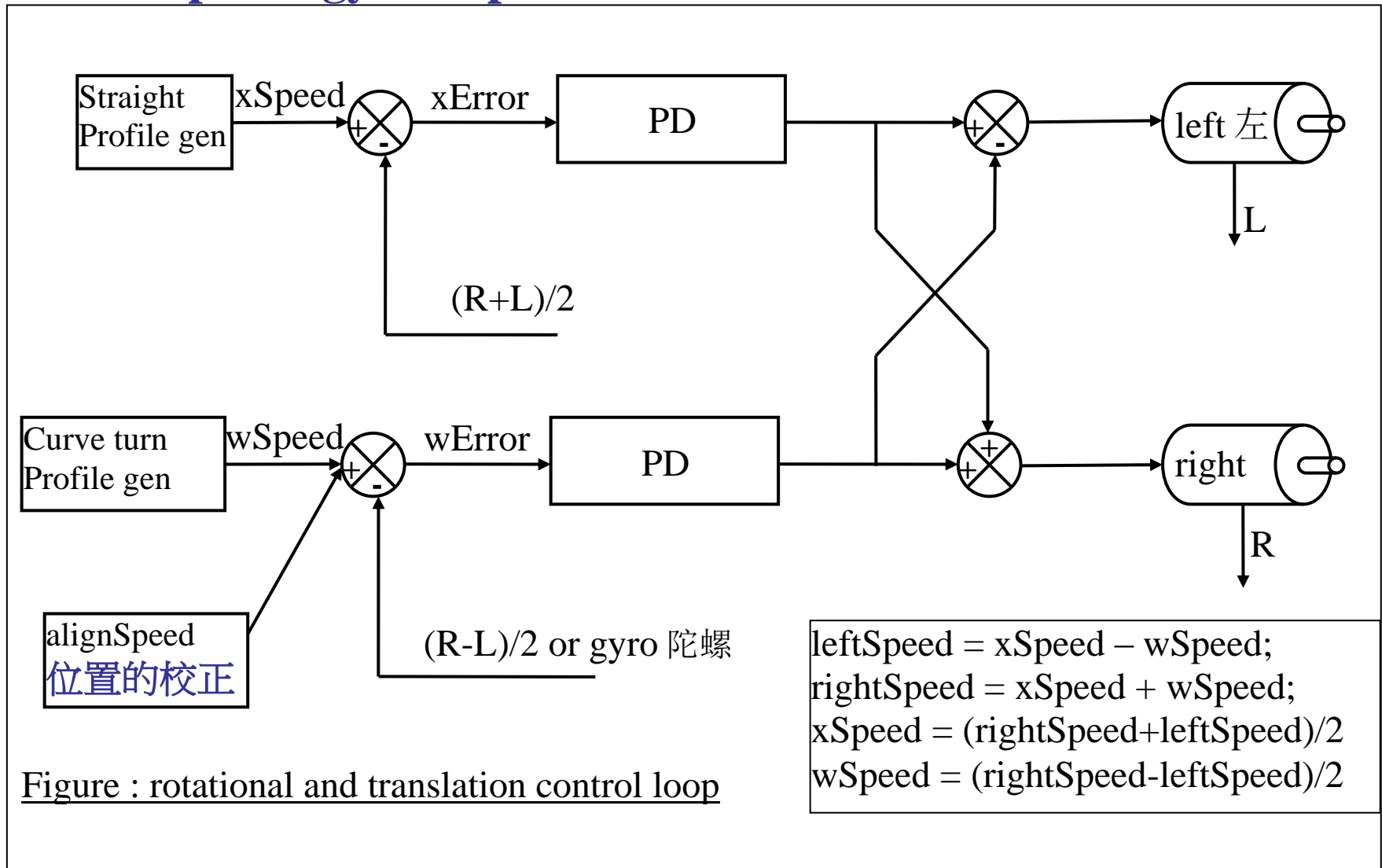
$$\circ t_2 = S_1/d$$

$$\circ (t_2 - t_1) = S_2/d$$

$$\begin{aligned} A &= (S_1 t_2)/2 - B \\ &= (S_1 t_2)/2 - S_2(t_2 - t_1)/2 \\ &= (S_1^2 - S_2^2)/2d \end{aligned}$$

$$d = (S_1^2 - S_2^2)/2A$$

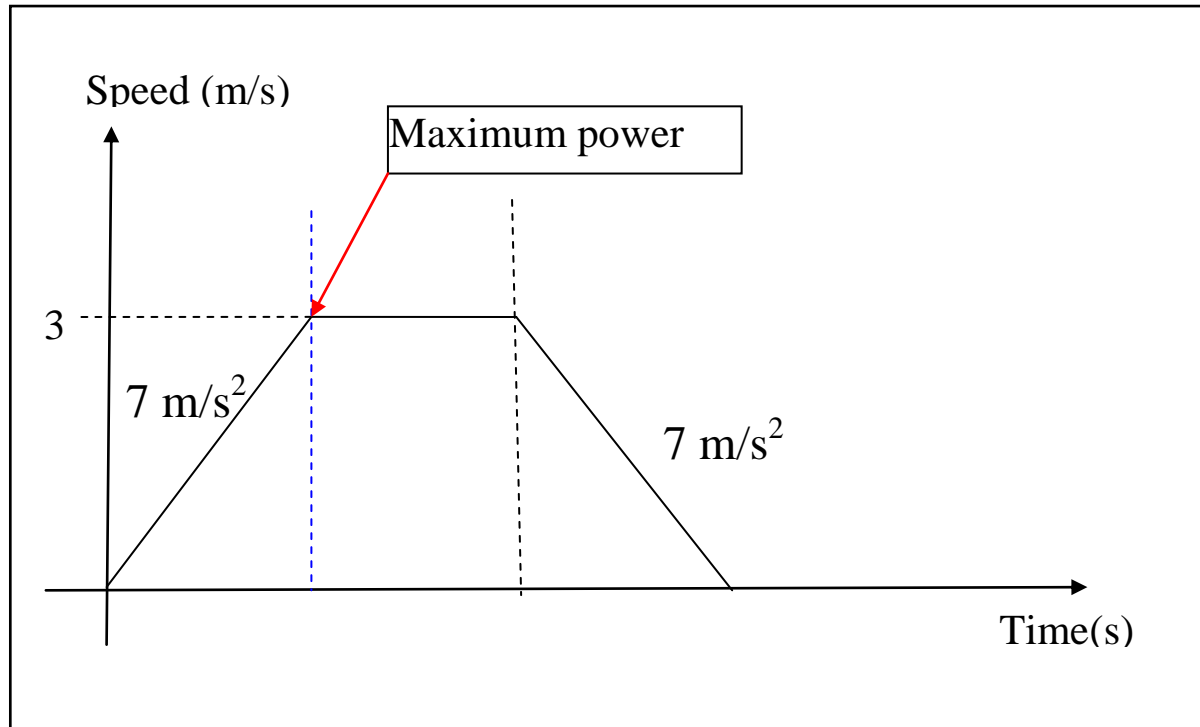
### 3.5 PD loop and gyroscope



- Gyro 陀螺 is fast in response
- Accurate for fast curve turn (not for very slow turn) / opposite of optical encoder 編碼器信號
- Need to calibrate 校準 before run due to DC drift 漂移?
- Not affected by tires size change



## 4.0 DC motor sizing 直流馬達的選擇



Step 1 : Calculate maximum power 功率 required

- Force(N) = mass(kg)  $\times$  acceleration( $\text{m/s}^2$ ) 動力 = 重量  $\times$  加速度
  - Desired acceleration =  $7 \text{ m/s}^2$  // experience required

- Force =  $0.12\text{kg} \times 7\text{m/s}^2 = 0.84\text{N}$
- Power (W) = force(N)  $\times$  speed(m/s) (功率 = 動力  $\times$  速度)
- Maximum power is required when robot is accelerating at  $7\text{ m/s}^2$  near top speed =  $3\text{m/s}$ .
- Max power required =  $0.84\text{N} \times 3\text{ m/s} = 2.52\text{ watt}$ .
- Since there are 2 motors, power required per motor =  $1.26\text{ W}$ .

## Step 2 : Select motor (Faulhaber 1717SR)

- Choose a motor with maximum Power 1.5 times to 2 times  $1.26\text{W} = 1.89\text{W}$  to  $2.52\text{ W}$ ,
- Which is less than the Pmax of  $1.96\text{ W}$  (Faulhaber 1717SR).

## Series 1717 ... SR

	1717 T		003 SR	006 SR	012 SR	018 SR	024 SR	
1 Nominal voltage	$U_N$		3	6	12	18	24	Volt
2 Terminal resistance	$R$		1,07	4,30	17,1	50,1	68,8	$\Omega$
3 Output power	$P_{2 \max.}$		1,97	1,96	1,97	1,50	1,96	W
4 Efficiency	$\eta_{\max.}$		69	69	70	68	70	%
5 No-load speed	$n_o$		14 000	14 000	14 000	12 300	14 000	rpm
6 No-load current (with shaft $\varnothing$ 1,5 mm)	$I_o$		0,091	0,046	0,023	0,013	0,011	A
7 Stall torque	$M_H$		5,37	5,34	5,38	4,66	5,36	mNm
8 Friction torque	$M_R$		0,18	0,18	0,18	0,18	0,17	mNm

- Note that I also overdrive the motor. 2x Lithium Polymer = 8.4V. Average around 7.8 volts
- Maximum power out at 7.8 V =  $(7.8/6)^2 \times 1.96 = 3.3$  watts

### Step 3 : Select gear ratio 齒輪比

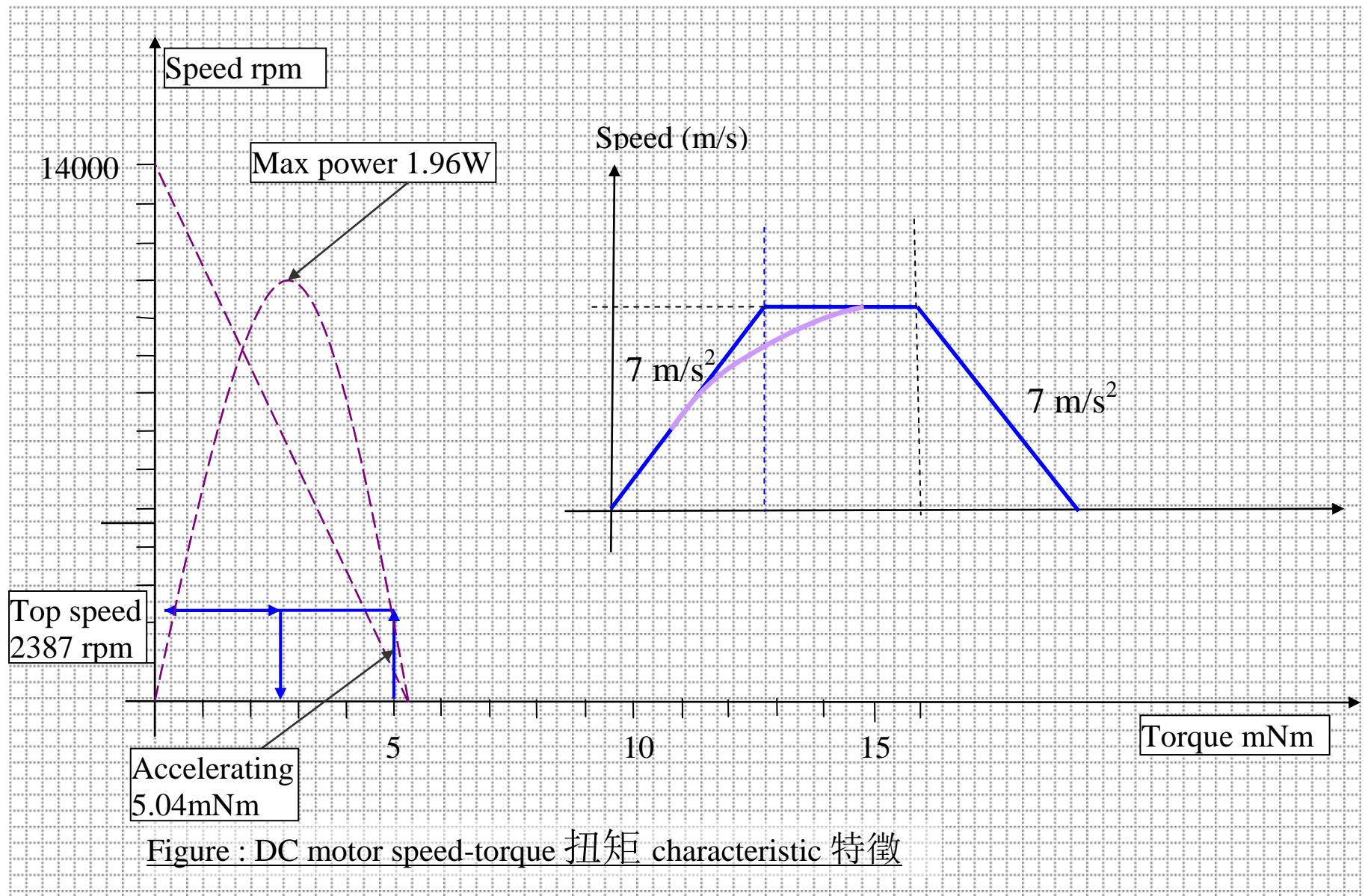
- Calculate torque and speed
  - Tires diameter 直徑 is 24mm
  - Torque required = Force  $\times$  radius (扭矩 = 動力  $\times$  半徑)

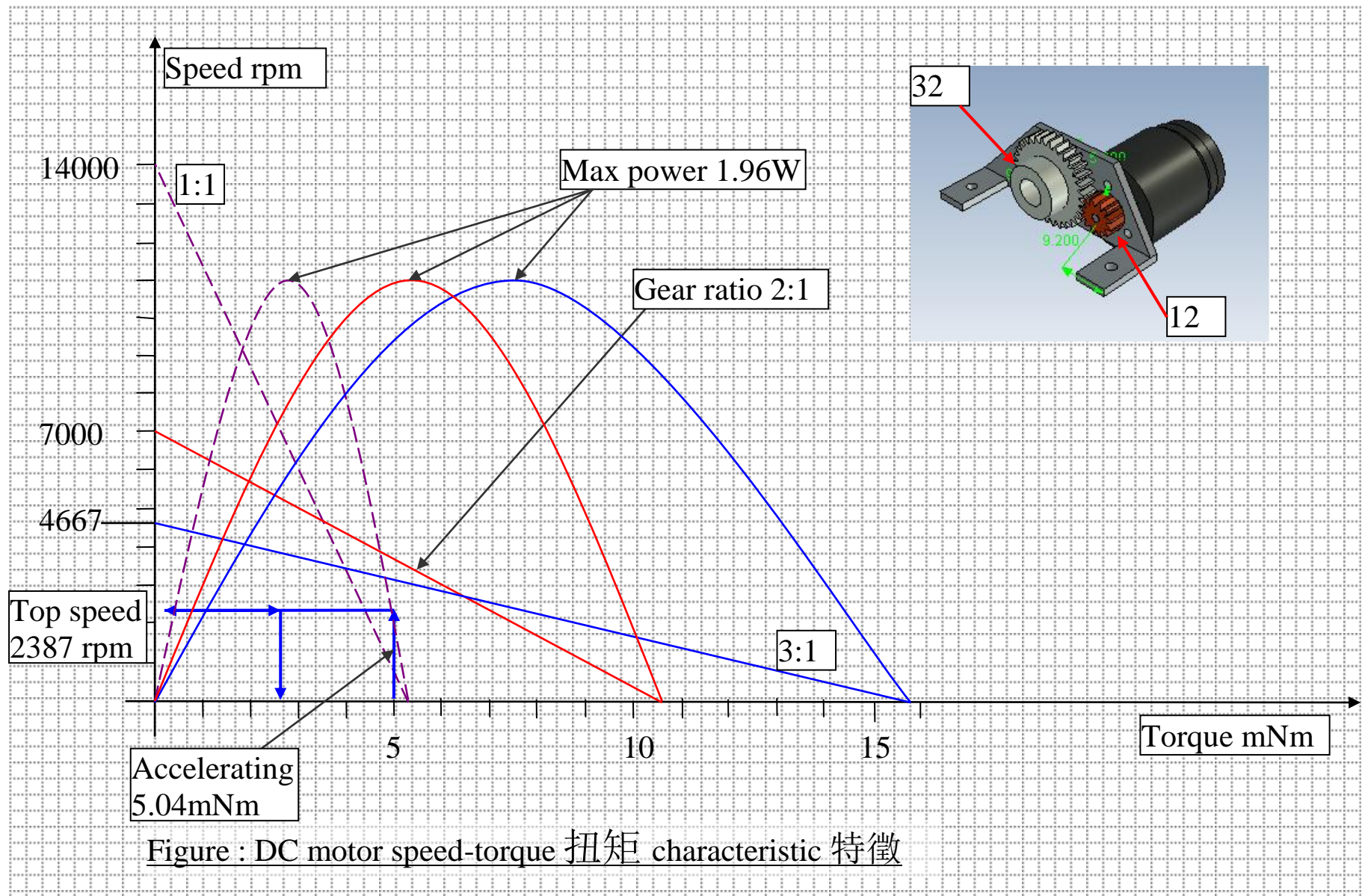
$$= 0.84\text{N} \times 12\text{mm} = 10.08 \text{ mNm}$$

- Torque required per motor = 5.04mNm.
- Wheel circumference 圓週 =  $\text{Pi} \times \text{diameter} = 0.0754\text{m}$
- At 3m/s, wheel revolution 旋轉 =  $\text{speed} / \text{circumference}$

$$= 3 / 0.0754\text{m} = 39.8 \text{ rps} = 2387 \text{ rpm}$$

- Therefore, near top speed, motor must be able to provide torque output of 5.04mNm at speed of 2387 rpm.

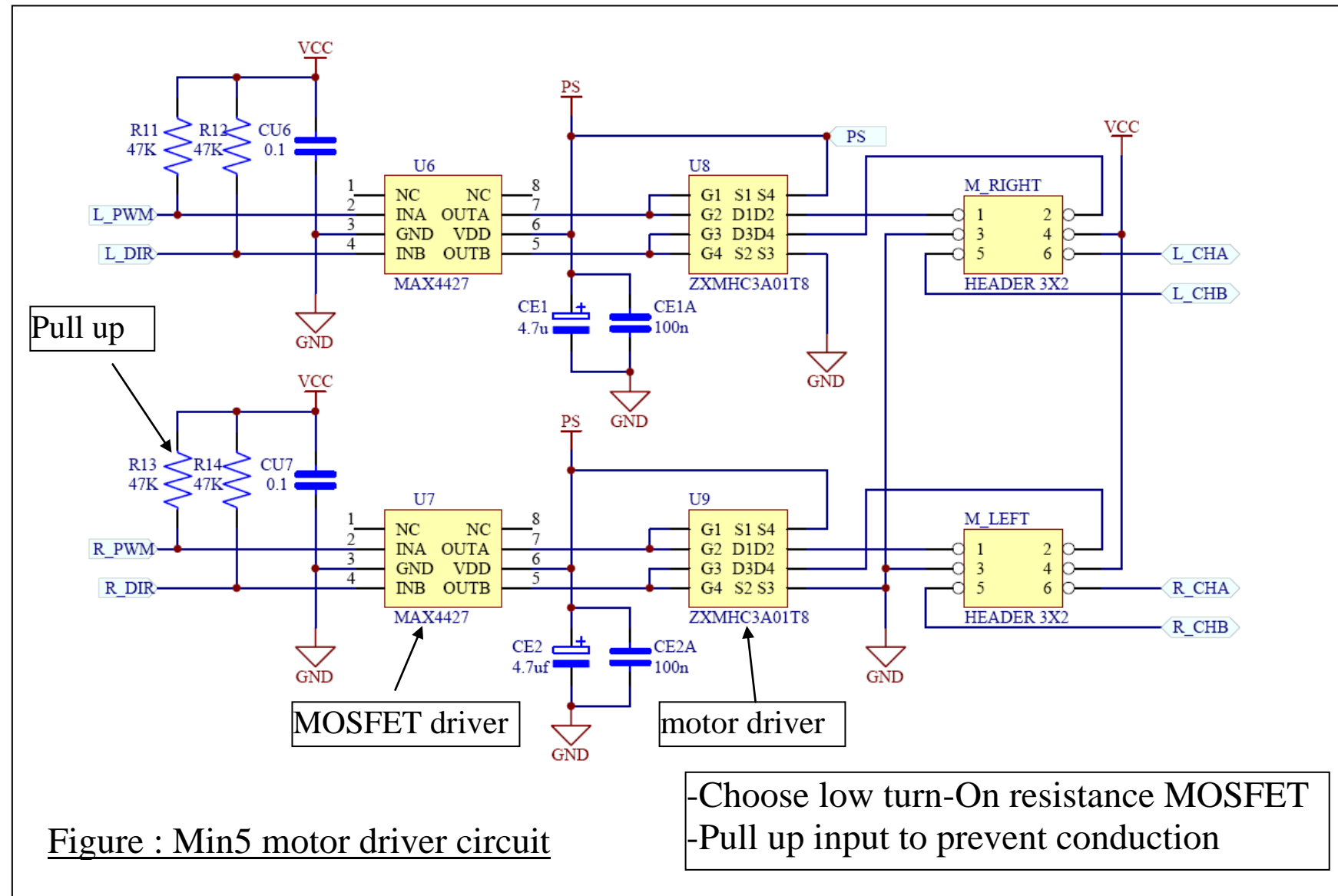




- There is a range of gear ratio to select from
- The higher the gear ratio, the more energy efficient 效率 the motor is.
- Allows spare power for alignment

Prefer long & slim 細長 motors to short and fat 肥短 motor. Lower c.g.

## 4.1 DC motor driver





## User interface

- Need feedback to tell what the mouse is doing
- LED lights
- Sound
- Menu driven (dotmatrix display & input switch)

## Websites

- Visit my website at [www.np.edu.sg/alpha/nbk](http://www.np.edu.sg/alpha/nbk)
- (A\* Pathfinding ) <http://www.policyalmanac.org/games/aStarTutorial.htm>
- (Nakashima website) <http://homepage1.nifty.com/hfd01577/index.html>
- (Pete Harrison) <http://micromouse.cannock.ac.uk>

Good Luck!