

## Radical and Rational Equations Answers

### Answers

1. B    2. C    3. D    4. B    5. A    6. C    7. C    8. A    9. C    10. A

### Answer Explanations

1. **B.** In this problem, we are given the expression  $\sqrt[3]{64x^6y^5}$  and asked to find an equivalent expression.

First, we should break down this expression  $\sqrt[3]{64} \times \sqrt[3]{x^6} \times \sqrt[3]{y^5}$ . Now that our expression has been broken down we can individually simplify each component  $\sqrt[3]{64} = 4$ ,  $\sqrt[3]{x^6} = x^{6/3} = x^2$ ,  $\sqrt[3]{y^5} = y^{5/3} = y\sqrt[3]{y^2}$ . After simplifying each component, we can multiply them back together to determine the equivalent expression  $4 \times x^2 \times y\sqrt[3]{y^2} \rightarrow 4x^2y\sqrt[3]{y^2}$ . Therefore, answer choice (B) is correct.

2. **C.** In this problem, we are given an expression containing two radical components that are being multiplied. We can rewrite this equation to make the multiplication process less erroneous.

$3\sqrt[3]{9} \times 3\sqrt[3]{3} \rightarrow 3\sqrt[3]{2^2} \times 3\sqrt[3]{3^1} \rightarrow 3^{2/3} \times 3^{1/3} \times 3^{1/3} \times 3^{1/3}$ . Remember, when multiplying exponents with the same base we add the exponents together.  $3^{2/3} \times 3^{1/3} \times 3^{1/3} \times 3^{1/3} = 3^{9/3} = 3^3 = 27$ . Therefore, answer choice (C) is correct.

3. **D.** In this problem, we are given the expression  $\left(\frac{27}{b^8}\right)^{-1/3}$  and asked to find an equivalent expression. We can rewrite this expression to the simplification much easier.

$\left(\frac{27}{b^8}\right)^{-1/3} \rightarrow \frac{1}{\left(\frac{27}{b^8}\right)^{1/3}} \rightarrow \frac{1}{\sqrt[3]{\frac{27}{b^8}}}$ . Now that we have rewritten our expression we can take the cube root of

$27$  and  $b^8$   $\frac{1}{\sqrt[3]{\frac{27}{b^8}}} = \frac{1}{\frac{3}{b^2}} = \frac{b^2}{3}$ , which makes answer choice (D) correct.

4. **B.** In this problem, we are given the equation  $n+3=\sqrt{2a-5}$  and asked to find the value of the constant  $a$ . First, we must get rid of the radical in order to further simplify our equation

$n+3=\sqrt{2a-5} \rightarrow (n+3)^2 = (\sqrt{2a-5})^2$ . Given that our  $n$ -value is equal to 4 we can plug this value in

before expanding our equation.  $(n+3)^2 = (\sqrt{2a-5})^2 = (4+3)^2 = 2a-5 \rightarrow 49 = 2a-5 \rightarrow 27$ , which makes answer choice (B) correct.

5. **A.** In this problem, we are given the equation  $x-6=\sqrt{4x-28}$  and asked to find the solution set for the equation. First, we must get rid of the radical in order to further simplify our equation

$x-6=\sqrt{4x-28} \rightarrow (x-6)^2 = (\sqrt{4x-28})^2 \rightarrow x^2 - 12x + 36 = 4x - 28 \rightarrow x^2 - 16x + 64 = 0 \rightarrow (x-8)^2 = 0$

. Knowing that the only solution to the given equation is 8, we can conclude that answer choice (A) is correct.

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6. C. In this problem, we are given the equation  $2x^{\frac{1}{2}} + 3x = 0$  and asked to find the least value of  $x$  that is a solution to the equation above. Therefore, we can factor out a  $x^{\frac{1}{2}}$  and find our solutions to the given equation.  $2x^{\frac{1}{2}} + 3x = 0 \rightarrow x^{\frac{1}{2}} \left( 3x^{\frac{1}{2}} + 2 \right) = 0$ .

$$\left( x^{\frac{1}{2}} \right)^2 = 0 \rightarrow x = 0 \mid 3x^{\frac{1}{2}} + 2 = 0 \rightarrow x^{\frac{1}{2}} = \frac{-2}{3} \rightarrow \left( x^{\frac{1}{2}} \right)^2 = \left( \frac{-2}{3} \right)^2 \rightarrow x = \frac{4}{9} .$$

Therefore, from our evaluation we can conclude that the solution with the least value is 0 which makes answer choice (C) correct.

7. C. In this problem, we are given the equation  $x = \sqrt{11+5x} - 3$  and asked to find the values of  $x$  that satisfy the equation. First, we must get rid of the radical in order to further simplify our equation

$$x = \sqrt{11+5x} - 3 \rightarrow (x+3)^2 = (\sqrt{11+5x})^2 \rightarrow x^2 + 6x + 9 = 11 + 5x \rightarrow x^2 + x - 2 \rightarrow (x+2)(x-1) = 0.$$

Knowing that our solutions to the given equation are -2 and 1, we can conclude answer choice (C) is correct.

8. A. In this problem, we are given the equation  $x - 6\sqrt{x} + 8 = 0$  and asked to find the values of  $x$  that satisfy the equation. First, we must get rid of the radical in order to further simplify our equation

$$x - 6\sqrt{x} + 8 = 0 \rightarrow (x+8)^2 = (6\sqrt{x})^2 \rightarrow$$

$$x^2 + 16x + 64 = 36x \rightarrow x^2 - 20x + 64 = 0 \rightarrow (x-4)(x-16) = 0 \rightarrow x = 4, 16 .$$

Given that the  $x$  solutions to the equation are 4 and 16, we can conclude answer choice (A) is correct.

9. C. In this problem, we are given the rational equation  $\frac{3x-5}{4x-5} = \frac{5}{6}$  and asked to find the solution to the equation. First, we can cross multiply and combine like terms to find our  $x$ -value.

$$\frac{3x-5}{4x-5} = \frac{5}{6} \rightarrow 18x - 30 = 20x - 25 \rightarrow -2x = 5 \rightarrow x = -\frac{5}{2} .$$

Knowing that our  $x$ -value is -2.5, we can conclude answer choice (C) is correct.

10. A. In this problem, we are given the equation  $18y - 6\sqrt{y} = 0$  and asked to find the least value of  $y$  that satisfies the given equation. First, we must get rid of the radical in order to further simplify our equation.

$$18y - 6\sqrt{y} = 0 \rightarrow 18y = 6\sqrt{y} \rightarrow (3y)^2 = (\sqrt{y})^2 \rightarrow 9y^2 = y .$$

Now that the radical has been removed, we can simplify our equation and solve for our  $y$ -solutions.  $9y^2 = y \rightarrow 9y^2 - y = 0 \rightarrow y(9y-1) = 0$ .

$$y = 0 \mid 9y - 1 = 0 \rightarrow 9y = 1 \rightarrow y = \frac{1}{9} .$$

Knowing that our  $y$ -solutions are 0 and  $\frac{1}{9}$ , we can conclude that answer choice (A) is correct.