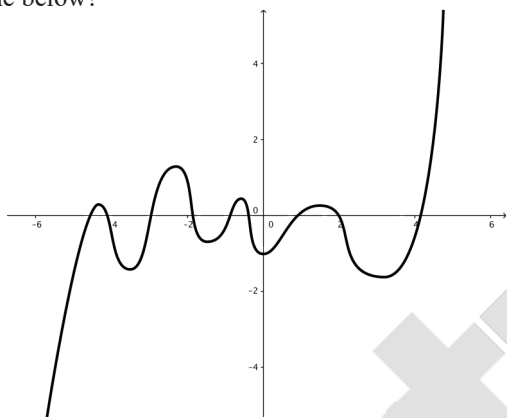


1. The sum of $(-3x^2 + 4x - 8)$ and which of the following polynomials is $(2x^2 - 7x + 10)$?

A. $5x^2 - 11x + 18$
 B. $-5x^2 + 11x - 18$
 C. $5x^2 + 18$
 D. $5x^2 - 18$
 E. $5x^2 - 11x$

2. What is the minimum degree possible for the polynomial function whose graph is shown in the standard (x, y) plane below?



A. 5
 B. 6
 C. 7
 D. 8
 E. 9

3. What is the solution set of the equation $-2x^2 + 7 = 0$?

A. $\left\{-\sqrt{\frac{7}{2}}, \sqrt{\frac{7}{2}}\right\}$
 B. $\{-\sqrt{3}, \sqrt{3}\}$
 C. $\left\{-\frac{4}{2}, \frac{4}{2}\right\}$
 D. $\{-3, 3\}$
 E. $\{-\sqrt{5}, \sqrt{5}\}$

4. The graph of $y = -3x^2 + 5$ passes through the point $(3, 4a)$ in the standard (x, y) coordinate plane. What is the value of a ?

A. 32
 B. -22
 C. 8
 D. -5.5
 E. -8

5. For what nonzero whole number k does the quadratic equation $x^2 + 4kx + k^3$ have exactly 1 real solution for x ?

A. 2
 B. 4
 C. 8
 D. 16
 E. 1

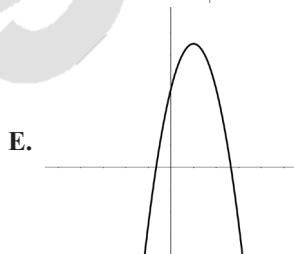
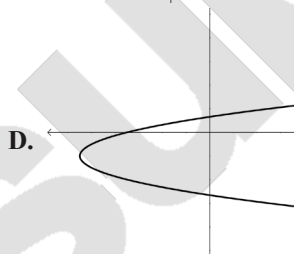
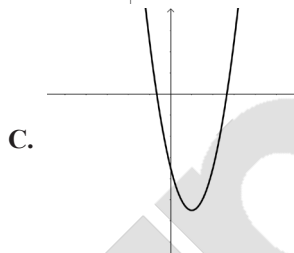
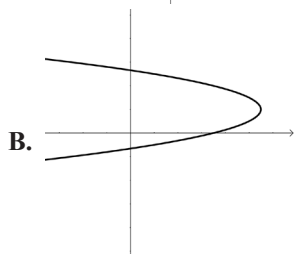
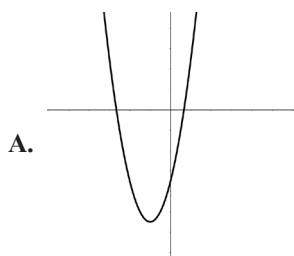
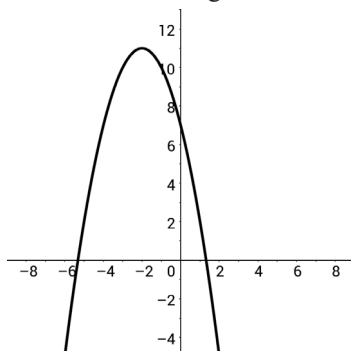
6. Which of the following is the set of real solutions for the equation $5x + 12 = 2(4x + 6)$?

A. The empty set
 B. The set of all real numbers
 C. $\{0, 5\}$
 D. $\left\{\frac{5}{8}\right\}$
 E. $\{0\}$

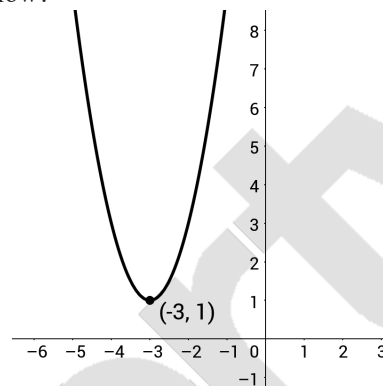
7. In the standard coordinate plane, what is the vertex of the parabola with the equation $y = -4(x + 7)^2 + 2$?

A. $(-7, -2)$
 B. $(7, 2)$
 C. $(7, -2)$
 D. $(-7, 2)$
 E. $(-14, 2)$

8. The graph of the parabola with the equation $y = -x^2 - 4x + 7$ is shown in the standard (x, y) coordinate plane below. Which of the following graphs is the graph of the given equation rotated 90° counterclockwise about the origin?



9. The graph of which of the following equations is the parabola shown in the standard (x, y) coordinate plane below?



A. $y - 1 = (x + 3)^2$

B. $y - 1 = 2(x + 3)^2$

C. $y + 1 = 2(x - 3)^2$

D. $y - 1 = \frac{1}{2}(x + 3)^2$

E. $y + 1 = \frac{1}{2}(x - 3)^2$

10. Using the quadratic formula, what are the two roots for the equation $7x^2 - 3x = 17$?

A. $\frac{3 \pm \sqrt{485}}{14}$

B. $\frac{3 \pm \sqrt{-467}}{14}$

C. $\frac{5}{7}$ and 3

D. $-\frac{5}{7}$ and -3

E. 7

11. For what integer k are both solutions of the equation $x^2 + kx + 19 = 0$ negative integers?

A. 20

B. 19

C. 1

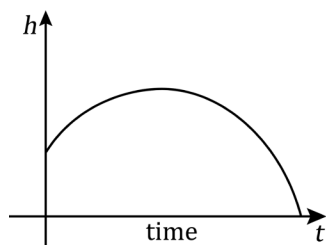
D. -19

E. -20

12. The solution set for x of the equation $x^2 + mx - 4 = 0$ is $\{-4, 1\}$. What does m equal?

A. 1
B. 4
C. -4
D. 3
E. -3

13. The graph of the equation $-at^2 + bt + c = 0$, which describes how the height, h , of an object that is thrown directly upward, changes over time, t , is shown below.



If you alter only this equations a term, the leading coefficient, the alteration has an effect on which of the following?

- I. The t -intercept
II. The h -intercept
III. The maximum value of h

A. I only
B. II only
C. III only
D. I and II only
E. I and III only

14. Which of the following equations shows a correct use of the quadratic formula to solve $2x^2 + 8x - 1 = 0$?

A. $x = \frac{8 \pm \sqrt{64 - 4(2)(-1)}}{2(2)}$
B. $x = \frac{-8 \pm \sqrt{64 - 4(2)(1)}}{2(2)}$
C. $x = \frac{-8 \pm \sqrt{64 - 4(2)(-1)}}{2(2)}$
D. $x = \frac{8 \pm \sqrt{64 - 4(2)(-1)}}{2}$
E. $x = \frac{-8 \pm \sqrt{64 - 4(2)(1)}}{2}$

15. In the equation $x^2 + 2mx - \left(\frac{1}{2}\right)n = 0$, m and n are integers. The *only* possible value for x is -2 . What is the value of n ?

A. -2
B. -8
C. 2
D. 8
E. 4

16. $7w^3 + 65w - w^3 - 20 - 35w + 2$ is equivalent to:

A. $8w^3 + 30w - 22$
B. $6w^3 + 30w - 22$
C. $6w^3 + 30w - 18$
D. $18w^3$
E. $18w$

17. What polynomial must be added to $2x^3 - 4x - 6$ so that the sum is $-x^3 - 4$?

A. $4x - x^3 + 2$
B. $4x - 3x^3 + 2$
C. $-x^3 - 4x - 2$
D. $-3x^3 - 4x - 2$
E. $-3x^3 - 4x + 2$

18. The height about the ground, h , of an object t seconds after being thrown from the top of a building is given by the equation $h = -3t^2 + 15t + 18$. An equivalent factored form of this equation shows that the object:

A. Starts at a point 6 units off the ground
B. Reaches the ground in 6 seconds
C. Reaches the ground in 1 second
D. Reaches a maximum in 18 seconds
E. Reaches a maximum in 1 second

19. Which of the following expressions is equivalent to $(3x^3 + 5) - (2x^2 - 6x + 7) + (7x - 5) - (5x^2 + 3x + 3x + 2x)$?

A. $3x^3 - 7x^2 + 5x - 7$
B. $3x^3 - 10x^2 + 9x + 7$
C. $-7x^2 + 5x - 7$
D. $3x^3 - 7$
E. $3x^3 + 5x - 7$

20. $(x+4y-2z)-(-3x+2y+5z)$ is equivalent to:

- A. $-2x+8y+3z$
- B. $-3x+2y-7z$
- C. $4x+2y-7z$
- D. $-3x+8y+3z$
- E. $4x+2y+3z$

21. If $f(x)=4x^3-64x$, which of the following correctly describes the zeroes of the polynomial? (Zeroes are the values where $f(x)=0$.)

- A. 2 different rational zeroes
- B. No real zeroes
- C. Only 1 rational zero
- D. 3 different rational zeroes
- E. 1 number is a double zero

22. One of the roots of $4x^3-18x^2+32x-24=0$ is 2. What are the other roots?

- A. $\frac{5}{2} \pm i\sqrt{23}$
- B. $\frac{5}{4} \pm \sqrt{23}$
- C. $\frac{5}{4} \pm \frac{i\sqrt{23}}{4}$
- D. $\frac{5}{2} \pm \frac{i\sqrt{23}}{2}$
- E. $5 \pm i\sqrt{23}$

23. What is the value of c if $x+1$ is a factor of $x^3+2x^2-cx-20$?

- A. 19
- B. 18
- C. 17
- D. 16
- E. 15

24. What is the equivalent of $(n+4)^3$?

- A. n^3+64
- B. $n^3+6n^2+24n+32$
- C. $n^3+12n^2+48n+64$
- D. $n^3+12n^2+48n+32$
- E. $n^3+24n^2+48n+64$

25. Consider the equation $y=-(x+2)^2-4$, where x and y are both real numbers. The table below gives the values of y for selected values of x .

x	y
-11	-85
-9	-53
-7	-29
-5	-13
-3	-5
-1	-5
1	-13

For the equation above, which of the following values of x gives the greatest value of y ?

- A. -8
- B. -6
- C. -4
- D. -2
- E. 0

26. Which of the following values is a zero of $f(x)=3x^4+8x^3+4x^2$?

- A. $\frac{2}{3}$
- B. $\frac{3}{2}$
- C. -2
- D. 3
- E. -3

27. Which of the following expressions is equivalent to $4x^4-8x^2-24$?

- A. $(x^2+1)(x^2-3)$
- B. $4(x+1)(x-3)$
- C. $4(x+8)(x-3)$
- D. $4(x^2+3)(x^2-8)$
- E. $4(x^2+1)(x^2-3)$

28. Which of the following is NOT a factor of $a^7 - 81a^3$?

- A. a
- B. a^2
- C. $a+3$
- D. $a-3$
- E. a^2+3

29. The function $f(x)$ is a cubic polynomial that has the value of 0 when x is 0, -3, and 4. If $f(1) = -6$, which of the following is an expression for $f(x)$?

- A. $x(x-3)(x+4)$
- B. $x(x+3)(x-4)$
- C. $2x(x+3)(x-4)$
- D. $\frac{x}{2}(x+3)(x-4)$
- E. $x^2(x-3)(x+4)$

30. $f(x)$ is a quartic (fourth order) polynomial that has zeroes at $x=2, 6, -4, -9$. If $f(3) = 63$, which of the following is an expression for $f(x)$?

- A. $(x-2)(x-6)(x+4)(x+9)$
- B. $\frac{1}{4}(x-2)(x-6)(x+4)(x+9)$
- C. $-\frac{1}{4}(x-2)(x-6)(x+4)(x+9)$
- D. $\frac{1}{4}(x+2)(x-6)(x+4)(x+9)$
- E. $-\frac{1}{4}(x+2)(x+6)(x-4)(x-9)$

ANSWER KEY

1. A 2. E 3. A 4. D 5. B 6. E 7. D 8. D 9. A 10. A 11. A 12. D 13. E 14. C
 15. B 16. C 17. B 18. B 19. A 20. C 21. D 22. C 23. A 24. C 25. D 26. C 27. E 28. E
 29. D 30. C

ANSWER EXPLANATIONS

- A.** We wish to solve the equation $-3x^2 + 4x - 8 + Y = 2x^2 - 7x + 10$ for the polynomial Y . So, subtracting $-3x^2 + 4x - 8$ on both sides, we get $Y = 2x^2 - 7x + 10 - (-3x^2 + 4x - 8)$. Distributing the negative sign, we get $Y = 2x^2 - 7x + 10 + 3x^2 - 4x + 8$. Now, combining like terms, we get $Y = 5x^2 - 11x + 18$.
- E.** For a polynomial with n turning points (whenever the slope of the graph changes signs, the minimum degree of the polynomial is $n+1$). The graph has 8 turning points, so the minimum degree of the polynomial is $8+1=9$.
- A.** Using the quadratic formula with $a=-2$, $b=0$, and $c=7$, we have:

$$x = \frac{0 \pm \sqrt{4(-2)(7)}}{2(-2)} = \pm \frac{\sqrt{56}}{-4} = \pm \frac{2\sqrt{14}}{4} = \pm \frac{\sqrt{14}}{2} = \pm \frac{\sqrt{14}}{\sqrt{4}} = \pm \sqrt{\frac{14}{4}} = \pm \sqrt{\frac{7}{2}}$$
- D.** Plugging in $x=3$, we get $y = -3(3)^2 + 5 = -3(9) + 5 = -27 + 5 = -22$. So, we can equate $4a = -22 \rightarrow a = -\frac{22}{4} = -5.5$
- B.** If the polynomial only has one solution, it means that it is a perfect square that can be factored into $(x+a)(x+a)$. So, we set $x^2 + 4kx + k^3 = (x+a)(x+a) = x^2 + 2ax + a^2$. This means that $2ax = 4kx$ and $a^2 = k^3$. Simplifying the first equation, we get $a = 2k$. Plugging in this value for a in $a^2 = k^3$, we get $(2k)^2 = k^3 \rightarrow 4k^2 = k^3 \rightarrow k = 4$.
- E.** Distributing the 2 on the right hand side of the equation, we get $5x + 12 = 8x + 12$. Subtracting 12 on both sides, we get $5x = 8x$. This is only true if $x = 0$.
- D.** The equation of a parabola is in the form $y = a(x-h)^2 + k$ where (h,k) is the vertex of the parabola. So, the parabola with equation $y = -4(x+7)^2 + 2$ has vertex $(-7,2)$.
- D.** Although we could attempt to figure out what the original parabola looked like and then try to match specific points to a graph, since we know that the original parabola was downward facing ($-x^2$), we know that rotating the graph 90° would produce a parabola that opens to the right. Only one answer choice has a rightwards-opening parabola.
- A.** The parabola shown has a vertex at $(-3,1)$, so when $x=-3$ and $y=1$, the equation must be true. We see that when we plug these values into answer choice A, we get $y-1 = 2(x+3)^2 \rightarrow 1-1 = 2(-3+3)^2 \rightarrow 0=0$. The vertex of answer choices A, B, and D are the same, but the parabola in the figure also passes through $(-2,2)$, which is only true of answer choice A.
- A.** We first subtract 17 on both sides to bring everything to the left side of the equation. We get $7x^2 - 3x - 17 = 0$. Now, we plug in $a=7$, $b=-3$, and $c=-17$ into the quadratic equation to get:

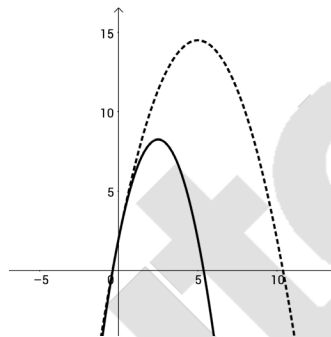
$$x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(7)(-17)}}{2(7)} = \frac{3 \pm \sqrt{9+476}}{14} = \frac{3 \pm \sqrt{485}}{14}$$

- A.** We plug in the values $a=1$, $b=k$ and into the quadratic equation to get the value of x . We get

$$x = \frac{-k \pm \sqrt{k^2 - 4(1)(19)}}{2(1)} = \frac{-k \pm \sqrt{k^2 - 76}}{2}$$
 If both solutions for x are negative, then we know that $\frac{-k + \sqrt{k^2 - 76}}{2}$ is negative and $\frac{-k - \sqrt{k^2 - 76}}{2}$. This means that k is positive because if k were negative, the negative sign in front of it

will cancel it out to make x a positive value. We also know that in order for $\frac{-k - \sqrt{k^2 - 76}}{2}$ to be an integer, $\sqrt{k^2 - 76}$ must be an integer. If we plug in the positive answer choices 20, 19 and 1 for k , we see that only $k = 20$ gives us an integer solution. $\sqrt{20^2 - 76} = 18$ while $\sqrt{19^2 - 76} = 16.88$ and $\sqrt{1^2 - 76} = \text{undefined}$.

12. **D.** The question says that -4 and 1 are solutions to a quadratic equation, so it's best to work backwards. If those are solutions, then $(x - 1)(x + 4) = 0$. FOIL to get $x^2 + 3x - 4 = 0$. Comparing the equation given with the one we found, we see that $m = 3$.
13. **E.** The best way to solve this is to graph our own made up, arbitrary examples on a calculator and see for ourselves. Try graphing $-x^2 + 5x + 2$ and $-\frac{1}{2}x^2 + 5x + 2$.



From the graphs we can see that the x -intercept (t in the question) and the vertex have moved, but the y -intercept (h in the question) hasn't. If we don't have a graphing calculator or don't have time to graph them, remember that the leading coefficient of a parabola can tell us only a couple things about the parabola: its sign indicates what direction the parabola is facing, its magnitude tells how 'fat' or 'skinny' the parabola is, and it's used to determine the x -value of the vertex, whose formula is $-\frac{b}{2a}$. Thus, altering the a term would potentially change both the x and y value of the vertex, and the y value is the maximum height. However, the only way to change the y -intercept would be to change the c value, so it makes sense that the y -intercept would stay the same, as c is not affected when changing the a value.

14. **C.** The quadratic formula is $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$, so plugging in 2 for a , 8 for b , and -1 for c , we get $\frac{-8 \pm \sqrt{64 - 4(2)(-1)}}{2(2)}$, answer (C).
15. **B.** We cannot solve this by plugging in -2 and trying to factor. Instead, work backwards. Think about what the question means by "the *only* possible value for x is -2 ". Putting together the fact that it must be a polynomial of degree two, which means that if factored there would be two expressions with x , and that both must show that $x = -2$, it makes sense to assume that $(x + 2)(x + 2) = 0$. Simplify to get $x^2 + 4x + 4$. Compare this with the expression given, and we realize that $2mx = 4$ and $-\frac{1}{2}n = 4$. Solving for n in the second equation gives us -8 .
16. **C.** Add like terms:

$$\begin{aligned} &7w^3 + 65w - w^3 - 20 - 35w + 2 \\ &= 7w^3 - w^3 + 65w - 35w - 20 + 2 \\ &= 6w^3 + 30w - 18 \end{aligned}$$

17. **B.** If $2x^3 - 4x - 2$ plus some random expression equals $-x^3 - 4$, then subtract the first from the second:

$$\begin{aligned} &(-x^3 - 4) - (2x^3 - 4x - 2) \\ &= -x^3 - 2x^3 - (-4x) - 4 - (-2) \\ &= -3x^3 + 4x - 2 \end{aligned}$$

which is answer (B).

18. **B.** Looking at the coefficients, realize that we can pull out -3 , which gives us $h(t) = -3(t^2 - 5t - 6)$, which is much easier to factor. $h(t) = -3(t^2 - 5t - 6)$ factored becomes $h(t) = -3(t - 6)(t + 1)$. Since the graph relates height and time, we know that $h = 0$ at $t = 6$ seconds and $t = -1$ seconds. There is no such thing as negative time, so we know that the ball is dropped from a height of 18 feet (our y -intercept found from the original form) and hits the ground at $t = 6$. Looking at our answer choices, hitting the ground after 6 seconds is the only correct statement.
19. **A.** Distributing out the negative signs, we write the expression as $3x^3 + 5 - 2x^2 + 6x - 7 + 7x - 5 - 5x^2 - 3x - 3x - 2x$. Adding like terms, we get $3x^3 - 2x^2 - 5x^2 + 6x + 7x - 3x - 3x - 2x + 5 - 7 - 5 = 3x^3 - 7x^2 + 5x - 7$.
20. **C.** Distributing out the negative sign, we get $x + 4y - 2z + 3x - 2y - 5z$. Adding like terms, we get $x + 3x + 4y - 2y - 2z - 5z = 4x + 2y - 7z$.
21. **D.** Factoring out $4x$, we get $f(x) = 4x(x^2 - 16)$. $x^2 - 16$ is a difference of squares, so we can rewrite the equation as $f(x) = 4x(x + 4)(x - 4)$. This gives us three different rational zeros. Namely, 0, 4, and -4 .
22. **C.** We can first factor out 2 from the equation because every term in the equation is divisible by 2. We get $2(2x^3 - 9x^2 + 16x - 12) = 0$. Knowing that 2 is a root, we know that when $x = 2$, the equation equals zero. Thus, it must have the factor $(x - 2)$. Using long division to factor out $(x - 2)$, we get $2(x - 2)(2x^2 - 5x + 6) = 0$. Now, we find the remaining two roots by using the quadratic formula on $2x^2 - 5x + 6$. Plugging in $a = 2$, $b = -5$, and $c = 6$, we get
$$x = \frac{-(-5) \pm \sqrt{(-5)^2 - 4(2)(6)}}{2(2)} = \frac{5 \pm \sqrt{25 - 48}}{4} = \frac{5 \pm \sqrt{-23}}{4} = \frac{5}{4} \pm \frac{i\sqrt{23}}{4}.$$
23. **A.** Using long division to factor out $(x + 1)$ from $x^3 + 2x^2 - cx - 20$, we get $(x + 1)(x^2 + x - (c + 1))$ where the constant term is equal to 20. $c + 1 = 20$ so $c = 19$.
24. **C.** Foiling out $(n + 4)^3$, we get $(n + 4)^3 = (n + 4)(n^2 + 8n + 16) = (n^3 + 4n^2 + 8n^2 + 32n + 16n + 64) = n^3 + 12n^2 + 48n + 64$
25. **D.** Without even looking at the table, we see that the equation is in vertex form. From the equation we see that it is a downward facing parabola (because the leading term is negative) with a vertex at $(-2, -4)$. Because the parabola is facing down, we know the vertex has the greatest y -value, so the answer is -2 . Alternatively, looking at the table we see that the y -values increase while $x < -3$, and decrease when $x > -1$, so the greatest point must be in between those two numbers, and -2 is the only answer that fulfills that condition.
26. **C.** First factor out an x^2 : $f(x) = 3x^4 + 8x^3 + 4x^2 \rightarrow f(x) = x^2(3x^2 + 8x + 4)$. Now we can factor by reverse foiling: $f(x) = x^2(3x + 2)(x + 2)$. Our zeros are: 0, $-\frac{2}{3}$, and -2 , and -2 is the only correct answer given.
27. **E.** Notice that we can pull out a constant of 4: $4x^4 - 8x^2 - 24 \rightarrow 4(x^4 - 2x^2 - 6)$. We don't know how to factor polynomials to the fourth degree easily, but we can substitute. If we let $w = x^2$, our expression becomes $4(w^2 - 2w - 6)$, which factors easily into $4(w + 1)(w + 3)$. When we plug back in x^2 for w , we get $4(x^2 + 1)(x^2 - 3)$.
28. **E.** Factor out a^3 and then look at the problem as the difference between squares:

$$a^7 - 81a^3 \rightarrow a^3(a^4 - 3^4) \rightarrow a^3((a^2)^2 - (3^2)^2) \rightarrow a^3(a^2 - 3^2)(a^2 + 3^2) \rightarrow a^3(a - 3)(a + 3)(a^2 + 9)$$
 Thus, $a, a^2, a^3, (a + 3), (a - 3), (a^2 - 9)$, and $(a^2 + 9)$ are all factors, but $a^2 + 3$ is not.
29. **D.** If our zeros are at 0, -3 , and 4, then we can say that $f(x) = x(x + 3)(x - 4)$. When we plug in 1 to test, $f(1) = 1(1 + 3)(1 - 4) = -12 \neq -6$. In order to satisfy the condition that says that $f(1) = -6$, we look at what our $f(1)$ currently equals and adapt the equation accordingly. In order to get $f(1) = -6$, we must divide our current $f(1)$ by 2, so our equation becomes $\frac{x}{2}(x + 3)(x - 4)$.

30. Since 2, 6, -4, and -9 are zeros for the polynomial, we know that it can be written in the form $(x-2)(x-6)(x+4)(x+9)k=0$ for some constant k . We are given that $f(3)=63$, so plugging in 3, we have $(3-2)(3-6)(3+4)(3+9)k=63 \rightarrow 1(-3)(7)(12)k=63 \rightarrow -252k=63 \rightarrow k=-\frac{63}{252}=-\frac{1}{4}$. So, the polynomial is $-\frac{1}{4}(x-2)(x-6)(x+4)(x+9)$.