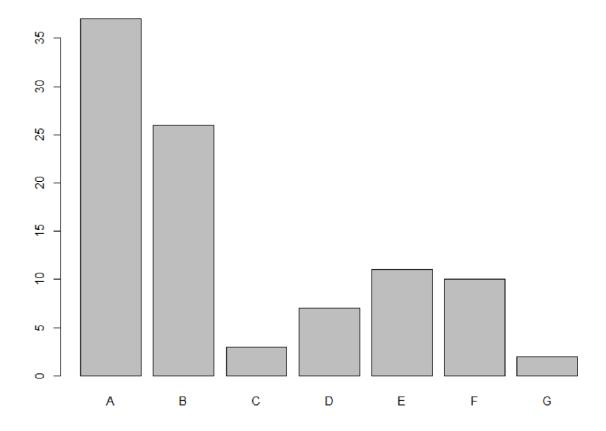


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(a) Use the same data splitting approach (if any) and pre-processing steps that you did in the previous chapter. Using the same classification statistic as before, build models described in this chapter for these data.

The data is not evenly distributed among all the classes. Classes A and B have the highest no of occurrences whereas C and G have the least no of occurrence. It is a multinomial problem since there are 5 categories of Oil so the data set can be summarized as follows No of predictors(p):

7 No of classes:5

No of instances(n): 96

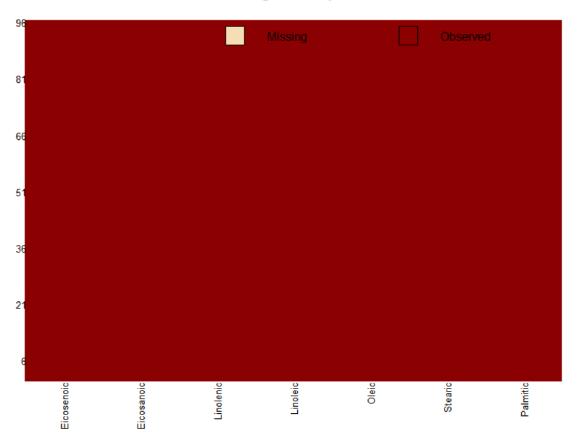
Preprocessing of Data:

Near Zero Variance mitigation:

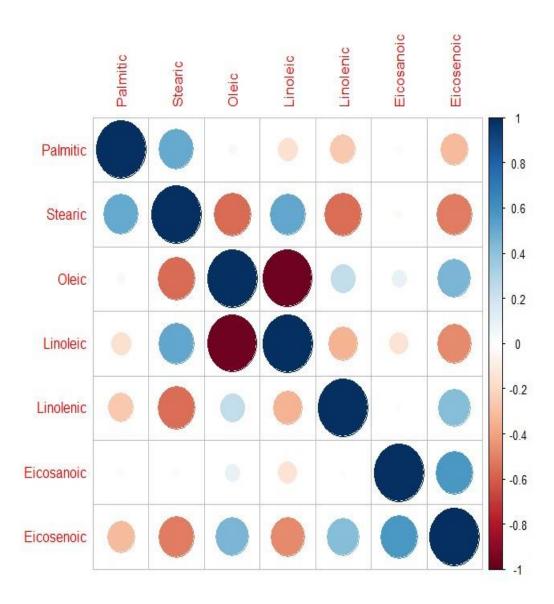
"Dropping 0 zero variance columns from 7 (fraction= Missing values:

0.000000)"

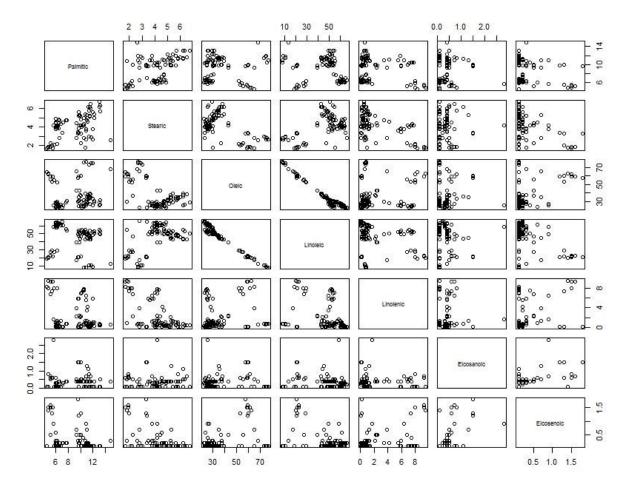
# **Missingness Map Test**



Linear Correlations:



As we can see from the plot linoleic and oleic show a very high negative correlation. And hence the 4th one is eliminated.



We may want to center and scale the data for better model performances. As required.

# Data Splitting and Resampling:

Dividing the Data into Training and testing is not the best approach for this data set as the data set is very small. Unless we upsample the data to get more instances of minority class. However we have decided **not to split the data**.

ctrl <- trainControl(method = 'LGOCV',classProbs = TRUE,savePredictions = TRUE, summaryFunction = multiClassSummary)

#### MODEL SELECTION:

Kappa is used as metric since there are more than two classes hence roc cannot be used, and kappa works best with imbalanced classes since it takes it account the distribution of classes.

#### Mixture Discriminant Analysis ####

Mixture Discriminant Analysis

96 samples

6 predictor

7 classes: 'A', 'B', 'C', 'D', 'E', 'F', 'G'

No pre-processing

Resampling: Repeated Train/Test Splits Estimated (4 reps, 75%)

Summary of sample sizes: 76, 76, 76, 76

Resampling results across tuning parameters:

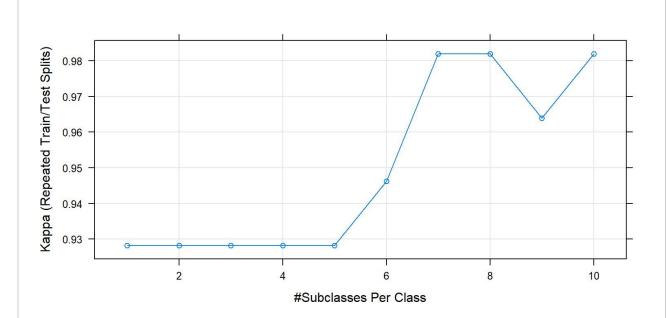
subclasses Accuracy Kappa

- 1 0.9500 0.9281846
- 2 0.9500 0.9281846
- 3 0.9500 0.9281846
- 4 0.9500 0.9281846
- 5 0.9500 0.9281846
- 6 0.9625 0.9462352
- 7 0.9875 0.9819495
- 8 0.9875 0.9819495
- 9 0.9750 0.9638989
- 10 0.9875 0.9819495

Kappa was used to select the optimal model using the largest value.

The final value used for the model was subclasses = 7.

Plot:



#### Regularized Discriminant Analysis ####

Regularized Discriminant Analysis

96 samples

6 predictor

7 classes: 'A', 'B', 'C', 'D', 'E', 'F', 'G'

Pre-processing: centered (6), scaled (6)

Resampling: Repeated Train/Test Splits Estimated (4 reps, 75%)

Summary of sample sizes: 76, 76, 76, 76

Resampling results across tuning parameters:

gamma lambda Accuracy Kappa

 $0.1\quad 0.0000000\ 0.9500\quad 0.9281846$ 

 $0.1 \quad 0.11111111 \ 0.9500 \quad 0.9281846$ 

0.1 0.2222222 0.9500 0.9281846

0.1 0.3333333 0.9500 0.9281846

0.1 0.4444444 0.9500 0.9281846

```
0.5555556 0.9500 0.9281846
0.1
    0.6666667 0.9500 0.9281846
0.1
0.1 0.7777778 0.9500 0.9281846
0.1 0.8888889 0.9500 0.9281846
0.1 1.0000000 0.9500 0.9281846
0.2 0.0000000 0.9375 0.9108954
0.2 0.1111111 0.9500 0.9281846
0.2 0.2222222 0.9500 0.9281846
0.2 0.3333333 0.9500 0.9281846
0.2 0.4444444 0.9500 0.9281846
0.2 0.5555556 0.9500 0.9281846
0.2 0.6666667 0.9500 0.9281846
0.2 0.7777778 0.9500 0.9281846
0.2 0.8888889 0.9500 0.9281846
0.2 1.0000000 0.9500 0.9281846
0.3 0.0000000 0.9375 0.9108954
0.3 0.1111111 0.9500 0.9281846
0.3 0.2222222 0.9500 0.9281846
0.3 0.3333333 0.9500 0.9281846
0.3 0.4444444 0.9500 0.9281846
0.3 0.5555556 0.9500 0.9281846
```

```
      0.3
      0.66666667
      0.9500
      0.9281846

      0.3
      0.7777778
      0.9500
      0.9281846

      0.3
      0.8888889
      0.9500
      0.9281846

      0.3
      1.0000000
      0.9500
      0.9281846

      0.4
      0.0000000
      0.9375
      0.9108954

      0.4
      0.1111111
      0.9375
      0.9108954

      0.4
      0.22222222
      0.9500
      0.9281846

      0.4
      0.44444444
      0.9500
      0.9281846

      0.4
      0.44444444
      0.9500
      0.9281846
```

```
0.4 0.5555556 0.9500 0.9281846
0.4 0.6666667 0.9500 0.9281846
0.4 0.7777778 0.9500 0.9281846
0.4 0.8888889 0.9500 0.9281846
0.4 1.0000000 0.9500 0.9281846
0.5 0.0000000 0.9375 0.9108954
0.5 0.1111111 0.9375 0.9108954
0.5 0.2222222 0.9500 0.9281846
0.5 0.3333333 0.9500 0.9281846
0.5 0.4444444 0.9500 0.9281846
0.5 0.5555556 0.9500 0.9281846
0.5 0.6666667 0.9500 0.9281846
0.5 0.7777778 0.9500 0.9281846
0.5 0.8888889 0.9500 0.9281846
0.5 1.0000000 0.9500 0.9281846
0.6 0.0000000 0.9375 0.9108954
0.6 0.1111111 0.9375 0.9108954
0.6 0.2222222 0.9375 0.9108954
0.6 0.3333333 0.9500 0.9281846
0.6 0.4444444 0.9500 0.9281846
0.6 0.5555556 0.9500 0.9281846
```

```
      0.6
      0.66666667
      0.9500
      0.9281846

      0.6
      0.7777778
      0.9500
      0.9281846

      0.6
      0.8888889
      0.9500
      0.9281846

      0.6
      1.0000000
      0.9500
      0.9281846

      0.7
      0.0000000
      0.9375
      0.9108954

      0.7
      0.22222222
      0.9375
      0.9108954

      0.7
      0.33333333
      0.9500
      0.9281846

      0.7
      0.44444444
      0.9500
      0.9281846
```

| 0.7 | 0.5555556 0.9500 | 0.9281846  |
|-----|------------------|------------|
| 0.7 | 0.6666667 0.9500 | 0.9281846  |
| 0.7 | 0.7777778 0.9500 | 0.9281846  |
| 0.7 | 0.8888889 0.9500 | 0.9281846  |
| 0.7 | 1.0000000 0.9500 | 0.9281846  |
| 0.8 | 0.0000000 0.9375 | 0.9108954  |
| 0.8 | 0.1111111 0.9375 | 0.9108954  |
| 0.8 | 0.2222222 0.9375 | 0.9108954  |
| 0.8 | 0.3333333 0.9375 | 0.9108954  |
| 0.8 | 0.4444444 0.9500 | 0.9281846  |
| 0.8 | 0.5555556 0.9500 | 0.9281846  |
| 0.8 | 0.6666667 0.9500 | 0.9281846  |
| 0.8 | 0.7777778 0.9500 | 0.9281846  |
| 0.8 | 0.8888889 0.9500 | 0.9281846  |
| 0.8 | 1.0000000 0.9500 | 0.9281846  |
| 0.9 | 0.0000000 0.9375 | 0.9108954  |
| 0.9 | 0.1111111 0.9375 | 0.9108954  |
| 0.9 | 0.2222222 0.9375 | 0.9108954  |
| 0.9 | 0.3333333 0.9375 | 0.9108954  |
| 0.9 | 0.4444444 0.9375 | 0.9108954  |
| 0.9 | 0.5555556 0.9500 | 0.9281846  |
| 0.9 | 0.6666667 0.9500 | 0.9281846  |
| 0.9 | 0.7777778 0.9500 | 0.9281846  |
| 0.9 | 0.8888889 0.9500 | 0.9281846  |
| 0.9 | 1.0000000 0.9500 | 0.9281846  |
| 1.0 | 0.0000000 0.9375 | 0.9108954  |
| 1.0 | 0.1111111 0.9375 | 0.9108954  |
| 1.0 | 0.2222222 0.9375 | 0.9108954  |
| 1.0 | 0.3333333 0.9375 | 0.9108954  |
| 1.0 | 0.4444444 0.9375 | 0.9108954  |
| 1.0 | 0.7515           | 0.710075 F |

1.0 0.5555556 0.9500 0.9281846

 $1.0\quad 0.6666667\ 0.9500\quad 0.9281846$ 

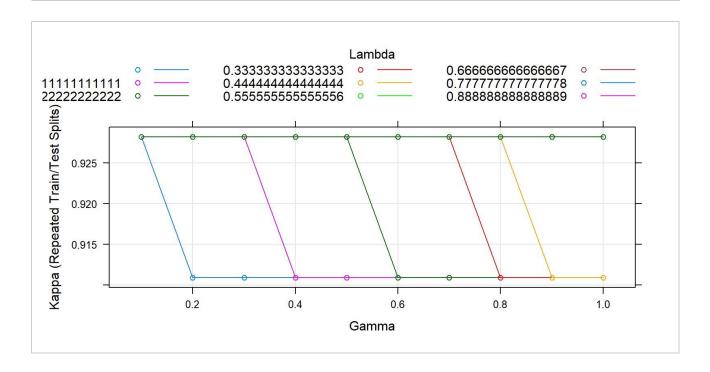
1.0 0.7777778 0.9500 0.9281846

1.0 0.8888889 0.9500 0.9281846

1.0 1.0000000 0.9500 0.9281846

Kappa was used to select the optimal model using the largest value.

The final values used for the model were gamma = 0.1 and lambda = 1.



#### Flexible Discriminant Analysis ####

Flexible Discriminant Analysis

96 samples

6 predictor

7 classes: 'A', 'B', 'C', 'D', 'E', 'F', 'G'

Pre-processing: centered (6), scaled (6)

Resampling: Repeated Train/Test Splits Estimated (4 reps, 75%)

Summary of sample sizes: 76, 76, 76, 76

Resampling results across tuning parameters:

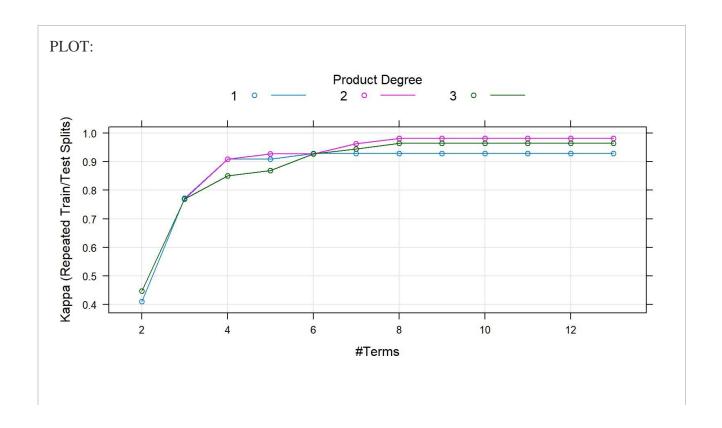
# degree nprune Accuracy Kappa

- 1 2 0.6250 0.4100043
- 1 3 0.8500 0.7722821
- 1 4 0.9375 0.9091981
- 1 5 0.9375 0.9091981
- 1 6 0.9500 0.9281846
- 1 7 0.9500 0.9281846
- 1 8 0.9500 0.9281846
- 1 9 0.9500 0.9281846
- 1 10 0.9500 0.9281846
- 1 11 0.9500 0.9281846
- 1 12 0.9500 0.9281846
- 1 13 0.9500 0.9281846
- 2 3 0.8500 0.7697925
- 2 4 0.9375 0.9084517
- 2 5 0.9500 0.9272487
- 2 6 0.9500 0.9272487
- 2 7 0.9750 0.9632229
- 2 8 0.9875 0.9819495
- 2 9 0.9875 0.9819495
- 2 10 0.9875 0.9819495
- 2 11 0.9875 0.9819495
- 2 12 0.9875 0.9819495
- 2 13 0.9875 0.9819495
- 3 2 0.6625 0.4466514
- 3 0.8500 0.7697925

```
0.9000 0.8499930
3
     4
3
     5
         0.9125
                 0.8687900
         0.9500 0.9272487
3
     6
3
     7
         0.9625
                 0.9449124
3
         0.9750
                 0.9638989
     8
                 0.9638989
3
         0.9750
     9
                 0.9638989
3
          0.9750
     10
3
     11
          0.9750
                 0.9638989
                 0.9638989
3
     12
          0.9750
                 0.9638989
3
     13
          0.9750
```

Kappa was used to select the optimal model using the largest value.

The final values used for the model were degree = 2 and nprune = 8.



#### SVM Radial ####

Support Vector Machines with Radial Basis Function Kernel

96 samples

6 predictor

7 classes: 'A', 'B', 'C', 'D', 'E', 'F', 'G'

Pre-processing: centered (6), scaled (6)

Resampling: Leave-One-Out Cross-Validation

Summary of sample sizes: 95, 95, 95, 95, 95, 95, ...

Resampling results across tuning parameters:

C Accuracy Kappa

0.015625 0.3854167 0.0000000

0.031250 0.3854167 0.0000000

0.062500 0.6250000 0.4159202

 $0.125000 \ 0.6250000 \ 0.4180839$ 

0.250000 0.7916667 0.7007015

0.500000 0.8437500 0.7801191

 $1.000000\ 0.8750000\ 0.8266105$ 

 $2.000000 \ 0.8958333 \ 0.8550287$ 

 $4.000000 \ 0.8958333 \ 0.8550287$ 

8.000000 0.8958333 0.8550287

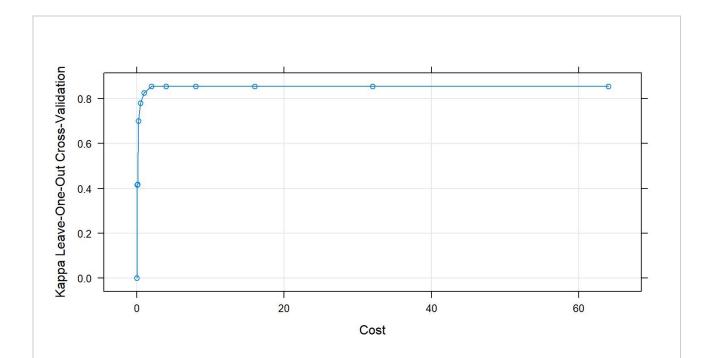
16.000000 0.8958333 0.8550287

32.000000 0.8958333 0.8550287

64.000000 0.8958333 0.8550287

Tuning parameter 'sigma' was held constant at a value of 0.04707239 Kappa was used to select the optimal model using the largest value.

The final values used for the model were sigma = 0.04707239 and C = 2.



#### SVM Polynomial ####

Support Vector Machines with Polynomial Kernel

96 samples

6 predictor

7 classes: 'A', 'B', 'C', 'D', 'E', 'F', 'G'

Pre-processing: centered (6), scaled (6)

Resampling: Leave-One-Out Cross-Validation

Summary of sample sizes: 95, 95, 95, 95, 95, 95, ...

Resampling results across tuning parameters:

degree scale C Accuracy Kappa 2

 $0.01 \quad 0.015625 \ \, 0.3854167 \ \, 0.00000000$ 

2 0.01 0.031250 0.3854167 0.0000000

2 0.01 0.062500 0.3854167 0.0000000

```
2
    0.01
         0.125000 0.3854167 0.0000000
2
          0.250000 0.3854167 0.0000000
    0.01
2
    0.01
         0.500000 0.7187500 0.5818006
2
          1.000000 0.7916667 0.7031081
    0.01
2
    0.01
          2.000000 0.9375000 0.9163884
2
    0.01
         4.000000 0.9375000 0.9167028
2
         8.000000 0.9270833 0.9027637
    0.01
2
    0.01 16.000000 0.9479167 0.9307259
2
    0.01 32.000000 0.9583333 0.9443720
2
    0.01 64.000000 0.9583333 0.9446526
2
    0.10 0.015625 0.4375000 0.1060528
2
    0.10 0.031250 0.4687500 0.1721339
2
    0.10 0.062500 0.7812500 0.6864209
2
    0.10 0.125000 0.9479167 0.9301717
2
    0.10 0.250000 0.9270833 0.9020265
2
    2
    0.10 \quad 1.000000 \quad 0.9270833 \quad 0.9027637
```

2 0.10 2.000000 0.9583333 0.9443720 2 0.10 4.000000 0.9583333 0.9443720 2 0.10 8.000000 0.9583333 0.9443720 2 0.10 16.000000 0.9687500 0.9582124 2 0.10 32.000000 0.9791667 0.9720971 2 0.10 64.000000 0.9791667 0.9720971 2 0.50 0.015625 0.8958333 0.8573339 2 0.50 0.031250 0.9375000 0.9157032 2 0.50 0.062500 0.9375000 0.9157032 2 0.50 0.125000 0.9479167 0.9296394 2 2 0.50 0.500000 0.9687500 0.9582124 2 0.50 1.000000 0.9687500 0.9582124

```
2
    0.50 2.000000 0.9791667 0.9720971
2
          4.000000 0.9791667 0.9720971
    0.50
2
    0.50 8.000000 0.9791667 0.9720971
2
    0.50 16.000000 0.9791667 0.9720971
2
    0.50 32.000000 0.9791667 0.9720971
2
    0.50 64.000000 0.9791667 0.9720971
3
          0.015625 0.3854167 0.0000000
    0.01
3
    0.01 0.031250 0.3854167 0.0000000
3
    0.01 0.062500 0.3854167 0.0000000
3
    0.01 0.125000 0.3854167 0.0000000
3
    0.01
          0.250000 0.4583333 0.1471040
3
    0.01
          0.500000 0.7500000 0.6369939
3
    0.01
          1.000000 0.9270833 0.9012636
3
    0.01
          2.000000 0.9375000 0.9163884
3
          4.000000 0.9270833 0.9027637
    0.01
3
    0.01 8.000000 0.9270833 0.9027637
    0.01 16.000000 0.9583333 0.9443720
3
```

```
3
    0.01 32.000000 0.9583333 0.9446526
3
    0.01 64.000000 0.9583333 0.9446526
3
    0.10 0.015625 0.4583333 0.1520299
3
    0.10 0.031250 0.8229167 0.7488458
3
    0.10 0.062500 0.8854167 0.8424586
3
    0.10 0.125000 0.9375000 0.9157032
3
    0.10 0.250000 0.9270833 0.9020265
3
    0.10
          0.500000 0.9375000 0.9157032
3
          1.000000 0.9687500 0.9582124
    0.10
         2.000000 0.9583333 0.9443720
3
    0.10
3
    0.10 4.000000 0.9687500 0.9582124
3
    0.10 8.000000 0.9687500 0.9582124
3
    0.10 16.000000 0.9791667 0.9720971
```

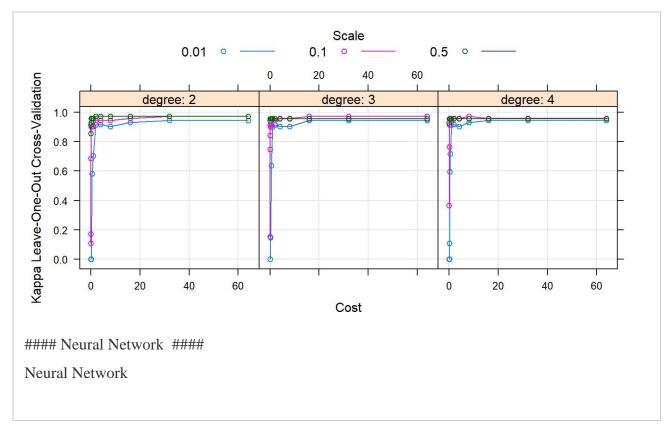
```
3
    0.10 32.000000 0.9791667 0.9720971
    0.10 64.000000 0.9791667 0.9720971
3
3
    3
    3
    0.50 0.062500 0.9583333 0.9439988
3
    0.50 0.125000 0.9687500 0.9579316
3
    0.50 0.250000 0.9687500 0.9579316
3
    3
    0.50
         1.000000 0.9687500 0.9579316
3
    0.50
         2.000000 0.9687500 0.9579316
3
    0.50
         4.000000 0.9687500 0.9579316
3
    0.50
         8.000000 0.9687500 0.9579316
3
    0.50 16.000000 0.9687500 0.9579316
3
    0.50 32.000000 0.9687500 0.9579316
    0.50 64.000000 0.9687500 0.9579316
3
    0.01 0.015625 0.3854167 0.0000000
4
    0.01 \quad 0.031250 \quad 0.3854167 \quad 0.0000000
4
```

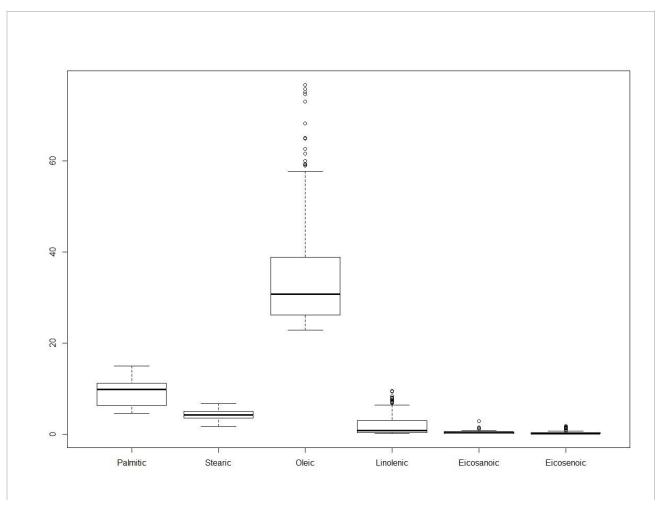
```
4
    0.01 0.062500 0.3854167 0.0000000
    0.01 0.125000 0.4375000 0.1060528
4
4
    0.01 0.250000 0.7291667 0.5962472
4
    0.01
         0.500000 0.8020833 0.7190821
4
    0.01
          1.000000 0.9375000 0.9163884
          2.000000 0.9375000 0.9167028
4
    0.01
         4.000000 0.9270833 0.9027637
4
    0.01
4
    0.01
         8.000000 0.9479167 0.9307259
    0.01 16.000000 0.9583333 0.9443720
4
    0.01 32.000000 0.9583333 0.9446526
4
    0.01 64.000000 0.9583333 0.9446526
4
    0.10  0.015625  0.5729167  0.3658772
4
4
    0.10
          0.031250 0.8333333 0.7663168
```

```
0.10
          0.062500 0.9375000 0.9157032
4
4
     0.10
          0.125000 0.9375000 0.9157032
4
     0.10 \quad 0.250000 \quad 0.9375000 \quad 0.9157032
     4
4
     0.10
          1.000000 0.9583333 0.9443720
4
     0.10
          2.000000 0.9687500 0.9582124
4
     0.10
          4.000000 0.9687500 0.9582124
     0.10 8.000000 0.9791667 0.9720971
4
4
     0.10\ 16.000000\ 0.9687500\ 0.9580786
4
     0.10 32.000000 0.9687500 0.9580786
4
     0.10 64.000000 0.9687500 0.9580786
     4
4
     0.50
          0.031250 0.9687500 0.9579316
4
     0.50
          0.062500 0.9687500 0.9579316
4
     0.50
          0.125000 0.9687500 0.9579316
4
     0.50
          0.250000 0.9687500 0.9579316
4
     0.50
          0.500000 0.9687500 0.9579316
     0.50
          1.000000 0.9687500 0.9579316
4
4
     0.50
          2.000000 0.9687500 0.9579316
     0.50
          4.000000 0.9687500 0.9579316
4
4
     0.50
          8.000000 0.9687500 0.9579316
     0.50 16.000000 0.9687500 0.9579316
4
4
     0.50 32.000000 0.9687500 0.9579316
    0.50 64.000000 0.9687500 0.9579316
4
```

Kappa was used to select the optimal model using the largest value.

The final values used for the model were degree = 2, scale = 0.5 and C = 2.





Since the boxplot shows outliers we will preprocess using spatial sign transformation to get rid of the outliers, as NNet is sensitive to outliers.

96 samples

6 predictor

7 classes: 'A', 'B', 'C', 'D', 'E', 'F', 'G'

Pre-processing: centered (6), scaled (6), spatial sign transformation (6)

Resampling: Repeated Train/Test Splits Estimated (4 reps, 75%)

Summary of sample sizes: 76, 76, 76, 76

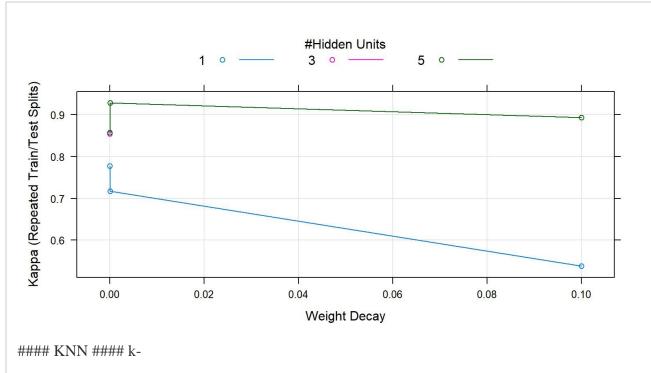
Resampling results across tuning parameters:

# size decay Accuracy Kappa 1 0e+00 0.850 0.7774847

- 1 1e-04 0.800 0.7169346
- 1 1e-01 0.700 0.5380597
- 3 0e+00 0.900 0.8545466
- 3 1e-04 0.950 0.9288247
- 3 1e-01 0.925 0.8934170
- 5 0e+00 0.900 0.8575515
- 5 1e-04 0.950 0.9283070
- 5 1e-01 0.925 0.8934170

Kappa was used to select the optimal model using the largest value.

The final values used for the model were size = 3 and decay = 1e-04.



Nearest Neighbors

96 samples

6 predictor

 $7 \; classes: \; 'A', \; 'B', \; 'C', \; 'D', \; 'E', \; 'F', \; 'G'$ 

Pre-processing: centered (6), scaled (6)

Resampling: Repeated Train/Test Splits Estimated (4 reps, 75%)

Summary of sample sizes: 76, 76, 76, 76

Resampling results across tuning parameters:

k Accuracy Kappa 1 0.9750 0.96428571

3 0.9500 0.92818463

5 0.9500 0.92818463

7 0.9500 0.92818463

9 0.9500 0.92818463

11 0.9375 0.91013409

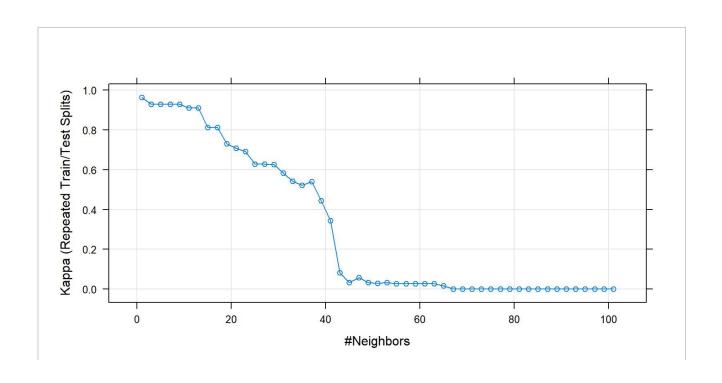
| 13 0.9375 | 0.91013409 |
|-----------|------------|
| 15 0.8750 | 0.81304196 |
| 17 0.8750 | 0.81304196 |
| 19 0.8250 | 0.73090295 |
| 21 0.8125 | 0.70919961 |
| 23 0.8000 | 0.69171428 |
| 25 0.7625 | 0.62765726 |
| 27 0.7625 | 0.62789069 |
| 29 0.7625 | 0.62609489 |
| 31 0.7375 | 0.58341179 |
| 33 0.7125 | 0.54203949 |
| 35 0.7000 | 0.52235445 |
| 37 0.7125 | 0.54038692 |
| 39 0.6625 | 0.44388795 |
| 41 0.6125 | 0.34388262 |
| 43 0.4750 | 0.08260464 |
| 45 0.4500 | 0.03292499 |
|           |            |

| 47 0.4625 | 0.05758242 |
|-----------|------------|
| 49 0.4500 | 0.03292499 |
| 51 0.4500 | 0.02973683 |
| 53 0.4500 | 0.03292499 |
| 55 0.4500 | 0.02654867 |
| 57 0.4500 | 0.02654867 |
| 59 0.4500 | 0.02654867 |
| 61 0.4500 | 0.02654867 |
| 63 0.4500 | 0.02654867 |
| 65 0.4500 | 0.01672685 |
| 67 0.4500 | 0.00000000 |
| 69 0.4500 | 0.00000000 |
| 71 0.4500 | 0.00000000 |

| 73  | 0.4500 | 0.00000000 |
|-----|--------|------------|
| 75  | 0.4500 | 0.00000000 |
| 77  | 0.4500 | 0.00000000 |
| 79  | 0.4500 | 0.00000000 |
| 81  | 0.4500 | 0.00000000 |
| 83  | 0.4500 | 0.00000000 |
| 85  | 0.4500 | 0.00000000 |
| 87  | 0.4500 | 0.00000000 |
| 89  | 0.4500 | 0.00000000 |
| 91  | 0.4500 | 0.00000000 |
| 93  | 0.4500 | 0.00000000 |
| 95  | 0.4500 | 0.00000000 |
| 97  | 0.4500 | 0.00000000 |
| 99  | 0.4500 | 0.00000000 |
| 101 | 0.4500 | 0.00000000 |
|     |        |            |

Kappa was used to select the optimal model using the largest value.

The final value used for the model was k = 1.



#### Naive Bayes ####

Naive Bayes

96 samples

6 predictor

7 classes: 'A', 'B', 'C', 'D', 'E', 'F', 'G'

No pre-processing

Resampling: Repeated Train/Test Splits Estimated (4 reps, 75%)

Summary of sample sizes: 76, 76, 76, 76

Resampling results across tuning parameters:

usekernel Accuracy Kappa

FALSE NaN NaN

TRUE 0.975 0.9642857

Tuning parameter 'fL' was held constant at a value of 0

Tuning

parameter 'adjust' was held constant at a value of 1

Kappa was used to select the optimal model using the largest value. The final values used for the model were fL = 0, usekernel = TRUE

and adjust = 1.

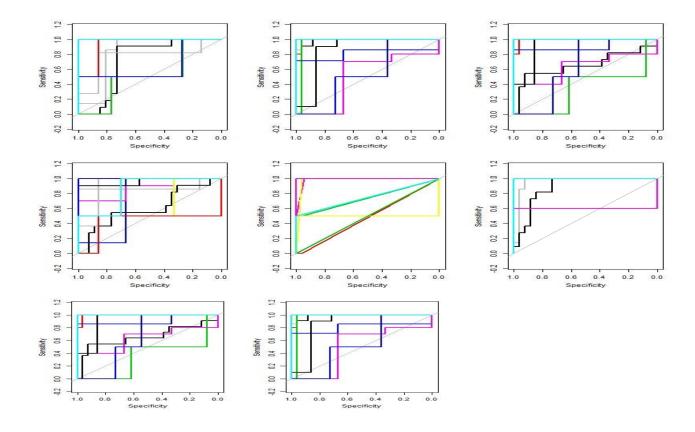
| Name                  | Tuning<br>Parameters          | Pre- Processing                               | Kappa     | Accuracy |
|-----------------------|-------------------------------|---|-----------|----------|
| Neural<br>Networ<br>k | size = 3 and decay = 1e-04.   | Centered Scaled & Spatial sign transformation | 0.8232    | 0.8778   |
| MDA                   | subclasses = 7                | None  | 0.9819495 | 0.9875   |
| FDA                   | degree = 2 and<br>nprune = 8. | Centered Scaled                               | 0.9819495 | 0.9875   |

| RDA            | gamma = 0.1<br>and lambda = 1        | Centered and Scaled | 0.9288247 | 0.950 |
|----------------|--------------------------------------|---------------------|-----------|-------|
| SVM<br>Radial: | sigma = 0.03<br>034568 and C<br>= 2. | Centered, Scaled    | 0.6545    | 0.762 |

| k-Nearest<br>Neighbors | k = 1                                     | Centered<br>Scaled | 0.3366 | 0.6039 |
|------------------------|---|--------------------|--------|--------|
| Naive<br>Bayes         | fL = 0,<br>usekernel = TRUE<br>adjust = 1 | None               | 0.9639 | 0.975  |
| SVM<br>Polynomial      | degree = 2,<br>scale = $0.5$ and $C = 2$  | Centered<br>Scaled | 0.8084 | 0.8615 |

# The Model Plots: Since the Models were run for 6 classes we used multi.class.ROC to get the values for ROC PLOT using the following code: rda.predictions\_all = predict(my\_model, train,type='prob') rda.rocCurve.all = pROC::multiclass.roc( response=oilType, predictor=rda.predictions\_all[,1]) rda.auc.all = rda.rocCurve.all\$auc[1]

The plots derived are as follows (in order of above table from left to right)



FDA, MDA, RDA and naïve bayes are the top best models choosen through the model predictions over different groups using LGOCV.

These values are obtained by using the code:

# confusionMatrix(data=my\_model\$pred\$pred\$pred, reference=my\_model\$pred\$obs)

After shortlisting the model we will use the predict function to find the confusion matrices for all the models.

The predict function is used in the following way:

# pred<-predict(my\_model,train) confusionMatrix(pred,oilType)</pre>

#### MDA:

Confusion Matrix and Statistics

Reference

## Prediction A B C D E F G

A 37 0 0 0 0 0 0

B 026 0 0 0 0 0

C 0 0 3 0 0 0 0

D 0 0 0 7 0 0 0

E 0 0 0 0 11 0 0

F 0 0 0 0 0 10 0

G 0 0 0 0 0 0 2

## **Overall Statistics**

Accuracy: 1

95% CI: (0.9623, 1)

No Information Rate: 0.3854

P-Value [Acc > NIR] : < 2.2e-16

# Kappa: 1

## RDA:

# Confusion Matrix and Statistics

Prediction A B C D E F G

A 34 0 0 0 0 0 0

B 2 26 0 0 0 0 0

C 0 0 3 0 0 0 0

D 0 0 0 7 0 0 0

E 1 0 0 0 11 0 0

F 0 0 0 0 0 10 0

G 0 0 0 0 0 0 2

## **Overall Statistics**

Accuracy: 0.9688

95% CI: (0.9114, 0.9935)

No Information Rate: 0.3854

P-Value [Acc > NIR] : < 2.2e-16

Kappa: 0.9585

FDA:

Confusion Matrix and Statistics

Reference

Prediction A B C D E F G

A 35 0 0 0 0 0 0

B 1 26 0 0 0 0 0

C 0 0 3 0 0 0 0

D 0 0 0 7 0 0 0

E 1 0 0 0 11 0 0

F 0 0 0 0 0 10 0

G 0 0 0 0 0 0 2

**Overall Statistics** 

Accuracy: 0.9792

95% CI: (0.9268, 0.9975)

No Information Rate: 0.3854

P-Value [Acc > NIR] : < 2.2e-16

Kappa: 0.9723

# Naïve Bayes:

Confusion Matrix and Statistics

Reference

Prediction A B C D E F G

A 37 0 0 0 0 0 0

B 0 26 0 0 0 0 0

C 0 0 3 0 0 0 0

D 0 0 0 7 0 0 0

E 0 0 0 0 11 0 0

F 0 0 0 0 0 10 0

G 0 0 0 0 0 0 2

**Overall Statistics** 

Accuracy: 1

95% CI: (0.9623, 1)

No Information Rate: 0.3854

P-Value [Acc > NIR] : < 2.2e-16

Kappa: 1

The above confusion matrices show that both MDA and Naïve Bayes have 1 Kappa,100 percent accuracy.

Which model has the best predictive ability?

The MDA model as well as the Naïve Bayes model has the best predictive ability among the linear models. With Kappa=1 and Accuracy=1.

How does this optimal model's performance compare to the best linear model's performance? The optimal model of the nonlinear set performs similar to the best model of linear modelling set as achieve achieve 100 percent accuracy and build ideal models. In the linear set of models the nearest shrunken centroid model as well as the Logistic regression model performed to full Accuracy in the nonlinear set Naïve Bayes and MDA models performed equally well.

Would you infer that the data have nonlinear separation boundaries based on this comparison?

Since linear models had similar performance on this data as nonlinear models we cannot make a conclusive statement for data to have nonlinear separation boundaries. We investigate further;

LDA 0.9620253

GLMNET 0.9367089

NSC 1

PLSDA 0.9493671

Logistic regression 1

LDA 0.9500527

GLMNET 0.9143353

NSC 1

PLSDA 0.9327516

Logistic regression 1

Performances of linear models.

FDA:Accuracy : 0.9688 Kappa : 0.9585 RDA:Accuracy : 0.9792 Kappa : 0.9723

Naïve Bayes: 1 Kappa=1 MDA:1 Kappa=1

Performance of non-linear models.

By comparing the performances of the model that are the top 4 performing we see that the nonlinear models in general show better accuracy and Kappa values than the linear models. Hence we can conclude that the boundaries are nonlinear.

(b) Which oil type does the optimal model most accurately predict? Least accurately, predict?

The optimal model predicts all oil types properly. Since it is an ideal model. In addition, none of the oil types wrongly.

```
#rcode: ```
{r data}
data(oil) data<-
fattyAcids
...
##my_model: ```{r
my_model_}
           trainControl(method="LGOCV",classProbs=TRUE,savePredictions=TRUE,
                                                                                         number=4)
ctrl
corr_bio <- cor(data) corrplot(corr_bio, tl.cex = 0.5)
remove <- findCorrelation(corr_bio,cutoff = 0.90) data<-data[,-remove]
train = data y_train
=oilType
```{r MDA}
cat('#### Mixture Discriminant Analysis ####') set.seed(1)
my_model <- train(train, y=y_train, method="mda", tuneGrid=expand.grid(subclasses=1:10),
metric="Kappa", trControl=ctrl)
my_model plot(my_model)
pred<-predict(my_model,train)</pre>
confusionMatrix(pred,oilType)
```{r RDA}
cat('#### Regularized Discriminant Analysis ####') set.seed(1)
grid \leftarrow expand.grid(.gamma = seq(0.1, 1, length = 10), .lambda = seq(0, 1, length = 10))
my_model <- train(train, y=y_train, method="rda",
```

```
tuneGrid=grid, metric="Kappa", trControl=ctrl, preProc=c('center', 'scale'))
my_model
confusionMatrix(data=my_model$pred$pred$pred, reference=my_model$pred$obs)
plot(my_model) plot(my_model) pred<-predict(my_model,train)</pre>
confusionMatrix(pred,oilType)
```{r FDA}
cat('#### Flexible Discriminant Analysis ####')
set.seed(1)
marsGrid <- expand.grid(.degree = 1:3, .nprune = 2:13)
my_model <- train(train, y=y_train, method="fda",
          tuneGrid=marsGrid, metric="Kappa", trControl=ctrl,
preProc=c('center', 'scale'))
my_model
plot(my_model)
confusionMatrix(data=my_model$pred$pred, reference=my_model$pred$obs)
pred<-predict(my_model,train)</pre>
confusionMatrix(pred,oilType)
```{r SVM_Radial}
```

```
cat('#### SVM Radial ####')
set.seed(1)
sigmaEst = kernlab::sigest(as.matrix(train))
svagrid = expand.grid(sigma=sigmaEst[1], C=2^seq(-6, +6))
my_model <- train(train, y=y_train, method="svmRadial",
metric="Kappa",trControl=trainControl(method = "LOOCV"),
preProc=c('center', 'scale'), fit=FALSE, tuneGrid = svagrid)
my_model
plot(my_model)
confusionMatrix(data=my_model$pred$pred$pred, reference=my_model$pred$obs)
pred<-predict(my_model,train)</pre>
confusionMatrix(pred,oilType)
...
```{r SVM_Polynomial}
cat('#### SVM Polynomial ####')
set.seed(1)
poly_grid = expand.grid(degree = c(2, 3, 4), C = 2^seq(-6, 6, length = 13),
scale = c(.5, .1, 0.01)
my_model <- train(train, y=y_train,
method="svmPoly",metric="Kappa",trControl=trainControl(method =
"LOOCV"),
          preProc=c('center', 'scale'), fit=FALSE, tuneGrid = poly_grid)
my_model
```

```
plot(my_model)
confusionMatrix(data=my_model$pred$pred, reference=my_model$pred$obs)
pred<-predict(my_model,train)</pre>
confusionMatrix(pred,oilType)
```{r NNET}
cat('#### Neural Network ####')
set.seed(1)
nnetGrid = expand.grid(size=1:10, decay=c(0, 0.1, 1, 2))
my_model <- train(train, y=y_train, method="nnet",
preProc=c("center","scale","spatialSign"),
           tunegrid=nnetGrid, metric="Kappa",trace=FALSE, maxit=3000,
trControl=ctrl)
my_model
plot(my_model)
confusionMatrix(data=my_model$pred$pred$pred, reference=my_model$pred$obs)
pred<-predict(my_model,train)</pre>
confusionMatrix(pred,oilType)
...
```{r KNN}
```

```
cat('#### KNN ####')
set.seed(1)
knngrid = data.frame(.k = seq(1, 101, by = 2))
my_model <- train(train, y=y_train, method="knn", tuneGrid = knngrid,
preProc=c("center","scale"), metric="Kappa", trControl=ctrl)
my_model
plot(my_model)
confusionMatrix(data=my_model$pred$pred, reference=my_model$pred$obs)
pred<-predict(my_model,train)</pre>
confusionMatrix(pred,oilType)
```{r NB}
cat('#### Naive Bayes ####')
set.seed(1)
my_model <- train(train, y=y_train, method="nb", metric="Kappa",
trControl=ctrl)
my_model
plot(my_model)
confusionMatrix(data=my_model$pred$pred$pred, reference=my_model$pred$obs)
pred<-predict(my_model,train)</pre>
confusionMatrix(pred,oilType)
```