Week 5 Practice Sheet

SECTION A: Coding Problems

Q1. Write a program to represent a matrix using 2D arrays and display it.

Answer:

Q2. Write a program to take input of an n × m matrix and print it in matrix format.

Q3. Write a program to find the transpose of a matrix.

Answer:

```
public class TransposeMatrix {
    public static void main(String[]
args) {
                int[][] matrix = {
            {1, 2, 3},
            {4, 5, 6}
                    int rows =
        };
matrix.length;
                       int cols
= matrix[0].length;
        int[][] transpose = new int[cols][rows];
         for (int i = 0; i < rows; i++) {
for (int j = 0; j < cols; j++) {
transpose[j][i] = matrix[i][j];
           }
        }
        System.out.println("Transpose:");
for (int i = 0; i < cols; i++) {
for (int j = 0; j < rows; j++) {
                System.out.print(transpose[i][j] + " ");
            System.out.println();
        }
    }
}
```

Q4. Write a program to rotate a square matrix by 90° clockwise.

```
for (int i = 0; i < n; i++) {
for (int j = i; j < n; j++) {
int temp = matrix[i][j];
matrix[i][j] = matrix[j][i];
matrix[j][i] = temp;
           }
        // Reverse rows
        for (int i = 0; i < n; i++) {
for (int j = 0; j < n / 2; j++) { int
temp = matrix[i][j]; matrix[i][j] =
matrix[i][n - 1 - j]; matrix[i][n - 1
-j] = temp;
           }
        }
        System.out.println("90° Clockwise Rotation:");
for (int[] row : matrix) {
            for (int val : row) System.out.print(val + " ");
            System.out.println();
        }
    }
}
```

Q5. Write a program to rotate a square matrix by 90° anticlockwise.

```
public class RotateAnticlockwise { public
static void main(String[] args) { int[][]
matrix = {
                                {1, 2,
3},
            {4, 5, 6},
            {7, 8, 9}
        } ;
        int n = matrix.length;
        // Transpose
        for (int i = 0; i < n; i++) {
for (int j = i; j < n; j++) {
int temp = matrix[i][j];
matrix[i][j] = matrix[j][i];
matrix[j][i] = temp;
           }
        }
        // Reverse columns
                                    for
(int j = 0; j < n; j++) {
                                        for
(int i = 0; i < n / 2; i++) {
int temp = matrix[i][j];
matrix[i][j] = matrix[n - 1 - i][j];
matrix[n - 1 - i][j] = temp;
           }
        }
```

Q6. Write a program to check whether a square matrix is symmetric ($A = A^T$).

Answer:

```
public class SymmetricMatrix {
   public static void main(String[]
args) {
               int[][] matrix = {
{1, 2, 3},
            {2, 5, 6},
            {3, 6, 9}
        };
        int n = matrix.length;
boolean isSymmetric = true;
         for (int i = 0; i < n; i++) {
for (int j = 0; j < n; j++) {
if (matrix[i][j] != matrix[j][i]) {
isSymmetric = false;
                                           break;
                }
            }
                                         if (isSymmetric)
}
                                             System.out.println("Matrix is
                                             Symmetric");
else
                                             System.out.println("Matrix is NOT
    }
                                             Symmetric");
```

Q7. Write a program to multiply two matrices (if dimensions allow).

```
public class MatrixMultiplication {
public static void main(String[] args) {
int[][] A = {
                        {1, 2, 3},
            {4, 5, 6}
        };
int[][] B = {
{7, 8},
            {9, 10},
            {11, 12}
                    int rows =
        } ;
A.length;
                  int cols =
B[0].length;
                    int sumLength =
B.length;
                  int[][] C = new
int[rows][cols];
```

Q8. Write a program to add two matrices.

Answer:

```
public class MatrixAddition {
  public static void main(String[]
args) {
               int[][] A = {
{1, 2},
            {3,
4 }
          } ;
int[][] B = {
{5, 6},
           {7, 8}
                  int rows =
                 int cols =
A.length;
A[0].length;
                    int[][] C = new
int[rows][cols];
        for (int i = 0; i < rows; i++) {
for (int j = 0; j < cols; j++) {
C[i][j] = A[i][j] + B[i][j];
           }
        }
        System.out.println("Matrix Addition Result:");
for (int[] row : C) {
           for (int val : row) System.out.print(val + " ");
System.out.println();
       }
   }
}
```

Q9. Write a program to convert a matrix into sparse matrix representation (row, col, value triplets).

```
public class SparseMatrix {
```

```
public static void main(String[]
args) {
               int[][] matrix = {
{0, 0, 3},
            {4, 0, 0},
            {0, 5, 0}
        };
        System.out.println("Sparse Matrix Representation (row, col,
        for (int i = 0; i < matrix.length; i++) {</pre>
for (int j = 0; j < matrix[0].length; <math>j++) {
                if (matrix[i][j] != 0) {
                     System.out.println(i + " " + j + " " + matrix[i][j]);
            }
       }
   }
}
```

Q10. Write a program to perform addition of two sparse matrices.

```
{4, 0, 0},
{0, 5, 0}
{0, 0, 6},
{7, 0, 0}
public class SparseMatrixAddition {
public static void main(String[] args) {
int[][] A = {
                          {0, 0, 3},
        };
int[][] B =
{0, 2, 0},
                   int rows = A.length,
        } ;
cols = A[0].length;
                      int[][] result =
new int[rows][cols];
        for (int i = 0; i < rows; i++) {
for (int j = 0; j < cols; j++) {
result[i][j] = A[i][j] + B[i][j];
        System.out.println("Sparse Matrix Addition Result (row, col,
value):");
        for (int i = 0; i < rows; i++) {
for (int i = 0; i < cols; i++) {
if (result[i][j] != 0) {
                    System.out.println(i + " " + j + " " + result[i][j]);
            }
        }
    }
```

Q11. Write a program to find the sum of diagonal elements of a square matrix.

Answer:

Q12. Write a program to check if a given matrix is an identity matrix.

Answer:

```
public class IdentityMatrix {
   public static void main(String[]
args) {
                int[][] matrix = {
{1, 0, 0},
            \{0, 1, 0\},\
            {0, 0, 1}
        } ;
                    boolean
isIdentity = true;
                           int
n = matrix.length;
       for (int i = 0; i < n; i++) {
for (int j = 0; j < n; j++) {
                if ((i == j && matrix[i][j] != 1) || (i != j &&
matrix[i][j]
!= 0)) {
                                              isIdentity = false;
break;
                                          }
            }
                                         if (isIdentity)
}
                                             System.out.println("Matrix is an
                                             Identity Matrix");
else
                                             System.out.println("Matrix is NOT
   }
                                             an Identity Matrix");
```

Q13. Write a program to find the maximum element in a matrix.

Answer:

```
public class MaxElement {
   public static void main(String[]
{1, 20, 3},
          {14, 5, 6},
          {7, 8, 9}
              int max =
       } ;
                for (int[] row
matrix[0][0];
: matrix) {
                   for (int val
                    if (val >
: row) {
max) max = val;
         }
       }
       System.out.println("Maximum Element: " + max);
   }
}
```

Q14. Write a program to count total number of zeros in a matrix.

Answer:

```
public class CountZeros {
   public static void main(String[]
               int[][] matrix = {
args) {
{0, 2, 0},
            {4, 0, 6},
            {0, 0, 9}
        };
        int count = 0;
                              for
(int[] row : matrix) {
for (int val : row) {
if (val == 0) count++;
           }
        }
        System.out.println("Total number of zeros: " + count);
   }
}
```

Q15. Write a program to search an element in a row-wise & column-wise sorted matrix.

```
matrix.length;
                     int m
= matrix[0].length;
     int i = 0, j = m
- 1;
         boolean found
= false;
       while (i < n && j >= 0) {
if (matrix[i][j] == target) {
found = true;
           } else if (matrix[i][j] >
target) {
                      j--;
} else {
                        i++;
           }
                                       if (found)
}
                                           System.out.println("Element " +
                                           target + " found.");
else
                                           System.out.println("Element " +
                                           target + " not
found.");
}
```

SECTION B:

Q1. Which of the following is the correct way to represent a matrix in memory? a) Row-major order

- b) Column-major order
- c) Both (depends on language)
- d) None

Answer: (c) Both (depends on language)

Q2. In C/C++, matrices are stored

in: a) Column-major order

- b) Row-major order
- c) Linked list format
- d) Hash table

Answer: (b) Row-major order

Q3. What is the space complexity of storing an $n \times m$ matrix in a 2D array? a) O(1)

- b) O(n)
- c) O(m)
- d) $O(n \times m)$

Answer: (d) $O(n \times m)$

Q4. A square matrix

means: a) Rows ≠ Columns

- b) Rows = Columns
- c) Only diagonal elements exist
- d) Matrix is symmetric

Answer: (b) Rows = Columns

Q5. Which of the following is a diagonal

matrix? a) All elements are 0

- b) All non-diagonal elements are 0
- c) All diagonal elements are 0
- d) All elements are 1

Answer: (b) All non-diagonal elements are 0

Q6. An identity matrix

is: a) All 0s

- b) All 1s
- c) Diagonal elements = 1, others = 0
- d) Diagonal elements = 0, others = 1

Answer: (c) Diagonal elements = 1, others = 0

Q7. Which of the following cannot be performed on matrices

directly? a) Addition

- b) Subtraction
- c) Division
- d) Multiplication Answer: (c) Division

Q8. Matrix addition is possible

if: a) Rows and columns are equal

- b) Only rows equal
- c) Only columns equal
- d) None

Answer: (a) Rows and columns are equal

Q9. Matrix multiplication is possible

if: a) Columns of first = Rows of second

- b) Rows of first = Columns of second
- c) Both dimensions equal
- d) Only square matrices allowed

Answer: (a) Columns of first = Rows of second

Q10. What is the order of the product matrix $C = A \times B$ if A is $m \times n$ and B is $n \times n$

 $\mathbf{p?}$ a) m × n

- b) n \times p
- c) $m \times p$
- d) $p \times m$

Answer: (c) m × p

Matrix Operations (Transpose, Rotation, Multiplication)

Q11. Transpose of a matrix

means: a) Interchanging rows and

columns

- b) Doubling each element
- c) Squaring elements
- d) Multiplying diagonals

Answer: (a) Interchanging rows and columns

Q12. The transpose of transpose of a matrix A

is: a) -A

- b) A
- c) A²
- d) None Answer: (b) A

Q13. If A is a symmetric matrix,

then: a) $A = -A^T$

- b) $A = A^T$
- c) $A^2 = I$
- d) $A = A^{-1}$ **Answer:** (b) $A = A^{T}$

Q14. A skew-symmetric matrix

satisfies: a) $A = A^T$

- b) $A = -A^T$
- c) A = I
- d) $A = A^2$

Answer: (b) $A = -A^T$

Q15. Time complexity of matrix multiplication (naive

method): a) O(n²)

- b) $O(n^3)$
- c) O(n log n)
- d) $O(n^2 \log n)$

Answer: (b) O(n³)

Q16. Rotating a matrix 90° clockwise is equivalent

to: a) Transpose + Reverse rows

- b) Transpose + Reverse columns
- c) Only transpose
- d) Only reverse rows

Answer: (a) Transpose + Reverse rows

Q17. Which algorithm is more efficient for large matrix

multiplication? a) Naive method

- b) Strassen's Algorithm
- c) Gaussian Elimination
- d) QuickSort

Answer: (b) Strassen's Algorithm

Q18. In Strassen's Algorithm, time complexity reduces

to: a) O(n²)

- b) $O(n^2.81)$
- c) $O(n^3)$
- d) O(log n)

Answer: (b) O(n².81)

Q19. The determinant of a matrix is defined only

for: a) Rectangular matrices

- b) Square matrices
- c) Identity matrices
- d) Symmetric matrices Answer: (b) Square matrices

Q20. The inverse of a matrix exists only

if: a) Matrix is symmetric

- b) Determinant $\neq 0$
- c) Diagonal elements are non-zero
- d) Matrix is diagonal

Answer: (b) Determinant $\neq 0$

Sparse Matrices

Q21. A sparse matrix is one

where: a) All elements are 0

- b) Non-zero elements < 50% of total
- c) Non-zero elements > 50% of total
- d) All diagonal elements are 1

Answer: (b) Non-zero elements < 50% of total

Q22. Common representation of a sparse matrix

is: a) Linked list

- b) 3-tuple form (row, col, value)
- c) Hash table
- d) Array of size n²

Answer: (b) 3-tuple form (row, col, value)

Q23. Which of the following is NOT an advantage of sparse

representation? a) Saves memory

- b) Faster traversal of non-zeros
- c) Easier arithmetic operations
- d) Always faster than dense representation Answer: (c) Easier arithmetic operations

Q24. What is the maximum number of non-zero elements a sparse matrix can

have? a) \leq n \times m

- $b) = n \times m$
- c) n
- d) Undefined Answer: (b) = $n \times m$

Q25. Time complexity of adding two sparse matrices (triplet

form): a) $O(n^2)$

- b) O(n)
- c) O(number of non-zero elements)
- d) O(1)

Answer: (c) O(number of non-zero elements)

Q26. If a sparse matrix has 1000 rows × 1000 columns with only 1000 non-zero elements, memory saved using sparse representation is approximately: a) Very small

- b) Significant
- c) No difference
- d) More costly

Answer: (b) Significant

Q27. Which storage is most efficient for sparse matrices in numerical computations? a) Dense array

- b) Compressed Sparse Row (CSR)
- c) Hash table
- d) Linked list

Answer: (b) Compressed Sparse Row (CSR)

Q28. In triplet representation, the first row usually

stores: a) Matrix order and count of non-zero elements

- b) Only rows
- c) Only columns
- d) Only diagonal

Answer: (a) Matrix order and count of non-zero elements

Q29. Which of the following applications commonly uses sparse

matrices? a) Graphs (Adjacency Matrix)

- b) Image compression
- c) Machine learning (large datasets)
- d) All of the above

Answer: (d) All of the above

Q30. Which of the following is true about sparse

matrices? a) They always store fewer elements

- b) They only store diagonal elements
- c) They reduce memory usage when most entries are 0
- d) They cannot be used in graph problems

Answer: (c) They reduce memory usage when most entries are 0

SECTION C:

Transpose of Matrix

```
import java.util.Scanner;
public class TransposeMatrix {
public
                           void
              static
main(String[] args) {
    Scanner sc = new Scanner(System.in);
    // Input matrix dimensions
System.out.print("Enter rows: ");
int n = sc.nextInt();
    System.out.print("Enter columns:
");
       int m = sc.nextInt();
    int[][] matrix = new int[n][m];
    System.out.println("Enter elements of matrix:");
    for (int i = 0; i < n; i++) {
for (int j = 0; j < m; j++) {
matrix[i][j] = sc.nextInt();
      }
    }
    // Print transpose
    System.out.println("Transpose of Matrix:");
```

```
for (int i = 0; i < m; i++)
{
     for (int j = 0; j < n;
j++) {
        System.out.print(matrix[j][i] + " ");
     }
     System.out.println();
    }
}</pre>
```

Rotate Matrix (90° Clockwise)

```
import java.util.Scanner;
public class RotateMatrix {
public static void main(String[]
args) {
    Scanner sc = new Scanner(System.in);
    // Input size of square matrix
    System.out.print("Enter size of square matrix
(n): "); int n = sc.nextInt();
    int[][] matrix = new int[n][n];
    System.out.println("Enter elements of matrix:");
    for (int i = 0; i < n; i++)
{
        for (int j = 0; j < n;
j++) {
               matrix[i][j]
= sc.nextInt();
```

```
}
     }
     // Step 1: Transpose
for (int i = 0; i < n; i++) {
for (int j = i; j < n; j++) {
int temp = matrix[i][j];
matrix[i][j] = matrix[j][i];
matrix[j][i] = temp;
       }
     }
    // Step 2: Reverse each row
     for (int i = 0; i < n; i++) {
int left = 0, right = n - 1;
while (left < right) {
                               int
temp = matrix[i][left];
matrix[i][left] =
matrix[i][right]; matrix[i][right]
= temp;
left++;
                 right--;
       }
    }
    // Print rotated matrix
     System.out.println("Matrix after 90° Clockwise Rotation:");
     for (int i = 0; i < n; i++)
{
         for (int j = 0; j < n;
j++) {
```

```
System.out.print(matrix[i][j] + " ");
}
System.out.println();
}
}
```