

Linear Quadratic Systems Answers and Explanations

ANSWERS

1. B 2. D 3. C 4. B 5. A 6. B 7. D 8. C 9. B 10. B

Answer Explanations

1. B In this problem, we are given two equations and asked to find ALL of the solutions to the system of equations. Given that these equations are both related through the y -variable we can substitute $2x-3$ for y in the second equation and factor our quadratic equation. $y = x^2 - 4x + 6 \rightarrow 2x - 3 = x^2 - 4x + 6 \rightarrow 0 = x^2 - 6x + 9 \rightarrow (x-3)^2 = 0$. Now that we've factored our quadratic equation, we can plug our x -values back into our system of equations to find our y -value solutions. $y = 2(-3) - 3 = -9$. This system of equations has one solution, $(-3, -9)$ which makes answer choice (B) correct.

2. D In this problem, we are given two equations and asked to find ALL of the solutions to the system of equations. Given that these equations are both related through the y -variable we can substitute $x+5$ into our second equation and factor our quadratic equation. $y = x^2 - 3x - 7 \rightarrow x + 5 = x^2 - 3x - 7 \rightarrow 0 = x^2 - 4x - 12 \rightarrow (x-6)(x+2) = 0$. Knowing our x -solutions are 6, -2 we can plug these values into our system of equations to find our y -solutions $(-2, 3)$ and $(6, 11)$ which makes answer choice (D) correct.

3. C In this problem, we are given two equations and asked to find the value of a knowing (a, b) is a solution and a is greater than zero. Given these equations are both related through the y -variable we can substitute $3x$ into our first equation and factor our quadratic equation.

$$-16x^2 = (y+4)(y-4) \rightarrow -16x^2 = (3x+4)(3x-4) \rightarrow -16x^2 = 9x^2 - 16 \rightarrow 0 = 25x^2 - 16 \rightarrow 0 = (5x-4)(5x+4).$$

Our a -solutions are $\frac{4}{5}, -\frac{4}{5}$, but we are told $a > 0$ so the answer is $a = \frac{4}{5}$.

4. B In this problem, we are given two equations and asked to find the number of solutions that satisfy the system of equations. Given these equations are both related through the y -variable we can substitute $7x-13$ into our first equation and factor our equation. $y = x^2 - 5x + 23 \rightarrow 7x - 13 = x^2 - 5x + 23 \rightarrow 0 = x^2 - 12x + 36 \rightarrow (x-6)^2 = 0$.

Knowing our x -solution is 6, we can only have one solution to the system of equations, which makes answer choice (B) correct.

5. A In this problem, we are given two equations and asked to find the value of x^2 . Given these equations are both related through the y -variable we can substitute $-2x$ into our first equation and combine like terms.

$$9x^2 + 2(-2x)^2 = 136 \rightarrow 17x^2 = 136 \rightarrow x^2 = 8 \text{ which makes answer choice (A) correct.}$$

6. B In this problem, we are given two equations and asked to find a value of x that is greater than zero. Given that these equations are both related through the y -variable we can substitute in $8x^2$ into our first equation and factor our quadratic equation. $8x^2 = 4 - 4x \rightarrow 8x^2 + 4x - 4 = 0 \rightarrow 4(2x^2 + x - 1) = 0 \rightarrow (2x-1)(x+1) = 0 \rightarrow x = \frac{1}{2}, -1$.

However, we know that $\frac{1}{2}$ is the only solution that is greater than zero. Therefore, the correct answer is (B).

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7. D In this problem, we are given two equations and asked to find a value of x that is greater than zero. Given that these equations are both related through the y -variable we can rewrite our second equation as follows:

$$\frac{y-2}{6} = 8 \rightarrow y-2 = 48 \rightarrow y = 50. \text{ Then we can substitute}$$

$(x-6)^2 + 1 = 50 \rightarrow \sqrt{(x-6)^2} = \sqrt{49} \rightarrow x-6 = 7 \rightarrow x = 13$. After simplifying our quadratic, we know that our x -solution is 13, which makes answer choice (D) correct.

8. C In this problem, we are given two equations and asked to find the value of b , if (a,b) is the solution to the system of equations. Given that these equations are related through the y -variable, we can substitute $5x-25$ into our second equation and factor our quadratic equation:

$5x-25 = x^2 - 17x + 96 \rightarrow x^2 - 22x + 121 = 0 \rightarrow (x-11)^2 = 0$. Now that we've found our x -solution, 11, we can plug this value to find our y -solution. $y = 5x-25 \rightarrow y = 5(11)-25 = 30$ which makes answer choice (C) correct.

9. B In this problem, we are given two equations and asked to find the product of the y -value of the two solutions. Given that these equations are related through the x -variable we can rewrite our second equation as follows:

$y = \frac{5-x}{3} \rightarrow 3y = 5-x \rightarrow x = 5-3y$. Now that we have our value of x in terms of y , we can substitute this value in our first equation and simplify our quadratic equation: $6y^2 = 25(5-3y) - 125 \rightarrow 6y^2 = 125 - 75y - 125 \rightarrow 6y^2 + 75y = 0 \rightarrow y(6y + 75) = 0$. Now that we know our y -values (0, -12.5), we know the product of any factor times zero is zero. Therefore, the product is zero.

10. B In this problem, we are given two equations and asked to find the y -coordinate of an intersection point. Given that these two equations are related through the y -coordinate we can substitute $7-3x$ into our first equation and simplify our quadratic equation. $7-3x = x^2 - x - 8 \rightarrow x^2 + 2x - 15 = 0 \rightarrow (x-3)(x+5) = 0$. Knowing that our x -solutions are 3 and -5, we can plug these values in to find our y -coordinates.

$y = 7-3x \rightarrow y = 7-3(3) = -2$; $y = 7-3x \rightarrow y = 7-3(-5) = 22$. Since -2 is an answer choice and 22 isn't, we know the correct answer is B.