Capstone TCD project note II

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```
library(caret)
## Loading required package: lattice
## Loading required package: ggplot2
library(class)
library(devtools)
## Loading required package: usethis
library(e1071)
library(ggplot2)
library(Hmisc)
## Loading required package: survival
## Attaching package: 'survival'
## The following object is masked from 'package:caret':
##
##
       cluster
## Loading required package: Formula
## Attaching package: 'Hmisc'
## The following object is masked from 'package:e1071':
##
##
       impute
```

```
## The following objects are masked from 'package:base':
##
##
       format.pval, units
library(klaR)
## Loading required package: MASS
library(MASS)
library(nnet)
library(plyr)
## Attaching package: 'plyr'
## The following objects are masked from 'package:Hmisc':
##
##
       is.discrete, summarize
library(pROC)
## Type 'citation("pROC")' for a citation.
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##
       cov, smooth, var
library(psych)
##
## Attaching package: 'psych'
## The following object is masked from 'package:Hmisc':
##
##
       describe
```

```
## The following objects are masked from 'package:ggplot2':
##
##
       %+%, alpha
library(scatterplot3d)
library(SDMTools)
## Registered S3 method overwritten by 'R.oo':
##
    method
                   from
     throw.default R.methodsS3
##
##
## Attaching package: 'SDMTools'
## The following object is masked from 'package:pROC':
##
##
       auc
## The following objects are masked from 'package:caret':
##
##
       sensitivity, specificity
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:plyr':
##
##
       arrange, count, desc, failwith, id, mutate, rename, summarise,
##
       summarize
## The following object is masked from 'package:MASS':
##
##
       select
## The following objects are masked from 'package:Hmisc':
##
##
       src, summarize
```

```
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
library(ElemStatLearn)
##
## Attaching package: 'ElemStatLearn'
## The following object is masked from 'package:plyr':
##
##
       ozone
library(rpart)
library(rpart.plot)
library(randomForest)
## randomForest 4.6-14
## Type rfNews() to see new features/changes/bug fixes.
##
## Attaching package: 'randomForest'
## The following object is masked from 'package:dplyr':
##
##
       combine
## The following object is masked from 'package:psych':
##
##
       outlier
## The following object is masked from 'package:ggplot2':
##
##
       margin
```

```
##
## Attaching package: 'neuralnet'

## The following object is masked from 'package:dplyr':
##
## compute
```

Recap of Project note 1

. In the data set earlier we found it consists 30000 observations with 25 variables. . The categorical data value like Sex , martial status and education has changed to numeric value . . We have realized that 22.1 % percent defaulter and 77.9% are not default cases . Default category whereas male customer are 9.6% and female category shows 12.5% . . University level - graduate or PG is more into default side . Married customers somehow leaning to tend defaulter . Average age of 25 to 30 is the highest risk . . We have also checked the multicollinearity problems is existed In the data set . . pay status categorical variables are dependent on each other and impact of REPAY_ SEP to REPAY_APR variables to default. Payment DEFAULT is high. . We have also created some dummy variables like ratio of the payment for each month SEP to APR and balance amount month wise from SEP to APR .

Suppllimantry Over view of EDA

We have been checking here the relationship of paid amount SEP to APR and balance amount((billed outstanding amount - paid amount) we assumed that bank is keep on adding the preceding month balance to current month)

importing the data from Note 1

Ratio is alrady added in the data set .

```
library(readx1)
#Importing Data set
setwd("C:/Users/SuprasannaPradhan/Documents/My Files/Great Lakes Projects/Capstone Pro
ject TCD")
bank_data_2nd=read.csv("bank_data_new.csv")
bank_data_2=read.csv("taiwan_bank3.csv")
names(bank_data_2)
```

Finding outliers and NA values

```
bank_data_n1 <- subset(bank_data_2nd, select = -c(1:2))
bank_data1 <- cbind(bank_data_n1,bank_data_2[21:26])
str(bank_data1)</pre>
```

```
## 'data.frame':
                   30000 obs. of 36 variables:
## $ LIMIT_BAL : num 20000 120000 90000 50000 50000 50000 100000 140000 200
00 ...
##
   $ SEX
                 : int 2 2 2 2 1 1 1 2 2 1 ...
##
   $ EDUCATION
                 : int
                        2 2 2 2 2 1 1 2 3 3 ...
   $ MARRIAGE
                       1 2 2 1 1 2 2 2 1 2 ...
##
                 : int
##
   $ AGE
                 : int
                        24 26 34 37 57 37 29 23 28 35 ...
   $ REPAY SEP
                : int 2 -1 0 0 -1 0 0 0 0 -2 ...
##
   $ REPAY_AUG
                : int 2 2 0 0 0 0 0 -1 0 -2 ...
##
   $ REPAY JUL
                 : int -1 0 0 0 -1 0 0 -1 2 -2 ...
   $ REPAY_JUN
                 : int -1 0 0 0 0 0 0 0 0 -2 ...
##
   $ REPAY MAY
                 : int -2 0 0 0 0 0 0 0 0 -1 ...
##
   $ REPAY_APR
                 : int -2 2 0 0 0 0 0 -1 0 -1 ...
##
   $ BILL AMT SEP: num 3913 2682 29239 46990 8617 ...
   $ BILL_AMT_AUG: num 3102 1725 14027 48233 5670 ...
##
   $ BILL AMT JUL: num 689 2682 13559 49291 35835 ...
##
   $ BILL AMT JUN: num 0 3272 14331 28314 20940 ...
##
   $ BILL AMT MAY: num 0 3455 14948 28959 19146 ...
##
   $ BILL AMT APR: num 0 3261 15549 29547 19131 ...
   $ PAID_AMT_SEP: num 0 0 1518 2000 2000 ...
##
##
   $ PAID AMT AUG: num 689 1000 1500 2019 36681 ...
   $ PAID AMT JUL: num 0 1000 1000 1200 10000 657 38000 0 432 0 ...
##
   $ PAID AMT JUN: num 0 1000 1000 1100 9000 ...
##
   $ PAID_AMT_MAY: num 0 0 1000 1069 689 ...
   $ PAID AMT APR: num 0 2000 5000 1000 679 ...
##
##
   $ DEFAULT
                 : int 1100000000...
##
   $ RATIO_SEP
                 : num 0 0 5 4 23 4 15 3 29 NA ...
##
   $ RATIO AUG
                 : num
                       22 58 11 4 647 3 10 158 0 NA ...
##
   $ RATIO JUL
                 : num
                        0 37 7 2 28 1 9 0 4 NA ...
   $ RATIO_JUN
                 : num NA 31 7 4 43 ...
##
   $ RATIO_MAY
                 : num NA 29 7 4 47 5 4 -365 8 100 ...
##
                 : num NA 31 6 4 47 5 4 102 27 93 ...
   $ RATIO_APR
   $ balance SEP : num 3913 2682 27721 44990 6617 ...
##
   $ balance_AUG : num 2413 725 12527 46214 -31011 ...
##
   $ balance JUL : num 689 1682 12559 48091 25835 ...
##
   $ balance_JUN : num  0 2272 13331 27214 11940 ...
   $ balance MAY : num  0 3455 13948 27890 18457 ...
  $ balance_APR : num  0 1261 10549 28547 18452 ...
```

```
summary(bank_data1)
```

```
##
      LIMIT_BAL
                          SEX
                                        EDUCATION
                                                        MARRIAGE
##
   Min. : 10000
                     Min. :1.000
                                     Min.
                                             :0.000
                                                     Min.
                                                            :0.000
    1st Ou.: 50000
                     1st Ou.:1.000
                                      1st Qu.:1.000
                                                      1st Qu.:1.000
##
    Median : 140000
                     Median :2.000
                                      Median :2.000
                                                     Median :2.000
##
   Mean
         : 167484
                     Mean :1.604
                                     Mean :1.853
                                                     Mean
                                                            :1.552
##
    3rd Qu.: 240000
                     3rd Qu.:2.000
                                      3rd Qu.:2.000
                                                      3rd Qu.:2.000
##
    Max.
           :1000000
                     Max.
                            :2.000
                                      Max.
                                             :6.000
                                                      Max.
                                                             :3.000
##
##
        AGE
                     REPAY_SEP
                                       REPAY AUG
                                                          REPAY_JUL
##
           :21.00
                    Min. :-2.0000
                                      Min. :-2.0000
                                                        Min. :-2.0000
   Min.
##
    1st Qu.:28.00
                    1st Qu.:-1.0000
                                      1st Qu.:-1.0000
                                                        1st Qu.:-1.0000
   Median :34.00
                    Median : 0.0000
                                      Median : 0.0000
##
                                                        Median : 0.0000
##
   Mean :35.49
                    Mean :-0.0167
                                     Mean :-0.1338
                                                        Mean :-0.1662
##
    3rd Ou.:41.00
                    3rd Ou.: 0.0000
                                      3rd Qu.: 0.0000
                                                        3rd Qu.: 0.0000
   Max. :79.00
##
                    Max.
                          : 8.0000
                                      Max.
                                             : 8.0000
                                                        Max. : 8.0000
##
##
      REPAY JUN
                        REPAY MAY
                                         REPAY APR
                                                           BILL AMT SEP
                                                         Min. :-165580
##
   Min.
          :-2.0000
                     Min.
                           :-2.0000
                                       Min.
                                              :-2.0000
    1st Qu.:-1.0000
                     1st Qu.:-1.0000
                                       1st Qu.:-1.0000
                                                          1st Qu.:
##
                                                                    3559
##
   Median : 0.0000
                     Median : 0.0000
                                       Median : 0.0000
                                                         Median : 22382
   Mean :-0.2207
                     Mean :-0.2662
                                       Mean :-0.2911
##
                                                          Mean
                                                                : 51223
##
    3rd Qu.: 0.0000
                     3rd Qu.: 0.0000
                                        3rd Qu.: 0.0000
                                                          3rd Qu.: 67091
##
          : 8.0000
                     Max. : 8.0000
                                       Max. : 8.0000
    Max.
                                                         Max.
                                                                : 964511
##
##
     BILL AMT AUG
                     BILL AMT JUL
                                        BILL AMT JUN
                                                          BILL AMT MAY
##
           :-69777
                     Min.
                          :-157264
                                       Min.
                                             :-170000
                                                         Min.
                                                               :-81334
   Min.
##
    1st Qu.: 2985
                     1st Qu.:
                               2666
                                       1st Qu.:
                                                 2327
                                                         1st Qu.: 1763
    Median : 21200
                     Median : 20089
                                       Median : 19052
                                                         Median : 18105
##
          : 49179
                                                              : 40311
                          : 47013
                                       Mean : 43263
##
    Mean
                     Mean
                                                         Mean
    3rd Qu.: 64006
                     3rd Qu.: 60165
                                       3rd Qu.: 54506
                                                         3rd Qu.: 50191
##
##
    Max.
          :983931
                    Max. :1664089
                                       Max. : 891586
                                                        Max. :927171
##
##
     BILL AMT APR
                      PAID AMT SEP
                                       PAID AMT AUG
                                                          PAID AMT JUL
##
   Min.
          :-339603
                     Min.
                                  0
                                       Min.
                                                    0
                                                        Min.
                                                                     0
                           :
                                                               :
##
    1st Qu.:
              1256
                     1st Qu.:
                               1000
                                       1st Qu.:
                                                  833
                                                         1st Qu.:
                                                                   390
    Median : 17071
                     Median :
                               2100
                                       Median :
                                                  2009
                                                         Median: 1800
##
##
    Mean
         : 38872
                     Mean
                           :
                               5664
                                       Mean
                                                  5921
                                                         Mean
                                                              : 5226
##
    3rd Qu.: 49198
                      3rd Qu.: 5006
                                       3rd Qu.:
                                                  5000
                                                         3rd Qu.: 4505
##
    Max.
          : 961664
                     Max.
                             :873552
                                       Max.
                                             :1684259
                                                         Max.
                                                                :896040
##
##
     PAID_AMT_JUN
                     PAID_AMT_MAY
                                        PAID AMT APR
                                                             DEFAULT
##
   Min.
                0
                    Min. :
                                 0.0
                                       Min. :
                                                     0.0
                                                          Min.
                                                                  :0.0000
              296
                               252.5
    1st Qu.:
                     1st Qu.:
                                        1st Qu.:
                                                  117.8
                                                           1st Qu.:0.0000
##
##
    Median: 1500
                     Median: 1500.0
                                        Median : 1500.0
                                                           Median :0.0000
           : 4826
                           : 4799.4
##
   Mean
                     Mean
                                       Mean
                                              : 5215.5
                                                           Mean
                                                                  :0.2212
    3rd Qu.: 4013
                     3rd Qu.: 4031.5
                                        3rd Qu.: 4000.0
                                                           3rd Qu.:0.0000
##
           :621000
                     Max. :426529.0
                                        Max. :528666.0
##
    Max.
                                                           Max.
                                                                  :1.0000
##
```

```
##
      RATIO SEP
                            RATIO AUG
                                                 RATIO JUL
##
    Min.
            :-3543600
                                 :-1025950
                                                       :-8215000
                         Min.
                                               Min.
##
    1st Qu.:
                     4
                         1st Qu.:
                                          4
                                               1st Qu.:
                                                                3
                                               Median :
##
    Median:
                     6
                         Median :
                                          6
                                                                5
##
    Mean
                   Inf
                                        Inf
                                                             Inf
                         Mean
                                               Mean
##
    3rd Qu.:
                    30
                         3rd Qu.:
                                         30
                                               3rd Qu.:
                                                               25
##
    Max.
                   Inf
                         Max.
                                        Inf
                                               Max.
                                                             Inf
    NA's
            :1468
                         NA's
                                 :1867
                                                       :2246
##
                                               NA's
##
      RATIO_JUN
                            RATIO_MAY
                                                RATIO_APR
                                                                    balance_SEP
                                 :-430667
                                                      :-1942500
##
    Min.
            :-1726667
                         Min.
                                              Min.
                                                                   Min.
                                                                           :-733744
    1st Ou.:
                         1st Ou.:
                                              1st Ou.:
                                                                   1st Ou.:
                                                                                 745
##
                                                               5
##
    Median:
                     4
                         Median :
                                         5
                                              Median :
                                                                   Median :
                                                                              18551
##
                   Inf
                                       Inf
                                                            Inf
                                                                              45560
    Mean
                         Mean
                                              Mean
                                                                   Mean
                    22
                                        70
                                                             38
                                                                   3rd Qu.:
##
    3rd Qu.:
                         3rd Qu.:
                                              3rd Qu.:
                                                                              62242
                   Inf
                                       Inf
                                                            Inf
                                                                           : 913727
##
    Max.
                         Max.
                                              Max.
                                                                   Max.
##
    NA's
            :2470
                         NA's
                                 :3449
                                              NA's
                                                      :2952
##
     balance_AUG
                             balance_JUL
                                                   balance_JUN
    Min.
            :-1702347.0
                           Min.
                                    :-854641.0
                                                          :-667000
##
    1st Qu.:
                   329.5
                            1st Qu.:
                                         262.8
                                                  1st Qu.:
                                                                230
##
    Median:
                18102.5
                           Median :
                                       17769.0
                                                  Median :
                                                             16970
                43257.9
                                       41787.5
                                                             38437
##
    Mean
                            Mean
                                                  Mean
##
    3rd Ou.:
                59077.8
                            3rd Ou.:
                                       56294.2
                                                  3rd Ou.:
                                                             50260
##
    Max.
               933208.0
                            Max.
                                    :1542258.0
                                                          : 841586
                                                  Max.
##
##
     balance MAY
                         balance APR
            :-414380
                                :-684896
##
    Min.
                        Min.
##
    1st Qu.:
                    0
                        1st Qu.:
                        Median :
##
    Median :
               15538
                                   13926
##
    Mean
               35512
                        Mean
                                   33656
               46962
##
    3rd Qu.:
                        3rd Qu.:
                                   46067
            : 877171
##
    Max.
                        Max.
                                : 911408
##
```

we got here few variables are having outliers ,found almost all continours frequency based variable are having outliers but variables are having extem outlier values these are limit balance, BILL_AMT_JUL ,PAID_AMT_AUG,balance_JUL Dummy ration created from SEP to APR shows lot of NA and inf values.

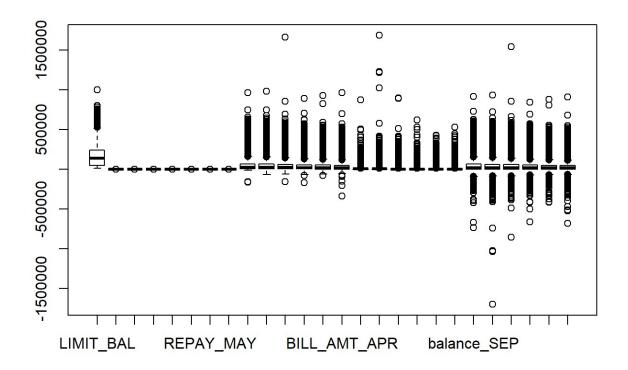
Handling of Ratio paybill amount

Ratio Pay Amount Bill Amount Negative/NaN number 1. If Bill Amount =0: Then convert Ratio to positive 2. Impute NaN to 1 (Higher the ratio, lesser the chance of Default)

```
bank_data1[is.na(bank_data1)] <- 0
sum(is.na(bank_data1))</pre>
```

```
## [1] 0
bank_data1$RATIO_SEP=ifelse(bank_data1$RATIO_SEP<=100,0,1)</pre>
bank_data1$RATIO_AUG=ifelse(bank_data1$RATIO_AUG<=100,0,1)</pre>
bank_data1$RATIO_JUL=ifelse(bank_data1$RATIO_JUL<=100,0,1)</pre>
bank_data1$RATIO_JUN=ifelse(bank_data1$RATIO_JUN<=100,0,1)</pre>
bank_data1$RATIO_MAY=ifelse(bank_data1$RATIO_MAY<=100,0,1)</pre>
bank_data1$RATIO_APR=ifelse(bank_data1$RATIO_APR<=100,0,1)</pre>
str(bank_data1[25:30])
                   30000 obs. of 6 variables:
## 'data.frame':
## $ RATIO_SEP: num 00000000000...
## $ RATIO_AUG: num 0000100100...
## $ RATIO JUL: num 00000000000...
## $ RATIO_JUN: num 000000101...
## $ RATIO_MAY: num 00000000000...
## $ RATIO_APR: num 000000100...
View(bank data1)
#write.csv(bank_data1, file = 'bank_data1.csv')
table(bank_data1$RATIO_SEP)
##
##
      0
            1
## 26302 3698
table(bank_data1$RATIO_AUG)
##
## 26174 3826
table(bank_data1$RATIO_JUL)
##
## 26423 3577
table(bank_data1$RATIO_JUN)
```

```
##
##
       0
             1
## 26613 3387
table(bank_data1$RATIO_MAY)
##
##
             1
       0
## 28992 1008
table(bank_data1$RATIO_APR)
##
##
## 26043 3957
bank_data_bp \leftarrow subset(bank_data1, select = -c(2,3,4,24:30))
names(bank_data_bp)
## [1] "LIMIT_BAL"
                       "AGE"
                                      "REPAY_SEP"
                                                      "REPAY_AUG"
                                      "REPAY_MAY"
                       "REPAY_JUN"
## [5] "REPAY_JUL"
                                                      "REPAY_APR"
## [9] "BILL_AMT_SEP" "BILL_AMT_AUG" "BILL_AMT_JUL" "BILL_AMT_JUN"
## [13] "BILL_AMT_MAY" "BILL_AMT_APR" "PAID_AMT_SEP" "PAID_AMT_AUG"
## [17] "PAID_AMT_JUL" "PAID_AMT_JUN" "PAID_AMT_MAY" "PAID_AMT_APR"
## [21] "balance_SEP"
                                                      "balance_JUN"
                       "balance_AUG"
                                      "balance_JUL"
## [25] "balance_MAY"
                       "balance_APR"
boxplot(bank_data_bp)
```

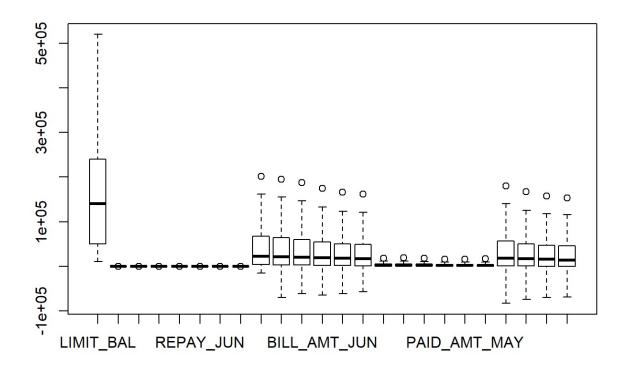


Ratio culmun we are not checking the outliers becuse it values are very low .it is show us the size of the amount ahs been paid for each month ,hence we not incluing these variabels for outlier checking

```
#Capping vairbale outlieres
capOutlier <- function(x){</pre>
   qnt <- quantile(x, probs=c(.25, .75), na.rm = T)</pre>
   caps <- quantile(x, probs=c(.05, .95), na.rm = T)</pre>
   H \leftarrow 1.5 * IQR(x, na.rm = T)
   x[x < (qnt[1] - H)] < - caps[1]
   x[x > (qnt[2] + H)] \leftarrow caps[2]
   return(x)
}
bank data1$LIMIT BAL=capOutlier(bank data1$LIMIT BAL)
bank_data1$BILL_AMT_SEP=capOutlier(bank_data1$BILL_AMT_SEP)
bank_data1$BILL_AMT_AUG=capOutlier(bank_data1$BILL_AMT_AUG)
bank_data1$BILL_AMT_JUL=capOutlier(bank_data1$BILL_AMT_JUL)
bank data1$BILL AMT JUN=capOutlier(bank data1$BILL AMT JUN)
bank_data1$BILL_AMT_MAY=capOutlier(bank_data1$BILL_AMT_MAY)
bank_data1$BILL_AMT_APR=capOutlier(bank_data1$BILL_AMT_APR)
bank_data1$PAID_AMT_SEP=capOutlier(bank_data1$PAID_AMT_SEP)
bank_data1$PAID_AMT_AUG=capOutlier(bank_data1$PAID_AMT_AUG)
bank data1$PAID AMT JUL=capOutlier(bank data1$PAID AMT JUL)
bank_data1$PAID_AMT_JUN=capOutlier(bank_data1$PAID_AMT_JUN)
bank data1$PAID AMT MAY=capOutlier(bank data1$PAID AMT MAY)
bank_data1$PAID_AMT_APR=capOutlier(bank_data1$PAID_AMT_APR)
bank data1$balance SEP=capOutlier(bank data1$balance SEP)
bank_data1$balance_AUG=capOutlier(bank_data1$balance_AUG)
bank data1$balance JUL=capOutlier(bank data1$balance JUL)
bank_data1$balance_JUN=capOutlier(bank_data1$balance_JUN)
bank_data1$balance_MAY=capOutlier(bank_data1$balance_MAY)
bank_data1$balance_APR=capOutlier(bank_data1$balance_APR)
```

Cappped outliers for these variables

```
bank_data_bp1 <- subset(bank_data1,select = -c(2,3,4,24:32))
boxplot(bank_data_bp1)</pre>
```



```
##Checking Data ##
colSums(is.na(bank_data1))
```

```
EDUCATION
                                                                   AGE
##
      LIMIT_BAL
                          SEX
                                                MARRIAGE
##
                                               REPAY_JUN
##
      REPAY_SEP
                    REPAY_AUG
                                  REPAY_JUL
                                                             REPAY_MAY
##
                                                                      0
##
      REPAY_APR BILL_AMT_SEP BILL_AMT_AUG BILL_AMT_JUL BILL_AMT_JUN
##
##
  BILL_AMT_MAY BILL_AMT_APR PAID_AMT_SEP PAID_AMT_AUG PAID_AMT_JUL
##
##
  PAID_AMT_JUN PAID_AMT_MAY PAID_AMT_APR
                                                 DEFAULT
                                                             RATIO_SEP
##
                                                        0
##
      RATIO_AUG
                    RATIO_JUL
                                  RATIO_JUN
                                               RATIO_MAY
                                                             RATIO_APR
##
    balance_SEP
                  balance_AUG
                               balance_JUL
                                             balance_JUN
##
                                                           balance_MAY
##
              0
                            0
                                          0
                                                        0
                                                                      0
    balance_APR
##
##
```

All NA are shown in the dummy variable of ratio, we understand this values are occured due to the paid amount by the cutomser are not paid as the outstanding bill amount shown each month or very less againg of outstandin billed amount .So we would be keeping in as it is , if needed in future we will make them zero .

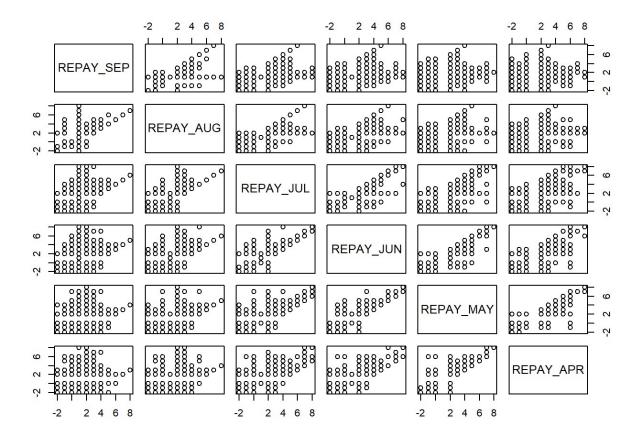
let us chekc the REPAY variables and clsifiy them, timely paid and delayed in payeemnt

According to the description, this REPAY_SEP TO REPAy_APR is a set of categorical variables with the levels:-2 is No consumption; -1 is Paid in full; 0 is The use of revolving credit; 1 is payment delay for one month; 2 is payment delay for two months; . . .; . 8=payment delay for eight months, We have already checked almost all months tend is very high with value of "0", so its indicate moreover people are paid very minimal amount with revolving credit

```
names(bank_data1[6:11])

## [1] "REPAY_SEP" "REPAY_AUG" "REPAY_JUL" "REPAY_JUN" "REPAY_MAY" "REPAY_APR"

plot(bank_data1[6:11])
```



table(bank_data1\$REPAY_SEP)

-2 -1 5686 14737

table(bank_data1\$REPAY_AUG)

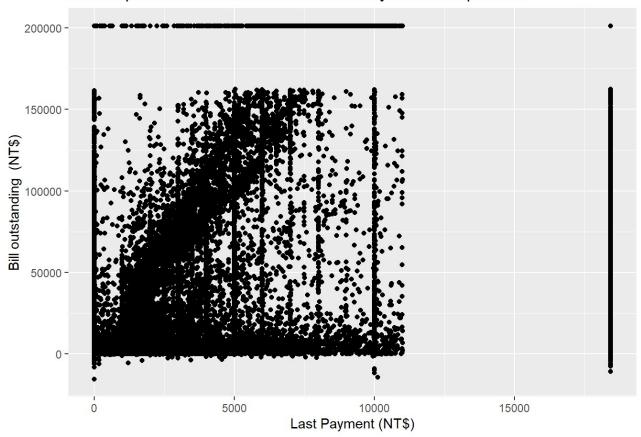
-2 -1 ## 3782 6050 15730 28 3927

table(bank_data1\$REPAY_JUL)

-2 -1 ## 5938 15764

```
table(bank_data1$REPAY_JUN)
##
##
     -2
          -1
                      1
                           2
                               3
                                     4
                                          5
                                                 6 7
                                                           8
## 4348 5687 16455
                      2 3159
                                           35
                                                     58
                                                           2
                               180
                                     69
table(bank data1$REPAY MAY)
##
     -2
          -1
##
                           3
                                4
                                      5
                                           6
                                                7
                                                      8
## 4546 5539 16947 2626
                         178
                                84
                                     17
                                                58
                                                      1
table(bank_data1$REPAY_APR)
##
     -2
##
          -1
                           3
                                      5
                                          6
                                                7
                                                      8
## 4895 5740 16286 2766
                         184
                                49
                                     13
                                          19
                                                46
                                                      2
library(ggplot2)
# plotting scatter plot
sepp <- ggplot(bank_data1, aes(x = PAID_AMT_SEP, y =BILL_AMT_SEP)) +</pre>
 ylab("Bill outstanding (NT$)") + geom_point()
sepp + labs(x = "Last Payment (NT$)") +
 labs(title="Scatter plot between Limit balance And Payment of September")
```

Scatter plot between Limit balance And Payment of September



#Important variables

Creat dummy variables from REPAY_SEP to REPAY_APR

-2 and -1 we have consiered here that customerare paid on time other than that all 0 to 8, we ahvecatogarized as late payer

```
bank_data1$TIMELY_PD_SEP=ifelse(bank_data1$REPAY_SEP>0,0,1)
bank_data1$TIMELY_PD_AUG=ifelse(bank_data1$REPAY_AUG>0,0,1)
bank_data1$TIMELY_PD_JUL=ifelse(bank_data1$REPAY_JUL>0,0,1)
bank_data1$TIMELY_PD_JUN=ifelse(bank_data1$REPAY_JUN>0,0,1)
bank_data1$TIMELY_PD_MAY=ifelse(bank_data1$REPAY_MAY>0,0,1)
bank_data1$TIMELY_PD_APR=ifelse(bank_data1$REPAY_APR>0,0,1)
str(bank_data1)
```

```
## 'data.frame': 30000 obs. of 42 variables:
## $ LIMIT_BAL : num 20000 120000 90000 50000 50000 50000 100000 140000 20
000 ...
   $ SEX
                 : int 2 2 2 2 1 1 1 2 2 1 ...
##
##
  $ EDUCATION
                 : int 2 2 2 2 2 1 1 2 3 3 ...
  $ MARRIAGE
                : int 1221122212...
##
##
   $ AGE
                 : int
                       24 26 34 37 57 37 29 23 28 35 ...
   $ REPAY SEP
               : int 2 -1 0 0 -1 0 0 0 0 -2 ...
##
##
   $ REPAY_AUG
               : int 2200000-10-2...
##
   $ REPAY JUL
                 : int
                       -1 0 0 0 -1 0 0 -1 2 -2 ...
   $ REPAY_JUN
                 : int
                       -1 0 0 0 0 0 0 0 0 -2 ...
                 : int
##
   $ REPAY MAY
                       -2 0 0 0 0 0 0 0 0 -1 ...
##
   $ REPAY_APR
                 : int
                       -2 2 0 0 0 0 0 -1 0 -1 ...
   $ BILL_AMT_SEP : num 3913 2682 29239 46990 8617 ...
##
   $ BILL_AMT_AUG : num 3102 1725 14027 48233 5670 ...
##
##
   $ BILL AMT JUL : num 689 2682 13559 49291 35835 ...
##
   $ BILL AMT JUN : num
                       0 3272 14331 28314 20940 ...
##
   $ BILL AMT MAY : num
                       0 3455 14948 28959 19146 ...
##
   $ BILL AMT APR : num
                       0 3261 15549 29547 19131 ...
##
   $ PAID_AMT_SEP : num
                       0 0 1518 2000 2000 ...
##
   $ PAID AMT AUG : num
                       689 1000 1500 2019 19004 ...
   $ PAID AMT JUL : num
                       0 1000 1000 1200 10000 ...
##
   $ PAID AMT JUN : num
                       0 1000 1000 1100 9000 ...
##
   $ PAID_AMT_MAY : num
                       0 0 1000 1069 689 ...
   $ PAID AMT APR : num
##
                       0 2000 5000 1000 679 ...
##
   $ DEFAULT
                 : int
                       11000000000...
##
   $ RATIO_SEP
                 : num
                       0000000000...
##
   $ RATIO AUG : num
                       0000100100...
##
   $ RATIO JUL
                 : num
                       00000000000...
##
   $ RATIO_JUN
                 : num
                       000000101...
##
   $ RATIO_MAY
                 : num
                       0000000000...
##
   $ RATIO_APR
                 : num
                       0000000100...
                       3913 2682 27721 44990 6617 ...
   $ balance SEP : num
##
   $ balance_AUG : num
                       2413 725 12527 46214 -31011 ...
##
   $ balance JUL
                : num
                       689 1682 12559 48091 25835 ...
##
   $ balance_JUN : num
                       0 2272 13331 27214 11940 ...
##
   $ balance MAY : num
                       0 3455 13948 27890 18457 ...
##
   $ balance APR : num
                       0 1261 10549 28547 18452 ...
##
   $ TIMELY_PD_SEP: num
                       0111111111...
   $ TIMELY PD AUG: num
                       0 0 1 1 1 1 1 1 1 1 ...
##
##
   $ TIMELY_PD_JUL: num
                       1111111101...
##
   $ TIMELY PD JUN: num
                       1111111111...
  $ TIMELY PD APR: num 1 0 1 1 1 1 1 1 1 ...
```

Checking the percentage of customers paid timely theri dues

```
table(bank_data1$TIMELY_PD_APR)
##
##
       0
   3079 26921
table(bank_data1$TIMELY_PD_MAY)
##
       0
## 2968 27032
table(bank_data1$TIMELY_PD_JUN)
##
## 3510 26490
table(bank_data1$TIMELY_PD_JUL)
##
##
             1
## 4213 25787
table(bank_data1$TIMELY_PD_AUG)
##
##
       0
## 4438 25562
table(bank_data1$TIMELY_PD_SEP)
##
##
       0
## 6818 23182
```

```
Per_Sep <- nrow(subset(bank_data1, TIMELY_PD_SEP == "0"))/nrow(bank_data1)</pre>
Per_Aug <- nrow(subset(bank_data1, TIMELY_PD_AUG == "0"))/nrow(bank_data1)</pre>
Per_Jul <- nrow(subset(bank_data1, TIMELY_PD_JUL == "0"))/nrow(bank_data1)</pre>
Per_Jun <- nrow(subset(bank_data1, TIMELY_PD_JUN == "0"))/nrow(bank_data1)</pre>
Per_May <- nrow(subset(bank_data1, TIMELY_PD_MAY == "0"))/nrow(bank_data1)</pre>
Per_Apr <- nrow(subset(bank_data1, TIMELY_PD_APR == "0"))/nrow(bank_data1)</pre>
Per_Sep
## [1] 0.2272667
Per_Aug
## [1] 0.1479333
Per_Jul
## [1] 0.1404333
Per_Jun
## [1] 0.117
Per_May
## [1] 0.09893333
Per_Apr
## [1] 0.1026333
```

we found in September22%, Auguest 14%, July 14%, June 11%, May 09 and April it is 10% customer are paid on time

Correlation between Variable

```
#Checking umeric values
names(bank_data1)
```

```
[1] "LIMIT_BAL"
##
                         "SEX"
                                         "EDUCATION"
                                                          "MARRIAGE"
   [5] "AGE"
                         "REPAY_SEP"
                                         "REPAY_AUG"
                                                          "REPAY_JUL"
##
   [9] "REPAY JUN"
                         "REPAY MAY"
                                         "REPAY APR"
                                                          "BILL AMT SEP"
## [13] "BILL_AMT_AUG"
                         "BILL_AMT_JUL"
                                         "BILL AMT JUN"
                                                          "BILL AMT MAY"
## [17] "BILL_AMT_APR"
                         "PAID_AMT_SEP"
                                         "PAID_AMT_AUG"
                                                          "PAID_AMT_JUL"
## [21] "PAID_AMT_JUN"
                         "PAID AMT MAY"
                                         "PAID AMT APR"
                                                          "DEFAULT"
## [25] "RATIO SEP"
                         "RATIO AUG"
                                         "RATIO JUL"
                                                          "RATIO JUN"
## [29] "RATIO_MAY"
                         "RATIO_APR"
                                         "balance_SEP"
                                                          "balance_AUG"
## [33] "balance_JUL"
                                         "balance_MAY"
                                                          "balance_APR"
                         "balance_JUN"
## [37] "TIMELY PD SEP"
                         "TIMELY PD AUG"
                                         "TIMELY PD JUL" "TIMELY PD JUN"
## [41] "TIMELY_PD_MAY" "TIMELY_PD_APR"
```

```
bank_data_num <- subset(bank_data1,select= -c(2,3,4))
numeric.list <- sapply(bank_data_num,is.numeric)
numeric.list</pre>
```

```
##
       LIMIT_BAL
                            AGE
                                     REPAY_SEP
                                                    REPAY_AUG
                                                                   REPAY_JUL
##
            TRUE
                           TRUE
                                          TRUE
                                                         TRUE
                                                                        TRUE
                                     REPAY_APR BILL_AMT_SEP
##
       REPAY_JUN
                      REPAY_MAY
                                                                BILL AMT AUG
##
            TRUE
                           TRUE
                                          TRUE
                                                         TRUE
                                                                        TRUE
##
    BILL_AMT_JUL
                   BILL_AMT_JUN
                                  BILL AMT MAY
                                                BILL AMT APR
                                                                PAID AMT SEP
##
            TRUE
                           TRUE
                                          TRUE
                                                         TRUE
                                                                        TRUE
##
    PAID_AMT_AUG
                   PAID_AMT_JUL
                                  PAID_AMT_JUN
                                                PAID_AMT_MAY
                                                                PAID_AMT_APR
##
            TRUE
                           TRUE
                                          TRUE
                                                         TRUE
                                                                        TRUE
##
         DEFAULT
                      RATIO SEP
                                     RATIO AUG
                                                    RATIO JUL
                                                                   RATIO JUN
##
            TRUE
                           TRUE
                                          TRUE
                                                         TRUE
                                                                        TRUE
##
       RATIO_MAY
                      RATIO_APR
                                   balance_SEP
                                                  balance_AUG
                                                                 balance_JUL
                           TRUE
                                                         TRUE
##
            TRUE
                                          TRUE
                                                                        TRUE
##
     balance_JUN
                    balance_MAY
                                   balance_APR TIMELY_PD_SEP TIMELY_PD_AUG
            TRUE
                           TRUE
                                          TRUE
                                                         TRUE
                                                                        TRUE
##
## TIMELY_PD_JUL TIMELY_PD_JUN TIMELY_PD_MAY TIMELY_PD_APR
##
            TRUE
                           TRUE
                                          TRUE
                                                         TRUE
```

```
sum(numeric.list)
```

```
## [1] 39
```

```
numeric.df1 <- bank_data_num[, numeric.list]</pre>
```

```
cor.mat <- cor(numeric.df1)
cor.mat</pre>
```

```
REPAY_SEP
                                                         REPAY_AUG
##
                   LIMIT_BAL
                                      AGE
                                                                     REPAY_JUL
## LIMIT_BAL
                  1.00000000
                              0.144411208 -0.27539728 -0.30132429 -0.29085210
## AGE
                  0.14441121
                              1.000000000 -0.03944738 -0.05014778 -0.05304844
## REPAY_SEP
                 -0.27539728 -0.039447376
                                           1.00000000
                                                        0.67216438
                                                                    0.57424509
## REPAY AUG
                 -0.30132429 -0.050147776
                                           0.67216438
                                                        1.00000000
                                                                    0.76655168
## REPAY JUL
                 -0.29085210 -0.053048437
                                           0.57424509
                                                        0.76655168
                                                                    1.00000000
  REPAY JUN
                 -0.27188031 -0.049721674
                                           0.53884063
                                                        0.66206713
                                                                    0.77735887
## REPAY MAY
                 -0.25386748 -0.053825976
                                           0.50942606
                                                        0.62278025
                                                                    0.68677451
## REPAY_APR
                 -0.23914673 -0.048773426
                                           0.47455309
                                                        0.57550086
                                                                    0.63268359
## BILL AMT SEP
                  0.22574850
                              0.044197956
                                           0.21169675
                                                        0.27123718
                                                                    0.24327442
## BILL_AMT_AUG
                  0.21928462
                              0.042399024
                                           0.21503351
                                                        0.27104464
                                                                    0.27565894
## BILL AMT JUL
                  0.22750648
                              0.041973628
                                           0.20737569
                                                        0.26239738
                                                                    0.26793965
## BILL_AMT_JUN
                              0.037627195
                                           0.20266794
                                                        0.25622637
                  0.23861623
                                                                    0.26389145
  BILL AMT MAY
                  0.24164395
                              0.035040604
                                           0.19997954
                                                        0.25153785
                                                                    0.25757598
## BILL_AMT_APR
                  0.23546407
                              0.032943061
                                           0.19718917
                                                        0.24936048
                                                                    0.25353730
## PAID_AMT_SEP
                  0.34472260
                              0.042630410 -0.12484300 -0.10516756
                                                                    0.03961255
## PAID AMT AUG
                  0.35155111
                              0.050324437 -0.12468940 -0.07193099 -0.10179544
## PAID AMT JUL
                  0.35154679
                              0.043465898 -0.11133798 -0.06310105 -0.05852685
                              0.044050199 -0.08842719 -0.04586198 -0.03315491
## PAID AMT JUN
                  0.34010202
## PAID_AMT_MAY
                              0.039833639 -0.08117923 -0.03531956 -0.02375237
                  0.34316453
## PAID AMT APR
                  0.35701221
                              0.035382567 -0.09170658 -0.04581591 -0.03972182
## DEFAULT
                 -0.15487161
                              0.013889834 0.32479373 0.26355120
                                                                   0.23525251
## RATIO SEP
                  0.17013688
                              0.033436180 -0.27133659 -0.30231144 -0.18319677
## RATIO_AUG
                  0.17174885
                              0.027530355 -0.27549031 -0.27338650 -0.29374069
  RATIO JUL
                              0.015291893 -0.24294682 -0.23830100 -0.24051176
                  0.16138355
## RATIO JUN
                              0.029853508 -0.22779673 -0.23147323 -0.23498005
                  0.13896766
## RATIO_MAY
                  0.07041878
                              0.011651845 -0.10768036 -0.10648743 -0.10779970
  RATIO APR
                  0.10713783
                              0.025828607 -0.21659451 -0.21259679 -0.21114396
## balance SEP
                  0.18863296
                              0.039584764 0.23322320 0.29261651
                                                                    0.24747342
## balance_AUG
                  0.17931334
                              0.038081037
                                           0.23749793
                                                        0.28911232
                                                                    0.29593154
## balance_JUL
                  0.18651671
                              0.038051625 0.22706449
                                                       0.27786665
                                                                    0.28247089
## balance_JUN
                                           0.22024351
                  0.20133969
                              0.032883393
                                                        0.26959462
                                                                    0.27695959
## balance MAY
                                           0.21873873
                                                        0.26544400
                                                                    0.27012025
                  0.20146957
                              0.030734691
## balance_APR
                  0.18973546
                              0.029652051
                                           0.21400990
                                                        0.26206908
                                                                    0.26574909
## TIMELY PD SEP
                  0.15921009
                              0.003073199 -0.76562288 -0.42343527 -0.29675183
  TIMELY_PD_AUG
                  0.20228766
                              0.009968067 -0.54364452 -0.79951598 -0.53347863
##
  TIMELY_PD_JUL
                  0.19645811
                              0.015262820 -0.41315133 -0.54291333 -0.78736082
## TIMELY_PD_JUN
                  0.18695974
                              0.007899190 -0.38081781 -0.44045458 -0.53977177
  TIMELY_PD_MAY
                  0.17589366
                              0.016556216 -0.36097705 -0.41144520 -0.44338770
##
  TIMELY PD APR
                  0.17327390
                              0.020612667 -0.32951861 -0.37321749 -0.40496551
##
                    REPAY_JUN
                                REPAY_MAY
                                             REPAY_APR BILL_AMT_SEP
## LIMIT BAL
                 -0.271880313 -0.25386748 -0.239146726
                                                         2.257485e-01
##
  AGE
                 -0.049721674 -0.05382598 -0.048773426
                                                         4.419796e-02
## REPAY SEP
                  0.538840627
                               0.50942606
                                           0.474553086
                                                         2.116968e-01
## REPAY_AUG
                  0.662067131 0.62278025
                                           0.575500862
                                                         2.712372e-01
## REPAY_JUL
                  0.777358873
                               0.68677451 0.632683593
                                                         2.432744e-01
## REPAY JUN
                  1.000000000
                               0.81983531
                                           0.716449482
                                                         2.382699e-01
## REPAY_MAY
                  0.819835311 1.00000000 0.816900160
                                                         2.400896e-01
```

```
## REPAY APR
                  0.716449482
                               0.81690016 1.000000000
                                                        2.407940e-01
## BILL_AMT_SEP
                  0.238269941 0.24008957
                                          0.240793973
                                                        1.000000e+00
## BILL AMT AUG
                  0.264887662
                               0.26413104 0.264006062
                                                        9.464939e-01
## BILL AMT JUL
                  0.289982280
                               0.28763824
                                          0.283762534
                                                        8.988444e-01
## BILL_AMT_JUN
                  0.287197846
                               0.31721377
                                          0.309800209
                                                        8.517570e-01
## BILL AMT MAY
                  0.280099508
                              0.31022107
                                          0.334516643
                                                        8.190675e-01
## BILL AMT APR
                  0.276027978
                               0.30222883
                                          0.327066503
                                                        7.930090e-01
## PAID AMT SEP
                  0.013794760
                               0.01322631
                                          0.020143779
                                                        3.834999e-01
## PAID_AMT_AUG
                  0.043295545 0.02931824 0.018074934
                                                        3.413154e-01
## PAID_AMT_JUL
                 -0.078448789
                               0.05826027
                                           0.042543946
                                                        3.198864e-01
## PAID AMT JUN
                 -0.025814044 -0.04034934
                                          0.080924968
                                                        3.355537e-01
## PAID_AMT_MAY
                 -0.007393487
                               0.00146192 -0.020659098 3.305207e-01
## PAID AMT APR
                -0.021266061 -0.00471918
                                          0.007348771
                                                       3.121608e-01
## DEFAULT
                  0.216613637
                               0.20414891
                                          0.186866362 -2.814973e-02
## RATIO SEP
                 -0.212483389 -0.21113715 -0.210955276 -2.651461e-01
## RATIO_AUG
                -0.185284356 -0.20154998 -0.206663748 -2.418946e-01
## RATIO JUL
                -0.268930470 -0.16836533 -0.185488444 -2.138381e-01
## RATIO JUN
                -0.239609132 -0.25741487 -0.159466469 -1.978175e-01
## RATIO MAY
                 -0.107523848 -0.14849786 -0.089690212 -7.965437e-02
## RATIO APR
                -0.213916829 -0.24676769 -0.165679338 -1.912840e-01
## balance_SEP
                 ## balance AUG
                  0.267579018 0.26743677 0.268899915
                                                       9.316748e-01
## balance_JUL
                 0.308161389 0.28923989 0.286952430
                                                       8.827723e-01
## balance JUN
                 0.300018629 0.33293165 0.310949495
                                                        8.349008e-01
## balance MAY
                  0.291352835
                               0.32093794 0.350326140
                                                        8.013733e-01
## balance_APR
                  0.286372817
                               0.31107739 0.334783721
                                                       7.696848e-01
## TIMELY_PD_SEP -0.259522794 -0.24244755 -0.221528224
                                                        6.326166e-02
## TIMELY PD AUG -0.429263308 -0.40063275 -0.365837679 -1.209009e-02
## TIMELY PD JUL -0.519510913 -0.42371136 -0.384725641
                                                        1.709903e-02
## TIMELY_PD_JUN -0.757320032 -0.53157511 -0.434655357
                                                       1.235628e-02
## TIMELY_PD_MAY -0.552610424 -0.73252120 -0.530848179
                                                        5.796195e-04
  TIMELY PD APR -0.447518324 -0.53617698 -0.734811807 -7.790246e-05
                 BILL AMT AUG BILL AMT JUL BILL AMT JUN BILL AMT MAY
##
## LIMIT_BAL
                  0.219284616
                                0.22750648
                                             0.23861623
                                                          0.24164395
## AGE
                  0.042399024
                                0.04197363
                                             0.03762719
                                                          0.03504060
## REPAY SEP
                  0.215033512
                                0.20737569
                                             0.20266794
                                                          0.19997954
## REPAY AUG
                  0.271044643
                                0.26239738
                                             0.25622637
                                                          0.25153785
## REPAY_JUL
                  0.275658942
                                0.26793965
                                             0.26389145
                                                          0.25757598
## REPAY JUN
                  0.264887662
                                0.28998228
                                             0.28719785
                                                          0.28009951
## REPAY_MAY
                  0.264131042
                                0.28763824
                                             0.31721377
                                                          0.31022107
## REPAY APR
                  0.264006062
                                0.28376253
                                             0.30980021
                                                          0.33451664
## BILL_AMT_SEP
                                             0.85175700
                  0.946493906
                                0.89884436
                                                          0.81906751
## BILL AMT AUG
                  1.000000000
                                0.93867414
                                             0.88704848
                                                          0.84930320
## BILL_AMT_JUL
                  0.938674143
                                             0.93047351
                                1.00000000
                                                          0.88564143
## BILL_AMT_JUN
                  0.887048480
                                0.93047351
                                             1.00000000
                                                          0.93603470
## BILL AMT MAY
                                             0.93603470
                  0.849303197
                                0.88564143
                                                          1.00000000
## BILL AMT APR
                  0.820514292
                                0.85169140
                                             0.89641600
                                                          0.94392171
## PAID AMT SEP
                  0.468478029
                                0.43426181
                                             0.41388446
                                                          0.39492124
## PAID_AMT_AUG
                  0.351474735
                                0.44508575
                                             0.40911219
                                                          0.38322288
```

```
## PAID_AMT_JUL
                   0.327217570
                                 0.33625027
                                               0.43489337
                                                             0.39365285
## PAID_AMT_JUN
                   0.339482536
                                 0.35041040
                                               0.36097186
                                                             0.44884284
## PAID AMT MAY
                   0.340047122
                                 0.35350936
                                               0.36421171
                                                             0.36807416
## PAID_AMT_APR
                   0.316717024
                                 0.33128864
                                               0.33916249
                                                             0.34296527
## DEFAULT
                  -0.021723287
                                -0.02032750
                                              -0.01636235
                                                            -0.01388112
## RATIO SEP
                  -0.182940008
                                              -0.17594266
                                                            -0.17464959
                                -0.18606840
## RATIO AUG
                  -0.267373326
                                -0.17500257
                                              -0.17928025
                                                            -0.17638374
  RATIO_JUL
##
                  -0.225673075
                                -0.25214778
                                              -0.15575877
                                                            -0.16466294
## RATIO_JUN
                 -0.210049070
                                -0.21774596
                                              -0.24343448
                                                            -0.14927365
  RATIO_MAY
                  -0.086221937
                                -0.08883390
                                              -0.10337786
                                                            -0.07914399
  RATIO APR
                  -0.199394553
                                -0.20128598
                                              -0.21133533
##
                                                            -0.17267815
## balance_SEP
                                 0.86959437
                                               0.82344593
                                                             0.79382779
                  0.910737084
## balance AUG
                  0.982600033
                                 0.90326440
                                               0.85756999
                                                             0.82311488
## balance_JUL
                  0.922485864
                                 0.98167162
                                               0.89312953
                                                             0.85632752
## balance JUN
                  0.871773905
                                 0.91427476
                                               0.98187199
                                                             0.90253251
## balance_MAY
                                               0.91496456
                                                             0.97903387
                  0.831076074
                                 0.86538377
## balance_APR
                   0.798042792
                                 0.82733590
                                               0.87109056
                                                             0.91915086
## TIMELY PD SEP
                   0.049986593
                                 0.04105088
                                               0.03156677
                                                             0.02353475
## TIMELY_PD_AUG -0.016100950
                                -0.02609613
                                              -0.03478733
                                                            -0.04198107
## TIMELY PD JUL -0.005309878
                                -0.00919752
                                              -0.02525567
                                                            -0.03411177
  TIMELY_PD_JUN -0.003318187
                                -0.02144914
                                              -0.03458244
                                                            -0.04836318
  TIMELY PD MAY -0.012438353
                                -0.02736164
                                              -0.05241539
                                                            -0.06393935
  TIMELY_PD_APR -0.012980333
                                -0.02633602
                                              -0.04799944
                                                            -0.07125941
##
                  BILL AMT APR PAID AMT SEP PAID AMT AUG PAID AMT JUL
## LIMIT BAL
                    0.23546407
                                 0.34472260
                                               0.35155111
                                                             0.35154679
## AGE
                   0.03294306
                                 0.04263041
                                               0.05032444
                                                             0.04346590
##
  REPAY_SEP
                    0.19718917
                                -0.12484300
                                              -0.12468940
                                                            -0.11133798
## REPAY AUG
                    0.24936048
                                -0.10516756
                                              -0.07193099
                                                            -0.06310105
## REPAY JUL
                    0.25353730
                                 0.03961255
                                              -0.10179544
                                                            -0.05852685
##
  REPAY_JUN
                   0.27602798
                                 0.01379476
                                               0.04329554
                                                            -0.07844879
## REPAY_MAY
                    0.30222883
                                 0.01322631
                                               0.02931824
                                                             0.05826027
  REPAY APR
                    0.32706650
                                 0.02014378
                                               0.01807493
                                                             0.04254395
  BILL_AMT_SEP
                   0.79300899
##
                                 0.38349991
                                               0.34131544
                                                             0.31988643
## BILL_AMT_AUG
                    0.82051429
                                 0.46847803
                                               0.35147474
                                                             0.32721757
## BILL_AMT_JUL
                    0.85169140
                                 0.43426181
                                               0.44508575
                                                             0.33625027
  BILL AMT JUN
                    0.89641600
                                 0.41388446
                                               0.40911219
                                                             0.43489337
## BILL_AMT_MAY
                    0.94392171
                                 0.39492124
                                               0.38322288
                                                             0.39365285
## BILL_AMT_APR
                   1.00000000
                                 0.37405952
                                               0.36165151
                                                             0.37493209
## PAID AMT SEP
                    0.37405952
                                 1.00000000
                                               0.49183698
                                                             0.45954130
## PAID_AMT_AUG
                    0.36165151
                                 0.49183698
                                               1.00000000
                                                             0.46780328
## PAID AMT JUL
                   0.37493209
                                 0.45954130
                                               0.46780328
                                                             1.00000000
## PAID_AMT_JUN
                    0.41044422
                                 0.43651346
                                               0.44472487
                                                             0.46276419
## PAID AMT MAY
                    0.45242774
                                 0.43100306
                                               0.43118614
                                                             0.45087100
## PAID_AMT_APR
                    0.33548428
                                 0.41310351
                                               0.42140998
                                                             0.43565445
## DEFAULT
                   -0.01040406
                                -0.12745405
                                              -0.12966646
                                                            -0.11305607
## RATIO SEP
                                 0.32347950
                   -0.17491029
                                               0.10842229
                                                             0.10237912
## RATIO AUG
                   -0.17848914
                                -0.04576346
                                               0.34781141
                                                             0.10361116
## RATIO JUL
                   -0.16375576
                                 0.02914445
                                              -0.04090644
                                                             0.37682163
## RATIO_JUN
                   -0.16314901
                                 0.02292415
                                               0.01921562
                                                            -0.04807343
```

```
## RATIO_MAY
                  -0.07273748
                                0.03928512
                                             0.03895988
                                                          0.04167422
## RATIO_APR
                  -0.24001114
                                0.04529049
                                             0.05321766
                                                          0.05318352
## balance SEP
                   0.77112130
                                0.26548174
                                             0.28824504
                                                          0.27244967
                   0.79762194
## balance AUG
                                0.41329519
                                             0.23088484
                                                          0.27858519
## balance_JUL
                   0.82714221
                                0.38802551
                                             0.39351355
                                                          0.21415716
## balance JUN
                   0.87055604
                                0.37127391
                                                          0.38708605
                                             0.36345339
  balance MAY
                   0.90619776
                                0.34978538
                                             0.33679100
                                                          0.34710418
## balance APR
                   0.97700844
                                0.32474088
                                             0.31168270
                                                          0.32654135
## TIMELY_PD_SEP
                                0.20228245
                   0.02043208
                                             0.15917116
                                                          0.13824251
## TIMELY_PD_AUG
                  -0.04533688
                                0.19666442
                                             0.12073611
                                                          0.10116083
  TIMELY PD JUL
                  -0.03736249
                                0.04891961
                                             0.19153266
                                                          0.11014202
                                0.08136572
## TIMELY_PD_JUN
                  -0.05633509
                                             0.05606436
                                                          0.15725552
## TIMELY PD MAY
                  -0.07233785
                                0.08778706
                                             0.07641425
                                                          0.04343556
  TIMELY_PD_APR
                  -0.07519381
                                0.07360718
                                             0.07879006
                                                          0.05991920
##
                 PAID AMT JUN PAID AMT MAY PAID AMT APR
                                                             DEFAULT
                   0.34010202
                               0.343164533
                                            0.357012214 -0.154871612
## LIMIT_BAL
## AGE
                   0.04405020
                               0.039833639
                                            0.035382567
                                                         0.013889834
## REPAY SEP
                  -0.08842719 -0.081179226 -0.091706581
                                                         0.324793728
## REPAY_AUG
                  -0.04586198 -0.035319556 -0.045815908
                                                         0.263551202
## REPAY JUL
                  -0.03315491 -0.023752366 -0.039721816
                                                         0.235252514
  REPAY_JUN
                  -0.02581404 -0.007393487 -0.021266061
                                                         0.216613637
## REPAY MAY
                  -0.04034934
                               0.001461920 -0.004719180
                                                         0.204148914
## REPAY_APR
                   0.08092497 -0.020659098
                                            0.007348771
                                                         0.186866362
## BILL AMT SEP
                   0.33555369
                               0.330520667
                                            0.312160768 -0.028149729
## BILL AMT AUG
                   0.33948254
                               0.340047122
                                            0.316717024 -0.021723287
## BILL_AMT_JUL
                   0.35041040
                               0.353509362
                                            0.331288637 -0.020327498
## BILL_AMT_JUN
                   0.36097186
                               0.364211711
                                            0.339162495 -0.016362354
## BILL AMT MAY
                   0.44884284 0.368074164
                                            0.342965266 -0.013881118
## BILL AMT APR
                   0.41044422
                               0.452427743
                                            0.335484278 -0.010404064
## PAID_AMT_SEP
                   0.43651346
                               0.431003065
                                            0.413103509 -0.127454051
                                            0.421409979 -0.129666463
## PAID_AMT_AUG
                   0.44472487
                               0.431186142
## PAID AMT JUL
                   0.46276419
                               0.450870997
                                            0.435654446 -0.113056071
## PAID_AMT_JUN
                   1.00000000
                               0.474034682
                                            0.449923096 -0.102892735
## PAID_AMT_MAY
                   0.47403468
                               1.000000000
                                            0.477744166 -0.102013983
## PAID AMT APR
                   0.44992310
                               0.477744166
                                            1.000000000 -0.105654753
## DEFAULT
                  -0.10289274 -0.102013983 -0.105654753
                                                         1.000000000
## RATIO SEP
                   0.06446055
                               0.067084558
                                            0.070884202 -0.068646633
## RATIO_AUG
                                            0.079786768 -0.074470210
                   0.07731871
                               0.066132090
## RATIO JUL
                                            0.072281342 -0.079113555
                   0.08560472
                               0.078354500
## RATIO_JUN
                   0.33503403
                               0.068170763
                                            0.072204428 -0.063494323
## RATIO MAY
                   0.17953527
                               0.070945958
                                            0.057443651 -0.041880561
## RATIO_APR
                                            0.047428424 -0.071744303
                   0.28291331 -0.083522152
## balance SEP
                   0.29228390
                               0.287637378
                                            0.269239018 -0.012262235
## balance_AUG
                               0.296699738
                                            0.271733317 -0.005010962
                   0.29429610
## balance_JUL
                   0.30253850
                               0.307315217
                                            0.283736658 -0.005809474
## balance_JUN
                   0.24241953
                               0.314799952
                                            0.292058510 -0.004326666
## balance MAY
                   0.40015487
                               0.244349847
                                            0.290201237 -0.000316773
## balance APR
                   0.36181742
                               0.397909698
                                            0.202999860
                                                         0.002000906
## TIMELY_PD_SEP
```

```
## TIMELY_PD_AUG
                  0.09269627 0.084497695
                                           0.089446466 -0.338022325
## TIMELY_PD_JUL
                  0.08834239 0.084769838
                                           0.094339069 -0.293583004
## TIMELY PD JUN
                  0.09344797 0.080055375
                                           0.088959256 -0.275494664
## TIMELY PD MAY
                  0.12530591 0.077100169 0.081013660 -0.266958955
## TIMELY_PD_APR
                  0.01556949 0.124737381 0.074600218 -0.246088912
##
                  RATIO_SEP
                              RATIO_AUG
                                          RATIO JUL
                                                      RATIO JUN
                                                                  RATIO MAY
## LIMIT BAL
                 0.17013688 0.17174885 0.16138355
                                                     0.13896766
                                                                 0.07041878
## AGE
                 0.03343618 0.02753035 0.01529189
                                                     0.02985351 0.01165185
## REPAY SEP
                -0.27133659 -0.27549031 -0.24294682 -0.22779673 -0.10768036
## REPAY_AUG
                -0.30231144 -0.27338650 -0.23830100 -0.23147323 -0.10648743
## REPAY JUL
                -0.18319677 -0.29374069 -0.24051176 -0.23498005 -0.10779970
## REPAY_JUN
                -0.21248339 -0.18528436 -0.26893047 -0.23960913 -0.10752385
## REPAY MAY
                -0.21113715 -0.20154998 -0.16836533 -0.25741487 -0.14849786
                 -0.21095528 -0.20666375 -0.18548844 -0.15946647 -0.08969021
## REPAY_APR
## BILL AMT SEP
                -0.26514609 -0.24189455 -0.21383812 -0.19781747 -0.07965437
## BILL_AMT_AUG
                -0.18294001 -0.26737333 -0.22567308 -0.21004907 -0.08622194
## BILL AMT JUL
                -0.18606840 -0.17500257 -0.25214778 -0.21774596 -0.08883390
## BILL AMT JUN
                 -0.17594266 -0.17928025 -0.15575877 -0.24343448 -0.10337786
## BILL_AMT_MAY
                 -0.17464959 -0.17638374 -0.16466294 -0.14927365 -0.07914399
## BILL AMT APR
                -0.17491029 -0.17848914 -0.16375576 -0.16314901 -0.07273748
## PAID_AMT_SEP
                 0.32347950 -0.04576346 0.02914445 0.02292415
                                                                 0.03928512
## PAID AMT AUG
                 0.10842229 0.34781141 -0.04090644
                                                     0.01921562
                                                                 0.03895988
## PAID_AMT_JUL
                 0.10237912  0.10361116  0.37682163  -0.04807343  0.04167422
## PAID AMT JUN
                 0.06446055
                            0.07731871 0.08560472 0.33503403 0.17953527
## PAID AMT MAY
                 0.06708456 0.06613209 0.07835450
                                                     0.06817076
                                                                 0.07094596
## PAID AMT APR
                 0.07088420
                            0.07978677 0.07228134
                                                     0.07220443
                                                                 0.05744365
## DEFAULT
                 -0.06864663 -0.07447021 -0.07911355 -0.06349432 -0.04188056
## RATIO SEP
                 1.00000000 0.16426179 0.23187564 0.19560123
                                                                 0.09157725
## RATIO AUG
                 0.16426179
                            1.00000000
                                        0.15258243
                                                     0.21378463
                                                                 0.09396729
## RATIO_JUL
                 0.23187564 0.15258243 1.00000000 0.12778559
                                                                 0.09008316
## RATIO_JUN
                 0.19560123 0.21378463 0.12778559
                                                     1.00000000
                                                                 0.19417478
## RATIO MAY
                 0.09157725 0.09396729 0.09008316
                                                     0.19417478
                                                                 1.00000000
## RATIO APR
                                         0.18487752
                                                     0.51709987
                 0.19484283 0.21036767
                                                                 0.27390498
## balance SEP
                -0.32851497 -0.24087456 -0.22286600 -0.20680206 -0.08945092
## balance AUG
                -0.20753379 -0.33240787 -0.22503166 -0.21702722 -0.09386626
## balance JUL
                -0.20497116 -0.19886523 -0.32286731 -0.21401356 -0.09703492
                -0.19124513 -0.19777880 -0.17650497 -0.30802110 -0.13837634
## balance JUN
## balance_MAY
                -0.19143096 -0.19354789 -0.18268254 -0.16459314 -0.09172357
## balance APR
                 -0.19121364 -0.19539494 -0.17958327 -0.17855459 -0.08296204
## TIMELY_PD_SEP
                 0.07414362
                             0.09145351
                                         0.07951001
                                                     0.07735065
                                                                 0.04462044
## TIMELY PD AUG
                 0.14909760
                             0.09625866 0.09072825
                                                     0.09198303
                                                                 0.04695335
## TIMELY_PD_JUL
                 0.05846244
                             0.14677139 0.07470394 0.08629354
                                                                 0.04501988
## TIMELY PD JUN
                 0.09106354
                             0.08445320 0.12753058
                                                     0.08070484
                                                                 0.03506964
## TIMELY_PD_MAY
                 0.09809638 0.09689908 0.08539828
                                                     0.11009603
                                                                 0.05868736
## TIMELY PD APR
                 0.09306310
                             0.09373738 0.08952012 0.06789340
                                                                 0.03197300
##
                  RATIO_APR
                             balance_SEP balance_AUG balance_JUL
## LIMIT BAL
                 0.10713783
                             0.188632956 0.179313344
                                                       0.186516714
## AGE
                 0.02582861
                             0.039584764 0.038081037
                                                       0.038051625
## REPAY_SEP
                -0.21659451 0.233223202 0.237497925 0.227064488
```

```
## REPAY AUG
                 -0.21259679
                              0.292616508
                                           0.289112324
                                                         0.277866646
## REPAY_JUL
                 -0.21114396
                              0.247473418
                                           0.295931537
                                                         0.282470887
## REPAY JUN
                 -0.21391683
                              0.244368739
                                           0.267579018
                                                         0.308161389
## REPAY MAY
                 -0.24676769
                              0.245851073
                                           0.267436766
                                                         0.289239887
## REPAY APR
                 -0.16567934
                              0.246105673
                                           0.268899915
                                                         0.286952430
## BILL AMT SEP
                 -0.19128404
                              0.982985681
                                           0.931674805
                                                         0.882772346
## BILL AMT AUG
                 -0.19939455
                              0.910737084
                                           0.982600033
                                                         0.922485864
## BILL_AMT_JUL
                 -0.20128598
                              0.869594373
                                           0.903264398
                                                         0.981671619
## BILL_AMT_JUN
                 -0.21133533
                              0.823445930
                                           0.857569987
                                                         0.893129526
## BILL_AMT_MAY
                 -0.17267815
                              0.793827793
                                           0.823114884
                                                         0.856327521
## BILL AMT APR
                 -0.24001114
                              0.771121295
                                           0.797621936
                                                         0.827142214
                              0.265481743
## PAID_AMT_SEP
                  0.04529049
                                           0.413295191
                                                        0.388025513
## PAID AMT AUG
                  0.05321766
                              0.288245042
                                           0.230884841
                                                         0.393513548
## PAID_AMT_JUL
                  0.05318352
                             0.272449674
                                           0.278585187
                                                         0.214157165
## PAID AMT JUN
                  0.28291331
                              0.292283904
                                           0.294296105
                                                         0.302538495
## PAID_AMT_MAY
                 -0.08352215
                              0.287637378
                                           0.296699738
                                                         0.307315217
## PAID AMT APR
                  0.04742842
                              0.269239018
                                          0.271733317
                                                         0.283736658
## DEFAULT
                 -0.07174430 -0.012262235 -0.005010962 -0.005809474
## RATIO SEP
                  0.19484283 -0.328514970 -0.207533786 -0.204971163
## RATIO AUG
                  0.21036767 -0.240874559 -0.332407866 -0.198865235
## RATIO_JUL
                  0.18487752 -0.222866005 -0.225031662 -0.322867312
## RATIO JUN
                  0.51709987 -0.206802059 -0.217027223 -0.214013558
## RATIO_MAY
                  0.27390498 -0.089450921 -0.093866264 -0.097034923
                  1.00000000 -0.203458612 -0.211308750 -0.213464434
## RATIO APR
## balance SEP
                 -0.20345861
                              1.000000000
                                          0.905501078
                                                        0.860485908
## balance AUG
                 -0.21130875
                              0.905501078 1.000000000
                                                         0.895522728
## balance_JUL
                 -0.21346443
                              0.860485908 0.895522728
                                                         1.000000000
## balance_JUN
                 -0.26274193
                              0.813521394   0.849299964
                                                         0.885126588
## balance MAY
                 -0.16603559
                              0.783262007
                                           0.811843057
                                                         0.843325604
## balance_APR
                 -0.25367998
                              0.754704888
                                           0.782494739
                                                         0.810332388
## TIMELY_PD_SEP
                  0.08539791
                              0.042350580
                                           0.031100511
                                                        0.023867637
## TIMELY PD AUG
                  0.09416249 -0.034901234 -0.032439019 -0.040489083
## TIMELY_PD_JUL
                              0.008255684 -0.028078790 -0.023218988
                  0.09064253
## TIMELY_PD_JUN
                  0.09561139
                              0.001047892 -0.012850703 -0.040607646
## TIMELY PD MAY
                  0.12553147 -0.010795433 -0.023549771 -0.036193790
##
  TIMELY PD APR
                  0.06723022 -0.010149039 -0.024113268 -0.036032296
##
                  balance JUN
                               balance MAY
                                            balance_APR TIMELY_PD_SEP
## LIMIT_BAL
                  0.201339693 0.201469566
                                            0.189735458
                                                           0.159210087
## AGE
                  0.032883393
                               0.030734691
                                            0.029652051
                                                           0.003073199
## REPAY SEP
                  0.220243515
                               0.218738727
                                            0.214009900
                                                          -0.765622881
## REPAY AUG
                  0.269594616
                               0.265443998
                                            0.262069079
                                                          -0.423435268
## REPAY_JUL
                  0.276959593
                               0.270120248
                                            0.265749088
                                                          -0.296751825
## REPAY JUN
                  0.300018629
                               0.291352835
                                            0.286372817
                                                          -0.259522794
## REPAY_MAY
                  0.332931646
                               0.320937944
                                            0.311077386
                                                          -0.242447549
## REPAY_APR
                  0.310949495
                               0.350326140
                                            0.334783721
                                                          -0.221528224
## BILL AMT SEP
                  0.834900833
                               0.801373312
                                            0.769684811
                                                           0.063261655
## BILL AMT AUG
                  0.871773905
                               0.831076074
                                            0.798042792
                                                           0.049986593
## BILL AMT JUL
                  0.914274761
                               0.865383767
                                            0.827335904
                                                           0.041050885
## BILL_AMT_JUN
                  0.981871989 0.914964557
                                            0.871090561
                                                           0.031566769
```

```
## BILL_AMT_MAY
                  0.902532508
                               0.979033867
                                             0.919150859
                                                           0.023534752
## BILL_AMT_APR
                  0.870556039
                               0.906197757
                                             0.977008443
                                                           0.020432076
## PAID AMT SEP
                  0.371273911 0.349785380
                                             0.324740876
                                                           0.202282446
## PAID AMT AUG
                  0.363453394   0.336791004
                                             0.311682698
                                                           0.159171164
## PAID_AMT_JUL
                  0.387086052 0.347104185
                                            0.326541348
                                                           0.138242507
## PAID AMT JUN
                  0.242419533 0.400154865
                                             0.361817420
                                                           0.127997924
## PAID AMT MAY
                  0.314799952
                               0.244349847
                                             0.397909698
                                                           0.122184613
## PAID AMT APR
                  0.292058510
                               0.290201237
                                            0.202999860
                                                           0.127541281
## DEFAULT
                 -0.004326666 -0.000316773
                                            0.002000906
                                                          -0.368116996
## RATIO_SEP
                 -0.191245132 -0.191430961 -0.191213644
                                                           0.074143617
  RATIO AUG
                 -0.197778802 -0.193547895 -0.195394939
                                                           0.091453506
## RATIO_JUL
                 -0.176504971 -0.182682538 -0.179583266
                                                           0.079510006
## RATIO JUN
                 -0.308021098 -0.164593139 -0.178554594
                                                           0.077350648
## RATIO_MAY
                 -0.138376341 -0.091723574 -0.082962039
                                                           0.044620436
## RATIO APR
                 -0.262741930 -0.166035590 -0.253679984
                                                           0.085397909
## balance_SEP
                  0.813521394 0.783262007
                                            0.754704888
                                                           0.042350580
## balance_AUG
                  0.849299964 0.811843057
                                            0.782494739
                                                           0.031100511
## balance JUL
                  0.885126588 0.843325604
                                             0.810332388
                                                           0.023867637
## balance_JUN
                  1.000000000 0.890808375
                                             0.853357164
                                                           0.016879958
## balance MAY
                  0.890808375 1.000000000
                                            0.892324948
                                                           0.007576236
## balance_APR
                  0.853357164
                               0.892324948
                                            1.000000000
                                                           0.005369907
## TIMELY PD SEP
                  0.016879958
                               0.007576236
                                            0.005369907
                                                           1.000000000
## TIMELY_PD_AUG -0.046665721 -0.054256351 -0.056938304
                                                           0.668175817
## TIMELY PD JUL -0.037384255 -0.046173663 -0.049948700
                                                           0.430527007
## TIMELY PD JUN -0.047592928 -0.061058867 -0.068687831
                                                           0.371030465
  TIMELY PD MAY -0.068534628 -0.076165754 -0.084544434
                                                           0.348586753
##
  TIMELY_PD_APR -0.054088112 -0.089079844 -0.086055344
                                                           0.309866549
##
                 TIMELY_PD_AUG TIMELY_PD_JUL TIMELY_PD_JUN TIMELY_PD_MAY
## LIMIT BAL
                   0.202287660
                                 0.196458106
                                                0.186959736
                                                             0.1758936622
## AGE
                   0.009968067
                                 0.015262820
                                                0.007899190
                                                             0.0165562164
## REPAY_SEP
                  -0.543644516
                                -0.413151326 -0.380817805 -0.3609770469
## REPAY AUG
                  -0.799515983
                                -0.542913332 -0.440454576 -0.4114452007
## REPAY_JUL
                                -0.787360818
                                              -0.539771775 -0.4433877046
                  -0.533478628
## REPAY JUN
                  -0.429263308
                                -0.519510913
                                              -0.757320032 -0.5526104236
## REPAY MAY
                  -0.400632748
                                -0.423711357
                                              -0.531575109 -0.7325212043
  REPAY APR
                  -0.365837679
                                -0.384725641
                                              -0.434655357 -0.5308481793
## BILL AMT SEP
                  -0.012090086
                                 0.017099033
                                                0.012356283
                                                             0.0005796195
## BILL_AMT_AUG
                  -0.016100950
                                -0.005309878
                                              -0.003318187 -0.0124383530
## BILL AMT JUL
                                               -0.021449145 -0.0273616413
                  -0.026096132
                                -0.009197520
## BILL AMT JUN
                  -0.034787329
                                -0.025255667
                                               -0.034582445 -0.0524153950
## BILL AMT MAY
                  -0.041981071
                                -0.034111766
                                               -0.048363175 -0.0639393540
                                -0.037362487
                                               -0.056335088 -0.0723378503
## BILL_AMT_APR
                  -0.045336876
## PAID AMT SEP
                   0.196664423
                                 0.048919610
                                                0.081365716
                                                             0.0877870606
## PAID_AMT_AUG
                   0.120736112
                                                             0.0764142506
                                 0.191532657
                                                0.056064365
## PAID_AMT_JUL
                   0.101160830
                                 0.110142024
                                                0.157255518
                                                             0.0434355606
## PAID AMT JUN
                   0.092696271
                                                0.093447967
                                 0.088342394
                                                             0.1253059102
## PAID AMT MAY
                   0.084497695
                                 0.084769838
                                                0.080055375
                                                             0.0771001690
## PAID AMT APR
                   0.089446466
                                 0.094339069
                                                0.088959256
                                                             0.0810136598
## DEFAULT
                  -0.338022325
                                              -0.275494664 -0.2669589548
                                -0.293583004
```

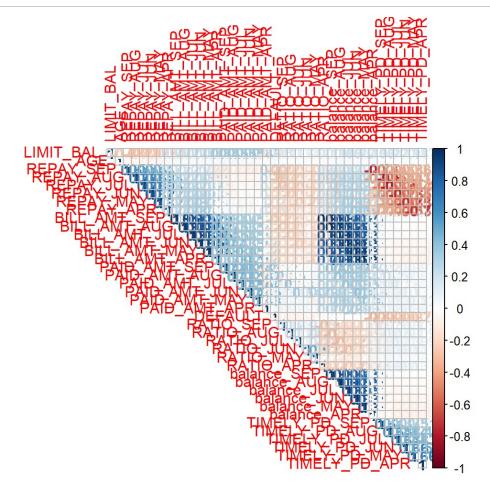
```
## RATIO_SEP
                   0.149097603
                                  0.058462440
                                                0.091063536
                                                              0.0980963770
## RATIO_AUG
                   0.096258655
                                  0.146771385
                                                0.084453199
                                                              0.0968990803
## RATIO JUL
                   0.090728247
                                  0.074703943
                                                0.127530575
                                                              0.0853982782
## RATIO JUN
                   0.091983026
                                  0.086293539
                                                0.080704840
                                                              0.1100960299
## RATIO_MAY
                   0.046953352
                                  0.045019877
                                                0.035069640
                                                              0.0586873582
## RATIO APR
                   0.094162488
                                  0.090642530
                                                0.095611389
                                                              0.1255314676
## balance SEP
                  -0.034901234
                                  0.008255684
                                                0.001047892 -0.0107954332
## balance AUG
                  -0.032439019
                                 -0.028078790
                                               -0.012850703 -0.0235497711
## balance_JUL
                  -0.040489083
                                 -0.023218988
                                               -0.040607646 -0.0361937896
## balance_JUN
                  -0.046665721
                                 -0.037384255
                                               -0.047592928 -0.0685346276
## balance MAY
                  -0.054256351
                                 -0.046173663
                                               -0.061058867 -0.0761657544
## balance_APR
                  -0.056938304
                                 -0.049948700
                                               -0.068687831 -0.0845444337
## TIMELY PD SEP
                   0.668175817
                                  0.430527007
                                                0.371030465
                                                              0.3485867526
## TIMELY_PD_AUG
                   1.000000000
                                  0.625247223
                                                0.478976661
                                                              0.4430469603
## TIMELY PD JUL
                                                0.625659761
                   0.625247223
                                  1.000000000
                                                              0.4823817389
## TIMELY_PD_JUN
                   0.478976661
                                                1.000000000
                                  0.625659761
                                                              0.6626371432
## TIMELY_PD_MAY
                   0.443046960
                                  0.482381739
                                                0.662637143
                                                              1.0000000000
  TIMELY PD APR
                   0.397391292
                                  0.434246955
                                                0.496442845
                                                              0.6626834794
##
                 TIMELY_PD_APR
## LIMIT BAL
                  1.732739e-01
## AGE
                  2.061267e-02
## REPAY SEP
                 -3.295186e-01
## REPAY_AUG
                 -3.732175e-01
## REPAY JUL
                 -4.049655e-01
## REPAY JUN
                 -4.475183e-01
## REPAY_MAY
                 -5.361770e-01
## REPAY_APR
                 -7.348118e-01
## BILL_AMT_SEP
                 -7.790246e-05
## BILL AMT AUG
                 -1.298033e-02
## BILL_AMT_JUL
                 -2.633602e-02
## BILL_AMT_JUN
                 -4.799944e-02
## BILL AMT MAY
                 -7.125941e-02
## BILL_AMT_APR
                 -7.519381e-02
## PAID_AMT_SEP
                  7.360718e-02
## PAID AMT AUG
                  7.879006e-02
## PAID AMT JUL
                  5.991920e-02
## PAID_AMT_JUN
                  1.556949e-02
## PAID_AMT_MAY
                  1.247374e-01
## PAID AMT APR
                  7.460022e-02
## DEFAULT
                 -2.460889e-01
## RATIO SEP
                  9.306310e-02
## RATIO_AUG
                  9.373738e-02
## RATIO JUL
                  8.952012e-02
## RATIO_JUN
                  6.789340e-02
## RATIO_MAY
                  3.197300e-02
## RATIO APR
                  6.723022e-02
## balance SEP
                 -1.014904e-02
## balance AUG
                 -2.411327e-02
## balance_JUL
                 -3.603230e-02
```

```
## balance_JUN -5.408811e-02
## balance_MAY -8.907984e-02
## balance_APR -8.605534e-02
## TIMELY_PD_SEP 3.098665e-01
## TIMELY_PD_AUG 3.973913e-01
## TIMELY_PD_JUL 4.342470e-01
## TIMELY_PD_JUN 4.964428e-01
## TIMELY_PD_MAY 6.626835e-01
## TIMELY_PD_APR 1.000000e+00
```

library(corrplot)

```
## corrplot 0.84 loaded
```

```
taiwan_bank1_matrix = cor(bank_data_num)
corrplot(taiwan_bank1_matrix, type="upper", method="number")
```



KMO Test

describe(bank_data1)

##		vars	n	mean	sd	median	trimmed	mad
##	LIMIT_BAL	1	30000		126722.92	140000.0	151607.40	
##	SEX	2	30000	1.60	0.49	2.0	1.63	0.00
##	EDUCATION		30000	1.85	0.79	2.0	1.78	1.48
##	MARRIAGE	4	30000	1.55	0.52	2.0	1.55	0.00
##	AGE	5	30000	35.49	9.22	34.0	34.69	8.90
##	REPAY_SEP	6	30000	-0.02	1.12	0.0	-0.06	1.48
##	REPAY_AUG	7	30000	-0.13	1.20	0.0	-0.20	0.00
##	REPAY_JUL	8	30000	-0.17	1.20	0.0	-0.24	0.00
##	REPAY_JUN	9	30000	-0.22	1.17	0.0	-0.31	0.00
##	REPAY_MAY	10	30000	-0.27	1.13	0.0	-0.36	0.00
##	REPAY_APR	11	30000	-0.29	1.15	0.0	-0.39	0.00
##	BILL_AMT_SEP	12	30000	47402.10	58937.52	22381.5	35359.66	32321.42
##	BILL_AMT_AUG	13	30000	45528.33	57005.11	21200.0	33836.10	30852.91
##	BILL_AMT_JUL	14	30000	43534.93	55081.75	20088.5	32064.43	29219.82
##	BILL_AMT_JUN	15	30000	40185.58	51604.88	19052.0	29212.37	27659.39
##	BILL_AMT_MAY	16	30000	37657.51	49383.59	18104.5	26920.95	26224.97
##	BILL_AMT_APR	17	30000	36262.58	48281.79	17071.0	25726.08	24840.96
##	PAID_AMT_SEP	18	30000	4175.04	5193.02	2100.0	2997.21	2864.38
##	PAID_AMT_AUG	19	30000	4123.77	5330.17	2009.0	2876.43	2951.86
##	PAID_AMT_JUL	20	30000	3634.39	4918.11	1800.0	2468.91	2661.27
##	PAID_AMT_JUN	21	30000	3359.59	4686.97	1500.0	2199.23	2223.90
##	PAID_AMT_MAY	22	30000	3350.00	4659.06	1500.0	2202.19	2223.90
##	PAID_AMT_APR	23	30000	3455.95	5037.28	1500.0	2165.33	2223.90
##	DEFAULT	24	30000	0.22	0.42	0.0	0.15	0.00
##	RATIO_SEP	25	30000	0.12	0.33	0.0	0.03	0.00
##	RATIO_AUG	26	30000	0.13	0.33	0.0	0.03	0.00
##	RATIO_JUL	27	30000	0.12	0.32	0.0	0.02	0.00
##	RATIO_JUN	28	30000	0.11	0.32	0.0	0.02	0.00
##	RATIO_MAY	29	30000	0.03	0.18	0.0	0.00	0.00
##	RATIO_APR	30	30000	0.13	0.34	0.0	0.04	0.00
##	balance_SEP	31	30000	42407.17	57907.66	18550.5	31661.62	28042.64
##	balance_AUG	32	30000	40712.70	55965.98	18102.5	30247.54	27328.02
##	balance_JUL	33	30000	39106.07	54197.24	17769.0	28875.89	26348.77
##	balance_JUN	34	30000	36240.28	50806.44	16970.0	26314.16	25159.72
##	balance_MAY	35	30000	33546.52	48076.22	15538.0	23994.38	23036.64
##	balance_APR	36	30000	32103.70	47142.10	13926.5	22794.62	20647.43
##	TIMELY_PD_SEP	37	30000	0.77	0.42	1.0	0.84	0.00
##	TIMELY_PD_AUG	38	30000	0.85	0.36	1.0	0.94	0.00
##	TIMELY_PD_JUL	39	30000	0.86	0.35	1.0	0.95	0.00
##	TIMELY_PD_JUN	40	30000	0.88	0.32	1.0	0.98	0.00
##	TIMELY_PD_MAY	41	30000	0.90	0.30	1.0	1.00	0.00
##	TIMELY_PD_APR	42	30000	0.90	0.30	1.0	1.00	0.00
##	_ _		in	max	range ske			
##	LIMIT_BAL	1000	00 520	000.00 510	000.00 0.8	37 -0.6	3 731.64	
	SEX		1	2.00	1.00 -0.4	42 -1.8	32 0.00	
##	EDUCATION		0	6.00	6.00 0.9			
##	MARRIAGE		0	3.00	3.00 -0.0			

```
## AGE
                     21
                            79.00
                                      58.00 0.73
                                                      0.04
                                                             0.05
## REPAY_SEP
                    -2
                            8.00
                                      10.00 0.73
                                                             0.01
                                                      2.72
                     -2
## REPAY AUG
                             8.00
                                      10.00 0.79
                                                      1.57
                                                             0.01
                                                      2.08
## REPAY JUL
                     -2
                             8.00
                                      10.00 0.84
                                                             0.01
                    -2
## REPAY JUN
                             8.00
                                      10.00 1.00
                                                      3.50
                                                             0.01
## REPAY MAY
                    -2
                             8.00
                                      10.00 1.01
                                                      3.99
                                                             0.01
                     -2
## REPAY APR
                             8.00
                                      10.00 0.95
                                                      3.43
                                                             0.01
## BILL_AMT_SEP
                -15308 201203.05 216511.05
                                            1.49
                                                      1.23 340.28
## BILL AMT AUG
                -69777 194792.20 264569.20 1.50
                                                      1.27 329.12
                -61506 187821.05 249327.05 1.53
                                                      1.34 318.01
## BILL_AMT_JUL
## BILL AMT JUN
                 -65167 174333.35 239500.35 1.56
                                                      1.38 297.94
## BILL_AMT_MAY
                 -61372 165794.30 227166.30 1.59
                                                      1.46 285.12
## BILL AMT APR
                -57060 161912.00 218972.00 1.59
                                                      1.47 278.76
## PAID_AMT_SEP
                         18428.20
                                  18428.20 1.82
                                                      2.39 29.98
## PAID AMT AUG
                        19004.35
                                  19004.35 1.90
                                                      2.67 30.77
## PAID_AMT_JUL
                     0 17589.40
                                  17589.40 1.93
                                                      2.81 28.39
## PAID_AMT_JUN
                     0 16014.95
                                  16014.95 1.88
                                                      2.44 27.06
                     0 16000.00
## PAID AMT MAY
                                  16000.00
                                            1.89
                                                      2.48 26.90
## PAID_AMT_APR
                     0 17343.80
                                  17343.80 1.98
                                                      2.81 29.08
## DEFAULT
                     0
                             1.00
                                       1.00 1.34
                                                     -0.20
                                                             0.00
## RATIO_SEP
                     0
                             1.00
                                       1.00 2.29
                                                      3.25
                                                             0.00
## RATIO AUG
                     0
                             1.00
                                       1.00 2.23
                                                      2.99
                                                             0.00
## RATIO_JUL
                     0
                             1.00
                                      1.00 2.35
                                                      3.52
                                                             0.00
## RATIO JUN
                     0
                             1.00
                                                      3.98
                                       1.00 2.45
                                                             0.00
## RATIO MAY
                     0
                             1.00
                                       1.00 5.18
                                                     24.79
                                                             0.00
                             1.00
## RATIO APR
                     0
                                       1.00 2.18
                                                      2.73
                                                             0.00
## balance SEP
                -90862 191911.60 282773.60 1.40
                                                      1.13 334.33
## balance AUG
                -87288 185663.85 272951.85 1.42
                                                      1.17 323.12
## balance JUL
                -83226 179756.00 262982.00 1.44
                                                      1.24 312.91
## balance JUN
                -74731 166742.10 241473.10 1.48
                                                      1.30 293.33
## balance_MAY
                -70034 157664.75 227698.75 1.51
                                                      1.38 277.57
                -69089 153520.35 222609.35 1.50
## balance APR
                                                      1.37 272.18
## TIMELY_PD_SEP
                             1.00
                                       1.00 -1.30
                                                     -0.31
                                                             0.00
## TIMELY_PD_AUG
                     0
                             1.00
                                       1.00 -1.98
                                                      1.93
                                                             0.00
## TIMELY_PD_JUL
                     0
                             1.00
                                       1.00 -2.07
                                                      2.28
                                                             0.00
## TIMELY PD JUN
                     0
                             1.00
                                       1.00 -2.38
                                                      3.68
                                                             0.00
## TIMELY PD MAY
                     0
                             1.00
                                       1.00 -2.69
                                                      5.22
                                                             0.00
## TIMELY_PD_APR
                     0
                             1.00
                                       1.00 -2.62
                                                      4.86
                                                             0.00
```

```
bank_data_cor <- subset(bank_data1, select = -c(1,2,3,4,5,24))
#is.na(bank_data1)
cormatrix_bank = cor(bank_data_cor)
library(psych)
cortest.bartlett(cormatrix_bank,100)</pre>
```

```
## $chisq
## [1] 4723.631
##
## $p.value
## [1] 0
##
## $df
## [1] 630
```

```
KMO(cormatrix_bank)
```

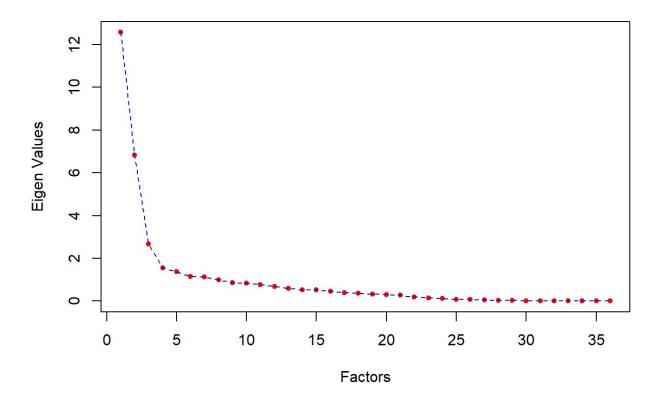
```
## Kaiser-Meyer-Olkin factor adequacy
## Call: KMO(r = cormatrix_bank)
## Overall MSA = 0.84
## MSA for each item =
##
       REPAY_SEP
                      REPAY_AUG
                                     REPAY_JUL
                                                    REPAY_JUN
                                                                  REPAY_MAY
                                                                        0.76
##
            0.72
                           0.72
                                          0.78
                                                         0.78
                                                BILL_AMT_JUL
##
       REPAY APR
                   BILL_AMT_SEP
                                  BILL_AMT_AUG
                                                               BILL AMT JUN
                                                         0.91
                                                                        0.91
##
            0.79
                           0.89
                                          0.91
##
    BILL_AMT_MAY
                   BILL_AMT_APR
                                 PAID_AMT_SEP
                                                PAID_AMT_AUG
                                                               PAID_AMT_JUL
##
            0.91
                           0.89
                                          0.84
                                                         0.83
                                                                        0.82
##
    PAID_AMT_JUN
                   PAID_AMT_MAY
                                  PAID_AMT_APR
                                                    RATIO_SEP
                                                                  RATIO_AUG
##
            0.84
                           0.83
                                          0.77
                                                         0.90
                                                                        0.88
       RATIO_JUL
                      RATIO_JUN
                                     RATIO MAY
                                                    RATIO_APR
                                                                balance SEP
##
##
            0.86
                           0.85
                                          0.87
                                                         0.86
                                                                        0.88
##
     balance AUG
                    balance_JUL
                                   balance JUN
                                                 balance MAY
                                                                balance APR
##
            0.90
                           0.90
                                          0.90
                                                         0.90
                                                                        0.89
## TIMELY PD SEP TIMELY PD AUG TIMELY PD JUL TIMELY PD JUN TIMELY PD MAY
                           0.62
                                          0.69
                                                         0.69
##
                                                                        0.66
## TIMELY_PD_APR
##
            0.70
```

We have checked Kaiser-Meyer-Olkin (KMO) to find the Test for Sampling Adequacy whereas the values in this case is greater than .5 , hence the data set is occurred with enough samples .

```
#Check eigen values
evector = eigen(cormatrix_bank)
eigen_value = evector$values
eigen_value
```

```
##
  [1] 12.564536917 6.837047228 2.673468931 1.545928586 1.384570984
##
   [6] 1.147488741 1.117272212 0.984109325 0.860073851 0.845526832
## [11]
        0.777669220 0.675126384
                                 0.595873143  0.529439215  0.520280068
## [16]
       0.454700120 0.395735592
                                 0.372796398 0.324856581 0.292909561
## [21] 0.268496618 0.191038994
                                 0.152532812  0.111790321  0.082502461
## [26] 0.076962738 0.065080659
                                 0.043633264
                                             0.028124844
                                                         0.020848150
## [31]
        0.017292527 0.011301741
                                 0.009076509 0.008154693
                                                         0.007504493
## [36] 0.006249286
```

```
plot(eigen_value, xlab = "Factors", ylab = "Eigen Values", col="red", pch=20)
lines(eigen_value, col="blue", lty = 2)
```



```
fa1 = fa(r= bank_data_cor, nfactors =8, rotate ="none", fm ="pa")
print(fa1)
```

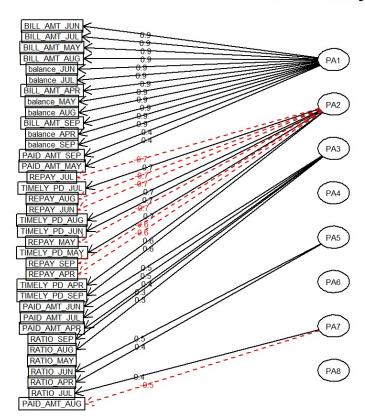
```
## Factor Analysis using method = pa
## Call: fa(r = bank_data_cor, nfactors = 8, rotate = "none", fm = "pa")
## Standardized loadings (pattern matrix) based upon correlation matrix
                  PA1
                        PA2
                              PA3
                                    PA4
                                          PA5
                                                PA6
                                                     PA7
                                                           PA8
                                                                 h2
##
                                                                       u2
## REPAY SEP
                 0.35 -0.64 -0.10
                                  0.35 -0.11 -0.12 -0.09
                                                          0.16 0.72 0.280
                 0.43 -0.70 -0.01 0.23 -0.05 0.12 0.00 0.24 0.80 0.200
## REPAY AUG
## REPAY JUL
                 0.45 -0.71 0.09 0.00 0.01 0.39 0.13
                                                          0.04 0.89 0.111
                 0.46 -0.69 0.15 -0.24
                                        0.05 0.17 -0.15 0.02 0.83 0.171
## REPAY JUN
                 0.47 -0.67 0.19 -0.36 -0.04 -0.08
                                                    0.00 0.16 0.86 0.137
## REPAY_MAY
                 0.47 -0.61 0.22 -0.31 0.14 -0.19
                                                    0.06 0.25 0.85 0.151
## REPAY APR
## BILL AMT SEP
                      0.21 -0.15 0.06
                                        0.08
                                              0.07 -0.01 0.11 0.90 0.101
## BILL AMT AUG
                 0.93 0.20 -0.12 0.05
                                        0.06 0.12 0.01 0.04 0.93 0.066
## BILL_AMT_JUL
                 0.94 0.20 -0.08 0.02 0.03 0.04 -0.12 -0.04 0.95 0.051
## BILL AMT JUN
                 0.94
                      0.19 -0.02 -0.01 -0.06 -0.08
                                                   0.03 -0.09 0.94 0.057
                 0.93 0.19
                            0.03 0.02 0.06 -0.15
                                                    0.07 -0.12 0.94 0.057
## BILL_AMT_MAY
## BILL AMT APR
                 0.91 0.17 0.02 0.01 0.00 -0.14 0.07 -0.13 0.89 0.105
## PAID AMT SEP
                 0.40
                       0.36
                            0.37 -0.05 -0.10 0.27
                                                    0.03 -0.05 0.52 0.481
## PAID AMT AUG
                 0.37
                       0.38
                            0.45 -0.06 -0.19 0.02 -0.48
                                                          0.03 0.76 0.238
## PAID AMT JUL
                 0.36
                       0.37
                             0.48 0.00 -0.37 -0.09
                                                    0.25
                                                          0.14 0.72 0.277
                             0.54 0.18 0.23 -0.01 0.04 0.15 0.66 0.340
## PAID_AMT_JUN
                 0.36 0.37
## PAID AMT MAY
                 0.36
                      0.33
                            0.36
                                  0.06 -0.18 0.09 -0.02 0.05 0.41 0.588
## PAID AMT APR
                      0.32 0.37 0.05 -0.12 0.09 -0.04 0.12 0.38 0.616
## RATIO SEP
                -0.24 0.21 0.31 -0.01 -0.07 0.12 0.06 -0.21 0.26 0.736
## RATIO_AUG
                -0.25 0.21
                            0.30
                                  0.00 -0.05 -0.12 -0.30 -0.09 0.31 0.687
                                  0.04 -0.20 -0.12 0.36 -0.01 0.36 0.637
## RATIO JUL
                -0.24
                       0.19
                            0.29
                -0.26
                       0.20 0.37
                                   0.22 0.49 -0.04
                                                    0.00 -0.01 0.54 0.464
## RATIO JUN
                      0.11 0.21
                                  0.11 0.18 0.01 0.02 0.02 0.11 0.887
## RATIO_MAY
                -0.11
## RATIO APR
                -0.26
                      0.19 0.36
                                  0.20
                                        0.42 -0.02 0.03 0.03 0.45 0.549
## balance SEP
                 0.87
                       0.16 - 0.21
                                  0.07 0.10
                                              0.03 -0.01 0.13 0.86 0.138
                       0.16 -0.19 0.06 0.09 0.12 0.09
## balance_AUG
                 0.90
                                                          0.04 0.91 0.088
## balance_JUL
                 0.92  0.16 -0.15  0.02  0.10  0.06 -0.17 -0.06  0.94  0.062
                 0.92  0.15  -0.11  -0.05  -0.11  -0.07  0.03  -0.12  0.92  0.079
## balance_JUN
## balance MAY
                 0.91 0.14 -0.03 0.01 0.10 -0.16 0.07 -0.12 0.90 0.099
                 0.88 0.13 -0.04 0.00 0.03 -0.16 0.08 -0.15 0.86 0.143
## balance_APR
                                                    0.11 0.08 0.80 0.203
## TIMELY PD SEP -0.06 0.58 -0.02 -0.57 0.18 0.27
## TIMELY_PD_AUG -0.17
                       0.69 -0.12 -0.43 0.10 0.02
                                                    0.02
                                                          0.01 0.71 0.289
## TIMELY PD JUL -0.16
                       0.70 -0.21 -0.17 0.00 -0.29 -0.18
                                                          0.27 0.78 0.225
## TIMELY PD JUN -0.18
                       0.68 -0.25 0.09 -0.07 -0.08 0.11 0.29 0.68 0.323
## TIMELY PD MAY -0.19
                       0.66 -0.26 0.22 -0.01 0.18 0.01
                                                          0.14 0.64 0.363
## TIMELY PD APR -0.17
                       0.59 -0.26 0.20 -0.13 0.25 -0.05 0.01 0.57 0.430
##
                COM
## REPAY SEP
                2.7
                2.3
## REPAY_AUG
## REPAY_JUL
                2.5
## REPAY_JUN
                2.4
## REPAY MAY
                2.8
## REPAY APR
                3.6
## BILL_AMT_SEP
                1.2
```

```
## BILL_AMT_AUG 1.2
## BILL_AMT_JUL 1.1
## BILL AMT JUN
                1.1
## BILL AMT MAY
## BILL_AMT_APR 1.2
## PAID AMT SEP 4.0
## PAID AMT AUG 4.2
## PAID_AMT_JUL
                4.7
## PAID_AMT_JUN
                3.6
## PAID_AMT_MAY
                3.7
## PAID AMT APR
                3.6
## RATIO_SEP
                4.2
## RATIO AUG
                4.3
## RATIO_JUL
                4.4
## RATIO JUN
                3.4
## RATIO_MAY
                3.9
## RATIO_APR
                3.7
## balance SEP
                1.3
## balance_AUG
                1.2
## balance JUL
                1.2
## balance_JUN
                1.2
## balance MAY
                1.2
## balance_APR
                1.2
## TIMELY_PD_SEP 2.8
## TIMELY PD AUG 2.0
## TIMELY_PD_JUL 2.4
## TIMELY_PD_JUN 2.0
## TIMELY_PD_MAY 2.0
## TIMELY_PD_APR 2.4
##
##
                          PA1 PA2 PA3 PA4 PA5 PA6 PA7 PA8
                      12.43 6.57 2.25 1.26 0.95 0.80 0.71 0.60
## SS loadings
## Proportion Var
                        0.35 0.18 0.06 0.03 0.03 0.02 0.02 0.02
## Cumulative Var
                        0.35 0.53 0.59 0.63 0.65 0.67 0.69 0.71
## Proportion Explained 0.49 0.26 0.09 0.05 0.04 0.03 0.03 0.02
## Cumulative Proportion 0.49 0.74 0.83 0.88 0.92 0.95 0.98 1.00
## Mean item complexity = 2.6
## Test of the hypothesis that 8 factors are sufficient.
## The degrees of freedom for the null model are 630 and the objective function was
54.82 with Chi Square of 1643833
## The degrees of freedom for the model are 370 and the objective function was 16.01
##
## The root mean square of the residuals (RMSR) is 0.03
## The df corrected root mean square of the residuals is 0.04
##
## The harmonic number of observations is 30000 with the empirical chi square 31288.
72 with prob < 0
```

```
## The total number of observations was 30000 with Likelihood Chi Square = 479933.5
with prob < 0
##
## Tucker Lewis Index of factoring reliability = 0.503
## RMSEA index = 0.208 and the 90 % confidence intervals are 0.207 0.208
## BIC = 476119.2
## Fit based upon off diagonal values = 0.99
## Measures of factor score adequacy
##
                                                     PA1 PA2 PA3 PA4 PA5
## Correlation of (regression) scores with factors
                                                    1.00 0.98 0.94 0.93 0.87
## Multiple R square of scores with factors
                                                    0.99 0.97 0.88 0.87 0.76
## Minimum correlation of possible factor scores
                                                    0.99 0.94 0.75 0.73 0.52
##
                                                     PA6 PA7 PA8
## Correlation of (regression) scores with factors
                                                    0.93 0.88 0.87
## Multiple R square of scores with factors
                                                    0.86 0.78 0.75
## Minimum correlation of possible factor scores
                                                    0.72 0.56 0.51
```

fa.diagram(fa1)

Factor Analysis



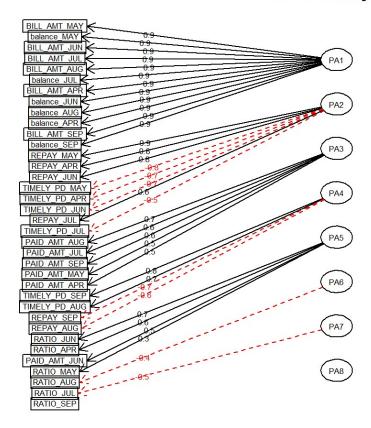
```
## Factor Analysis using method = pa
## Call: fa(r = bank_data_cor, nfactors = 8, rotate = "varimax", fm = "pa")
## Standardized loadings (pattern matrix) based upon correlation matrix
                  PA1
                        PA2
                             PA3
                                   PA4
                                         PA5
                                               PA6
                                                    PA7
                                                          PA8
                                                                h2
##
                                                                      u2
## REPAY SEP
                 0.19 0.51 -0.01 -0.56 -0.14 0.36 0.17
## REPAY AUG
                                                         0.11 0.80 0.200
## REPAY JUL
                 0.18
                      0.65 0.02 -0.30 -0.14 0.51 0.17 -0.19 0.89 0.111
                           0.05 -0.17 -0.17 0.16 0.29 -0.06 0.83 0.171
## REPAY JUN
                 0.19 0.79
                 0.20 0.85 0.05 -0.10 -0.23 0.09 0.03
## REPAY_MAY
                                                         0.15 0.86 0.137
                      0.83 -0.02 -0.08 -0.04 0.10 -0.02
## REPAY APR
                 0.24
                                                         0.28 0.85 0.151
## BILL AMT SEP
                           0.17 -0.03 -0.07
                                             0.18
                                                   0.14
                                                         0.13 0.90 0.101
## BILL AMT AUG
                 0.92 0.02 0.19 -0.01 -0.08 0.18
                                                   0.13
                                                         0.04 0.93 0.066
                 0.92 0.06 0.23 -0.02 -0.10 0.02 0.17
## BILL_AMT_JUL
                                                         0.01 0.95 0.051
## BILL AMT JUN
                 0.93 0.10
                           0.22 -0.02 -0.14 -0.01 -0.05
                                                         0.00 0.94 0.057
                 0.94 0.14
                           0.16 -0.02 0.00 -0.05 -0.08 0.00 0.94 0.057
## BILL_AMT_MAY
                 0.91 0.13 0.17 -0.03 -0.06 -0.05 -0.10 -0.02 0.89 0.105
## BILL AMT APR
## PAID AMT SEP
                 0.35 -0.03
                            0.55
                                 0.18
                                       0.09 0.08 -0.04 -0.19 0.52 0.481
## PAID AMT AUG
                 0.28 - 0.01
                            0.71
                                 0.07
                                        0.05 -0.36 0.20
                                                         0.02 0.76 0.238
## PAID AMT JUL
                 0.28 -0.02
                           0.64
                                 0.05
                                       0.00 0.00 -0.48
                                                         0.08 0.72 0.277
                            0.48 0.03 0.53 0.01 -0.11 0.08 0.66 0.340
## PAID_AMT_JUN
                 0.36 0.00
## PAID AMT MAY
                 0.31 -0.07
                            0.55
                                 0.02 0.07 -0.01 -0.10 -0.03 0.41 0.588
## PAID AMT APR
                 0.26 -0.05
                           0.54 0.04 0.13 0.00 -0.07 0.03 0.38 0.616
## RATIO SEP
                -0.21 -0.11 0.23 0.14 0.16 -0.08 -0.15 -0.29 0.26 0.736
## RATIO_AUG
                -0.24 -0.10
                            0.25 0.06 0.16 -0.39 0.04 -0.04 0.31 0.687
## RATIO JUL
                -0.22 - 0.12
                           0.18 0.06
                                       0.10 0.00 -0.50 -0.05 0.36 0.637
## RATIO JUN
                            0.02 0.05 0.70 -0.08 -0.01 -0.03 0.54 0.464
                -0.15 -0.09
                -0.08 -0.05 0.07 0.02 0.31 -0.01 -0.03 -0.01 0.11 0.887
## RATIO_MAY
## RATIO APR
                -0.17 -0.09
                           0.05 0.06 0.64 -0.03 -0.03 -0.01 0.45 0.549
## balance SEP
                 0.88
                      0.01 0.09 -0.05 -0.08 0.16 0.15
                                                         0.17 0.86 0.138
                           0.09 -0.02 -0.09 0.25
## balance_AUG
                 0.91 0.03
                                                   0.09
                                                         0.04 0.91 0.088
## balance_JUL
                 0.91 0.07
                           0.14 -0.02 -0.10 0.02 0.26
                                                         0.00 0.94 0.062
                           0.16 -0.02 -0.24 -0.02 -0.03 -0.02 0.92 0.079
## balance_JUN
                 0.91 0.10
## balance MAY
                            0.08 -0.03 -0.01 -0.04 -0.07
                 0.93 0.15
                                                         0.01 0.90 0.099
                 0.90 0.14
                           0.09 -0.03 -0.08 -0.05 -0.09 -0.02 0.86 0.143
## balance_APR
## TIMELY PD SEP
                 0.04 -0.21
                            0.14 0.84 0.04 0.13 0.04 0.04 0.80 0.203
## TIMELY_PD_AUG
                 0.02 - 0.40
                            0.05
                                 0.72 0.02 -0.12 -0.03
                                                         0.09 0.71 0.289
## TIMELY PD JUL
                 0.03 -0.54
                           0.06
                                 0.41
                                       0.00 -0.31 -0.01 0.46 0.78 0.225
## TIMELY_PD_JUN
                 0.02 -0.69 0.06 0.24 0.03 0.03 -0.15
                                                         0.33 0.68 0.323
## TIMELY PD MAY
                 0.01 -0.76 0.08 0.17 0.08 0.11 0.06
                                                         0.09 0.64 0.363
## TIMELY PD APR -0.01 -0.72 0.12 0.13 -0.05 0.08 0.10 -0.06 0.57 0.430
##
                com
## REPAY SEP
                2.2
## REPAY_AUG
                3.4
## REPAY_JUL
                3.1
## REPAY_JUN
                1.7
## REPAY MAY
                1.4
## REPAY APR
                1.5
## BILL_AMT_SEP
                1.3
```

```
## BILL_AMT_AUG 1.2
## BILL_AMT_JUL 1.2
## BILL AMT JUN
                1.2
## BILL_AMT_MAY
## BILL_AMT_APR 1.2
## PAID_AMT_SEP
                2.4
## PAID AMT AUG 2.1
## PAID_AMT_JUL
                2.3
## PAID_AMT_JUN
                2.9
## PAID_AMT_MAY
                1.7
## PAID AMT APR
                1.7
## RATIO_SEP
                5.2
## RATIO AUG
                3.2
## RATIO_JUL
                1.9
## RATIO JUN
                1.2
## RATIO_MAY
                1.3
## RATIO_APR
                1.2
## balance SEP
                1.3
## balance_AUG
                1.2
## balance JUL
                1.3
## balance_JUN
                1.2
## balance MAY
                1.1
## balance_APR
                1.1
## TIMELY_PD_SEP 1.2
## TIMELY PD AUG 1.7
## TIMELY_PD_JUL 3.5
## TIMELY_PD_JUN 1.8
## TIMELY_PD_MAY 1.2
## TIMELY_PD_APR 1.2
##
##
                          PA1 PA2 PA3 PA4 PA5 PA6 PA7 PA8
## SS loadings
                      11.01 5.10 2.56 2.51 1.67 1.05 0.97 0.71
## Proportion Var
                        0.31 0.14 0.07 0.07 0.05 0.03 0.03 0.02
## Cumulative Var
                        0.31 0.45 0.52 0.59 0.63 0.66 0.69 0.71
## Proportion Explained 0.43 0.20 0.10 0.10 0.07 0.04 0.04 0.03
## Cumulative Proportion 0.43 0.63 0.73 0.83 0.89 0.93 0.97 1.00
## Mean item complexity = 1.8
## Test of the hypothesis that 8 factors are sufficient.
## The degrees of freedom for the null model are 630 and the objective function was
54.82 with Chi Square of 1643833
## The degrees of freedom for the model are 370 and the objective function was 16.01
##
## The root mean square of the residuals (RMSR) is 0.03
## The df corrected root mean square of the residuals is 0.04
##
## The harmonic number of observations is 30000 with the empirical chi square 31288.
72 with prob < 0
```

```
## The total number of observations was 30000 with Likelihood Chi Square = 479933.5
with prob < 0
##
## Tucker Lewis Index of factoring reliability = 0.503
## RMSEA index = 0.208 and the 90 % confidence intervals are 0.207 0.208
## BIC = 476119.2
## Fit based upon off diagonal values = 0.99
## Measures of factor score adequacy
##
                                                     PA1 PA2 PA3 PA4 PA5
## Correlation of (regression) scores with factors
                                                    0.99 0.97 0.92 0.95 0.88
## Multiple R square of scores with factors
                                                    0.98 0.94 0.85 0.89 0.78
## Minimum correlation of possible factor scores
                                                    0.96 0.88 0.70 0.79 0.55
##
                                                     PA6 PA7 PA8
## Correlation of (regression) scores with factors
                                                    0.91 0.90 0.88
## Multiple R square of scores with factors
                                                    0.84 0.81 0.77
## Minimum correlation of possible factor scores
                                                    0.67 0.63 0.54
```

fa.diagram(fa2)

Factor Analysis



#Renaming vairbles

```
bank_final <- subset(bank_data1,select = c(1,2,3,4,5,24))
bank_final_data = cbind(bank_final,fa2$scores)
head(bank_final_data)</pre>
```

```
##
   LIMIT BAL SEX EDUCATION MARRIAGE AGE DEFAULT
                                    PA1
                                            PA2
## 1
     20000
                 2
                      1 24
                              1 -0.65505048 -1.566069537
          2
## 2
     120000
          2
                2
                      2 26
                             1 -0.85452952 1.053568856
## 3
     90000
          2
                2
                      2 34
                              0 -0.52269375  0.096085124
                2
                      1 37
## 4
     50000
          2
                              0 -0.04871894 -0.002544749
     50000
                2
                      1 57
## 5
          1
                              0 -0.85332389 0.266568820
     50000
## 6
          1
                1
                      2 37
                              0 -0.08186224 -0.065224365
##
       PA3
              PA4
                     PA5
                            PA6
                                   PA7
                                          PA8
## 1 -0.5853008 -2.7396537 -0.28868694 -0.3336919 0.4391205 0.1522075
## 4 -0.4353623 0.5266916 -0.39476438 0.4034434 0.5480870 0.5670916
```

colnames(bank_final_data) = c("LIMIT_BAL","SEX","EDUCATION","MARRIAGE","AGE","DEFAUL
T","BILLED _AMT", "REPAY_STATUS ", "PAID_AMT", "TIMELY_PAID_AMT", "RATIO_PADI_AM
T1", "RATIO_PADI_AMT2", "RATIO_PADI_AMT3","RATIO_PADI_AMT4")
str(bank_final_data)

```
## 'data.frame': 30000 obs. of 14 variables:
## $ LIMIT BAL : num 20000 120000 90000 50000 50000 50000 100000 140000
20000 ...
##
  $ SEX
                  : int 2 2 2 2 1 1 1 2 2 1 ...
##
  $ EDUCATION
                  : int 2 2 2 2 2 1 1 2 3 3 ...
  $ MARRIAGE
                   : int 1221122212...
##
  $ AGE
                  : int 24 26 34 37 57 37 29 23 28 35 ...
## $ DEFAULT
                  : int 1100000000...
## $ BILLED _AMT
                   : num -0.6551 -0.8545 -0.5227 -0.0487 -0.8533 ...
  $ REPAY_STATUS : num -1.56607 1.05357 0.09609 -0.00254 0.26657 ...
##
##
  $ PAID AMT
                   : num -0.585 -0.416 -0.3 -0.435 1.929 ...
## $ TIMELY PAID AMT: num -2.74 0.164 0.487 0.527 -0.191 ...
## $ RATIO_PADI_AMT1: num -0.2887 -0.0338 -0.4383 -0.3948 -0.1997 ...
  $ RATIO PADI AMT2: num -0.334 0.465 0.44 0.403 -1.972 ...
## $ RATIO_PADI_AMT3: num 0.439 -0.132 0.264 0.548 0.866 ...
   $ RATIO PADI AMT4: num 0.152 1.461 0.74 0.567 1.09 ...
```

The variable we would be considering

Check the proportion of data

```
### Check the proportion of data #
#Default payment in June, 2005 (1=yes, 0=no)
table(bank_final_data$DEFAULT)
```

```
##
## 0 1
## 23364 6636
```

```
nrow(subset(bank_final_data, DEFAULT == 1))/nrow(bank_final_data)
```

```
## [1] 0.2212
```

Take the sample subset from the major class (here negative)

```
set.seed(123)
train_idx <- sample(c(6:nrow(bank_final_data)), round(nrow(bank_final_data) * 0.7,0),
replace = FALSE)
train_data <- bank_final_data[train_idx,]
test_data <- bank_final_data[-train_idx,]</pre>
table(train_data$DEFAULT)
```

```
##
## 0 1
## 16360 4640
```

```
table(test_data$DEFAULT)
```

Checking the samples counts

```
train.pos <- subset(train_data, DEFAULT == 1)
train.neg <- subset(train_data, DEFAULT == 0)

dim(train.pos)

## [1] 4640    14

dim(train.neg)

## [1] 16360    14</pre>
```

Take the sample subset from the major class (here negative)

```
## Set the seed
set.seed(108)

train.neg.sub_idx <- sample(c(24:nrow(train.neg)), nrow(train.pos), replace = FALSE)
train_new <- train.neg[train.neg.sub_idx,]
dim(train_new)</pre>
## [1] 4640 14
```

Merge the negative and positive cases

4640 4640

```
train_new <- rbind(train_new, train.pos)
table(train_new$DEFAULT)

##
##
##
0 1</pre>
```

Rendomizing the data

```
train_new <- train_new[sample(6:nrow(train_new)),]
### Now check the proportion of target in the sample
## in train_data
nrow(subset(train_data, DEFAULT == 1))/nrow(train_data)</pre>
## [1] 0.2209524
```

```
## [1] 0.2209524

## in train.new
nrow(subset(train_new, DEFAULT == 1))/nrow(train_new)

## [1] 0.5002695

table(train_new$DEFAULT)

## ## 0 1
## 4635 4640
```

```
str(train_new)
```

```
## 'data.frame':
                  9275 obs. of 14 variables:
                  : num 80000 30000 150000 40000 500000 180000 20000 310000 10000
## $ LIMIT_BAL
30000 ...
## $ SEX
                   : int 1122211211...
## $ EDUCATION
                  : int 3 1 1 3 1 1 2 3 2 1 ...
## $ MARRIAGE
                  : int 2121221221...
## $ AGE
                   : int 30 37 52 41 34 31 25 38 43 32 ...
## $ DEFAULT
                  : int 1100001011...
                  : num -0.57 -0.212 -0.585 -0.585 0.724 ...
## $ BILLED _AMT
## $ REPAY_STATUS : num 0.0364 0.08 0.0362 1.7462 -0.0812 ...
## $ PAID AMT
                   : num -0.5159 -0.3857 2.9588 -0.0822 -0.4153 ...
## $ TIMELY_PAID_AMT: num 0.4542 0.5058 0.0266 -1.7071 0.481 ...
## $ RATIO_PADI_AMT1: num -0.4017 -0.4105 0.0517 -0.4185 -0.3699 ...
## $ RATIO PADI AMT2: num 0.672 0.303 0.966 0.126 0.206 ...
## $ RATIO_PADI_AMT3: num 0.567 0.152 0.235 0.181 0.233 ...
## $ RATIO PADI AMT4: num 1.292 0.519 1.933 -1.44 0.348 ...
```