

Assignment 9.momentum optimiser.

X	Y
0.2	3.4
0.4	3.8

step 1:  $\{x, y\}, m=1, c=-1, \eta=0.1$  epochs = 2

$$\gamma = 0.9; v_m = v_c = 0$$

Step 2:  $i_{t_2} = 1$ 

Step 3: example = 1

$$\text{step 4: } \frac{\partial E}{\partial m} = -(y_i - m x_i - c) x_i$$

$$= -(3.4 - 1(0.2) + 1)(0.2)$$

$$\frac{\partial E}{\partial m} = -0.84.$$

$$g_c = \frac{\partial E}{\partial c} = -[3.4 - 1(0.2) + 1].$$

$$\frac{\partial E}{\partial c} = -4.2.$$

$$\text{Step 5: } v_m = \gamma v_m - \eta g_m.$$

$$= (0.9)(0) - (0.1)(-0.84).$$

$$v_m = 0.084.$$

$$v_c = \gamma v_c - \eta g_c.$$

$$= (0.9)(0) - (0.1)(-0.2)$$

$$V_C = 0.02.$$

$$\text{Step 6: } m = m + V_m = 1 + 0.084 = 1.084.$$

$$c = c + V_C = -1 + 0.02 = -0.98.$$

$$\text{Step 7: sample} = 1 + 1 = 2$$

$$\text{Step 8: if (sample > m)}$$

$2 > 2$

$$\text{Step 9: } g_m = \frac{\partial E}{\partial m} = - \left[ 3.8 - (1.084)(0.02) + 0.58 \right] / (0.02).$$

$$g_m = -1.57856.$$

$$g_C = \frac{\partial E}{\partial C} = - \left[ 3.8 - (1.084)(0.02) + 0.58 \right].$$

$$g_C = \frac{\partial E}{\partial C} = -3.9464.$$

$$\text{Step 5: } V_m = \gamma V_m - \gamma g_m,$$

$$= (0.9)(0.084) - (0.1)(-1.57856)$$

$$V_m = 0.233456.$$

$$V_C = \gamma V_C - \gamma g_C$$

$$= (0.9)(0.02) - (0.1)(-3.9464),$$

$$V_C = 0.77264.$$

$$\text{Step 6: } m = m + v_m = 1.084 + 0.233456.$$

$$m = 1.3194.$$

$$c = c + v_c = -0.58 + 0.19264$$

$$c = 0.19264$$

Step 7:- compare  $|z| = 2 > 1$ .

Step 8:- if ( $|z| > 2$ )

Step 9:-  $i^{th} = i^{th} + 1 = 1 + 1 = 2$ .

Step 10:- if ( $|z| > 2$ ):

Step 3:- compare 1.

$$\text{Step 6: } g_m = \frac{\partial E}{\partial m} = -[3.4 - (1.3194)(0.2) - 0.19264] \\ (0.2)$$

$$g_m = -0.5887$$

$$g_c = \frac{\partial E}{\partial c} = -[3.4 - (1.3194)(0.2) - 0.19264].$$

$$g_c = -2.9438.$$

$$\text{Step 5: } V_m = 8V_m - \eta g_m. \\ = (0.9)(0.23345) - (0.1)(-0.5887).$$

$$V_m = 0.26892.$$

$$V_c = 8V_c - \eta g_c.$$

$$= (0.9)(0.19264) - (0.1)(-2.9438).$$

$$V_c = 0.9897.$$

$$\text{Step 6: } m = m + v_m = 1.3154 + 0.26897$$

$$m = 1.5868$$

$$c = c + v_c = 0.19264 + 0.9897$$

$$c = 1.18284$$

$$\text{Step 7: } \text{sample} = 1 + 1 \leq 2$$

$$\text{Step 8: if } (\text{sample} > n)$$

$$2 > 2$$

$$\text{Step 9: } g_m = \frac{\partial E}{\partial m} = - \left( 3.3 - [1.5864(0.01) + 0.1828] \right)$$

$$g_m = -1.4391$$

$$g_c = \frac{\partial E}{\partial c} = -4.3479$$

$$\begin{aligned} \text{Step 5: } v_m &= \gamma v_m - n g_m \\ &= (0.9)(0.26897) - (0.1)(-1.4391) \end{aligned}$$

$$v_m = 0.41604$$

$$v_c = \gamma v_c - n g_c = 1.3255$$

$$\text{Step 6: } m = m + v_m$$

$$= 1.5868 + 0.41604$$

$$= 2.0023$$

$$c = c + v_c = 1.18284 + 1.3255$$

$$c = 2.507$$

step 7: example = 5+1+3

step 8: i+=1 (852)

step 9: i+=2+1+3

step 10: i+=1 (872)

step 11: m=0.11861

$$C = 1.381 \dots$$

]

15(2) 3000

of fixed point

fixed point

## Assignment 13.

### Adagrad Optimizer

Sample(i)	$x_i^a.$	$y_i^a.$
1	0.2	8.4
2	0.4	2.3
3	0.6	4.2
4	0.8	4.6

Step 1:  $[x, y]$ , epochs = 2,  $m=1$ ,  $c=1$ ,  $g_m = h_c = 0$

$$\gamma = 0.1, \epsilon = 10^{-8}$$

Step 2:  $\hat{H}Y = 1$

Step 3: sample = 1

$$\begin{aligned} \text{Step 4: } g_m &= -(y_i - mx_i - c)x_i \\ &= -(8.4 - (1)(0.2) + 1) 0.2. \end{aligned}$$

$$g_m = -0.84.$$

$$\begin{aligned} g_c &= 0 - [y - mx_i - c]. \\ &= -(8.4 - (1)(0.2) + 1). \end{aligned}$$

$$g_c = -8.2$$

Step 5:

$$G_m = G_m + (g_m)^2; \quad (n_c = n_c + \epsilon g_c)^2.$$

$$G_m = 0 + (-0.9056)^2; \quad n_c = 0 + (-0.2)^2.$$

$$G_m = 0.9056$$

$$n_c = 0.04.$$

$$\text{Step 6: } \Delta m = \frac{-\gamma}{\sqrt{G_m + \epsilon}} \quad g_m = \frac{-0.1}{\sqrt{0.9056 + 10^{-8}}} \times (0.8)$$

$$\Delta m = 0.099.$$

$$\Delta g = \frac{-\gamma}{\sqrt{n_c + \epsilon}} \quad g_c = \frac{-0.1}{\sqrt{0.04 + 10^{-8}}} \times (-0.2)$$

$$\Delta c = 0.099.$$

$$\text{Step 7: } m = m + \Delta m = 1 + 0.099.$$

$$m = 1.099.$$

$$c = c + \Delta c = 1 + 0.099.$$

$$c = -0.901.$$

$$\text{Step 8: } \text{sample} = \text{sample} + 1 = 1 + 1 = 2$$

Step 9: if [sample > n].

$$2 > 2.$$

false  $\rightarrow$  goes to step ①

$$\text{Step 10: } g_m = -[3.8 - (1.099)(0.4) + 0.901] (0.8)$$

$$g_m = -1.040456.$$

$$g_c = - [3.8 - (1.099)(0.4) + 0.901].$$

$$g_c = -4.2614.$$

$$\text{Step 5: } G_m = g_m + (g_m)^2 \quad ; \quad g_c = g_c + (g_c)^2.$$

$$g_m = 3.6111 + (-1.40086)^2 \quad g_c = 1.764 + (-4.2614)^2.$$

$$g_m = 3.6111.$$

$$g_c = 35.499.$$

Step 6:

$$\Delta m = \frac{-\eta}{\sqrt{g_m + \epsilon}} \times g_m = \frac{-0.1}{\sqrt{3.6111 + 10^{-8}}} \times (-1.40086).$$

$$\Delta m = 0.0896.$$

$$\Delta c = \frac{-\eta}{\sqrt{g_c + \epsilon}} \times g_c = \frac{-0.1}{\sqrt{35.499 \times 10^{-8}}} \times (-4.2614).$$

$$8 \quad \Delta c = 0.07122.$$

$$\text{Step 7: } m = m + \Delta m = 1.099 + 0.0896.$$

$$m = 1.1886.$$

$$c = c + \Delta c = -0.901 + 0.07122.$$

$$c = -0.82948.$$

$$\text{Step 8: sample} = 2+1=3.$$

$$\text{Step 9: if (sample > n)} \\ n > 2.$$

$$\text{Step 10: } ^i\text{itr} = ^i\text{itr} + 1 = 1 + 1 = 2.$$

$$\text{Step 11: if (itr > epoch)} \\ 2 > 2.$$

Step 3: sample = 1

$$\text{Step 4: } g_m = -[3.4 - (1.1886)(0.2) + 0.82978](0.2)$$

$$g_m = -0.498412.$$

$$g_c = -[3.4 - (1.1886)(0.2) + 0.82978]$$

$$g_c = -3.99206.$$

$$\text{Step 5: } G_m = g_m + (g_m)^2, \quad C_C = C_C + (g_c)^2$$

$$= 3.611 + (-0.498412)^2 \quad C_C = 35.499 + (-3.99206)^2$$

$$G_m = 41.2084$$

$$C_C = 51.4355$$

$$\text{Step 6: } \Delta m = \frac{-n}{\sqrt{G_m + \epsilon}} \quad g_m = \frac{-0.1}{\sqrt{41.2084 + 10^{-8}}} (0.4984)$$

$$\Delta m = 0.0387.$$

$$\Delta c = \frac{-n}{\sqrt{C_C + \epsilon}} \quad g_c = \frac{-0.1}{\sqrt{51.4355 + 10^{-8}}} (-3.99206)$$

$$\Delta c = 0.0555.$$

Step 7:

$$m = m + \Delta m = 1.1826 + 0.0387,$$

$$m = 1.2273.$$

$$c = c + \Delta c = -0.82978 + 0.0555$$

$$c = -0.77428.$$

Step 8: sample = sample + 1 = 1 + 1 = 2.

$$2 > 2.$$

go to step 4

$$\text{Step 4: } g_m = [3.8 - (1.122 \times 10^{-4} u) + 0.98 u^{2.8}] \times 10^{-4}$$

$$g_m = -4.083 \times 10^{-4}$$

$$g_c = [3.8 - (1.122 \times 10^{-4} u) + 0.98 u^{2.8}]$$

$$g_c = -4.083.$$

$$\text{Step 5: } G_m = 1.2 \times 10^{-4} + (-1.6)^2 = 6.91$$

$$a_c = 51.9855 \cdot (-4.083)^2 = 68.3817$$

$$\text{Step 6: } \Delta m = \frac{-0.1}{\sqrt{6.91 \times 10^{-8}}} \times (-4.083)$$

$$\Delta m = 0.0621.$$

$$\Delta c = \frac{-0.1}{\sqrt{68.3817 \times 10^{-8}}} \times (-4.083)$$

$$\Delta c = 0.0496$$

$$\text{Step 7: } m = m + \Delta m = 1.2894.$$

$$c = c + \Delta c = -0.22818.$$

$$\text{Step 8: sample} = \text{sample} + 1$$

$$= 2 + 1 = 3.$$

Step 9: if (sample > ns)

$$3 > 2$$

$$\text{Step 10: } ^0t_2 = ^0t_2 + 1$$

$$= 2 + 1 = 3.$$

Step 11: if ( $i_{tr} > \text{epoch}$ )

$3 > 2$

Step 12:  $m = \frac{1}{2} \cdot 2896 \cdot 0.49 = 1.2896$

$$C = -0.42518.$$

### Assignment 15

#### RMS prop optimizer

sample (i)	$\alpha_i$	$y_i^a$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Step 1:  $(\alpha, g) , \eta = 0.1, \text{epoch} = 2, m = 1, C = -1$ .

$$\gamma = 0.9, \epsilon_m = 60 = 0, \epsilon = 10^{-8}.$$

Step 2:  $i_{tr} = 1$

Step 3: sample 1.

$$\text{Step 4: } g_m = [3 \cdot 4 \cdot (-1) (0.2) + 1] (0.2) = 0.84$$

$$g_C = -[3 \cdot 4 \cdot (-1) (0.2) + 1] \cdot 0.2 = -0.2.$$

$$\text{Step 5: } E_m = (0.9)(0) + (1-0.9)(-0.8u)^2 \\ = 0.041$$

$$E_c = (0.9)(0) + (1-0.9)(-0.2)^2 \\ = 0.046$$

$$\text{Step 6: } \Delta m = \frac{-0.1}{\sqrt{0.041 + 10}} \times (-0.8u) = 0.31$$

$$\Delta C = \frac{-0.1}{\sqrt{0.046 + 10}} \times (-0.2) = 0.31$$

$$\text{Step 7: } m = m + \Delta m = 1 + 0.31 = 1.31$$

$$c = c + \Delta C = -1 + 0.31 = -0.69$$

$$\text{Step 8: sample} = 1+1=2$$

Step 9: if (sample > n),

$$2 > 2$$

$$\text{Step 10: } g_m = \frac{1}{2} [8.8 - (1.31)(0.4) + 0.69] (0.4)$$

$$g_m = -1.5$$

$$g_C = -[8.8 - (1.31)(0.4) + 0.69]$$

$$g_C = -3.9$$

$$\text{Step 11: } E_m = (0.9)(0.041) + (0.1)(-1.5)^2$$

$$= 0.28$$

$$E_C = (0.9)(1.46) + (0.1)(-3.9)^2 = 3.1$$

$$\text{Step 6: } \Delta m = \frac{-0.1}{\sqrt{0.28 + 10^{-8}}} \times 10^5 = 0.28 -$$

$$\Delta c = \frac{-0.1}{\sqrt{8.1 \times 10^{-8}}} \times 3.09 = 0.22 -$$

$$\text{Step 7: } m = m + \Delta m = 1.31 + 0.28 = 1.59$$

$$c = c + \Delta c = -0.69 + 0.22 = -0.47 -$$

Step 8: sample = 2+1=3.

Step 9: if (sample > n)

3 > 2

Step 10: ite = ite + 1 = 1 + 1 = 2

Step 11: if (ite > epoch)

2 > 2

Step 12: sample = 1

$$\text{Step 13: } g_m = [8.4 - (1.59)(0.2) + 0.47](0.2)$$

$$g_m = -0.4$$

$$g_c = -[8.4 - (1.59)(0.2) + 0.47]$$

$$g_c = 3.5$$

$$\text{Step 14: } f_m = (0.9)(0.2) + (0.1)(-0.4)^2 \\ = 0.3 -$$

$$E_C = (0.9)(5.1) + (0.1)(-3.8)^2 = 6.6$$

$$\text{Step 6: } \Delta m = \frac{-0.1}{\sqrt{0.3+10^{-8}}} \times 0.9 = 0.12.$$

$$\Delta C = \frac{-0.1}{\sqrt{6.6+10^{-8}}} \times 3.8 = 0.14.$$

$$\text{Step 7: } m = m + \Delta m = 1.59 + 0.12 = 1.71$$

$$C = C + \Delta C = 0.47 + 0.14 = 0.6$$

$$\text{Step 8: } \text{sample} = \text{sample} + 1 = 1 + 1 = 2$$

Step 9: if (sample > ns)

$$2 > 2.$$

$$\text{Step 10: } g_m = -[3.8 - (1.41)(0.4) + 0.3](0.4)$$

$$g_m = -1.6.$$

$$g_C = -[3.8 - (1.41)(0.4) + 0.3].$$

$$g_C = -3.6.$$

$$\text{Step 11: } f_m = (0.9)(0.3) + (0.1)(-1.4)^2 = 0.46.$$

$$E_C = (0.9)(0.3) + (0.1)(-3.8)^2 = 6.89$$

Step 12:

$$\Delta m = \frac{-0.1}{\sqrt{0.46+1.0^{-8}}} \times -1.4 = 0.12.$$

$$\Delta C = \frac{-0.1}{\sqrt{6.89+10^{-8}}} \times -3.6 \approx 0.16$$

$$\text{Step 7: } m = m + \Delta m = 1.91 + 0.2 = 1.91$$

$$c = c + \Delta c = -0.8 + 0.16 = -0.64.$$

$$\text{Step 8: } \text{sample} = \text{sample} + 1 = 2 + 1 = 3.$$

Step 9: if (sample > ns)

$$3 > 2$$

$$\text{Step 10: } \text{itr} = \text{itr} + 1 = 2 + 1 = 3.$$

Step 11: if (itr > epoch)

$$3 > 2$$

$$\text{Step 12: } m = 1.91$$

$$c = -0.64$$