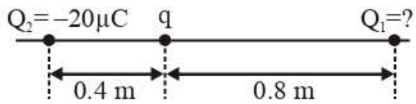
EXERCISE (S-1)

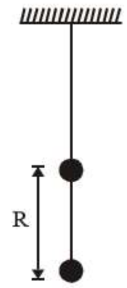
Properties of charge and Coulomb's law

1. Three charges are positioned in a straight line as depicted in the diagram. Using the information given in the diagram, determine the magnitude of charge 'Q_1' (in μC) if the charge q is to remain stationary.



ES0001

2. Two identical balls of mass m = 0.9 g each are charged by the same charges, joined by a thread and suspended from the ceiling (figure). Find the charge (in μC) that each ball should have so that the tension in both the threads are same? The distance between the centers of balls is R = 3m.

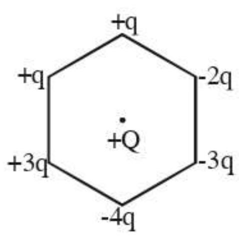


ES0002

3. Four identical charges q are placed at the corners of a square of side a, what charges Q must be placed at the centre of the square so that whole system of charges is in equilibrium?

ES0003

4. Six charges are kept at the vertices of a regular hexagon as shown in the figure. If magnitude of force applied by +Q on +q charge is F, then net electric force on the +Q is nF. Find the value of n.



ES0004

5. Two charged balls are connected by an inextensible thread of length 3 m. Masses of balls are 2kg and 1 kg, the charges are +20 μC and –100 μC. What minimum constant external force F (in N) must be applied to the ball of mass 1 kg so that the thread does not slack? Neglect gravity and friction.

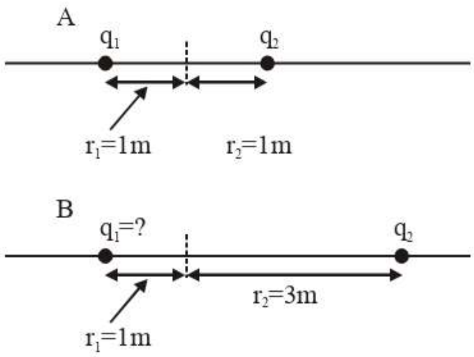
ES0005

Electric field

6. Two point charge –4Q and 9Q are placed at a distance 2m from each other. The position at which net electric field is zero from the charge –4Q is x (in m). What is the value of x.

ES0006

7. Two charges are separated as shown in the diagram A below. Each charge has a magnitude of 50 nC in diagram A. If the charge on the right is moved further to the right as depicted in diagram B, additional charge that must be removed from the left in order to maintain the initial electric field magnitude at the center (in nC) is given by $\frac{\alpha}{9}$ nC. Fill the value of α in OMR sheet.

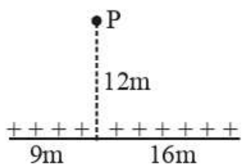


ES0007

8. A clock face has negative charges $-q, -2q, -3q, ..., -12q$ fixed at the positions of the corresponding numerals on the dial. Assume that the clock hands do not disturb the net field due to point charges. At what time does the hour hand point in the same direction is electric field at the centre of the dial.

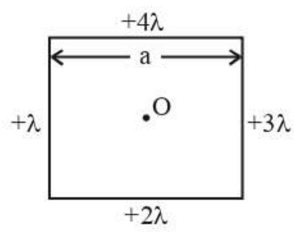
ES0008

9. Find the magnitude of electric field (in N/C) due to a line charge of $\lambda = \left(2\sqrt{2}\right)$ nC/m at a point P as shown.



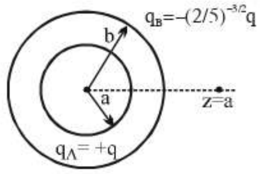
ES0009

10. Four uniformly charged wires of length a are arranged to form a square. Linear charge density of each wire is as shown. Electric field intensity at centre of square is $\frac{nk\lambda}{a}$ then value of n



ES0010

11. Two concentric rings, one of radius 'a' and the other of radius 'b' have the charges +q and $-(2/5)^{-3/2}$ q respectively as shown in the figure. Find the ratio b/a if a charge particle placed on the axis at z = a is in equilibrium.

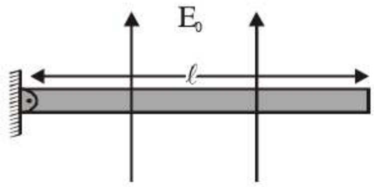


ES0011

12. The intensity of elecric field is required to exert a force on a proton equal to its weight at sea level is given by $\alpha \times 10^{-7}$ V/m. Fill the value of α (Given g = 10 m/s^2, mass of proton = 1.6×10^{-27} kg and charge on proton = 1.6×10^{-19}C).

ES0012

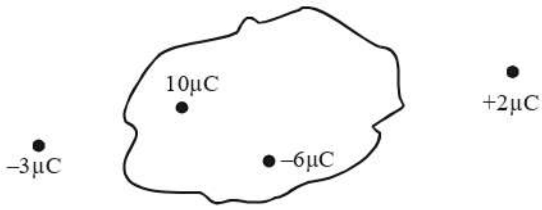
13. A thin insulating uniformly charged (linearly charged density λ) rod is hinged about one of its ends. It can rotate in vertical plane. If rod is in equilibrium by applying vertical electric field E as shown in figure. Find the value of E(in N/C). (Given that mass of rod 2 kg, $\lambda = 10\ C/m$, ℓ=1m, g=10 m/s^2)



ES0013

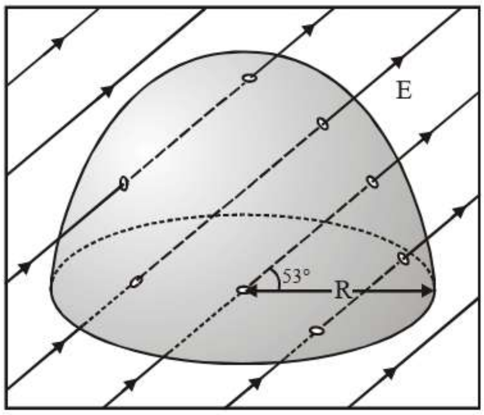
Gauss' law

14. In a particular system, if number of electric field lines associated by 1C charge is 10^9. Then net number of electric field lines passing through the given closed surface is n $\times 10^3$ find n.



ES0014

15. A uniform electric field E = 500 N/C passes through a hemispherical surface of radius R = 1.2 m as shown in figure. The net electric flux (in S.I. units) through the hemispherical surface only is Nπ. Then find the value of N.



ES0015

16. A non-uniform electric field in x-direction is increasing uniformly from 2N/C at x = 1m to 8 N/C at x = 7m. The center of cube is at x = 2m. If the charge enclosed inside a small cube of side length 10cm is 8.85×10^{-5n} C. The value of n will be.

ES0016

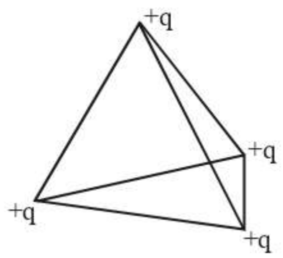
17. 20 μC charge is placed inside a closed surface then flux related to surface is ϕ. If 80 μC charge is added inside the surface then change in flux is given by $\alpha\phi$. Fill the value of α.

ES0017

18. A sphere of radius R has charge density given by $\rho = \rho_0\left(1 - \frac{nr}{3R}\right)$, where ρ_0 is a constant, r is distance from centre of sphere. For a spherical gaussian surface of radius R centered at the centre of sphere, the flux is zero. Find 'n'.

ES0018

19. Four point charges are kept at the vertices of a regular tetrahedron of side R. Total electrostatic energy of the configuration is $\frac{\alpha k q^2}{R}$. The value of α is



ES0019

Electric potential energy and electric potential

20. Four identical free point positive charges q (=1μC) each are located at the four corners of a square of side 1 m. A negative charge is placed at the centre of the square to obtain equilibrium of all the charges. What is the total potential energy (in milli Joules) of the system assuming the reference point at infinity?

ES0020

21. Consider the configuration of a system of four charges each of value +q. Find the work done by external agent in changing the configuration of the system from figure (i) to fig (ii).

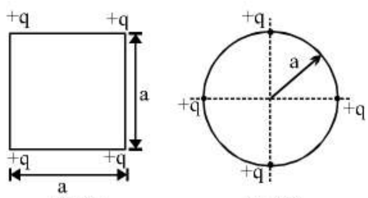
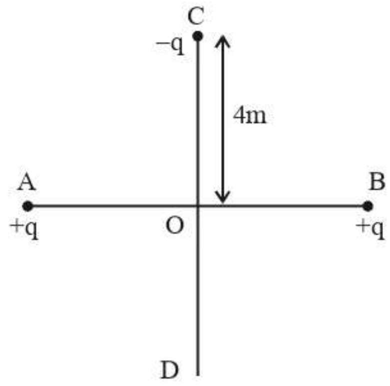


fig (i) fig (ii)

ES0021

22. Two fixed, equal positive charges, each +q are located at point A & B separated by a distance of 6 m. A particle of mass m having equal and opposite charge –q moves towards them along the perpendicular bisector line COD where O is the centre of line joining A and B. If –q charge is released from rest from point C, then speed of charge –q at O is given by

$v = q\sqrt{\dfrac{x}{15\pi \in_0 m}}$ find value of x. (Neglect gravity)



ES0022

23. An electric field $(-30\hat{i} + 20\hat{j})$ Vm^{-1} exists in the space. If potential at the origin is zero then find the potential at (5m,3m) in volts.

ES0023

24. A circular ring of radius a with uniform charge density λ is in the xy plane with centre at origin. A particle of mass m and charge q is projected from P (0, 0, a√3) on +z-axis towards origin with initial velocity u. The minimum value of the velocity so that the particle does not return to P is $\sqrt{\dfrac{\lambda q}{x\varepsilon_0 m}}$.

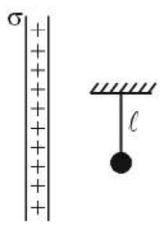
Find 'x' (neglect gravity).

ES0024

25. A particle of mass m carrying charge 'q' is projected with velocity (v) from point P towards an infinite line charge from a distance 'a'. Its speed reduces to zero momentarily at point Q which is at a distance a/2 from the line charge. If another particle with mass m and charge –q is projected with the same velocity v from point P towards the line charge. Its speed is found to be $\dfrac{Nv}{\sqrt{2}}$ at point 'Q'. Find the value of N.

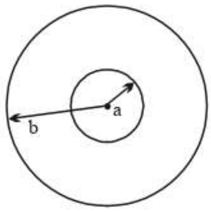
ES0025

26. A simple pendulum of length ℓ and bob mass m is hanging in front of a large nonconducting sheet of surface charge density σ. If suddenly a charge $+q$ is given to the bob in the position shown in figure. Find the maximum angle through which the string is deflected from vertical.



ES0026

27. Outer cylinder of the coaxial nonconductor of radius 'b' is given a positive potential V relative to the inner cylinder of radius 'a' as shown in the figure (charge distribution is uniform). A charge q (mass = m) is set free with negligible velocity at the surface of the inner cylinder. Find the velocity (in m/s), when it hits the outer cylinder. [consider V = 10, q = –20, m = 1 all in S.I. Units]



ES0027

28. A positive charge Q is uniformly distributed throughout the volume of a nonconducting sphere of radius R. A point mass having charge $+q$ and mass m is fired towards the centre of the sphere with velocity v from a point at distance $r(r > R)$ from the centre of the sphere. Find the minimum velocity v so that it can penetrate $R/2$ distance of the sphere. Neglect any resistance other than electric interaction. Charge on the small mass remains constant throughout the motion.

ES0028

Electric dipole

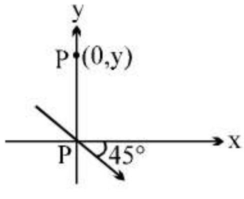
29. A plastic rod of length 1.0 m carries uniform positive charge +4.0 μC on half of its length and uniform negative charge –4.0 μ C on the remaining half of its length. Find magnitude of it's net dipole moment in μC–m.

ES0029

30. A dipole of dipole moment $\vec{p} = 2\hat{i} - 3\hat{j} + 4\hat{k}$ is placed at point A(2,–3,1). The electric potential due to this dipole at the point B(4,–1,0) is (ab) × 10^9 volt here 'a' represents sign (for negative answer select 0 for positive answer select 1. Write the value of $(a+b)^2$. The parameters specified here are in S.I. units.

ES0030

31. A dipole is placed at origin of coordinate system as shown in figure, find the electric field at point P (0, y).



ES0031

32. A small rigid object carries positive and negative charge of magnitude 4 coulomb each. It is oriented so that the positive charge has coordinates (–1.2mm, 1.1 mm) and negative charge has coordinates (1.4 mm, –1.3 mm). The object is kept in an electric field of $\left(2500\hat{i}-5000\hat{j}\right)$ N/C. Find the magnitude of torque (in N-m) acting on the dipole.

ES0032

33. A charge $+Q$ is fixed at the origin of the coordinate system while a small electric dipole of dipole-moment $\vec{p}$ pointing away from the charge along the x-axis is set free from a point far away from the origin.

(a) calculate the K.E. of the dipole when it reaches to a point $(d, 0)$ **[IIT-JEE 2003]**

(b) calculate the force on the charge $+Q$ due to the dipole at this moment.

ES0033

Conductors

34. A conducting sphere of radius R has two spherical cavities of radius a and b. The cavities have charges q_a and q_b respectively at their centres. Find:

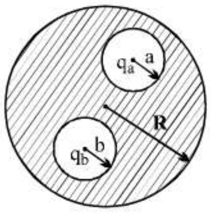
(a) The electric field and electric potential at a distance r

  (i) r (distance from O, the centre of sphere > R)

  (ii) r (distance from B, the centre of cavity b) < b

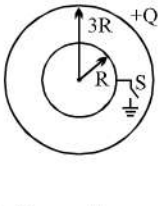
(b) Surface charge densities on the surface of radius R, radius a and radius b.

(c) What is the force on q_a and q_b?



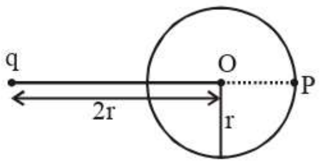
ES0034

35. Two thin conducting shells of radii R and $3R$ are shown in figure. The outer shell carries a charge $+Q$ and the inner shell is neutral. The inner shell is earthed with the help of switch S. Find the charge attained by the inner shell.



ES0035

36. A point charge q is placed at a distance 2r from the centre O of a conducting neutral sphere of radius r. Due to the induced charge on the sphere, the electric potential at point P on the surface of sphere is x volt. Then find the value of x. (If $\frac{kq}{r}$ = 18 volt)

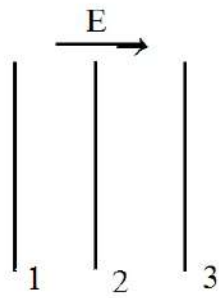


ES0036

37. A conducting liquid bubble of radius a and thickness t (t <<a) is charged to potential V. If the bubble collapses to a droplet, find the potential on the droplet. **[IIT-JEE 2005]**

ES0037

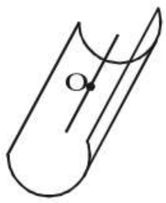
38. Three uncharge conducing large plates are placed parallel to each other in a uniform electric field. Find the induced charge density on each surface of each plate.



ES0038

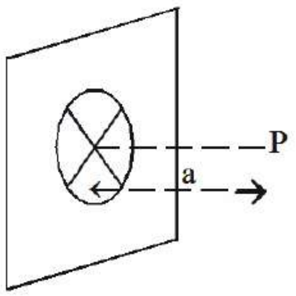
EXERCISE (S-2)

1. A thin long strip whose cross-section is a semicircle carries a uniform surface charge of density σ on its inner surface. Find the electric field at a point O located midway on its axis.



ES0039

2. An infinitely long non-conducting plane of charge density σ has circular aperture of certain radius carved out from it. The electric field at a point which is at a distance 'a' from the centre of the aperture is $\sigma/2\sqrt{2}\in_0$. Find the radius of aperture.

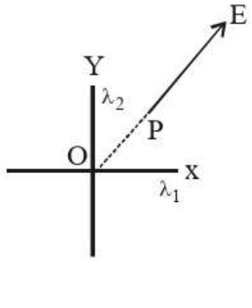


ES0040

3. A disc of radius R is kept such that its axis coincide with the x-axis and its centre is at (d,0,0). The thickness of disc is t and it carries a uniform volume charge density ρ. The external electric field in the space is given by $\vec{E} = K\vec{r}$ where K = Constant and $\vec{r}$ is position vector of any point in space with respect to the origin of the coordinate system. Find the electric force on the disc.

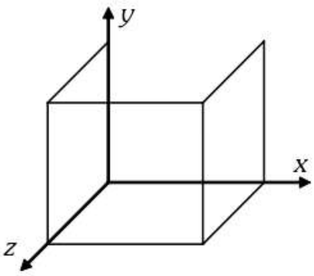
ES0041

4. Two mutually perpendicular infinite wires along x-axis and y-axis carry charge densities λ_1 and λ_2. The electric line of force at P is along the line $y = \frac{1}{\sqrt{3}}x$, where P is also a point lying on the same line then find λ_2/λ_1.



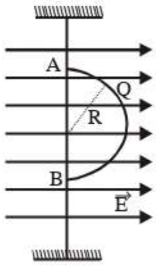
ES0042

5. An electric field given by $\vec{E} = 4\hat{i} - 3(y^2 + 2)\hat{j}$ pierces Gaussian's cube of side 1m placed at origin such that its three sides represents x, y and z axes. The net charge enclosed within the cube is given by $-n\varepsilon_0$. Find the value of n.



ES0043

6. The charge $Q = \pi C$ is distributed on a thin semicircular ring of radius R = 2m. There is a uniform electrostatic field $|\vec{E}| = 2N/C$ directed horizontally. The semicircular ring can rotate freely about a fixed vertical axis AB. Initially the ring is in static equilibrium as shown in figure. If we want to rotate it about the fixed axis by 90° then minimum work required on the ring is *x* J. Find the value of x.



ES0044

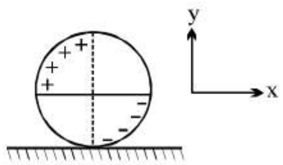
7. Four point charges $+8\mu C$, $-1\mu C$, $-1\mu C$ and $+8\mu C$, are fixed at the points, $-\sqrt{\frac{27}{2}}$ m, $-\sqrt{\frac{3}{2}}$ m, $+\sqrt{\frac{3}{2}}$ m and $+\sqrt{\frac{27}{2}}$ m respectively on the y-axis. A particle of mass 6×10^{-4} kg and of charge $+0.1\ \mu C$ moves along the $-x$ direction. Its speed at $x = +\infty$ is v_0. Find the least value of v_0 for which the particle will cross the origin. Find also the kinetic energy of the particle at the origin. Assume that space is gravity free. (Given : $1/(4\pi\varepsilon_0) = 9 \times 10^9\ Nm^2/C^2$)

ES0045

8. The electric potential in a region is given by $V(x, y, z) = ax^2 + ay^2 + abz^2$. 'a' is a positive constant of appropriate dimensions and b, a positive constant such that V is volts when x, y, z are in m. Let b = 2. The work done by the electric field when a point charge $+4\mu C$ moves from the point (0, 0, 0.1m) to the origin is 50 μJ. The radius of the circle of the equipotential curve corresponding to V = 6250 volts and $z = \sqrt{2}$ m is α m. Fill α^2 in OMR sheet.

ES0046

9. A nonconducting ring of mass m and radius R is charged as shown. The charged density i.e. charge per unit length is λ. It is then placed on a rough nonconducting horizontal surface plane. At time t = 0, a uniform electric field $\vec{E} = E_0 i$ is switched on and the ring start rolling without sliding. Determine the friction force (magnitude and direction) acting on the ring, when it starts moving.

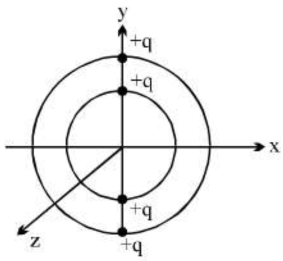


ES0047

10. Small identical balls with equal charges are fixed at vertices of regular 2008 - gon with side *a*. At a certain instant, one of the balls is released & a sufficiently long time interval later, the ball adjacent to the first released ball is freed. The kinetic energies of the released balls are found to differ by *K* at a sufficiently long distance from the polygon. Determine the charge *q* of each ball.

ES0048

11. Two concentric rings of radii r and 2r are placed with centre at origin. Two charges +q each are fixed at the diametrically opposite points of the rings as shown in figure. Smaller ring is now rotated by an angle 90° about Z-axis then it is again rotated by 90° about Y-axis. Find the work done by electrostatic forces in each step. If finally larger ring is rotated by 90° about X-axis, find the total work required to perform all three steps.



ES0049

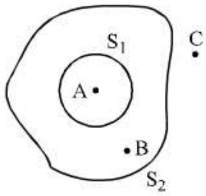
12. A non-conducting disc of radius a and uniform positive surface charge density σ is placed on the ground, with its axis vertical. A particle of mass m & positive charge q is dropped, along the axis of the disc, from a height H with zero initial velocity. The particle has $\frac{q}{m} = \frac{4\varepsilon_0 g}{\sigma}$.

(a) Find the value of H if the particle just reaches the disc.

(b) Sketch the potential energy of the particle as a function of its height and find its equilibrium position.

ES0050

13. S_1 and S_2 are two conducting surfaces. Between S_1 and S_2 and inside S_1 is air. S_1 is spherical with A its centre. S_1 has total charge Q. S_2 is uncharged. Find (if possible) :



(i) Charges induced on inner and outer surface of S_2.

(ii) Total electric field at A, B.

(iii) Electric field at B due to induced charges on S_2.

(iv) Electric field at C due to induced charges on inner surface of S_2.

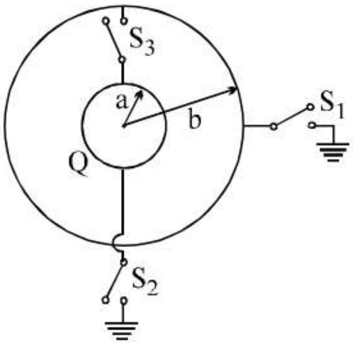
(v) Electric field produced by induced charges on outer surface of S_2 inside the body of S_2.

(vi) Can you find electric field at C easily ?

(take the required distances from A). Which charge will produce electric field here.

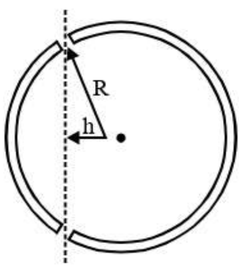
ES0051

14. The figure shows a conducting sphere 'A' of radius 'a' which is surrounded by a neutral conducting spherical shell B of radius 'b' (>a). Initially switches S_1, S_2 and S_3 are open and sphere 'A' carries a charge Q. First the switch 'S_1' is closed to connect the shell B with the ground and then opened. Now the switch 'S_2' is closed so that the sphere 'A' is grounded and then S_2 is opened. Finally, the switch 'S_3' is closed to connect the spheres together. Find the heat (in joule) which is produced after closing the switch S_3. [Consider b = 4 cm, a = 2 cm and Q = 80 μC]



ES0052

15. Consider a metal sphere, of radius R that is cut in two along a plane whose minimum distance from the sphere's centre is h. Sphere is uniformly charged by a total electric charge Q. What force is necessary to hold the two parts of the sphere together ?



ES0053

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16. Two fixed charges –2Q and Q are located at the points with co-ordinates (–3a, 0) and (3a, 0) respectively in the x-y plane. (a) Show that all the points in the x-y plane where the electric potential due to the two charges is zero lie on a circle. Find its radius and the location of its centre. (b) Give the expression for the potential $V_{(x)}$ at a general point on the x-axis and sketch the function $V_{(x)}$ on the whole x-axis. (c) If a particle of charge +q starts from rest at the centre of the circle, show by a short qualitative argument that the particle eventually crosses the circle. Find its speed when it does so.

ES0054

17. The electric field strength depends only on the x, y and z coordinates according to the law

$E = \dfrac{a(x\hat{i} + y\hat{j} + z\hat{k})}{\left(x^2 + y^2 + z^2\right)^{3/2}}$, where a = 122.5 SI unit and is a constant. Find the potential difference (in volt) between (3, 2, 6) and (0, 3, 4).

ES0055

EXERCISE (O-1)

SINGLE CORRECT TYPE QUESTIONS

<u>Properties of charges and coulomb's law</u>

1. If an object made of substance A rubs an object made of substance B, then A becomes positively charged and B becomes negatively charged. If, however, an object made of substance A is rubbed against an object made of substance C, then A becomes negatively charged. What will happen if an object made of substance B is rubbed against an object made of substance C?

(A) B becomes positively charged and C becomes positively charged.

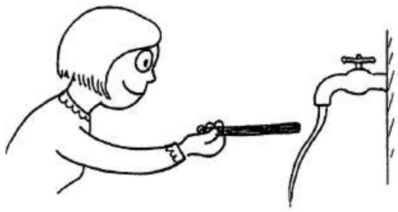
(B) B becomes positively charged and C becomes negatively charged.

(C) B becomes negatively charged and C becomes positively charged.

(D) B becomes negatively charged and C becomes negatively charged.

ES0056

2. In normal cases thin stream of water bends toward a negatively charged rod. When a positively charged rod is placed near the stream, it will bend in the



(A) Opposite direction. (B) Same direction.

(C) It won't bend at all. (D) Can't be predicted.

ES0057

3. Two charged bodies A and B exert repulsive forces on each other. If charge on A is more then that on B, which of the following statement is true.

(A) Body A experiences more Colombian force then B.

(B) Body A experiences less Colombian force then B.

(C) Both of them experience Colombian forces of equal magnitude.

(D) It depends whether the bodies can be treated as point like charges or not.

ES0058

4. Given are four arrangements of three fixed electric charges. In each arrangement, a point labeled P is also identified — test charge, +q, is placed at point P. All of the charges are of the same magnitude, Q, but they can be either positive or negative as indicated. The charges and point P all lie on a straight line. The distances between adjacent items, either between two charges or between a charge and point P, are all the same. Correct order of choices in a decreasing order of magnitude of force on P is

I. (+) (+) (+) • P

II. (+) (+) • P (−)

III. (+) (+) (−) • P

IV. (+) (−) (+) • P

(A) II > I > III > IV (B) I > II > III > IV (C) II > I > IV > III (D) III > IV > I > II

ES0059

5. Two point charge of 100 μC and –4 μC are positioned at points $(-2\sqrt{3}, 3\sqrt{3}, -4)$ and $(4\sqrt{3}, -5\sqrt{3}, 6)$ respectively of a Cartesian coordinate system. Find the force vector on the –4 μC charge? All the coordinates are in meters.

(A) $9\times10^{-4}\left(3\sqrt{3}\hat{i}-4\sqrt{3}\hat{j}+5\hat{k}\right)$

(B) $9\times10^{-4}\left(-3\sqrt{3}\hat{i}+4\sqrt{3}\hat{j}-5\hat{k}\right)$

(C) $2.25\times10^{-4}\left(-3\sqrt{3}\hat{i}+4\sqrt{3}\hat{j}-5\hat{k}\right)$

(D) $2.25\times10^{-4}\left(3\sqrt{3}\hat{i}-4\sqrt{3}\hat{j}+5\hat{k}\right)$

ES0060

Electric field

6. Five positive equal charges are placed at vertices of a regular hexagon and net electric field at the centre is E_1. A negative charge having equal magnitude is placed sixth vertex and then net electric field is E_2. Find $\frac{E_2}{E_1}$.

(A) 2 (B) 1 (C) 3 (D) None of these

ES0061

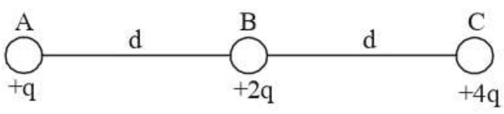
7. There are two point charges q_1 and q_2 lying on a circle of unit radius. Electric field intensity at the center of circle due to these charges is $\vec{E}$. Find the position vector of the center with respect to q_2 if the position vector of the center with respect to q_1 is $\vec{r}_1$.

(A) $\frac{\vec{E}+kq_1\vec{r}_1}{kq_2}$ (B) $-\left(\frac{\vec{E}+kq_1\vec{r}_1}{kq_2}\right)$

(C) $\frac{kq_1\vec{r}_1-\vec{E}}{kq_2}$ (D) $\frac{\vec{E}-kq_1\vec{r}_1}{kq_2}$

ES0062

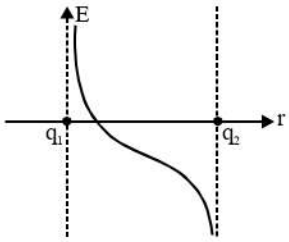
8. Three charges +q, +2q and +4q are connected by strings as shown in the figure. What is ratio of tensions in the strings AB and BC.



(A) 1 : 2 (B) 1 : 3 (C) 2 : 1 (D) 3 : 1

ES0063

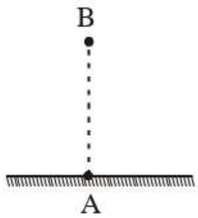
9. The variation of electric field between the two charges q_1 and q_2 along the line joining the charges is plotted against distance from q_1 (taking rightward direction of electric field as positive) as shown in the figure. Then the correct statement is :-



(A) q_1 and q_2 are positive and $q_1 < q_2$
(B) q_1 and q_2 are positive and $q_1 > q_2$
(C) q_1 is positive and q_2 is negative and $q_1 < q_2$
(D) q_1 and q_2 are negative and $q_1 < q_2$

ES0064

10. Particle *B* of charge *Q* and mass m is in equilibrium under weight and electrostatics force applied by a fixed charged *A*, which is directly beneath the particle *B* as shown in figure. When particle B is disturbed along vertical, the equilibrium is



(A) stable
(B) unstable
(C) neutral
(D) there can not be in equilibrium

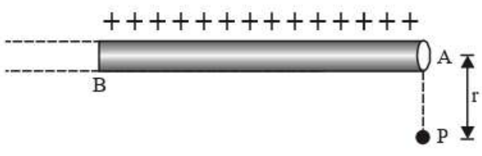
ES0065

11. A charge q is placed at the centroid of an equilateral triangle. Three equal charges Q are placed at the vertices of the triangle. The system of four charges will be in equilibrium if q is equal to :-

(A) $\frac{-Q}{\sqrt{3}}$
(B) $\frac{-Q}{3}$
(C) $-Q\sqrt{3}$
(D) $\frac{Q}{\sqrt{3}}$

ES0066

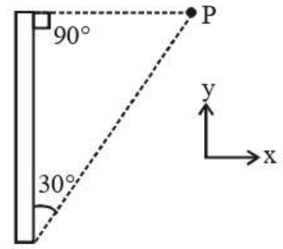
12. A semi-infinite insulating rod has linear charge density λ. The electric field at the point P shown in figure is :-



(A) $\frac{2\lambda^2}{(4\pi\varepsilon_0 r)^2}$ at 45° with AB
(B) $\frac{\sqrt{2}\lambda}{4\pi\varepsilon_0 r^2}$ at 45° with AB
(C) $\frac{\sqrt{2}\lambda}{4\pi\varepsilon_0 r}$ at 45° with AB
(D) $\frac{\sqrt{2}\lambda}{4\pi\varepsilon_0 r}$ at perpendicular to AB

ES0067

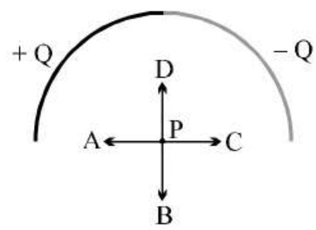
13. The direction (θ) of $\vec{E}$ at point P due to uniformly charged finite rod will be :-



(A) at angle 30^0 from x-axis
(B) 45^0 from x - axis
(C) 60^0 from x-axis
(D) none of these

ES0068

14. As shown in the figure, an insulating rod is set into the shape of a semicircle. The left half of the rod has a charge of + Q uniformly distributed along its length, and the right half of the rod has a charge of –Q uniformly distributed along its length. What vector shows the correct direction of the electric field at point P, the centre of the semicircle ?



(A) A
(B) B
(C) C
(D) D

ES0069

15. A nonconducting ring of radius R has uniformly distributed positive charge Q. A small part of the ring, of length d, is removed ($d << R$). The electric field at the centre of the ring will now be
(A) directed towards the gap, inversely proportional to R^3.
(B) directed towards the gap, inversely proportional to R^2.
(C) directed away from the gap, inversely proportional to R^3.
(D) directed away from the gap, inversely proportional to R^2.

ES0070

16. The maximum electric field at a point on the axis a uniformly charged ring is E_0. At how many points on the axis will the magnitude of electric field be $E_0/2$:-
(A) 1
(B) 2
(C) 3
(D) 4

ES0071

17. A particle of mass m, charge –Q is constrained to move along the axis of a ring of radius a. The ring carries a uniform charge density + λ along its circumference. Initially, the particle lies in the plane of the ring at a point where no net force acts on it. The period of oscillation of the particle when it is displaced slightly from its equilibrium position is

(A) $T = 4\pi\sqrt{\dfrac{\varepsilon_0 ma^2}{\lambda Q}}$
(B) $T = 2\pi\sqrt{\dfrac{2\varepsilon_0 ma^2}{\lambda Q}}$
(C) $T = 2\pi\sqrt{\dfrac{4\varepsilon_0 ma^2}{\lambda Q}}$
(D) $T = 2\pi\sqrt{\dfrac{\varepsilon_0 ma^2}{2\lambda Q}}$

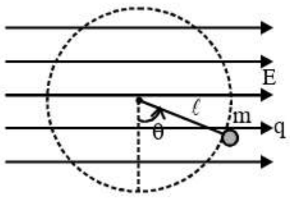
ES0072

18. The surface charge density of a thin charged disc of radius R is σ. The value of the electric field at the centre of the disc is $\frac{\sigma}{2\epsilon_0}$. With respect to the field at the centre, the electric field along the axis at a distance $\sqrt{3}$ R from the centre of the disc :

(A) reduces by 70.7% (B) reduces by 29.3% (C) reduces by 86.6% (D) reduces by 13.4%

ES0073

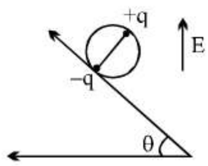
19. A small ball of mass m and charge +q tied with a string of length ℓ, is rotating in a vertical circle under gravity and a uniform horizontal electric field E as shown. The tension in the string will be minimum for:-



(A) $\theta = \tan^{-1}\left(\frac{qE}{mg}\right)$ (B) $\theta = \pi$ (C) $\theta = \pi - \tan^{-1}\left(\frac{qE}{mg}\right)$ (D) $\theta = \pi + \tan^{-1}\left(\frac{qE}{mg}\right)$

ES0074

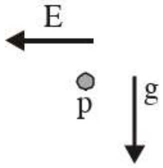
20. A wheel having mass m has charges +q and –q on diametrically opposite points. It remains in equilibrium on a rough inclined plane in the presence of uniform vertical electric field E =

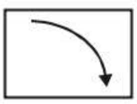
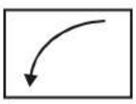
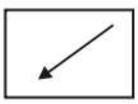
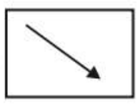


(A) $\frac{mg}{q}$ (B) $\frac{mg}{2q}$ (C) $\frac{mg\tan\theta}{2q}$ (D) none

ES0075

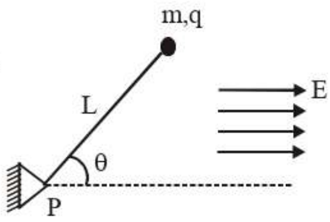
21. A negatively charged particle *p* is placed, initially at rest, in a constant, uniform gravitational field and a constant, uniform electric field as shown in the diagram. What qualitatively, is the shape of the trajectory of the electron ?



(A)  (B)  (C)  (D) 

ES0076

22. A particle of mass m and charge q is attached to a light rod of length L. The rod can rotate freely in the plane of paper about the other end, which is hinged at P. The entire assembly lies in a uniform electric field E also acting in the plane of paper as shown. The rod is released from rest when it makes an angle θ with the electric field direction. Determine the speed of the particle when the rod is parallel to the electric field.

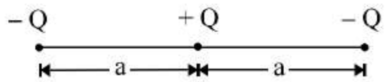


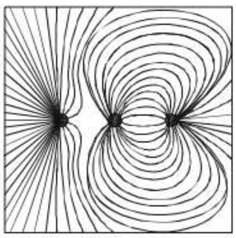
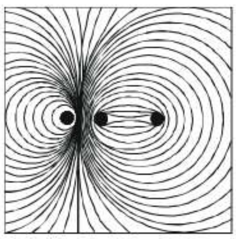
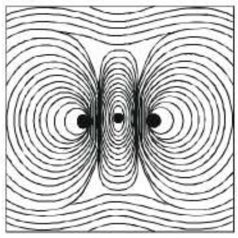
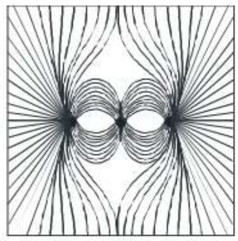
(A) $\left(\frac{2qEL(1-\cos\theta)}{m}\right)^{1/2}$ (B) $\left(\frac{2qEL(1-\sin\theta)}{m}\right)^{1/2}$

(C) $\left(\frac{qEL(1-\cos\theta)}{2m}\right)^{1/2}$ (D) $\left(\frac{2qEL\cos\theta}{m}\right)^{1/2}$

ES0077

23. The fig. shows the distribution of three charges –Q, +Q and –Q on the X-axis. Which of the following figures shows the possible electric field lines for the distribution?

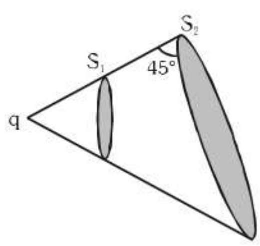


(A)  (B)  (C)  (D) 

ES0078

Gauss' law

24. In the given figure flux through surface S_1 is ϕ_1 & through S_2 is ϕ_2. Which is correct ?

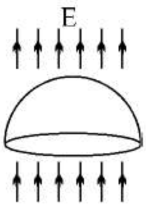


(A) $\phi_1 = \phi_2$ (B) $\phi_1 > \phi_2$

(C) $\phi_1 < \phi_2$ (D) None of these

ES0079

25. A hemispherical surface (half of a spherical surface) of radius R is located in a uniform electric field E that is parallel to the axis of the hemisphere. What is the magnitude of the electric flux through the hemisphere surface?

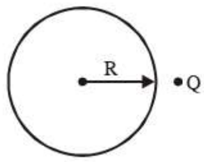


(A) 0 (B) $4\pi R^2E/3$ (C) $2\pi R^2E$ (D) πR^2E

ES0080

26. **Statement 1:** A charge is outside the Gaussian sphere of radius R. Then electric field on the surface of sphere is zero.

and

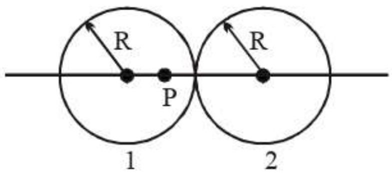


Statement 2 : As $\oint \vec{E}\cdot d\vec{s} = \frac{q_{in}}{\varepsilon_0}$, for the sphere q_{in} is zero, so $\oint \vec{E}\cdot d\vec{s} = 0$.

(A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.
(B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.
(C) Statement-1 is true, statement-2 is false.
(D) Statement-1 is false, statement-2 is true.

ES0081

27. Figure shows, in cross section, two solid spheres with uniformly distributed charge throughout their volumes. Each has radius R. Point P lies on a line connecting the centres of the spheres, at radial distance R/2 from the center of sphere 1. If the net electric field at point P is zero and Q_1 is 64 μC, what is Q_2(in μC).



(A) 64 (B) 36 (C) 32 (D) 72

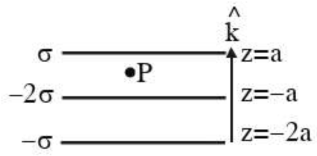
ES0082

28. A sphere of radius R carries charge density proportional to the square of the distance from the center: $\rho = Ar^2$, where A is a positive constant. At a distance of R/2 from the center, the magnitude of the electric field is :-

(A) $A/4\pi\varepsilon_0$ (B) $AR^3/40\varepsilon_0$ (C) $AR^3/24\varepsilon_0$ (D) $AR^3/5\varepsilon_0$

ES0083

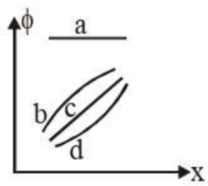
29. Three large parallel plates have uniform surface charge densities as shown in the figure. What is the electric field at *P*? **[IIT-JEE 2005 (Scr)]**



(A) $-\frac{4\sigma}{\epsilon_0}\hat{k}$ (B) $\frac{4\sigma}{\epsilon_0}\hat{k}$ (C) $-\frac{2\sigma}{\epsilon_0}\hat{k}$ (D) $\frac{2\sigma}{\epsilon_0}\hat{k}$

ES0084

30. A line of charge extends along a X-axis whose linear charge density varies directly as x. Imagine a spherical volume with its centre located on X-axis and is moving gradually along it. Which of the graphs shown in figure correspond to the flux ϕ with the x coordinate of the centre of the volume?



(A) a (B) b (C) c (D) d

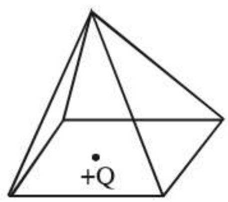
ES0085

31. The electric field in a region is given by $\vec{E} = 200\hat{i}$ N/C for x > 0 and $-200\hat{i}$ N/C for x < 0. A closed cylinder of length 2m and cross-section area 10^2 m^2 is kept in such a way that the axis of cylinder is along X-axis and its centre coincides with origin. The total charge inside the cylinder is
[Take : $\varepsilon_0 = 8.85 \times 10^{-12}$ C^{2}m^2.N)

(A) 0 (B) 1.86×10^{-5}C (C) 1.77×10^{-11}C (D) 35.4×10^{-8} C

ES0086

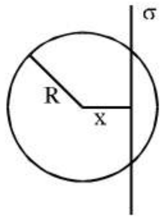
32. A point charge +Q is positioned at the center of the base of a square pyramid as shown. The flux through one of the four identical upper faces of the pyramid is :-



(A) $\frac{Q}{16\varepsilon_0}$ (B) $\frac{Q}{4\varepsilon_0}$ (C) $\frac{Q}{8\varepsilon_0}$ (D) None of these

ES0087

33. An infinite, uniformly charged sheet with surface charge density σ cuts through a spherical Gaussian surface of radius R at a distance x from its center, as shown in the figure. The electric flux Φ through the Gaussian surface is :-



(A) $\frac{\pi R^2 \sigma}{\varepsilon_0}$ (B) $\frac{2\pi\left(R^2 - x^2\right)\sigma}{\varepsilon_0}$ (C) $\frac{\pi(R-x)^2 \sigma}{\varepsilon_0}$ (D) $\frac{\pi\left(R^2 - x^2\right)\sigma}{\varepsilon_0}$

ES0088

34. Consider a circle of radius R. A point charge lies at a distance 'a' from its center and on its axis such that $R = a\sqrt{3}$. If electric flux passing through the circle is ϕ then the magnitude of the point charge is:-

(A) $\sqrt{3}\varepsilon_0\phi$ (B) $2\varepsilon_0\phi$ (C) $4\varepsilon_0\phi/\sqrt{3}$ (D) $4\,\varepsilon_0\phi$

ES0089

Electric potential energy and electric potential

35. Two particles X and Y, of equal mass and with unequal positive charges, are free to move and are initially far away from each other. With Y at rest, X begins to move towards it with initial velocity u. After a long time, finally :-

(A) X will stop, Y will move with velocity u.

(B) X and Y will both move with velocities u/2 each.

(C) X will stop, Y will move with velocity < u.

(D) both will move with velocities < u/2.

ES0090

36. Two positively charged particles X and Y are initially far away from each other and at rest. X begins to move towards Y with some initial velocity. The total momentum and energy of the system are p and E.

(A) If Y is fixed, both p and E are conserved.

(B) If Y is fixed, E is conserved, but not p.

(C) If both are free to move, p is conserved but not E.

(D) If both are free, E is conserved, but not p.

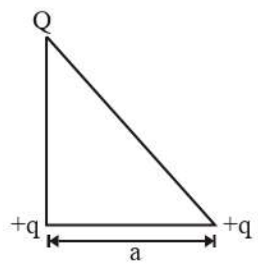
ES0091

37. Potential energy of a system comprising of point charges is U_1. When a charge q is added in the system without disturbing other charges, the potential energy becomes U_2. The potential of the point where the charge q is placed in the system is

(A) $\frac{U_2 - U_1}{q}$ (B) $\frac{U_1 - U_2}{q}$ (C) $\frac{U_1 + U_2}{2q}$ (D) $\frac{U_2 - U_1}{2q}$

ES0092

38. Three charges Q, +q and +q are placed at the vertices of a right-angled isosceles triangle as shown. The net electrostatic energy of the configuration is zero if Q is equal to :**[JEE 2000(Scr) 1 + 1]**



(A) $\frac{-q}{1+\sqrt{2}}$ (B) $\frac{-2q}{2+\sqrt{2}}$ (C) $-2q$ (D) $+q$

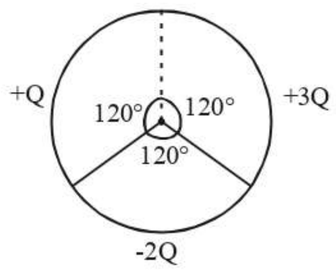
ES0093

39. Two fixed charges A and B of 5 μC each are separated by a distance of 6m. C is the mid point of the line joining A and B. A charge 'Q' of –5μC is shot perpendicular to the line joining A and B through C with a kinetic energy of 0.06J. The charge 'Q' comes to rest at a point D. The distance CD is:-

(A) 3 m (B) $\sqrt{3}$ m (C) $3\sqrt{3}$ m (D) 4 m

ES0094

40. Figure shows three circular arcs, each of radius R and total charge as indicated. The net electric potential at the centre of curvature is :-

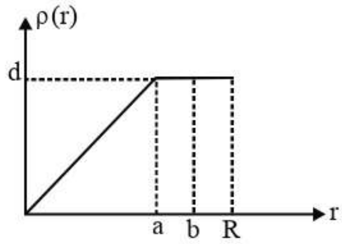


(A) $\frac{Q}{4\pi \epsilon_0 R}$ (B) $\frac{Q}{2\pi \epsilon_0 R}$

(C) $\frac{2Q}{\pi \epsilon_0 R}$ (D) $\frac{Q}{\pi \epsilon_0 R}$

ES0095

41. The nuclear charge (Ze) is non-uniformly distribute within a nucleus of radius R. The charge density $\rho(r)$ [charge per unit volume] is dependent on the radial distance r from the centre of the nucleus as shown in figure. Select correct alternative/s.



(A) Electric field at r = R is independent of b

(B) Electric potential at r = R is proportional to b

(C) Electric field at r = R is proportional to a

(D) Electric potential at r = R is proportional to a

ES0096

42. A solid sphere of radius R is charged uniformly. At what distance from its surface is the electrostatic potential half of the potential at the centre?

(A) R (B) R/2 (C) R/3 (D) 2R

ES0097

43. When a negative charge is released and moves in electric field, it moves toward a position of

(A) lower electric potential and lower potential energy

(B) lower electric potential and higher potential energy

(C) higher electric potential and lower potential energy

(D) higher electric potential and higher potential energy

ES0098

44. A positively charged particle is released from rest in an uniform electric field. The electric potential energy of the charge

(A) remains a constant because the electric field is uniform.

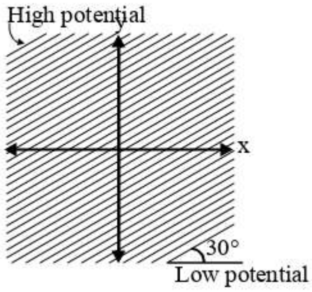
(B) increases because the charge moves along the electric field.

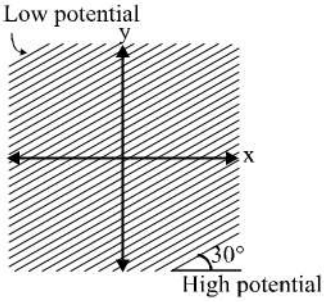
(C) decreases because the charge moves along the electric field.

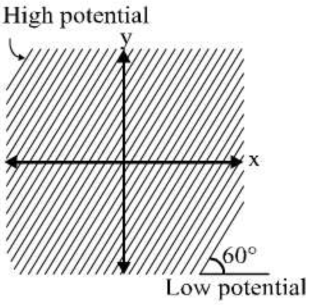
(D) decreases because the charge moves opposite to the electric field.

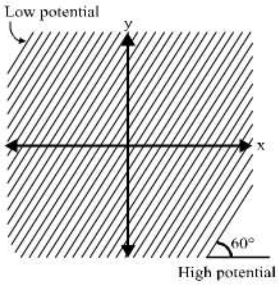
ES0099

45. The electric field intensity at all points in space is given by $\vec{E} = \sqrt{3}\hat{i} - \hat{j}$ volts/metre. The nature of equipotential lines in x-y plane is given by :-

(A) 

(B) 

(C) 

(D) 

ES0100

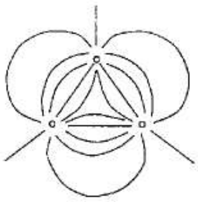
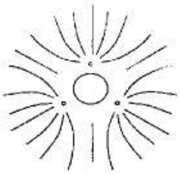
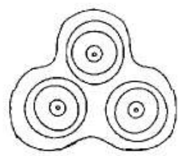
46. Equipotential at a great distance from a collection of charges whose total sum is not zero are approximately

(A) spheres. (B) planes.

(C) paraboloids (D) ellipsoids.

ES0101

47. Three positive charges of equal value q are placed at the vertices of an equilateral triangle. The resulting lines of force should be sketched as in **[JEE 2001 (Scr)]**

(A)  (B)  (C)  (D) 

ES0102

48. In an electric field the potential at a point is given by the following relation $V = \frac{343}{r}$. The electric field at $\vec{r} = 3\hat{i} + 2\hat{j} + 6\hat{k}$ is :

(A) $21\hat{i} + 14\hat{j} + 42\hat{k}$ (B) $3\hat{i} + 2\hat{j} + 6\hat{k}$ (C) $\frac{1}{7}\left(3\hat{i} + 2\hat{j} + 6\hat{k}\right)$ (D) $-\left(3\hat{i} + 2\hat{j} + 6\hat{k}\right)$

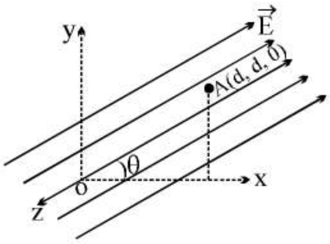
ES0103

49. From a point if we move in a direction making an angle θ measured from +ve x-axis , the potential gradient is given as $\frac{dv}{dr}$=2 cos θ. Find the direction and magnitude of electric field at that point.

(A) $2\hat{i}$ (B) $-2\hat{i}$ (C) $\hat{i}+\hat{j}$ (D) $-\hat{i}+\hat{j}$

ES0104

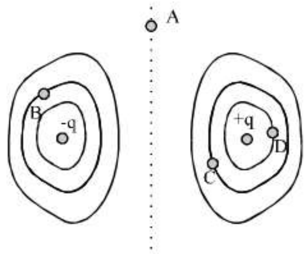
50. A uniform electric field having strength $\vec{E}$ is existing in x-y plane as shown in figure. Find the p.d. between origin O & A(d, d, 0)



(A) Ed (cosθ + sinθ) (B) –Ed (sinθ – cosθ) (C) $\sqrt{2}$ Ed (D) none of these

ES0105

51. Figure shows equi-potential surfaces for a two charges system. At which of the labeled points point will an electron have the highest potential energy?



(A) Point A (B) Point B (C) Point C (D) Point D

ES0106

52. Figure shows some equipotential lines distributed in space. A charged object is moved from point A to point B.

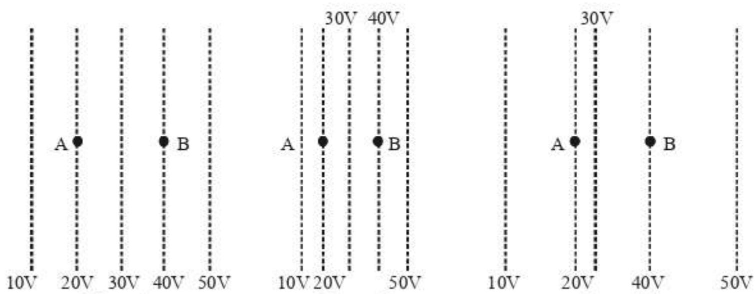


Figure-I (i) Figure-II (ii) Figure-III (iii)

(A) The work done in Fig. (i) is the greatest.
(B) The work done in Fig. (ii) is least.
(C) The work done is the same in Fig. (i), Fig. (ii) and Fig. (iii).
(D) The work done in Fig. (iii) is greater than Fig. (ii)but equal to that in Fig. (i).

ES0107

53. Consider the following conclusions regarding the components of an electric field at a certain point in space given by

$E_x = -Ky$ $E_y = Kx$ $E_z = 0$

(I) The field is conservative.
(II) The field is non-conservative.
(III) The lines of force are staright lines
(IV) The lines of force are circles.

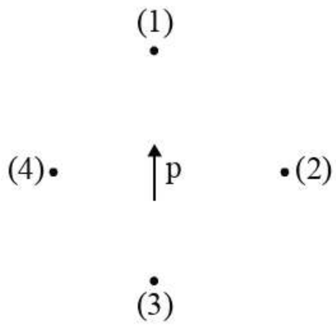
Of these conclusions

(A) II and IV are valid
(B) I and III are valid
(C) I and IV are valid
(D) II and III are valid

ES0108

Electric dipole

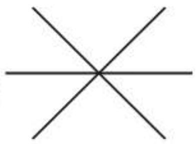
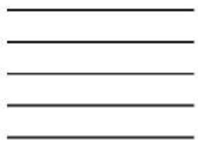
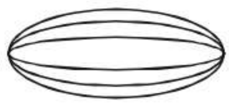
54. The drawing shows four points surrounding an electric dipole. Which one of the following expressions best ranks the electric potential at these four locations?



(A) $1 > 2 = 4 > 3$ (B) $3 > 2 > 4 > 1$ (C) $3 > 2 = 4 > 1$ (D) $2 = 4 > 1 = 3$

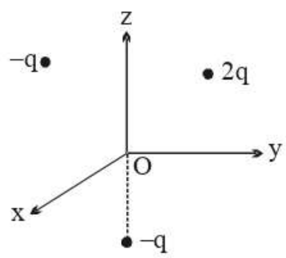
ES0109

55. Which of the following represents the equipotential lines of a dipole (two equal and opposite charges placed at small separation)?

(A)  (B)  (C)  (D) 

ES0110

56. Three point charges 2q, –q and –q are located respectively at (0, a, a), (0, a, –a) and (0, 0, – a) as shown. The dipole moment of this distribution is :-



(A) 2qa in the y–z plane at $\tan^{-1}\left(\frac{1}{4}\right)$ with z-axis

(B) $\sqrt{17}$qa in the y–z plane at $\tan^{-1}\left(\frac{1}{4}\right)$ with z-axis

(C) $\sqrt{5}$qa in the x–y plane at $\tan^{-1}$ (4) with y-axis

(D) 4qa in the x–y plane at $\tan^{-1}$ (4) with y-axis

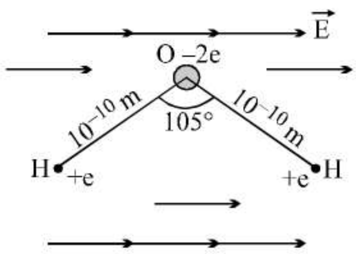
ES0111

57. Point P lies on the axis of a dipole. If the dipole is rotated by 90° anticlock wise, the electric field vector $\vec{E}$ at P will rotate by

(A) 90° clock wise
(B) 180° clock wise
(C) 90° anti clock wise
(D) none

ES0112

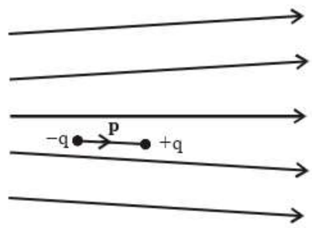
58. A water molecule as shown is in a region of uniform electric field $\vec{E} = 1000\hat{i}$ V/m. This molecule experiences



(A) A counterclockwise torque
(B) A clockwise torque
(C) A net force to the right
(D) A net force to the left

ES0113

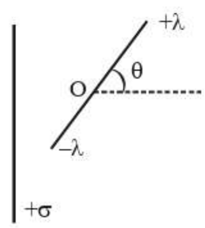
59. Electric field lines in which an electric dipole **p** is placed as shown. Which of the following statements is correct ?



(A) The dipole will not experience any force.
(B) The dipole will experience a force towards right.
(C) The dipole will experience a force towards left.
(D) The dipole will experience a force upwards.

ES0114

60. A large sheet carries uniform surface charge density σ. A rod of length 2ℓ has a linear charge density λ on one half and – λ on the other half. The rod is hinged at mid point O and makes angle θ with the normal to the sheet. The torque experienced by the rod is :-



(A) $\dfrac{\sigma\lambda\ell^2}{2\varepsilon_0}\cos\theta$
(B) $\dfrac{\sigma\lambda\ell}{\varepsilon_0}\cos^2\theta$
(C) $\dfrac{\sigma\lambda\ell^2\sin\theta}{2\varepsilon_0}$
(D) $\dfrac{\sigma\lambda\ell\sin^2\theta}{\varepsilon_0}$

ES0115

61. An electric dipole (dipole moment p) is placed at a radial distance r >> a (where a is dipole length) from a infinite line of charge having linear charge density $+\lambda$. Dipole moment vector is aligned along radial vector $\vec{r}$ force experienced by dipole is :-

(A) $\frac{\lambda p}{2\pi\varepsilon_0 r^2}$, attractive (B) $\frac{\lambda p}{2\pi\varepsilon_0 r^3}$, attractive

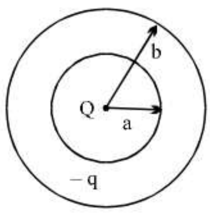
(C) $\frac{\lambda p}{2\pi\varepsilon_0 r^2}$, repulsive (D) $\frac{\lambda p}{2\pi\varepsilon_0 r^3}$, repulsive

ES0116

Conductors

62. Both question (a) and (b) refer to the system of charges as shown in the figure. A spherical shell with an inner radius 'a' and an outer radius 'b' is made of conducting material. A point charge +Q is placed at the centre of the spherical shell and a total charge – q is placed on the shell.

a. Charge – q is distributed on the surfaces as



(A) – Q on the inner surface, – q on outer surface

(B) – Q on the inner surface, – q + Q on the outer surface

(C) +Q on the inner surface, –q – Q on the outer surface

(D) The charge –q is spread uniformly between the inner and outer surface.

b. Assume that the electrostatic potential is zero at an infinite distance from the spherical shell. The electrostatic potential at a distance R (a < R < b) from the centre of the shell is (where $K = \frac{1}{4\pi\varepsilon_0}$)

(A) 0 (B) $\frac{KQ}{a}$ (C) $K\frac{Q-q}{R}$ (D) $K\frac{Q-q}{b}$

ES0117

63. The electrostatic potential on the surface of a charged conducting sphere is 100V. Two statements are made in this regard:

S_1 : At any point inside the sphere, electric intensity is zero.

S_2 : At any point inside the sphere, the electrostatic potential is 100V.

Which of the following is a correct statement?

(A) S_1 is true but S_2 is false.

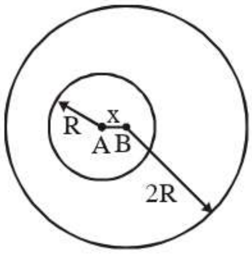
(B) Both S_1 & S_2 are false.

(C) S_1 is true, S_2 is also true and S_1 is the cause of S_2.

(D) S_1 is true, S_2 is also true but the statements are independent.

ES0118

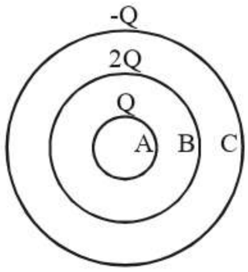
64. Figure shows two shells of radii R and 2R. The inner shell (centre at A) is nonconducting and uniformly charged wih charge Q while the outer shell (centre at B) is conducting and uncharged. the potential at the point B is :-



(A) zero (B) $\frac{KQ}{R}$ (C) $\frac{KQ}{x}$ (D) None of these

ES0119

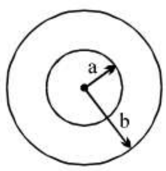
65. Charge Q, 2Q and –Q are given to three concentric conducting spherical shells A, B and C respectively. The ratio of charges on the inner and the outer surfaces of the shell 'C' will be :-



(A) $\frac{3}{4}$ (B) $-\frac{3}{4}$ (C) $\frac{3}{2}$ (D) $-\frac{3}{2}$

ES0120

66. If the electric potential of the inner metal sphere is 10 volt & that of the outer shell is 5 volt, then the potential at the centre will be :



(A) 10 volt (B) 5 volt (C) 15 volt (D) 0

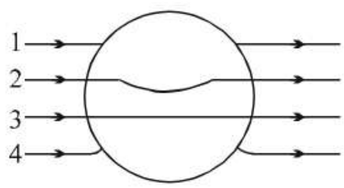
ES0121

67. n small drops of same size are charged to V volts each. If they coalesce to form a signal large drop, then its potential will be :-

(A) V/n (B) Vn (C) $Vn^{1/3}$ (D) $Vn^{2/3}$

ES0122

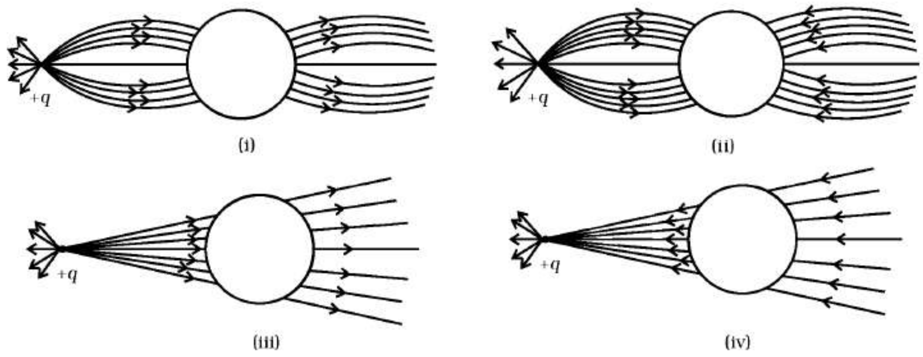
68. A metallic solid sphere is placed in a uniform electric field. The lines of force follow the path (s) shown in figure as :



(A) 1 (B) 2 (C) 3 (D) 4

ES0123

69. A point positive charge is brought near an isolated conducting sphere. The electric field is best given by



(A) Fig (i) (B) Fig (iii) (C) Fig (ii) (D) Fig (iv)

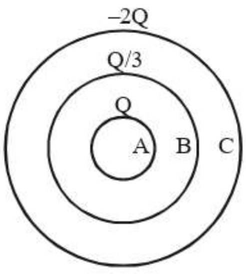
ES0124

70. There are two uncharged identical metallic spheres 1 and 2 of radius r separated by a distance d (d >> r). A charged metallic sphere of same radius having charge q is touched with one of the sphere. After some time it is moved away from the system. Now the uncharged sphere is earthed. Charge on earthed sphere is

(A) q (B) – q (C) – qr/2d (D) 0

ES0125

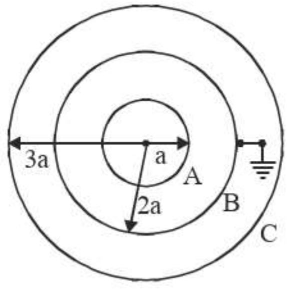
71. Three conducting concentric spherical shells of radius R, 2R and 3R have charges Q, $\frac{Q}{3}$ and – 2Q respectively. The intermediate shell is now grounded. Find the charge flow into the earth.



(A) $\frac{Q}{3}$ (B) $\frac{2Q}{3}$ (C) Q (D) 0

ES0126

72. Figure shows a system of three concentric metal shells A, B and C with radii a, 2a and 3a respectively. Shell B is earthed and shell C is given a charge Q. Now if shell C is connected to shell A, then the final charge on the shell B, is equal to :

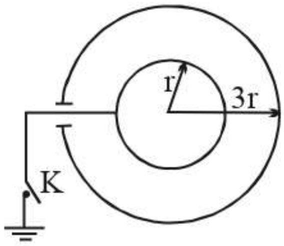


(A) $-\frac{4Q}{13}$ (B) $-\frac{8Q}{11}$

(C) $-\frac{5Q}{3}$ (D) $-\frac{3Q}{7}$

ES0127

73. Figure shows two conducting thin concentric shells of radii r and 3r. The outer shell carries charge q and inner shell is neutral. The amount of charge which flows from inner shell to the earth after the key K is closed, is equal to :-

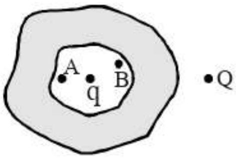


(A) –q/3 (B) q/3 (C) 3q (D) –3q

ES0128

74. **Statement-1 :** A point charge q is placed inside a cavity of conductor as shown. Another point charge Q is placed outside the conductor as shown. Now as the point charge Q is pushed away from conductor, the potential difference ($V_A - V_B$) between two points A and B within the cavity of sphere remains constant.

Statement-2 : The electric field due to charges on outer surface of conductor and outside the conductor is zero at all points inside the conductor.



(A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.

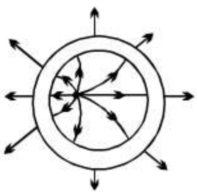
(B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.

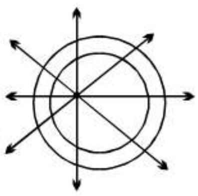
(C) Statement-1 is true, statement-2 is false.

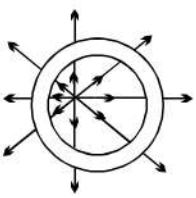
(D) Statement-1 is false, statement-2 is true.

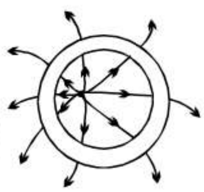
ES0129

75. A point charge *q* is placed at a point inside a hollow conducting sphere. Which of the following electric force pattern is correct ? **[IIT-JEE'2003 (scr)]**

(A) 

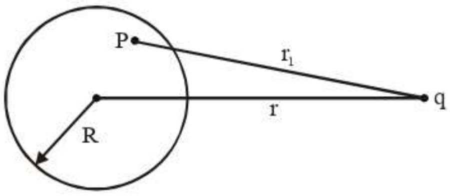
(B) 

(C) 

(D) 

ES0130

76. A point charge q is placed at a distance r from center of a conducting neutral sphere of radius R (r>R). The potential at any point P inside the sphere at a distance r_1 from point charge due to induced charge of the sphere is given by :-



(A) $\frac{Kq}{r_1}-\frac{Kq}{R}$ (B) $\frac{Kq}{r_1}-\frac{Kq}{R}$ (C) $\frac{Kq}{r}-\frac{Kq}{r_1}$ (D) $-\frac{Kq}{r_1}+\frac{Kq}{R}$

ES0131

77. Consider a conductor with a spherical cavity in it. A point charge q_0 is placed at the centre of cavity and a point charge Q is placed outside conductor.

Statement-1 : Total charge induced on cavity wall is equal and opposite to the charge inside.

Statement-2 : If cavity is surrounded by a Gaussian surface, where all parts of Gaussian surface are located inside the conductor, $\oint \vec{E}.d\vec{A}=0$; hence $q_{induced} = -q_0$

(A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.

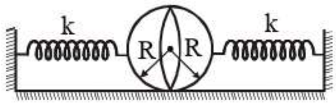
(B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.

(C) Statement-1 is true, statement-2 is false.

(D) Statement-1 is false, statement-2 is true.

ES0132

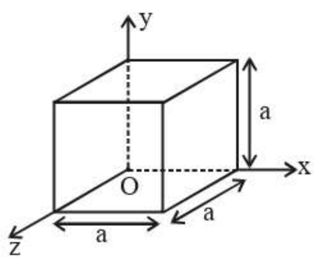
78. Two non-conducting hemispherical surfaces, which are having uniform charge density σ are placed on smooth horizontal surface as shown in figure. Assuming springs are ideal, calculate compression in each spring if both the hemispherical surface are just touching each other.



(A) $\frac{\sigma^2 R^2}{2\varepsilon_0 k}$ (B) R (C) $\frac{\sigma^2 \pi R^2}{2\varepsilon_0 k}$ (D) None of these

ES0133

79. Electric field in a region is found to be $E = 3y\hat{j}$. The total energy stored in electric field inside the cube shown will be



(A) $9a^5 \in_0$ (B) $3 \in_0 a^5$

(C) $\frac{3}{2} \in_0 a^5$ (D) 0

ES0134

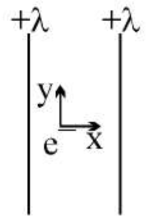
MULTIPLE CORRECT TYPE QUESTIONS

80. If a body is charged by rubbing it with another body then its weight :-

(A) may increase slightly
(B) may decrease slightly
(C) must increase slightly
(D) remains precisely constant

ES0135

81. An electron is placed just in the middle between two long fixed line charges of charge density $+\lambda$ each. The wires are in the xy plane (Do not consider gravity)



(A) The equilibrium of the electron will be unstable along x-direction
(B) The equilibrium of the electron will be neutral along y-direction
(C) The equilibrium of the electron will be stable along z-direction
(D) The equilibrium of the electron will be stable along y-direction

ES0136

82. Which statement(s) concerning electrostatic fields is/are **CORRECT**?

(A) Electric field lines never cross each other.
(B) Positive charge experiences force in the direction of electric field line.
(C) Electric field lines always start on negative charges and end on positive charges.
(D) Electric field lines that are closer indicate a stronger electric field while electric field lines that are far apart indicate a weaker electric field.

ES0137

83. Two point charges Q and $-\frac{Q}{4}$ are separated by distance L then

(A) Potential is zero at a point on the axis which is at a distance L/3 on the right side of charge $-\frac{Q}{4}$

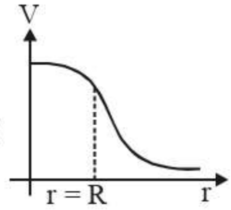
(B) Potential is zero at a point on the axis which is at a distance L/5 on the left side of charge $-\frac{Q}{4}$

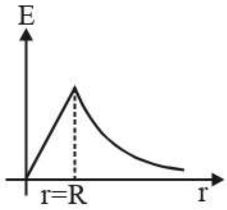
(C) Electric field is zero at a point on the axis which is at a distance L on the right side of charge $-\frac{Q}{4}$

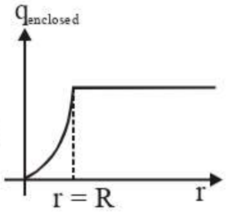
(D) There exist two points on the axis, where electric field is zero

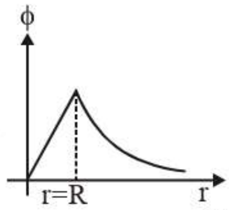
ES0138

84. Graph shows the variation of potential (V), magnitude of electric field (E), charge enclosed ($q_{enclosed}$) within the concentric sphere and net flux (ϕ) through a concentric spherical Gaussian surface as a function of distance (r) from centre of a uniformly positive charged solid sphere of radius R. Choose the **CORRECT** option(s):-

(A) 

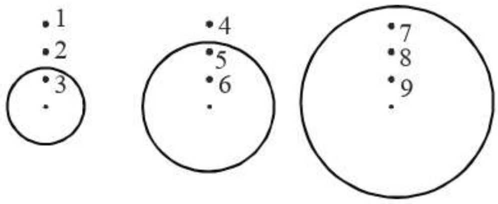
(B) 

(C) 

(D) 

ES0139

85. Figure shows three spherical shells in separate situations, with each shell having the same uniform positive net charge. Points 1, 4 and 7 are at the same radial distances from the centre of the their respective shells; so are points 2, 5 and 8 ; and so are points 3, 6 and 9. With the electric potential taken equals to zero at an infinite distance, choose correct statement.



(A) Point 3 has highest potential
(B) point 1, 4 and 7 are at same potential
(C) Point 9 has lowest potential
(D) point 5 and 8 are at same potential

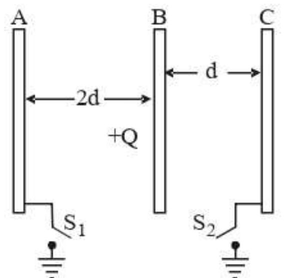
ES0140

86. Which of the following represent(s) an electrostatic field :-

(A) $\vec{E} = y\hat{i} + x\hat{j}$
(B) $\vec{E} = y\hat{i}$
(C) $\vec{E} = y\hat{i} + x\hat{j} + z\hat{k}$
(D) $\vec{E} = \alpha\vec{r}$ (α is constant)

ES0141

87. Three identical, parallel conducting plates A, B and C are placed as shown. Switches S_1 and S_2 are open, and can connect A and C to earth when closed. +Q charge is given to B.



(A) If S_1 is closed with S_2 open, a charge of amount Q will pass through S_1

(B) If S_2 is closed with S_1 open, a charge of amount Q will pass through S_2

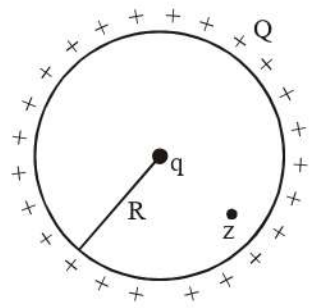
(C) If S_1 and S_2 are closed together, a charge of amount Q/3 will pass through S_1, and a charge of amount 2Q/3 will pass through S_2.

(D) All the above statements are incorrect

ES0142

node06\B0B0-BA\Kota\JEE(Advanced)\Enthuse\Physics\Sheet\Electrostatics\Eng\02_O-1 & O-2.p65

88. A positive charge Q is uniformly distributed along a circular ring of radius R. A small test charge q is placed at the centre of the ring. Then



(A) If $q > 0$ and is displaced away from the centre in the plane of the ring, it will be pushed back towards the centre.

(B) If $q < 0$ and is displaced away from the centre in the plane of the ring, it will never return to the centre and will continue moving till it hits the ring.

(C) If $q < 0$, it will perform SHM for small displacement along the axis.

(D) q at the centre of the ring is in an unstable equilibrium within the plane of the ring for $q > 0$.

ES0143

89. If there were only one type of charge in the universe, then

(A) $\oint_s E.dS \neq 0$ on any surface.

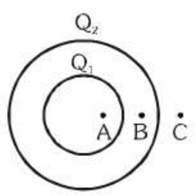
(B) $\oint_s E.dS = 0$ if the charge is outside the surface.

(C) $\oint_s E.dS$ could not be defined.

(D) $\oint_s E.dS = \frac{q}{\varepsilon_0}$ if charges of magnitude q were inside the surface.

ES0144

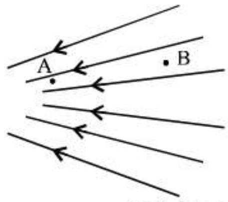
90. Figure shows two uniform charged concentric spherical shell. Both charges are positive, Select correct statement



(A) Electric field intensity at B may be greater than electric field intensity at C.
(B) Electric field intensity at B must be greater than electric field intensity at C.
(C) Potential at A greater than potential at B
(D) If a charge moves from B to C work done by electric force must be positive.

ES0145

91. Which of the following is true for the figure showing electric lines of force? (E is electrical field, V is potential)



(A) $E_A > E_B$ (B) $E_B > E_A$ (C) $V_A > V_B$ (D) $V_B > V_A$

ES0146

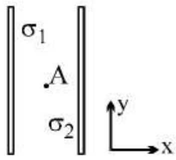
92. Consider a uniform electric field in the $\hat{z}$ direction. The potential is a constant

(A) in all space. (B) for any x for a given z.

(C) for any y for a given z. (D) on the x-y plane for a given z.

ES0147

93. Two large conducting sheets are kept parallel to each other as shown. In equilibrium, the charge density on facing surfaces is σ_1 and σ_2. What is the value of electric field at A.



(A) $\frac{\sigma_1}{\varepsilon_0}\hat{i}$ (B) $-\frac{\sigma_2}{\varepsilon_0}\hat{i}$ (C) $\frac{\sigma_1+\sigma_2}{2\varepsilon_0}\hat{i}$ (D) $\frac{\sigma_1-\sigma_2}{2\varepsilon_0}\hat{i}$

ES0148

94. A hollow closed conductor of irregular shape is given some charge. Which of the following statements are correct ?

(A) The entire charge will appear on its outer surface.

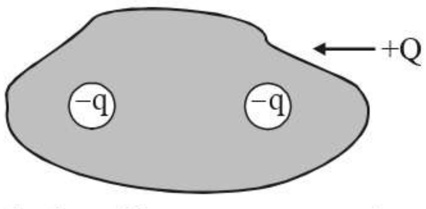
(B) All points on the conductor will have the same potential.

(C) All points on its surface will have the same charge density.

(D) All points just outside it will have the same electric intensity.

ES0149

95. A conducting body is given charge Q and charge –q has been placed in each of the cavity, which of the following statements is/are true?



(A)If Q = 2q, then conducting body will be at zero potential.

(B)If an external electric field is applied then the charge distribution on the outer surface of conductor would change.

(C)The potential of any point inside the cavity is less than that of conducting body.

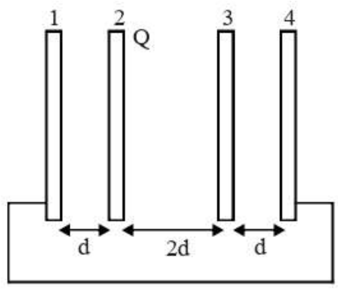
(D)None of these

ES0150

COMPREHENSION TYPE QUESTIONS

Paragraph for Question No. 96 to 98

Four metallic plates are placed as shown in the figure. Plate 2 is given a charge Q whereas all other plates are uncharged. Plates 1 and 4 are joined together. The area of each plate is same.



96. The charge appearing on the right side of plate 3 is

(A) 0 (B) +Q/4 (C) –3Q/4 (D) Q/2

ES0151

97. The charge appearing on right side of plate 4 is

(A) 0 (B) –Q/4 (C) –3Q/4 (D) +Q/2

ES0151

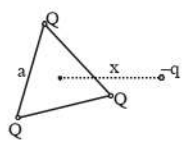
98. The potential difference between plates 1 and 2 is

(A) $\frac{3}{2}\frac{Qd}{\varepsilon_0 A}$ (B) $\frac{Qd}{\varepsilon_0 A}$ (C) $\frac{3}{4}\frac{Qd}{\varepsilon_0 A}$ (D) $\frac{3Qd}{\varepsilon_0 A}$

ES0151

Paragraph for Questions No. 99 to 101

Three charged particles each of +Q are fixed at the corners of an equilateral triangle of side 'a'. A fourth particle of charge –q and mass m is placed at a point on the line passing through centroid of triangle and perpendicular to the plane of triangle at a distance x from the centre of triangle.



99. Magnitude of resultant force on the fourth charged particle is

(A) $\frac{1}{4\pi\epsilon_0}\frac{9\sqrt{3}\,Qqx}{(3x^2+a^2)^{3/2}}$ (B) $\frac{1}{4\pi\epsilon_0}\frac{27\sqrt{3}\,Qqx}{(3x^2+a^2)^{3/2}}$

(C) $\frac{1}{4\pi\epsilon_0}\frac{2\sqrt{2}\,Qqx}{(2x^2+a^2)^{3/2}}$ (D) $\frac{1}{4\pi\epsilon_0}\frac{4\sqrt{2}\,Qqx}{(2x^2+a^2)^{3/2}}$

ES0152

100. Value of x for which the force is maximum is

(A) $\frac{a}{\sqrt{3}}$ (B) $\frac{a}{\sqrt{2}}$ (C) $\frac{a}{\sqrt{6}}$ (D) $\frac{a}{\sqrt{5}}$

ES0152

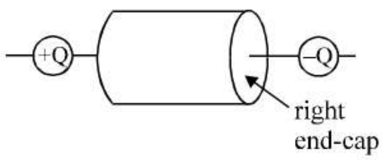
101. For small oscillation the period of oscillation of fourth particle is

(A) $2\pi\sqrt{\frac{4\pi \in_0 ma^3}{9\sqrt{3}Qq}}$ (B) $\pi\sqrt{\frac{4\pi \in_0 ma^3}{9\sqrt{3}\,Qq}}$ (C) $2\pi\sqrt{\frac{2\pi \in_0 ma^3}{27\sqrt{3}\,Qq}}$ (D) $2\pi\sqrt{\frac{\pi \in_0 ma^3}{27\sqrt{3}\,Qq}}$

ES0152

Paragraph for Question No. 102 and 103

The figure applies to the following two questions. Positive and negative charges of equal magnitude lie along the symmetry axis of a cylinder. The distance from the positive charge to the left end-cap of the cylinder is the same as the distance from the negative charge to the right end -cap.



102. What is the flux of the electric field through the closed cylinder ?

(A) 0 (B) + Q / ε_0 (C) + 2Q / ε_0 (D) – Q / ε_0

ES0153

103. What is the sign of the flux through the right end-cap of the cylinder ?

(A) Positive

(B) Negative

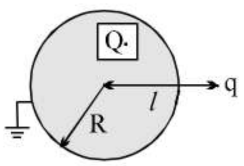
(C) There is no flux through the right end-cap.

(D) None of these

ES0153

Paragraph for Question No. 104 to 106

There is a cubical cavity inside a conducting sphere of radius R. A positive point charge Q is placed at the centre of the cube and another positive charge q is placed at a distance l (>R) from the centre of the sphere. The sphere is earthed



104. Charge induced on the inner surface of cavity is

(A) –Q, uniformly distributed (B) –Q, non-uniformly distributed

(C) –(Q+q) non-uniformly distributed (D) none

ES0154

105. Net charge on the outer surface of conducting sphere is

(A) +Q (B) Q – qR/l

(C) –qR/l (D) none

ES0154

106. Potential at a point inside the cavity is

(A) zero (B) positive

(C) negative (D) can not be determined.

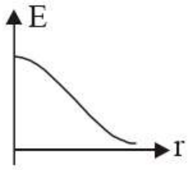
ES0154

MATRIX MATCH TYPE QUESTION

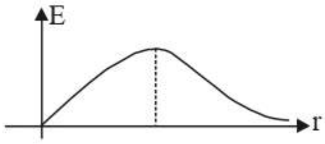
107. Column II corresponds to the graph of magnitude of electric field versus distance from centre of charge distribution in Column I.

Column-I **Column-II**

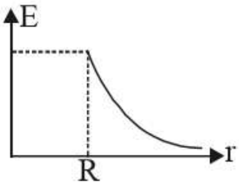
(A) Ring along its axis

(P) 

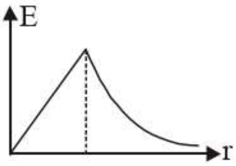
(B) Uniformly charged solid sphere

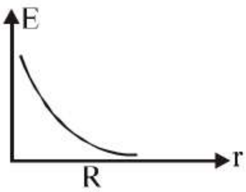
(Q) 

(C) Uniformly charged spherical shell

(R) 

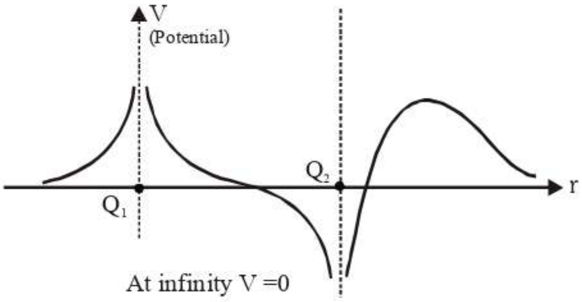
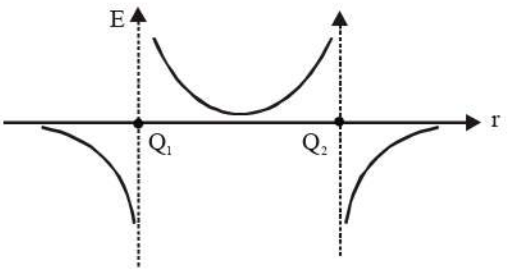
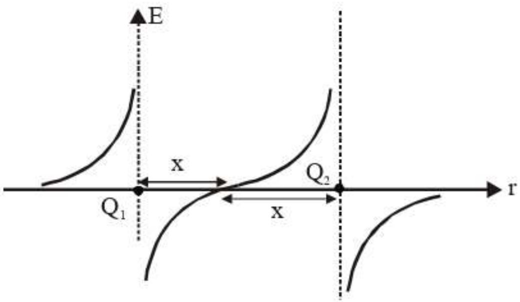
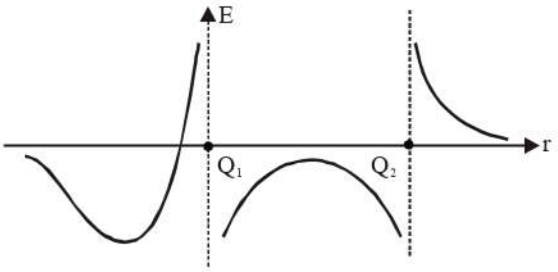
(D) Combination of charge +Q and –Q at the perpendicular bisector

(S) 

(T) 

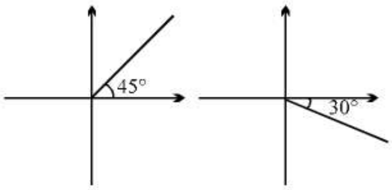
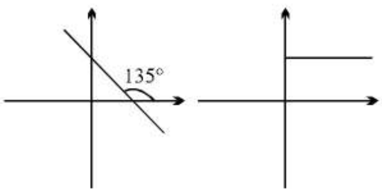
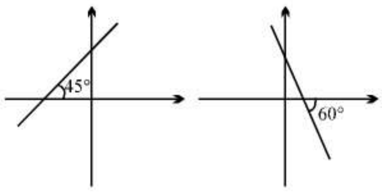
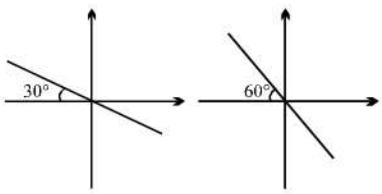
ES0155

108. As shown in column I their are graphs of electric field (E) and potential (V) along the line joining charges Q_1 and Q_2 are drawn against distance (r) on x–axis for charges Q_1 and Q_2. Take potential at infinity equal to zero. [Take direction of E in righward direction as positive]

Column-I	**Column-II**
(A) 	(P) $Q_1 < 0, Q_2 > 0$
(B) 	(Q) $Q_1 > 0, Q_2 < 0$
(C) 	(R) $\lvert Q_1\rvert > \lvert Q_2\rvert$
(D) 	(S) $Q_1 < 0, Q_2 < 0$
	(T) $\lvert Q_1\rvert = \lvert Q_2\rvert$

ES0156

109. Column I shows graphs of electric potential V versus x and y in a certain region for four situations. Column II shows the range of angle which the electric field vector makes with positive x-direction.

Column I		**Column II**
	V–x, V–y	**(Range of angle)**
(A)		(P) $0 \leq \theta < 45°$
(B)		(Q) $45° \leq \theta < 90°$
(C)		(R) $90° \leq \theta < 135°$
(D)		(S) $135° \leq \theta \leq 180°$

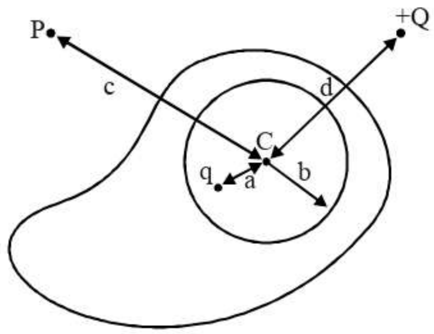
ES0157

110. A spherical metallic conductor has a spherical cavity. A positive charge is placed inside the cavity at its centre. Another positive charge is placed outside it. The conductor is initially electrically neutral.

Column I	**Column II**
(Cause)	**(Effect)**
(A) If outside charge is shifted to other position	(P) distribution of charge on inner surface of cavity changes
(B) If inside charge is shifted to other position within cavity	(Q) distribution of charge on outer surface of of conductor changes
(C) If magnitude of charge inside cavity is increased	(R) electric potential at centre of conductor due to charges present on outer surface of conductor changes
(D) If conductor is earthed	(S) force on the charge placed inside cavity changes

ES0158

111. In the shown figure the conductor is uncharged and a charge q is placed inside a spherical cavity at a distance a from its centre (C). Point P and charge $+Q$ are as shown. a, b, c, d are known.



	Column-I		Column-II
(A)	Electric field due to induced charges on the inner surface of cavity at point P	(P)	zero
(B)	Electric potential due to charges on the inner surface of cavity and q at P	(Q)	non-zero
(C)	Electric field due to induced charges on the outer surface of conductor and Q at C	(R)	value can be stated with the given data.
(D)	Electric potential due to induced charges on the inner surface of cavity at C	(S)	value cannot be stated from the given data

ES0159

EXERCISE (O-2)

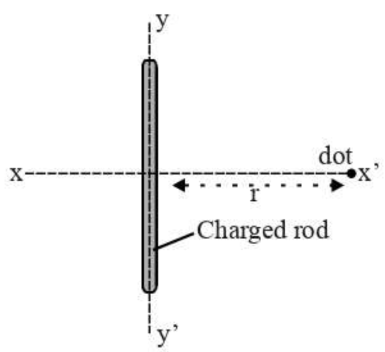
SINGLE CORRECT TYPE QUESTIONS

1. A square of side b centred at the origin with sides parallel to axes of x and y has surface charge density σ (x, y) = $\sigma_0 xy$ within its boundaries. Total charge on the square is

(A) 0 (B) $\sigma_0 b^2$ (C) $2\sigma_0 b^2$ (D) $4\sigma_0 b^2$

ES0160

2. A uniformly charged rod is kept on y-axis with centre at origin, as shown. Which of the following actions will increase the electric field strength at the position of the dot ?



(A) make the rod longer without changing the charge

(B) make the rod shorter without changing the charge

(C) make the rod shorter without changing the linear charge density

(D) rotate the rod about yy'

ES0161

3. A charged particle having some mass is resting in equilibrium at a height H above the centre of a uniformly charged non-conducting horizontal ring of radius R. The force of gravity acts downwards. The equilibrium of the particle will be stable

(A) for all values of H (B) only if $H > \frac{R}{\sqrt{2}}$ (C) only if $H < \frac{R}{\sqrt{2}}$ (D) only if $H = \frac{R}{\sqrt{2}}$

ES0162

4. **Statement-1 :** A positive point charge initially at rest in a uniform electric field starts moving along electric lines of forces. (Neglect all other forces except electric forces)

Statement-2 : Electric lines of force represents path of charged particle which is released from rest in it.

(A) Statement-1 is true, statement-2 is true and statement-2 is correct explanation for statement-1.

(B) Statement-1 is true, statement-2 is true and statement-2 is NOT the correct explanation for statement-1.

(C) Statement-1 is true, statement-2 is false.

(D) Statement-1 is false, statement-2 is true.

ES0163

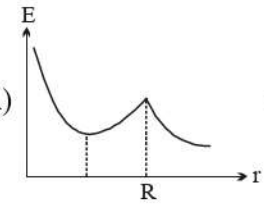
node06\B0B0-BA\Kota\JEE(Advanced)\Enthuse\Physics\Sheet\Electrostatics\Eng\02_O-1 &O-2.p65

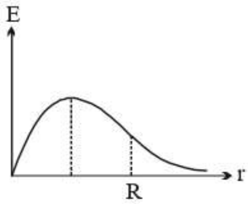
5. A system consists of uniformly charged sphere of radius R and a surrounding medium filled by a charge with the volume density $\rho = \frac{\alpha}{r}$, where α is a positive constant and r is the distance from the centre of the sphere. The charge of the sphere for which electric field intensity E outside the sphere is independent of r is

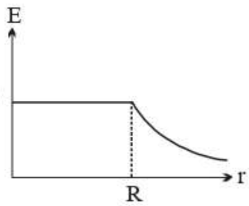
(A) $\frac{\alpha}{2 \in_0}$ (B) $\frac{2}{\alpha \in_0}$ (C) $2\pi\alpha R^2$ (D) αR^2

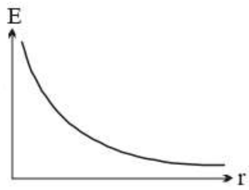
ES0164

6. A spherical insulator of radius R is charged uniformly with a charge Q throughout its volume and contains a point charge $\frac{Q}{16}$ located at its centre. Which of the following graphs best represent qualitatively, the variation of electric field intensity E with distance r from the centre.

(A) 

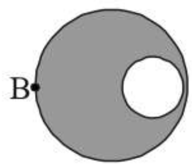
(B) 

(C) 

(D) 

ES0165

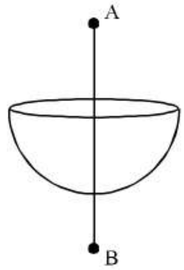
7. A positively charged sphere of radius r_0 carries a volume charge density ρ_E (Figure). A spherical cavity of radius $r_0/2$ is then scooped out and left empty, as shown. What is the direction and magnitude of the electric field at point B ?



(A) $\frac{17\rho r_0}{54 \in_0}$ left (B) $\frac{\rho r_0}{6 \in_0}$ left (C) $\frac{17\rho r_0}{54 \in_0}$ right (D) $\frac{\rho r_0}{6 \in_0}$ right

ES0166

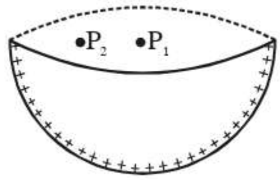
8. The diagram shows a uniformly charged hemisphere of radius R. It has volume charge density ρ. If the electric field at a point 2R distance above its center is E then what is the electric field at the point which is 2R below its center?



(A) $\rho R/6\varepsilon_0 + E$ (B) $\rho R/12\varepsilon_0 - E$ (C) $-\rho R/6\varepsilon_0 + E$ (D) $\rho R/24\varepsilon_0 + E$

ES0167

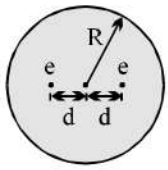
9. Consider a uniformly charged hemispherical shell shown below. Indicate the directions (not magnitude) of the electric field at the central point P_1 and an off-centre point P_2 on the drumhead of the shell.



(A) $\uparrow$; $\nwarrow$ (B) $\uparrow$; $\nearrow$ (C) $\uparrow$; $\uparrow$ (D) $\uparrow$; $\leftarrow$

ES0168

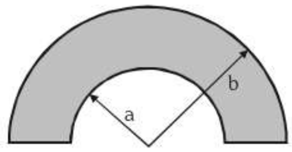
10. Using thomson's model of the atom, consider an atom consisting of two electrons, each of charge –e, embeded in a sphere of charge + 2e and radius R. In equilibrium each electron is at distance d from the centre of the atom. What is equilibrium separation between electrons?



(A) R (B) R/2 (C) R/3 (D) R/4

ES0169

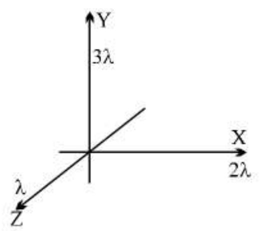
11. A non conducting semicircular disc (as shown in figure) has a uniform surface charge density σ. The electric potential at the centre of the disc :-



(A) $\frac{\sigma}{2\pi\epsilon_0}\frac{\ell n(b/a)}{(b-a)}$ (B) $\frac{\sigma(b-a)}{2\epsilon_0}$ (C) $\frac{\sigma(b-a)}{4\epsilon_0}$ (D) $\frac{\sigma(b-a)}{4\pi\epsilon_0}$

ES0170

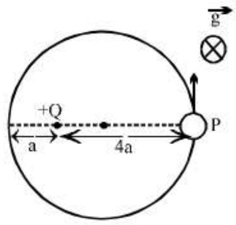
12. The diagram shows three infinitely long uniform line charges placed on the X, Y and Z axis. The work done in moving a unit positive charge from (1, 1, 1) to (0, 1, 1) is equal to



(A) $(\lambda \ln 2) / 2\pi\varepsilon_0$ (B) $(\lambda \ln 2) / \pi\varepsilon_0$ (C) $(3\lambda \ln 2) / 2\pi\varepsilon_0$ (D) None

ES0171

13. The diagram shows a small bead of mass m carrying charge q. The bead can freely move on the smooth fixed ring placed on a smooth horizontal plane. In the same plane a charge +Q has also been fixed as shown. The potential at the point P due to +Q is V. The velocity with which the bead should projected from the point P so that it can complete a circle should be greater than



(A) $\sqrt{\frac{6qV}{m}}$ (B) $\sqrt{\frac{qV}{m}}$ (C) $\sqrt{\frac{3qV}{m}}$ (D) none

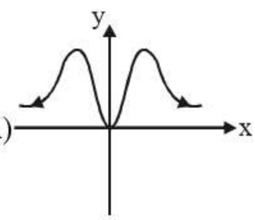
ES0172

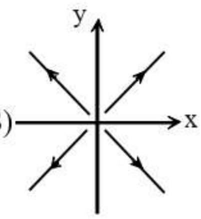
14. A charged particle of charge Q is held fixed and another charged particle of mass m and charge q (of the same sign) is released from a distance r. The impulse of the force exerted by the external agent on the fixed charge by the time distance between Q and q becomes 2r is

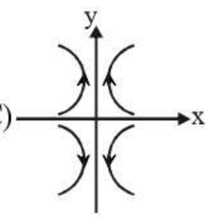
(A) $\sqrt{\frac{Qq}{4\pi\epsilon_0 mr}}$ (B) $\sqrt{\frac{Qqm}{4\pi\epsilon_0 r}}$ (C) $\sqrt{\frac{Qqm}{\pi\epsilon_0 r}}$ (D) $\sqrt{\frac{Qqm}{2\pi\epsilon_0 r}}$

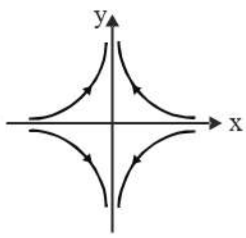
ES0173

15. In a certain region of space, the potential field depends on x and y coordinates as $V = (x^2 - y^2)$. The corresponding electric field lines in x-y plane are correctly represented by :

(A) 

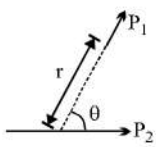
(B) 

(C) 

(D) 

ES0174

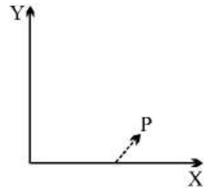
16. Two short electric dipoles are placed as shown. The energy of electric interaction between these dipoles will be :-



(A) $\frac{2kP_1P_2\cos\theta}{r^3}$ (B) $\frac{-2kP_1P_2\cos\theta}{r^3}$ (C) $\frac{-2kP_1P_2\sin\theta}{r^3}$ (D) $\frac{-4kP_1P_2\cos\theta}{r^3}$

ES0175

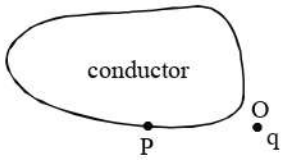
17. A small electric dipole $\vec{P}$ is placed on the X axis at the point (1, 0). The dipole vector forms an angle of 30° with the X axis. Consider a non uniform electric field to have been applied in the region given by the vector $\vec{E} = x^2\hat{i} + y^2\hat{j}$. What is the force acting on the dipole?



(A) $2\vec{P}\cos 30° (\hat{i}+2\hat{j})$ (B) $2\vec{P}\cos 30° (\hat{i})$ (C) $2\vec{P}\cos 30° (2\hat{j})$ (D) None

ES0176

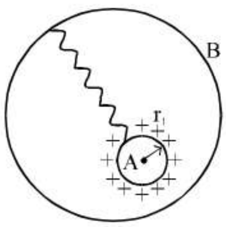
18. The density of charge at P on the conductor is σ. The resultant electric field near P will [$\hat{n}$ = unit normal vector at point P. $\vec{r}$ = vector along OP] where K = 1/4 πε



(A) $\left(\frac{\sigma}{\epsilon_0}\right)\hat{n}+\left(\frac{Kq\vec{r}}{r^3}\right)$ (B) $\left(\frac{\sigma}{2\epsilon_0}\right)\hat{n}+\left(\frac{Kq\vec{r}}{r^3}\right)$ (C) $\left(\frac{\sigma}{\epsilon_0}\right)\hat{n}$ (D) $\left(\frac{\sigma}{2\epsilon_0}\right)\hat{n}$

ES0177

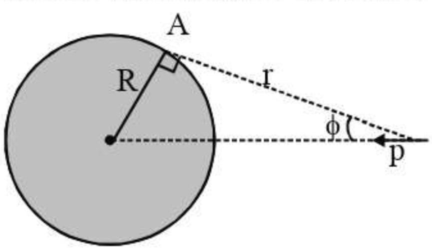
19. A metal sphere A of radius r_1 charged to a potential ϕ_1 is enveloped by a thin walled conducting spherical shell B of radius r_2. Then ϕ_2 of the sphere A after it is connected by a thin wire to the shell B will be :-



(A) $\phi_1 \frac{r_1}{r_2}$ (B) $\phi_1\left(\frac{r_2}{r_1}\right)$ (C) $\phi_1\left(1-\frac{r_1}{r_2}\right)$ (D) $\phi_1\left(\frac{r_1 r_2}{r_1+r_2}\right)$

ES0178

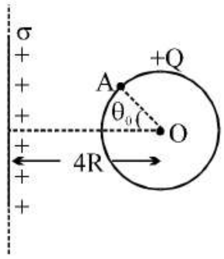
20. A dipole having dipole moment p is placed in front of a solid uncharged conducting sphere as shown in the diagram. The net potential at point A lying on the surface of the sphere is :-



(A) $\frac{kp\cos\phi}{r^2}$ (B) $\frac{kp\cos^2\phi}{r^2}$ (C) 0 (D) $\frac{2kp\cos^2\phi}{r^2}$

ES0179

21. A conducting sphere of radius R and charge Q is placed near a uniformly charged nonconducting infinitely large thin plate having surface charge density σ. Then find the potential at point A (on the surface of sphere) due to charge on sphere (here $K = \frac{1}{4\pi \epsilon_0}$, $\theta_0 = \frac{\pi}{3}$)



(A) $K\frac{Q}{R} - \frac{\sigma}{4 \epsilon_0}R$ (B) $K\frac{Q}{R} - \frac{\sigma R}{\epsilon_0}$ (C) $K\frac{Q}{R}$ (D) none of these

ES0180

22. The intensity of an electric field depends only on the coordinates x, y and z as follows :

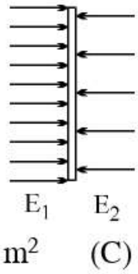
$$\vec{E} = a\frac{\left(x\hat{i} + y\hat{j} + z\hat{k}\right)}{\left(x^2 + y^2 + z^2\right)^{3/2}} \text{ unit}$$

The electrostatic energy stored between two imaginary concentric spherical shells of radii R and 2R with centre at origin is :-

(A) $\frac{4\pi\varepsilon_0 a^2}{R}$ (B) $\frac{2\pi\varepsilon_0 a^2}{R}$ (C) $\frac{\pi\varepsilon_0 a^2}{R}$ (D) $\frac{\pi\varepsilon_0 a^2}{2R}$

ES0181

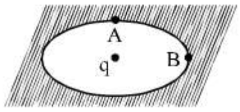
23. A charged large metal sheet is placed into uniform electric field, perpendicularly to the electric field lines. After placing the sheet into the field, the electric field on the left side of the sheet is $E_1 = 5 \times 10^5$ V/m and on the right it is $E_2 = 3 \times 10^5$ V/m. The sheet experiences a net electric force of 0.08 N. Find the area of one face of the sheet. Assume external field to remain constant after introducing the large sheet. Use $\left(\frac{1}{4\pi\varepsilon_0}\right) = 9 \times 10^9$ Nm^2/C^2



(A) $3.6\,\pi \times 10^{-2}$ m^2 (B) $0.9\,\pi \times 10^{-2}$ m^2 (C) $1.8\,\pi \times 10^{-2}$ m^2 (D) none

ES0182

24. An ellipsoidal cavity is carved within a perfect conductor. A positive charge q is placed at the center of the cavity. The points A & B are on the cavity surface as shown in the figure. Then :

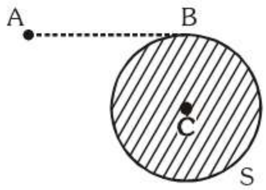


(A) electric field near A in the cavity = electric field near B in the cavity
(B) charge density at A = charge density at B
(C) potential at A = potential at B
(D) total electric field flux through the surface of the cavity is q/ε_0.

ES0183

MULTIPLE CORRECT TYPE QUESTIONS

25. S is a solid neutral conducting sphere. A point charge q of 1×10^{-6}C is placed at point A. C is the centre of sphere and AB is a tangent. BC = 3m and AB = 4m.



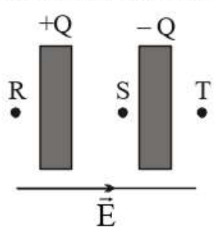
(A) The electric potential of the conductor is 1.8 kV.
(B) The electric potential of the conductor is 2.25 kV.
(C) The electric potential at B due to induced charges on the sphere is –0.45 kV.
(D) The electric potential at B due to induced charges on the sphere is 0.45 kV.

ES0184

26. Four identical particles each having mass m and charge q are placed at the vertices of a square of side ℓ. All the particles are free to move without any friction and released simultaneously from rest. Then
(A) At all instants, the particles remains at vertices of square whose edge length is changing
(B) The configuration is changing (not remaining square) as the time passes
(C) The speed of the particles when one of the particles get displaced by $\frac{\ell}{\sqrt{2}}$ is $\sqrt{\frac{q^2}{8\pi\varepsilon_0 m\ell}\left(2+\frac{1}{\sqrt{2}}\right)}$
(D) Speed of the particles can not be found

ES0185

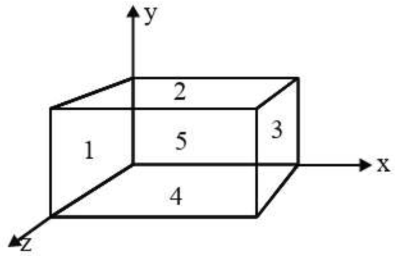
27. Two large thin conducting plates with small gap in between are placed in a uniform electric field E (perpendicular to the plates). Area of each plate is A and charges $+Q$ and $-Q$ are given to these plates as shown in the figure. If points R,S and T as shown in the figure are three points in space, then the



(A) field at point R is E
(B) field at point S is E
(C) field at point T is $\left(E+\frac{Q}{\varepsilon_o A}\right)$
(D) field at point S is $\left(E+\frac{Q}{A\varepsilon_o}\right)$

ES0186

28. In a region of space, the electric field $\vec{E} = E_0 x\hat{i} + E_0 y\hat{j}$. Consider an imaginary cubical volume of edge 'a' with its edges parallel to the axes of coordinates. Now,



(A) the total electric flux through the faces 1 and 3 is E_0a^3

(B) the charge inside the cubical volume is $2\varepsilon_0E_0a^3$

(C) the total electric flux through the faces 2 and 4 is $2E_0a^3$

(D) the charge inside the cubical volume is $\varepsilon_0E_0a^3$

ES0187

29. Equipotential surfaces :-

(A) are closer in regions of large electric fields compared to regions of lower electric fields.

(B) will be more crowded near sharp edges of a conductor.

(C) will be more crowded near regions of large charge densities.

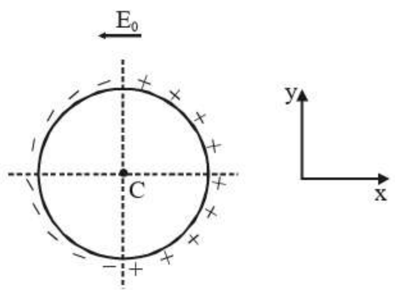
(D) will always be equally spaced.

ES0188

COMPREHENSION TYPE QUESTIONS

Paragraph for Question No. 30 and 31

A uniform ring of mass m and radius R can rotate freely about an axis passing through centre C and perpendicular to plane of paper. Half of ring is positively charge and other half is negatively charge. Uniform electric field E_0 is switched on along –ve x-axis (axis are shown in figure) [Magnitude of charge density λ]



30. The dipole moment of ring is :-

(A) $2\lambda R^2$ (B) $4\lambda R^2$ (C) $2\pi\lambda R^2$ (D) $4\pi\lambda R^2$

ES0189

31. If ring is slightly disturb from given position, find the angular speed of ring when it rotate by $\pi/2$.

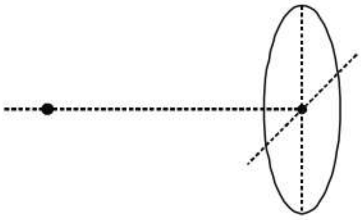
(A) $2\sqrt{\dfrac{\lambda E_0}{m}}$ (B) $\sqrt{\dfrac{\lambda E_0}{m}}$ (C) $\sqrt{\dfrac{8\lambda E_0}{m}}$ (D) None

ES0189

MATCHING LIST TYPE (4 × 4 × 4) SINGLE OPTION CORRECT (THREE COLUMNS AND FOUR ROWS)

Answer Q.32, 33 & 34 by appropriately matching the information given in the three columns of the following table.

Consider a non conducting ring of radius r and mass m and a particle of same mass, both at rest in free space. The particle is on the axis of the ring and far away from the ring. An amount Q of positive charge is uniformly distributed on the ring and the particle is given a positive charge q. The particle is imparted a velocity v towards the centre of the ring. Consider the consequences given in the columns and answer the following questions.



	Column 1		**Column 2**		**Column 3**
(I)	Maximum speed of the ring is v	(i)	Minimum speed of the particle is v/2	(P)	Final speed of the ring and particle is v and zero respectively.
(II)	Maximum speed of the ring is v/2	(ii)	Minimum speed of the particle is zero	(Q)	Final speed of the ring and particle is zero and v respectively.
(III)	Maximum speed of the ring is $\frac{v}{2}\left[1+\sqrt{1-\frac{Qq}{\pi\varepsilon_0 mrv^2}}\right]$	(iii)	Minimum speed of the particle is $\frac{v}{2}\left[1+\sqrt{1-\frac{Qq}{\pi\varepsilon_0 mrv^2}}\right]$	(R)	Final speed of the ring and particle is v/4 and 3v/4 respectively.
(IV)	Maximum speed of the ring is $\frac{v}{2}\left[1-\sqrt{1-\frac{Qq}{\pi\varepsilon_0 mrv^2}}\right]$	(iv)	Minimum speed of the particle is $\frac{v}{2}\left[1-\sqrt{1-\frac{Qq}{\pi\varepsilon_0 mrv^2}}\right]$	(S)	Final speed of the ring and particle is v/2 for both.

32. Which of following options is the correct representation if $v=\sqrt{\frac{Qq}{2\pi\varepsilon_0 mr}}$

(A) (II) (i) S (B) (I) (ii) P (C) (III) (iv) R (D) (IV) (iii) Q

ES0190

33. Which of following options is the correct representation if $v=\sqrt{\frac{Qq}{\pi\varepsilon_0 mr}}$

(A) (II) (i) S (B) (I) (ii) P (C) (III) (iv) R (D) (IV) (iii) Q

ES0190

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34. Which of following options is the correct representation if $v = \sqrt{\dfrac{2Qq}{\pi\varepsilon_0 mr}}$

(A) (II) (i) S (B) (I) (ii) P (C) (III) (iv) Q (D) (IV) (iii) (Q)

ES0190

MATRIX MATCH TYPE QUESTION

35. Column-II shows some charge distributions and column-I has some statements about electric field at four points A, B, C, D. Match column-I with column-II.

Column-I

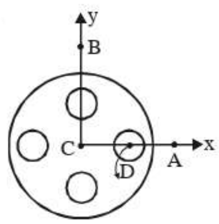
(A) $\vec{E}_A$ has x component only

(B) $\vec{E}_B$ has y component only

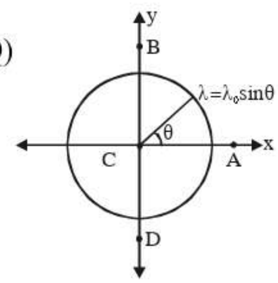
(C) $\vec{E}_C$ has y component only

(D) $|\vec{E}_D|$ is zero

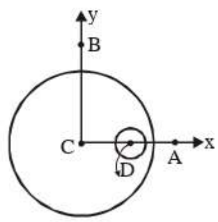
Column-II

(P) 

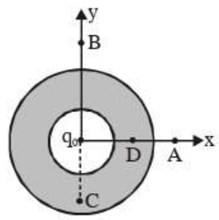
A solid non conducting sphere of radius R of volumetric charge density ρ with four symmetrical spherical cavities. All the five sphere's centre lie in same plane.

(Q) 

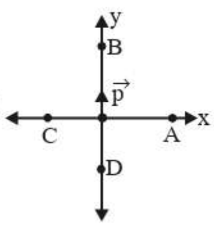
A very small circular filament lying in xy-plane. All points lie in same plane. A, B and D are at large distance compared to radius of circle.

(R) 

A charged spherical conductor with an empty cavity in it.

(S) 

A hollow thick spherical neutral conductor with a concentric cavity. Charge q_0 is placed inside at centre of cavity.

(T) 

A small electric dipole $\vec{p}$ is placed at origin. A, B, C and D are four points at large distance from origin.

ES0191

EXERCISE-JM

1. Two identical charged spheres suspended from a common point by two massless string of length ℓ are initially a distance $d(d << \ell)$ apart because of their mutual repulsion. The charge begins to leak from both the spheres at a constant rate. As a result the charges approach each other with a velocity v. Then as a function of distance x between them :- **[AIEEE - 2011]**

(1) $v \propto x^{1/2}$ (2) $v \propto x$ (3) $v \propto x^{-1/2}$ (4) $v \propto x^{-1}$

ES0192

2. The electrostatic potential inside a charged spherical ball is given by $\phi = ar^2 + b$ where r is the distance from the centre; a, b are constant. Then the charge density inside the ball is :-

[AIEEE - 2011]

(1) $-24\pi a\epsilon_0$ (2) $-6 a\epsilon_0$ (3) $-24\pi a\epsilon_0 r$ (4) $-6 a\epsilon_0 r$

ES0193

3. Two positive charges of magnitude 'q' are placed at the ends of a side (side 1) of a square of side '2a'. Two negative charges of the same magnitude are kept at the other corners. Starting from rest, if a charge Q moves from the middle of side 1 to the centre of square, its kinetic energy at the centre of square is :- **[AIEEE - 2011]**

(1) $\frac{1}{4\pi\epsilon_0}\frac{2qQ}{a}\left(1-\frac{1}{\sqrt{5}}\right)$ (2) zero

(3) $\frac{1}{4\pi\epsilon_0}\frac{2qQ}{a}\left(1+\frac{1}{\sqrt{5}}\right)$ (4) $\frac{1}{4\pi\epsilon_0}\frac{2qQ}{a}\left(1-\frac{2}{\sqrt{5}}\right)$

ES0194

4. **This question has Statement-1 and Statement-2. Of the four choices given after the statements, choose the one that best describes the two statements.** **[AIEEE - 2012]**

An insulating solid sphere of radius R has a uniformaly positive charge density ρ. As a result of this uniform charge distribution there is a finite value of electric potential at the centre of the sphere, at the surface of the sphre and also at a point out side the sphere. The electric potential at infinity is zero.

Statement-1: When a charge 'q' is taken from the centre to the surface of the sphere, its potential energy changes by $\frac{q\rho}{3\epsilon_0}$

Statement-2 : The electric field at a distance r (r < R) from the centre of the sphere is $\frac{\rho r}{3\epsilon_0}$

(1) Statement-1 is true, Statement-2 is true and Statement-2 is the correct explanation of Statement-1.

(2) Statement-1 is true, Statement-2 is true and Statement-2 is not the correct explanation of statement-1.

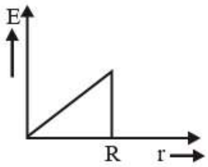
(3) Statement-1 is true, Statement-2 is false

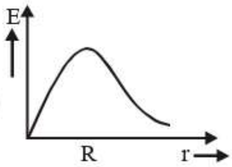
(4) Statement-1 is false, Statement-2 is true

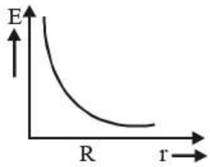
ES0195

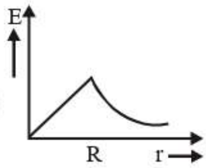
5. In a uniformly charged sphere of total charge Q and radius R, the electric field E is plotted as a function of distance from the centre. The graph which would correspond to the above will be :-

[AIEEE - 2012]

(1) 

(2) 

(3) 

(4) 

ES0196

6. Let $[\in_0]$ denote the dimensional formula of the permittivity of vacuum. If M = mass, L = Length, T = Time and A = electric current, then : **[JEE-Main-2013]**

(1) $[\in_0] = [M^{-1} L^{-3} T^2 A]$ (2) $[\in_0] = [M^{-1} L^{-3} T^4 A^2]$

(3) $[\in_0] = [M^{-1} L^2 T^{-1} A^{-2}]$ (4) $[\in_0] = [M^{-1} L^2 T^{-1} A]$

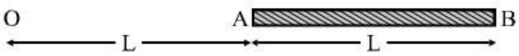
ES0197

7. Two charges, each equal to q, are kept at x = –a and x = a on the x-axis. A particle of mass m and charge $q_0 = \frac{q}{2}$ is placed at the origin. If charge q_0 is given a small displacement ($y << a$) along the y-axis, the net force acting on the particle is proportional to **[JEE-Main-2013]**

(1) y (2) –y (3) $\frac{1}{y}$ (4) $-\frac{1}{y}$

ES0198

8. A charge Q is uniformly distributed over a long rod AB of length L as shown in the figure. The electric potential at the point O lying at a distance L from the end A is :- **[JEE-Main-2013]**



(1) $\frac{Q}{8\pi \in_0 L}$ (2) $\frac{3Q}{4\pi \in_0 L}$ (3) $\frac{Q}{4\pi \in_0 L \ln 2}$ (4) $\frac{Q \ln 2}{4\pi \in_0 L}$

ES0199

9. Assume that an electric field $\vec{E} = 30x^2\hat{i}$ exists in space. Then the potential difference $V_A - V_O$, where V_O is the potential at the origin and V_A the potential at x = 2 m is :- **[JEE-Main-2014]**

(1) –80 J (2) 80 J (3) 120 J (4) –120 J

ES0200

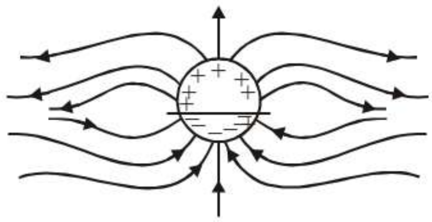
10. A uniformally charged solid sphere of radius R has potential V_0 (measured with respect to ∞) on its surface. For this sphere the equipotential surfaces with potentials $\frac{3V_0}{2}, \frac{5V_0}{4}, \frac{3V_0}{4}$ and $\frac{V_0}{4}$ have radius R_1, R_2, R_3 and R_4 respectively. Then **[JEE-Main-2015]**

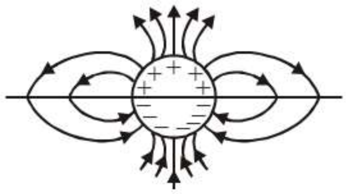
(1) $R_1 = 0$ and $R_2 < (R_4 - R_3)$ (2) $2R < R_4$

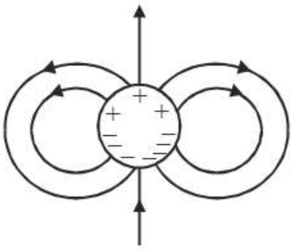
(3) $R_1 = 0$ and $R_2 > (R_4 - R_3)$ (4) $R_1 \neq 0$ and $(R_2 - R_1) > (R_4 - R_3)$

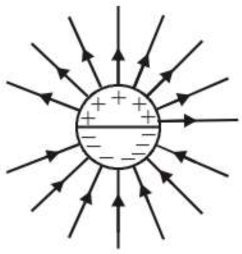
ES0201

11. A long cylindrical shell carries positive surface charge σ in the upper half and negative surface charge $-\sigma$ in the lower half. The electric field lines around the cylinder will look like figure given in: (figures are schematic and not drawn to scale) **[JEE-Main-2015]**

(1) 

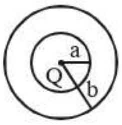
(2) 

(3) 

(4) 

ES0202

12. The region between two concentric spheres of radii 'a' and 'b', respectively (see figure), has volume charge density $\rho = \frac{A}{r}$, where A is a constant and r is the distance from the centre. At the centre of the spheres is a point charge Q. The value of A such that the electric field in the region between the spheres will be constant, is :- **[JEE-Main-2016]**



(1) $\frac{2Q}{\pi a^2}$ (2) $\frac{Q}{2\pi a^2}$ (3) $\frac{Q}{2\pi(b^2 - a^2)}$ (4) $\frac{2Q}{\pi(a^2 - b^2)}$

ES0203

13. An electric dipole has a fixed dipole moment $\vec{p}$, which makes angle θ with respect to x-axis. When subjected to an electric field $\vec{E}_1 = E\hat{i}$, it experiences a torque $\vec{T}_1 = \tau\hat{k}$. When subjected to another electric field $\vec{E}_2 = \sqrt{3}E_1\hat{j}$ it experiences torque $\vec{T}_2 = -\vec{T}_1$. The angle θ is : **[JEE-Main-2017]**

(1) 60° (2) 90° (3) 30° (4) 45°

ES0204

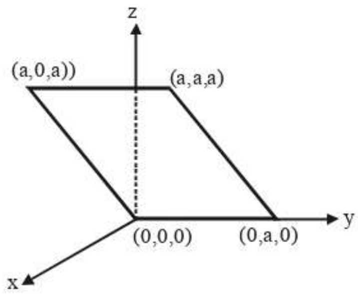
14. Three concentric metal shells A, B and C of respective radii a, b and c (a < b < c) have surface charge densities $+\sigma$, $-\sigma$ and $+\sigma$ respectively. The potential of shell B is :- **[JEE-Main-2018]**

(1) $\frac{\sigma}{\varepsilon_0}\left[\frac{a^2 - b^2}{b} + c\right]$ (2) $\frac{\sigma}{\varepsilon_0}\left[\frac{b^2 - c^2}{b} + a\right]$ (3) $\frac{\sigma}{\varepsilon_0}\left[\frac{b^2 - c^2}{c} + a\right]$ (4) $\frac{\sigma}{\varepsilon_0}\left[\frac{a^2 - b^2}{a} + c\right]$

ES0205

EXERCISE-(JA)

1. Consider an electric field $\vec{E} = E_0\hat{x}$, where E_0 is a constant. The flux through the shaded area (as shown in the figure) due to this field is **[IIT-JEE 2011]**



(A) $2E_0a^2$ (B) $\sqrt{2}E_0a^2$ (C) E_0a^2 (D) $\frac{E_0a^2}{\sqrt{2}}$

ES0206

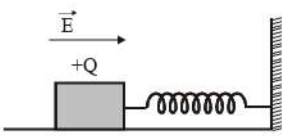
2. A spherical metal shell A of radius R_A and a solid metal sphere B of radius $R_B(<R_A)$ are kept far apart and each is given charge $+Q$. Now they are connected by a thin metal wire. Then

[IIT-JEE 2011]

(A) $E_A^{inside} = 0$ (B) $Q_A > Q_B$ (C) $\frac{\sigma_A}{\sigma_B} = \frac{R_B}{R_A}$ (D) $E_A^{on\ surface} < E_B^{on\ surface}$

ES0207

3. A wooden block performs SHM on a frictionless surface with frequency, ν_0. The block carries a charge $+Q$ on its surface. If now a uniform electric field $\vec{E}$ is switched-on as shown, then the SHM of the block will be :- **[IIT-JEE 2011]**



(A) of the same frequency and with shifted mean position
(B) of the same frequency and with the same mean position
(C) of changed frequency and with shifted mean position
(D) of changed frequency and with the same mean position

ES0208

node06\B0B0-BA\Kota\JEE(Advanced)\Enthuse\Physics\Sheet\Electrostatics\Eng\03_JM&JA.p65

4. Which of the following statement(s) is/are correct? **[IIT-JEE 2011]**

(A) If the electric field due to a point charge varies as $r^{-2.5}$ instead of r^{-2}, then the Gauss law will still be valid.

(B) The Gauss law can be used to calculate the field distribution around an electric dipole.

(C) If the electric field between two point charges is zero somewhere, then the sign of the two charges is the same.

(D) The work done by the external force in moving a unit positive charge from point A at potential V_A to point B at potential V_B is $(V_B - V_A)$

ES0209

5. Four point charges, each of +q, are rigidly fixed at the four corners of a square planar soap film of side 'α'. The surface tension of the soap film is γ. The system of charges and planar film are in equilibrium, and $a = k\left[\frac{q^2}{\gamma}\right]^{1/N}$, where 'k' is a constant. Then N is **[IIT-JEE 2011]**

ES0210

Paragraph for Question Nos. 6 and 7

A dense collection of equal number of electrons and positive ions is called neutral plasma. Certain solids containing fixed positive ions surrounded by free electrons can be treated as neutral plasma. Let 'N' be the number density of free electrons, each of mass 'm'. When the electrons are subjected to an electric field, they are displaced relatively away from the heavy positive ions. If the electric field becomes zero, the electrons begins to oscillate about the positive ions with a natural angular frequency 'ω_ρ', which is called the plasma frequency. To sustain the oscillations, a time varying electric field needs to be applied that has an angular frequency ω, where a part of the energy is absorbed and a part of it is reflected. As ω approaches ω_ρ, all the free electrons are set to resonance together and all the energy is reflected. This is the explanation of high reflectivity of metals.

[IIT-JEE 2011]

6. Taking the electronic charge as 'e' and the permittivity as 'ε_0', use dimensional analysis to determine the correct expression for ω_ρ.

(A) $\sqrt{\frac{Ne}{m\varepsilon_0}}$ (B) $\sqrt{\frac{m\varepsilon_0}{Ne}}$ (C) $\sqrt{\frac{Ne^2}{m\varepsilon_0}}$ (D) $\sqrt{\frac{m\varepsilon_0}{Ne^2}}$

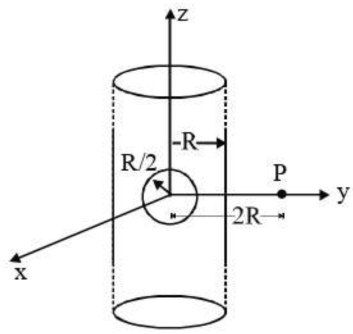
ES0211

7. Estimate the wavelength at which plasma reflection will occur for a metal having the density of electrons $N \approx 4 \times 10^{27} m^{-3}$. Take $\varepsilon_0 \approx 10^{-11}$ and $m \approx 10^{-30}$, where these quantities are in proper SI units

(A) 800 nm (B) 600 nm (C) 300 nm (D) 200 nm

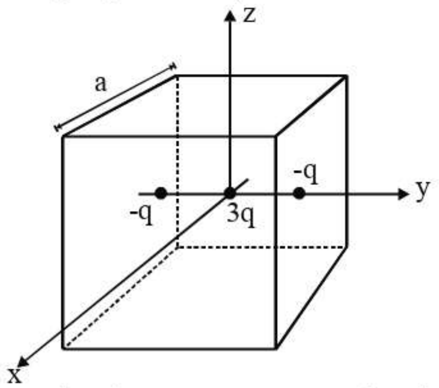
ES0211

8. An infinitely long solid cylinder of radius R has a uniform volume charge density ρ. It has a spherical cavity of radius R/2 with its centre on the axis of the cylinder, as shown in the figure. The magnitude of the electric field at the point P, which is at a distance 2R from the axis of the cylinder, is given by the expression $\frac{23\rho R}{16k\varepsilon_0}$. The value of k is **[IIT-JEE 2012]**



ES0212

9. A cubical region of side a has its centre at the origin. It encloses three fixed point charges, –q at (0, –a/4, 0), +3q at (0,0,0) and –q at (0, +a/4, 0). Choose the correct option(s). **[IIT-JEE 2012]**



(A) The net electric flux crossing the plane x = +a/2 is equal to the net electric flux crossing the plane x = – a/2

(B) The net electric flux crossing the plane y = +a/2 is more than the net electric flux crossing the plane y = –a/2.

(C) The net electric flux crossing the entire region is $\frac{q}{\varepsilon_0}$

(D) The net electric flux crossing the plane z = +a/2 is equal to the net electric flux crossing the plane x = +a/2.

ES0213

node06\B0B0-BA\Kota\JEE(Advanced)\Enthuse\Physics\Sheet\Electrostatics\Eng\03_JM&JA.p65

10. Two large vertical and parallel metal plates having a separation of 1 cm are connected to a DC voltage source of potential difference X. A proton is released at rest midway between the two plates. It is found to move at 45° to the vertical JUST after release. Then X is nearly

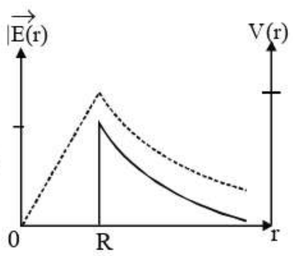
[IIT-JEE 2012]

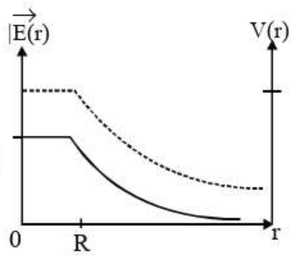
(A) 1×10^{-5} V (B) 1×10^{-7} V
(C) 1×10^{-9} V (D) 1×10^{-10} V

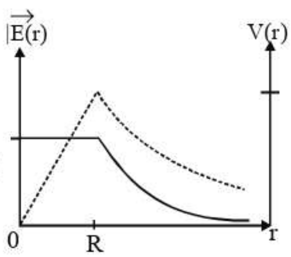
ES0214

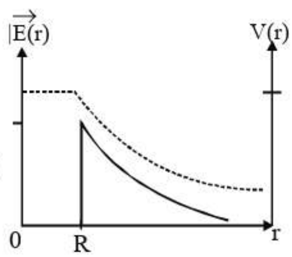
11. Consider a thin spherical shell of radius R with its centre at the origin, carrying uniform positive surface charge density. The variation of the magnitude of the electric field $|\vec{E}(r)|$ and the electric potential V(r) with the distance r from the centre, is best represented by which graph?

[IIT-JEE 2012]

(A)


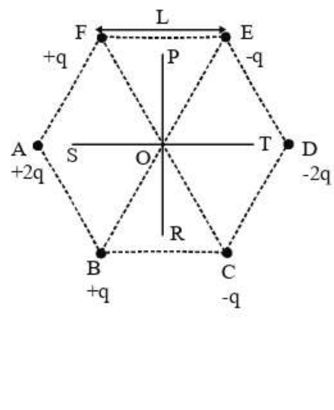
(B)


(C)


(D)


ES0215

12. Six point charges are kept at the vertices of a regular hexagon of side L and centre O, as shown in figure. Given that $K = \frac{1}{4\pi \epsilon_0} \frac{q}{L^2}$, which of the following statement(s) is(are) correct? **[IIT-JEE 2012]**



(A) The electric field at O is 6 K along OD.
(B) The potential at O is zero.
(C) The potential at all points on the line PR is same.
(D) The potential at all points on the line ST is same.

ES0216

13. Two non-conducting solid spheres of radii R and 2R, having uniform volume charge densities ρ_1 and ρ_2 respectively, touch each other. The net electric field at a distance 2R from the centre of the smaller sphere, along the line joining the centres of the spheres, is zero. The ratio $\frac{\rho_1}{\rho_2}$ can be

[JEE-Advance-2013]

(A) –4 (B) $-\frac{32}{25}$ (C) $\frac{32}{25}$ (D) 4

ES0217

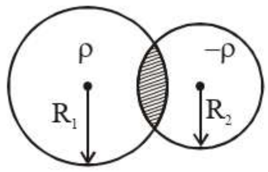
14. Two non-conducting spheres of radii R_1 and R_2 and carrying uniform volume charge densities $+\rho$ and $-\rho$, respectively, are placed such that they partially overlap, as shown in the figure. At all points in the overlapping region :- **[JEE-Advance-2013]**

(A) the electrostatic field is zero

(B) the electrostatic potential is constant

(C) the electrostatic field is constant in magnitude

(D) the electrostatic field has same direction



ES0218

15. Let $E_1(r)$, $E_2(r)$ and $E_3(r)$ be the respective electric fields at a distance r from a point charge Q, an infinitely long wire with constant linear charge density λ, and an infinite plane with uniform surface charge density σ. If $E_1(r_0) = E_2(r_0) = E_3(r_0)$ at a given distance r_0, then :-

[JEE-Advance-2014]

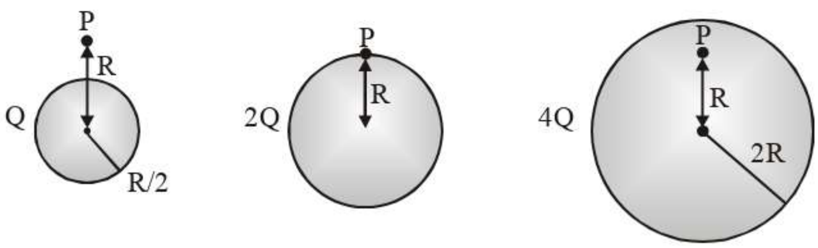
(A) $Q = 4\sigma\pi r_0^2$ (B) $r_0 = \frac{\lambda}{2\pi\sigma}$

(C) $E_1(r_0/2) = 2E_2(r_0/2)$ (D) $E_2(r_0/2) = 4E_3(r_0/2)$

ES0219

16. Charges Q, 2Q and 4Q are uniformly distributed in three dielectric solid spheres 1, 2 and 3 of radii R/2, R and 2R respectively, as shown in figure. If magnitudes of the electric fields at point P at a distance R from the centre of spheres 1, 2 and 3 are E_1, E_2 and E_2 respectively, then

[JEE-Advance-2014]



Sphere 1 Sphere 2 Sphere 3

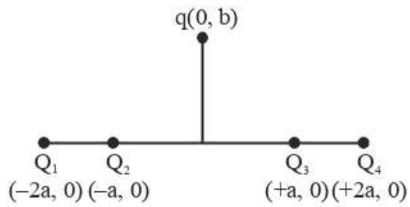
(A) $E_1 > E_2 > E_3$ (B) $E_3 > E_1 > E_2$ (C) $E_2 > E_1 > E_3$ (D) $E_3 > E_2 > E_1$

ES0220

17. Four charges Q_1, Q_2, Q_3 and Q_4 of same magnitude are fixed along the x axis at x = –2a, –a, +a and +2a, respectively. A positive charge q is placed on the positive y axis at a distance b > 0. Four options of the signs of these charges are given in List I. The direction of the forces on the charge q is given in List II. Match List I with List II and select the correct answer using the code given below the lists.

[JEE-Advance-2014]

List-I		List-II	
(P)	Q_1, Q_2, Q_3, Q_4 all positive	(1)	+x
(Q)	Q_1, Q_2 positive ; Q_3, Q_4 negative	(2)	–x
(R)	Q_1, Q_4 positive ; Q_2, Q_3 negative	(3)	+y
(S)	Q_1, Q_3 positive ; Q_2, Q_4 negative	(4)	–y



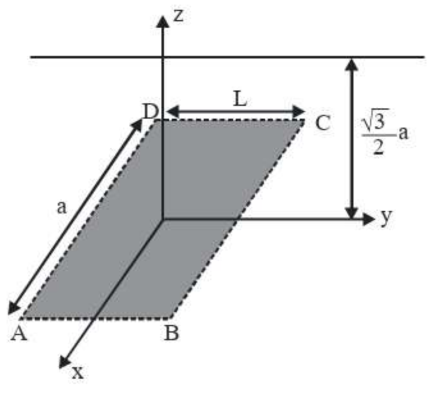
Code :

(A) P-3, Q-1, R-4, S-2 (B) P-4, Q-2, R-3, S-1

(C) P-3, Q-1, R-2, S-4 (D) P-4, Q-2, R-1, S-3

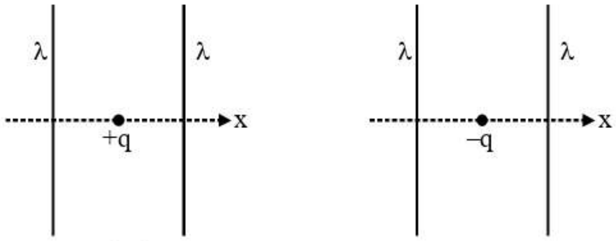
ES0221

18. An infinitely long uniform line charge distribution of charge per unit length λ lies parallel to the y-axis in the y-z plane at $z = \frac{\sqrt{3}}{2}a$ (see figure). If the magnitude of the flux of the electric field through the rectangular surface ABCD lying in the x-y plane with its centre at the origin is $\frac{\lambda L}{n\varepsilon_0}$ (ε_0 = perimittivity of free space) then the value of n is. **[JEE-Advance-2015]**



ES0222

19. The figures below depict two situations in which two infinitely long static line charges of constant positive line charge density λ are kept parallel to each other. In their resulting electric field, point charges q and –q are kept in equilibrium between them. The point charges are confined to move in the x direction only. If they are given a small displacement about their equlibrium positions, then the correct statement(s) is (are) : **[JEE-Advance-2015]**



(A) Both charges execute simple harmonic motion

(B) Both charges will continue moving in the direction of their displacement

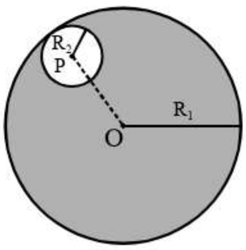
(C) Charge +q executes simple harmonic motion while charge –q continues moving in the direction of its displacement.

(D) Charge –q executes simple harmonic motion while charge +q continues moving in the direction of its displacement.

ES0223

20. Consider a uniform spherical distirbution of radius R_1 centred at the origin O. In this distibution, a spherical cavity of radius R_2, centred at P with distance OP = a = $R_1 - R_2$ (see figure) is made. If the electric field inside the cavity at position $\vec{r}$ is $\vec{E}(\vec{r})$, then the correct statement(s) is(are) :

[JEE-Advance-2015]



(A) $\vec{E}$ is uniform, its magnitude is independent of R_2 but its direction depends on $\vec{r}$

(B) $\vec{E}$ is uniform, its magnitude depends on R_2 and its direction depends on $\vec{r}$

(C) $\vec{E}$ is uniform, its magnitude is independent of a but its direction depends on $\vec{a}$

(D) $\vec{E}$ is uniform and both its magnitude and direction depend on $\vec{a}$

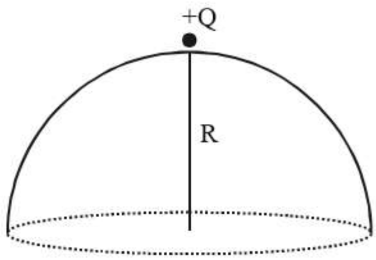
ES0224

21. A length-scale (ℓ) depends on the permittivity (ε) of a dielectric material, Boltzmann constant k_B, the absolute temperature T, the number per unit volume (n) of certain charged particles, and the charge (q) carried by each of the particles, Which of the following expressions(s) for ℓ is(are) dimensionally correct? **[JEE-Advance-2016]**

(A) $\ell = \sqrt{\left(\frac{nq^2}{\varepsilon k_B T}\right)}$ (B) $\ell = \sqrt{\left(\frac{\varepsilon k_B T}{nq^2}\right)}$ (C) $\ell = \sqrt{\left(\frac{q^2}{\varepsilon n^{2/3} k_B T}\right)}$ (D) $\ell = \sqrt{\left(\frac{q^2}{\varepsilon n^{1/3} k_B T}\right)}$

ES0225

22. A point charge +Q is placed just outside an imaginary hemispherical surface of radius R as shown in the figure. Which of the following statements is/are correct ? **[JEE-Advance-2017]**



(A) The circumference of the flat surface is an equipotential

(B) The electric flux passing through the curved surface of the hemisphere is $-\frac{Q}{2\varepsilon_0}\left(1-\frac{1}{\sqrt{2}}\right)$

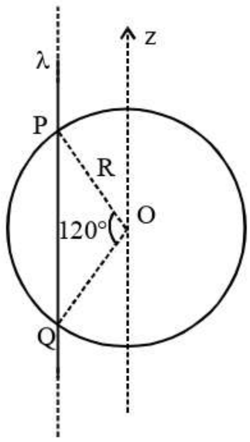
(C) Total flux through the curved and the flat surfaces is $\frac{Q}{\varepsilon_0}$

(D) The component of the electric field normal to the flat surface is constant over the surface.

ES0226

23. An infinitely long thin non-conducting wire is parallel to the z-axis and carries a uniform line charge density λ. It pierces a thin non-conducting spherical shell of radius R in such a way that the arc PQ subtends an angle 120° at the centre O of the spherical shell, as shown in the figure. The permittivity of free space is ε_0. Which of the following statements is (are) true ?

[JEE-Advance-2018]



(A) The electric flux through the shell is $\sqrt{3}\,R\lambda/\varepsilon_0$

(B) The z-component of the electric field is zero at all the points on the surface of the shell

(C) The electric flux through the shell is $\sqrt{2}\,R\lambda/\varepsilon_0$

(D) The electric field is normal to the surface of the shell at all points

ES0227

24. A particle, of mass 10^{-3} kg and charge 1.0 C, is initially at rest. At time t = 0, the particle comes under the influence of an electric field $\vec{E}(t) = E_0 \sin\omega t\,\hat{i}$ where E_0 = 1.0 N C^{-1} and $\omega=10^3$ rad s^{-1}. Consider the effect of only the electrical force on the particle. Then the maximum speed, in ms^{-1}, attained by the particle at subsequent times is.......................... **[JEE-Advance-2018]**

ES0228

25. The electric field E is measured at a point P(0,0,d) generated due to various charge distributions and the dependence of E on d is found to be different for different charge distributions. List-I contains different relations between E and d. List-II describes different electric charge distributions, along with their locations. Match the functions in List-I with the related charge distributions in List-II.

[JEE-Advance-2018]

	List–I		List–II
P.	E is indpendent of d	**1.**	A point charge Q at the origin
Q.	$E \propto \frac{1}{d}$	2.	A small dipole with point charges Q at $(0,0,\ell)$ and – Q at $(0,0,-\ell)$. Take $2\ell << d$
R.	$E \propto \frac{1}{d^2}$	3.	An infinite line charge coincident with the x-axis, with uniform linear charge density λ.
S.	$E \propto \frac{1}{d^3}$	4.	Two infinite wires carrying uniform linear Charge density parallel to the x - axis. The one along $(y = 0, z = \ell)$ has a charge density $+\lambda$ and the one along $(y = 0, z = -\ell)$ has a charge density $-\lambda$. Take $2\ell << d$
		5.	Infinite plane charge coincident with the xy-plane with uniform surface charge density

(A) $P \to 5$; $Q \to 3, 4$; $R \to 1$; $S \to 2$
(B) $P \to 5$; $Q \to 3,$; $R \to 1,4$; $S \to 2$
(C) $P \to 5$; $Q \to 3,$; $R \to 1,2$; $S \to 4$
(D) $P \to 4$; $Q \to 2, 3$; $R \to 1$; $S \to 5$

ES0229

26. A thin spherical insulating shell of radius R carries a uniformly distributed charge such that the potential at its surface is V_0. A hole with a small area $\alpha 4\pi R^2$ ($\alpha << 1$) is made on the shell without affecting the rest of the shell. Which one of the following statements is correct ?

[JEE-Advance-2019]

(1) The ratio of the potential at the center of the shell to that of the point at $\frac{1}{2}$R from center towards the hole will be $\frac{1-\alpha}{1-2\alpha}$

(2) The magnitude of electric field at the center of the shell is reduced by $\frac{\alpha V_0}{2R}$

(3) The magnitude of electric field at a point, located on a line passing through the hole and shell's center on a distance 2R from the center of the spherical shell will be reduced by $\frac{\alpha V_0}{2R}$

(4) The potential at the center of the shell is reduced by $2\alpha V_0$

ES0230

27. A charged shell of radius R carries a total charge Q. Given Φ as the flux of electric field through a closed cylindrical surface of height h, radius r and with its center same as that of the shell. Here, center of the cylinder is a point on the axis of the cylinder which is equidistant from its top and bottom surfaces. Which of the following option(s) is/are correct ? [ϵ_0 is the permittivity of free space]

[JEE-Advance-2019]

(1) If $h > 2R$ and $r > R$ then $\Phi = \frac{Q}{\epsilon_0}$

(2) If $h < \frac{8R}{5}$ and $r = \frac{3R}{5}$ then $\Phi = 0$

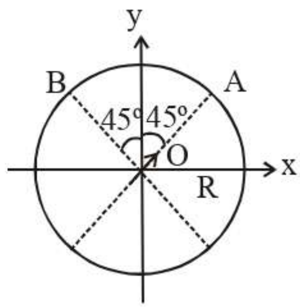
(3) If $h > 2R$ and $r = \frac{4R}{5}$ then $\Phi = \frac{Q}{5\epsilon_0}$

(4) If $h > 2R$ and $r = \frac{3R}{5}$ then $\Phi = \frac{Q}{5\epsilon_0}$

ES0231

28. An electric dipole with dipole moment $\frac{p_0}{\sqrt{2}}(\hat{i}+\hat{j})$ is held fixed at the origin O in the presence of an uniform electric field of magnitude E_0. If the potential is constant on a circle of radius R centered at the origin as shown in figure, then the correct statement(s) is/are:

(ε_0 is permittivity of free space, R >> dipole size) **[JEE-Advance-2019]**



(1) $R = \left(\frac{p_0}{4\pi\varepsilon_0 E_0}\right)^{1/3}$

(2) The magnitude of total electric field on any two points of the circle will be same

(3) Total electric field at point A is $\vec{E}_A = \sqrt{2}E_0(\hat{i}+\hat{j})$

(4) Total electric field at point B is $\vec{E}_B = 0$

ES0232

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ELECTROSTATICS

(CBSE Previous Year's Questions)

1. An electrostatic field line cannot be discontinuous. Why ? **[1; CBSE-2005]**

2. Define electric field intensity. Write its S.1 unit. Write the magnitude and direction of electric field intensity due to an electric dipole of length 2a at the mid- point of the line joining the two charges. **[2; CBSE-2005]**

3. State Gauss' theorem. Apply this theorem to obtain the expression for the electric field intensity at a point due to an infmitely long, thin, umformly charged straight wire. **[3; CBSE-2005]**

4. Define the term electric dipole moment. Is it a scalar or a vector quantity? **[1; CBSE-2006]**

5. A point charge 'q' is placed at O as shown in the figure. **[2; CBSE-2006]**

Is $V_P - V_Q$ positive or negative when (i) $q > 0$, (ii) $q < 0$? Justify your answer.

6. Using Gauss's theorem, show mathematically that for any point outside the shell, the field due to a uniformly charged thin spherical shell is the sai as if the entire charge of the shell is concentrated at the centre. Why do you expect the electric field inside the shell to be zero according to this theorem? **[3; CBSE-2006]**

7. Two point charges 4μC and –2μC are separated by a distance of 1 m in air. Calculate at what point on the line joining the two charges is the electric potential zero. **[1; CBSE-2007]**

8. State Gauss's theorem in electrostatics. Apply this theorem to derive an expression for electric field intensity at a point near an infinitely long straight charged wire. **[2; CBSE-2007]**

9. A 500 μC Charge is at the centre of a square of side 10cm. Find the work done in moving a charge of 10 μC between two diagonally opposite points on the square. **[1; CBSE-2008]**

10. Derive the expression for the electric potential at any point along the axial line of an electric dipole. **[1; CBSE-2008]**

11. (i) Can two equi- potential surfaces intersect each other? Give reasons.

(ii) Two charges –q and +q are located at points A (0,0, –a) and B (0,0, + a) respectively. How much work is done in moving a test charge from point P (7,0,0) to Q (–3,0,0)? **[2; CBSE-2009]**

12. State Gauss's law in electrostatics. Using this law derive an expression for the electric field due to a uniformly charged infinite plane sheet. **[3; CBSE-2009]**

13. Name the physical quantity whose S .1. unit is JC^{-1}. Is it a scalar or a vector quantity ? **[1; CBSE-2010]**

14. Define electric dipole moment. Write its S.I. unit. **[1; CBSE-201I]**

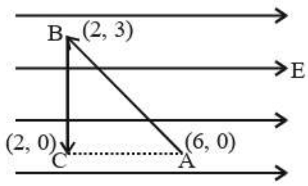
15. A hollow metal sphere of radius 5 cm is charged such that the potential on its surface is 10 V, What is the potential at the centre of the sphere ? **[1; CBSE-2011]**

16. A thin straight infinitely long conducting wire having charge density λ is enclosed by a cylindrical surface of radius r and length l, its axis coinciding with the length of the wire. Find the expression for the electric flux through the surface of the cylinder. **[2; CBSE-2011]**

17. Plot a graph showing the variation of coulomb force (F) versus $\left(\frac{1}{r^2}\right)$, where r is the distance between the two charges of each pair of charges: (1μC, 2μC) and (2μC, – 3μC), interpret the graphs obtained. **[2; CBSE-2011]**

18. Two wires of equal length, one of copper and the other of manganin have the same resistance. Which wire is thicker? **[1; CBSE-2012]**

19. Acharge 'q' is moved without acceleration from A to C along the path from Ato B and then from B to C in electric field E as shown in the figure, (i) Calculate the potential difference between A and C. (ii) At which point (of the two) is the electric potential more and why?



20. An electric dipole is held in a uniform electric field.

(i) Show that the net force acting on it is zero

(ii) The dipole is aligned parallel to the field. Find the work done in rotating it through the angle of 180°. **[2; CBSE-2012]**

21. Two charges of magnitudes – 2Q and + Q are located at points (a, 0) and (4a, 0) respectively. What is the electric flux due to these charges through a sphere of radius '3a' with its centre at the origin?

[CBSE-2013]

22. (a) Define electric dipole moment. Is it a scalar or a vector? Derive the expression for the electric field of a dipole at a point on the equatorial plane of the dipole.

(b) Draw the equipotential surfaces due to an electric dipole. Locate the points where the potential due to the dipole is zero.

OR

Using Gauss' law deduce the expression for the electric field due to a uniformly charged spherical conducting shell of radius R at a point (i) outside and (ii) inside the shell.

Plot a graph showing variation of electric field as a function of r > Rand r < R. (r being the distance from the centre of the shell) **[CBSE-2013]**

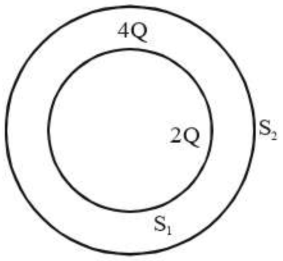
23. Why do the electrostatic field lines not form closed loops ? **[CBSE-2014]**

24. Draw a labelled diagram of Van de Graaft generator. State its working principle to show how by introducing a small charged sphere, into a larger sphere, a large amount of charge can be transferred to the outer sphere state the use of this machine and also point out its limitations.

OR

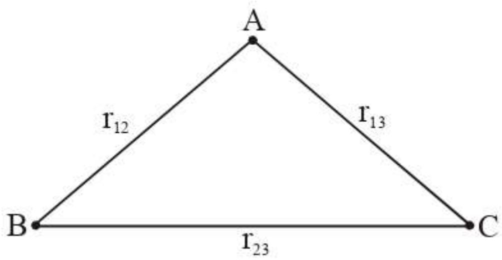
(a) Deduce the expression for the torque acting on a dipole of dipole moment $\vec{p}$ in the presence of a uniform electric field $\vec{E}$.

(b) Consider two hollow concentric spheres, S_1 and S_2, enclosing charges 2Q and 4Q respectively as shown in the figure, (i) Find out the ratio of the electric flux through them, (ii) How will the electric flux through the sphere S_1 change if a medium of dielectric constant 'ε_r' is introduced in the space inside S_1 in place of air ? Deduce the necessary expression. **[CBSE-2014]**



25. Determine the distance of closest approach when an alpha particle of kinetic energy 4.5 MeV strikes a nucleus of Z = 80, stops and reverses its direction. **[2; CBSE-2015]**

26. (a) State Gauss's law in electrostatics. Show, with the help of a suitable example along with the figure, that the outward flux due to a point charge 'q', in vacuum within a closed surface, is independent of its size or shape and is given by q/ε_0. **[5; CBSE-2015]**



(b) Two parallel uniformly charged infinite plane sheets, '1' and '2', have charge densities + σ and –2 σ respectively. Give the magnitude and direction of the net electric field at a point

(i) in between the two sheets and

(ii) outside near the sheet '1'.

27. What is the amount of work done in moving a point charge Q around a circular arc of radius 'r' at the centre of which another point charge 'q' is located? **[1; CBSE-2016]**

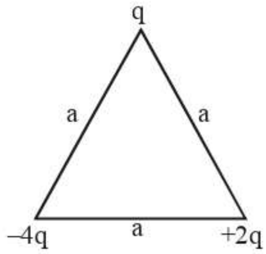
28. Find the electric field intensity due to a uniformly charged spherical shell at a point (i) outside the shell and (ii) inside the shell. Plot the graph of electric field with distance from the centre of the shell.

[3; CBSE-2016]

29. (a) Explain why, for any charge configuration, the equipotential surface through a point is normal to the electric field at the point. **[5; CBSE-2016]**

Draw a sketch of equipotential surfaces due to a single charge (–q), depicting the electric field lines due to the charge.

(b) Obtain an expression for the work done to dissociate the system of three charges placed at the vertices of an equilateral triangle of side 'a' as shown below.



30. (a) Derive an expression for the electric field E due to a dipole of length '2a' at a point distant r from the centre of the dipole on the axial line. **[CBSE-2017]**

(b) Draw a graph of E versus r for r >> a.

(c) If this dipole were kept in a uniform external electric field E_0, diagrammatically represent the position of the dipole in stable and unstable equilibrium and write the expressions for the torque acting on the dipole in both the cases.

OR

(a) Use Gauss's theorem to find the electric field due to a uniformly charged infinitely large plane thin sheet with surface charge density σ.

(b) An infinitely large thin plane sheet has a uniform surface charge density +σ. Obtain the expression for the amount of work done in bringing a point charge q from infinity to a point, distant r, in front of the charged plane sheet.

ANSWER KEY

EXERCISE (S-1)

1. Ans. 80 **2. Ans.** 003 **3. Ans.** $(1+2\sqrt{2})/4\,Q$ **4. Ans.** 9

5. Ans. 3 **6. Ans.** 4 **7. Ans.** 400 **8. Ans.** 9.30

9. Ans. 3 **10. Ans.** 8 **11. Ans.** 2 **12. Ans.** 1

13. Ans. 2 **14. Ans.** 4 **15. Ans.** 576 **16. Ans.** 3

17. Ans. 4 **18. Ans.** 4 **19. Ans.** 6 **20. Ans.** 0

21. Ans. $-\frac{kq^2}{a}\left(3-\sqrt{2}\right)$ **22. Ans.** 2 **23. Ans.** 90 **24. Ans.** 2

25. Ans. 2 **26. Ans.** $2\tan^{-1}\left(\frac{\sigma q}{2\varepsilon_0 mg}\right)$ **27. Ans.** 20

28. Ans. $\left[\frac{2KQq}{mR}\left(\frac{r-R}{r}+\frac{3}{8}\right)\right]^{1/2}$ **29. Ans. 2** **30. Ans.** 4

31. Ans. $\frac{kP}{\sqrt{2}\,y^3}(-\hat{i}-2\hat{j})$ **32. Ans.** 028

33. Ans. (a) $K.E=\frac{P}{4\pi\varepsilon_0}\frac{Q}{d^2}$, (b) $\frac{QP}{2\pi\varepsilon_0 d^3}$ along positive x-axis

34. Ans. (a) (i) $V=\frac{k(q_a+q_b)}{r}$, $E=\frac{k(q_a+q_b)}{r^2}$; (ii) $\frac{k(q_a+q_b)}{R}+\frac{kq_b}{r}-\frac{kq_b}{b}$; $\frac{kq_b}{r^2}$

(b) $\sigma_R=\left(\frac{q_a+q_b}{4\pi R^2}\right)$, $\sigma_a=-\frac{q_a}{4\pi a^2}$; $\sigma_b=-\frac{q_b}{4\pi b^2}$; (c) f = 0]

35. Ans. $-Q/3$ **36. Ans. 3** **37. Ans.** $V'=\left(\frac{a}{3t}\right)^{1/3}V$

38. Ans. $-\varepsilon E, \varepsilon E$ and so on

EXERCISE (S-2)

1. Ans. $\frac{\sigma}{\pi\epsilon_0}$ **2. Ans.** a **3. Ans.** $\pi K d t \rho R^2$ **4. Ans.** 3

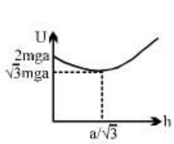
5. Ans. 3 **6. Ans.** 8

7. Ans. $v_0 = 3$ m/s ; K.E. at the origin $=\left(27-10\sqrt{6}\right)\times 10^{-4}$ J approx. 2.5×10^{-4} J

8. Ans. 6 **9. Ans.** $\lambda R E_0\,\hat{i}$ **10. Ans.** $\sqrt{4\pi\varepsilon_o Ka}$

11. Ans. $W_{\text{first step}}=\left(\frac{8}{3}-\frac{4}{\sqrt{5}}\right)\frac{Kq^2}{r}$, $W_{\text{second step}}=0$, $W_{\text{total}}=0$

12. Ans. (a) $H = \frac{4a}{3}$, (b) $U = mg\left[2\sqrt{h^2+a^2}-h\right]$ equilibrium at $h = \frac{a}{\sqrt{3}}$,



13. Ans. (i) -Q, + Q (ii) $E_A = 0$, can't be found (iii) can't be found (iv) can't be found (v) 0 (vi) No, induced charge on outer surface]

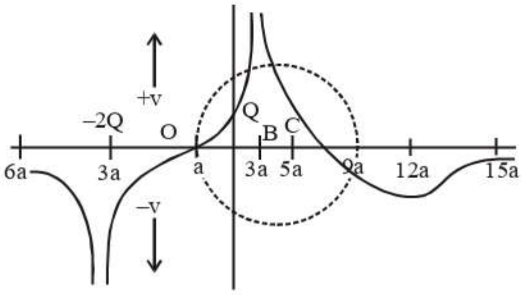
14. Ans. 180

15. Ans. $F = \frac{Q^2}{32\pi\varepsilon_0 R^4}\left(R^2 - h^2\right)$

16. Ans. (a) radius = 4a & center (5a, 0)

(b) $V = \frac{1}{4\pi\varepsilon_0}\left[\frac{-2Q}{\left|(x+3a)\right|} + \frac{Q}{\left|(x-3a)\right|}\right]$

(c) speed $v = \sqrt{\frac{1}{4\pi\varepsilon_0} \times \frac{qQ}{2ma}}$



17. Ans. 7

EXERCISE (O-1)

1. Ans. (C)	**2. Ans. (B)**	**3. Ans. (C)**	**4. Ans. (C)**	**5. Ans. (B)**	**6. Ans. (A)**
7. Ans. (D)	**8. Ans. (B)**	**9. Ans. (A)**	**10. Ans. (A)**	**11. Ans. (A)**	**12. Ans. (C)**
13. Ans. (A)	**14. Ans. (C)**	**15. Ans. (A)**	**16. Ans. (D)**	**17. Ans. (B)**	**18. Ans. (C)**
19. Ans. (D)	**20. Ans. (B)**	**21. Ans. (D)**	**22. Ans. (A)**	**23. Ans. (D)**	**24. Ans. (A)**
25. Ans. (D)	**26. Ans. (D)**	**27. Ans. (D)**	**28. Ans. (B)**	**29. Ans. (C)**	**30. Ans. (C)**
31. Ans. (D)	**32. Ans. (C)**	**33. Ans. (D)**	**34. Ans. (D)**	**35. Ans. (A)**	**36. Ans. (B)**
37. Ans. (A)	**38. Ans. (B)**	**39. Ans. (D)**	**40. Ans. (B)**	**41. Ans. (A)**	**42. Ans. (C)**
43. Ans. (C)	**44. Ans. (C)**	**45. Ans. (C)**	**46. Ans. (A)**	**47. Ans. (C)**	**48. Ans. (B)**
49. Ans. (B)	**50. Ans. (A)**	**51. Ans. (B)**	**52. Ans. (C)**	**53. Ans. (A)**	**54. Ans. (A)**
55. Ans. (D)	**56. Ans. (B)**	**57. Ans. (A)**	**58. Ans. (A)**	**59. Ans. (C)**	**60. Ans. (C)**
61. Ans. (A)	**62. Ans. a. (B); b. (D)**		**63. Ans. (C)**	**64. Ans. (B)**	**65. Ans. (D)**
66. Ans. (A)	**67. Ans. (D)**	**68. Ans. (D)**	**69. Ans. (A)**	**70. Ans. (C)**	**71. Ans. (D)**
72. Ans. (B)	**73. Ans. (B)**	**74. Ans. (A)**	**75. Ans. (A)**	**76. Ans. (C)**	**77. Ans. (A)**
78. Ans. (C)	**79. Ans. (C)**	**80. Ans. (A,B)**	**81. Ans. (A,B,C)**	**82. Ans. (A,B,D)**	

83. Ans. (A,B,C)	**84. Ans. (A,B,C)**	**85. Ans. (AC)**	**86. Ans. (A,C,D)**
87. Ans. (A,B,C)	**88. Ans. (A,B,C)**	**89. Ans. (B,D)**	**90. Ans. (A,C)**
91. Ans. (A, D)	**92. Ans. (B,C,D)**	**93. Ans. (A, B, D)**	**94. Ans. (A, B)**

95. Ans. (A,B,C)	**96. Ans. (B)**	**97. Ans. (D)**	**98. Ans. (C)**	**99. Ans. (A)**
100. Ans. (C)	**101. Ans. (A)**	**102. Ans. (A)**	**103. Ans. (A)**	**104. Ans. (B)**
105. Ans. (C)	**106. Ans. (B)**	**107. Ans. (A)→(Q); (B)→(S); (C)→(R); (D)→(P)**		

108. Ans. **(A) → (Q, R) ; (B) → (Q,T) ; (C) → (S,T) (D) → (P)**

109. Ans. **(A) – S; (B) – P; (C) – R; (D) – Q**

110. Ans. **A → Q; B → P, S; C → P, Q, R; D → Q, R**

111. Ans. **(A)-Q,S, (B)-P,R (C)-P,R (D)-Q,R**

EXERCISE (O-2)

1. Ans. (A)	**2. Ans. (B)**	**3. Ans. (B)**	**4. Ans. (C)**	**5. Ans. (C)**	**6. Ans. (A)**
7. Ans. (A)	**8. Ans. (B)**	**9. Ans. (C)**	**10. Ans. (A)**	**11. Ans. (C)**	**12. Ans. (B)**
13. Ans. (A)	**14. Ans. (B)**	**15. Ans. (D)**	**16. Ans. (B)**	**17. Ans. (B)**	**18. Ans. (C)**
19. Ans. (A)	**20. Ans. (B)**	**21. Ans. (A)**	**22. Ans. (C)**	**23. Ans. (A)**	**24. Ans. (C)**
25. Ans. (A, C)		**26. Ans. (A,C)**	**27. Ans. (A,D)**	**28. Ans. (A,B)**	**29. Ans. (A,B,C)**
30. Ans. (B)	**31. Ans. (C)**	**32. Ans. (B)**	**33. Ans. (A)**	**34. Ans. (D)**	

35. Ans. (A) P,R,S (B) P,Q,R,S,T (C) Q,T (D) R,S

EXERCISE-JM

1. Ans. (3)	**2. Ans. (2)**	**3. Ans. (1)**	**4. Ans. (4)**	**5. Ans. (4)**	**6. Ans. (2)**
7. Ans. (1)	**8. Ans. (4)**	**9. Ans. (1)**	**10. Ans. (1 or 2)**	**11. Ans. (3)**	**12. Ans. (2)**
13. Ans. (1)	**14. Ans. (1)**				

EXERCISE-(JA)

1. Ans. (C)	**2. Ans. (A,B,C,D)**	**3. Ans. (A)**	**4. Ans. (C,D)**	**5. Ans. 3**
6. Ans. (C)	**7. Ans. (B)**	**8. Ans. 6**	**9. Ans. (A,C,D)**	**10. Ans. (C)**
11. Ans. (D)	**12. Ans. (A, B, C)**	**13. Ans. (B, D)**	**14. Ans. (C, D)**	**15. Ans. (C)**
16. Ans. (C)	**17. Ans. (A)**	**18. Ans. 6**	**19. Ans. (C)**	**20. Ans. (D)**
21. Ans. (B,D)	**22. Ans. (A) (B)**	**23. Ans. (A,B)**	**24. Ans. 2 [1.99, 2.01]**	
25. Ans. (B)	**26. Ans. (1)**	**27. Ans. (1,2,4)**	**28.Ans. (1,4)**	