

ENG 60104 Computing Applications for Engineers
PALS 1

Answer using hand calculation

Calculation

Question 1

Water is flowing in a trapezoidal channel at a rate of $Q=20\text{m}^3/\text{s}$. The critical depth y for such a channel must satisfy the equation

$$0 = 1 - \frac{Q^2}{gA_c^3}B$$

where $g=9.81\text{m/s}^2$, A_c =the cross sectional area (m^2) and B =width of the channel at the surface (m). For this case, the width and the cross-sectional area can be related to depth y by

$$B = 3 + x$$

and

$$A_c = 3x + \frac{x^2}{2}$$

Solve for the criterion depth using the bisection and false position method. The initial guesses for both methods are $x_l=0.5$ and $x_u=2.5$. Iterate until the relative error falls below 5%. Then, write the Matlab script for both methods.

Answer: [q1.m](#)

Question 2

Determine the root of $f(x) = 0.95x^3 - 5.9x^2 + 10.9x - 6$ using the Newton Raphson method (three iterations, $x_i = 3.5$) and the Secant method (three iterations, $x_{i-1} = 2.5$ and $x_i = 3.5$)

Question 3

Determine the value of x_1 , x_2 and x_3 for the following equations using Cramer's rule and Gauss Elimination method.

$$\begin{aligned} 50 &= 5x_3 - 7x_2 \\ 4x_2 + 7x_3 + 30 &= 0 \\ x_1 - 7x_3 &= 40 - 3x_2 + 5x_1 \end{aligned}$$