

ALUNA: FÁBIA DA SILVA FURTOSO

Exercício 1 - Semana 07

03 moedas

$$P(C) = p = 1/2$$

$$P(C) = 1 - p$$

Resultados possíveis

Ω
 $\left\{ \begin{array}{l} CCC \\ CC\bar{C} \\ C\bar{C}\bar{C} \\ \bar{C}\bar{C}\bar{C} \\ \bar{C}\bar{C}C \\ \bar{C}CC \\ C\bar{C}\bar{C} \\ CCC \end{array} \right.$

Probabilidades associadas

$$\begin{aligned}
 p^3 &= (1/2)^3 = 1/8 \\
 pp(1-p) &= p^2(1-p) = (1/2)^2 \cdot (1 - 1/2) = 1/8 \\
 p \cdot (1-p)^2 &= 1/2 \cdot (1 - 1/2)^2 = 1/8 \\
 (1-p)^3 &= (1 - 1/2)^3 = 1/8 \\
 (1-p)^2 p &= (1 - 1/2)^2 \cdot 1/2 = 1/8 \\
 (1-p) \cdot p^2 &= (1 - 1/2) \cdot (1/2)^2 = 1/8 \\
 (1-p)^2 \cdot p &= 1/8 \\
 p^2(1-p) &= 1/8
 \end{aligned}$$

Nº caras

3
2
1
0
1
2
1
2

$$X \in \{0, 1, 2, 3\}$$

$$P(X=i) > 0$$

$$P(X=0) = (1-p)^3 = 1/8$$

$$\begin{aligned}
 P(X=1) &= (1-p)^2 \cdot p + (1-p) \cdot p^2 + p(1-p)^2 \\
 &= 1/8 + 1/8 + 1/8 + 1/8 \\
 &= 3/8
 \end{aligned}$$

$$P(X=2) = (1-p) \cdot p^2 + p^2(1-p) + p^2(1-p) = 3/8$$

$$P(X=3) = p^3 = 1/8$$

FDP

$$F(x) = \begin{cases} 1/8 & \text{se } x=0 \\ 3/8 & \text{se } x=1 \\ 3/8 & \text{se } x=2 \\ 1/8 & \text{se } x=3 \\ 0 & \text{caso contrário} \end{cases}$$

FDA

$$F(x) = P(X \leq x) \quad x \in \mathbb{R}$$

$$F(x) = \begin{cases} 0 & x < 0 \\ 1/8 & 0 \leq x < 1 \\ 3/8 & 1 \leq x < 2 \\ 7/8 & 2 \leq x < 3 \\ 1 & x \geq 3 \end{cases}$$

