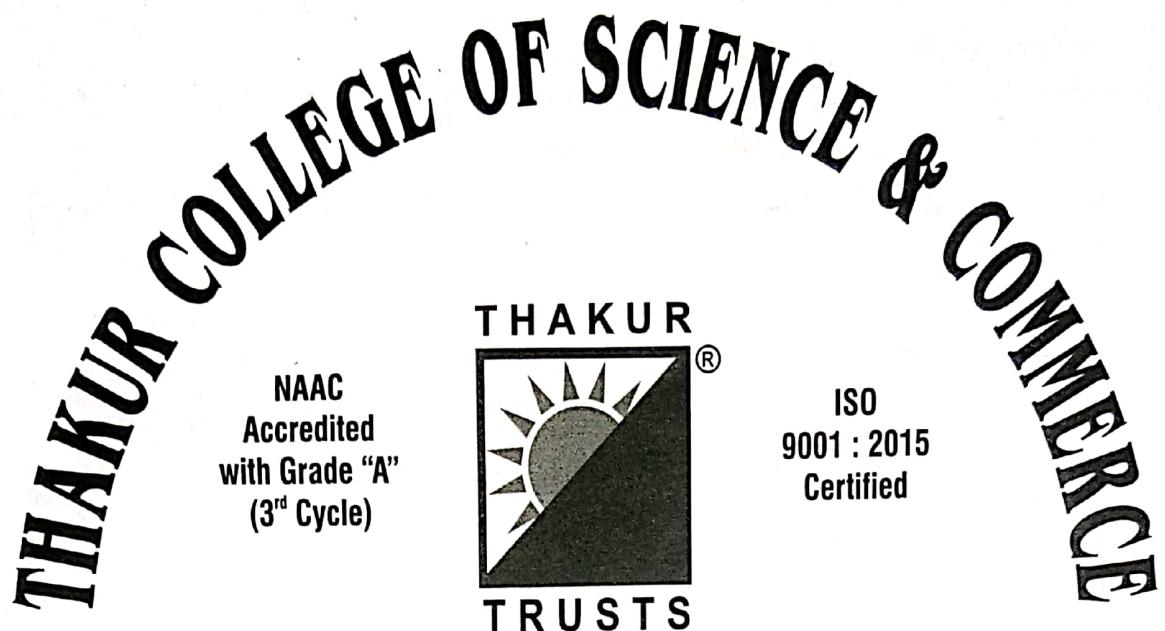


PERFORMANCE

Term	Remarks	Staff Member's Signature
I	<i>Excell</i>	<i>A. M.</i>
II	<i>Good</i>	<i>A. M.</i>

Exam Seat No. _____



Degree College
Computer Journal
CERTIFICATE

SEMESTER II UID No. _____

Class FYBSCS Roll No. 1738 Year 2019 - 2020

This is to certify that the work entered in this journal
is the work of Mst. / Ms. Anukul Suraj Shivkumar

who has worked for the year _____ in the Computer
Laboratory.

A. Nair
Teacher In-Charge

Head of Department

Date : 27.02.20

Examiner

★ ★ INDEX ★ ★

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PRACTICAL-01

* Basic of R Software:-

- R is a software for statistical analysis and data computing
- It is an effective data handling software and outcome storage is possible.
- It is capable of graphical display
- R is a Free software

Q1 Solve the following

$$\text{i) } 4 + 6 + 8 \div 2 - 5$$

$$\text{ii) } 2^2 + | -3 | + \sqrt{45}$$

$$\text{iii) } 5^3 + 7 \times 5 \times 8 + 46 / 5$$

$$\text{iv) } \sqrt{4^2 + 5 \times 3 + 7} / 6$$

v) Round off

$$46 \div 7 + 9 \times 8$$

Code:-

$$\text{i) } 4 + 6 + 8 / 2$$

[1] 14

- 2) $2^1 2 + \text{abs}(-3) + \text{sqrt}(45)$
 $[1] 44.137082$
- 3) $5^1 3 + 7 * 5 * 8 + 46/5$
 $[1] 414.2$
- 4) $\text{sqrt}(4^1 2 + 5 * 3 + 7/6)$
 $[1] 5.671567$
- 5) $46/7 + 9 * 8$
 $[1] 78.57143$
- Q2] Solve the following:
(i) $C(2, 3, 5, 7)^* 2$
 $[1] 4 6 10 14$
- (ii) $C(2, 3, 5, 7)^* C(2, 3)$
 $[1] 4 9 10 21$
- (iii) $C(2, 3, 5, 7)^* C(2, 3, 6, 2)$
 $[1] 4 9 30 14$
- (iv) $C(1, 6, 2, 3)^* C(-2, -3, -4, -1)$
 $[1] -2 -18 -8 -3$
- (v) $C(2, 3, 5, 7)^2$
 $[1] 4 9 25 49$

vi) $(C(4, 6, 8, 9, 4, 5))^* C(1, 2, 3)$
 $[1] 7 4 36 512 9 16 125$

Q3] Solve the following

$x=20, y=30, z=2$

Find, i) $x^2 + y^3 + z$

ii) $\sqrt{x^2+y}$

iii) $x^2 + y^2$

code :-

i) $a = x^2 + y^3 + z$

>a

[1] 27402

ii) $b = \sqrt{x^2 + y}$

>b

[1] 20.73644

iii) $c = x^2 + y^2$

>c

[1] 1300

Q4] Convert the data in Matrix form:

1	5
2	6
3	7
4	8

Code

```
u=matrix(nrow=4, ncol=2, data=c(1,2,3,4,5,6,7))
```

[,1]	[,2]
[1,] 1 5	
[2,] 2 6	
[3,] 3 7	
[4,] 4 8	

Q5] Find $u+y$ and $2u+3y$ where

$$u = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix} \quad y = \begin{bmatrix} 10 & -5 & 7 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$$

Code :-

```
>x=matrix(nrow=3, ncol=3, data=c(4,7,9,-2,0,-5,6,7,3))
>x
 [,1] [,2] [,3]
 [1,] 4 -2 6
 [2,] 7 0 7
 [3,] 9 -5 3
```

```
>y=matrix(nrow=3, ncol=3, data=c(10,12,15, -5, -4, -6, 7, 9, 5))
>y
 [,1] [,2] [,3]
 [1,] 10 -5 7
 [2,] 12 -4 9
 [3,] 15 -6 5
```

> $2^T x + 3^T y$

[,1]	[,2]	[,3]
[1,] 38	-19	33
[2,] 50	-12	41
[3,] 63	-28	21

> $x+y$

[,1]	[,2]	[,3]
[1,] 14	-7	13
[2,] 19	-4	16
[3,] 24	-11	8

Q6] Marks of Statistics of Computer Science Student
 59, 20, 35, 24, 46, 56, 55, 45, 27, 22, 27, 58, 54,
 40, 50, 32, 36, 29, 35, 39

Code :-

```
>x=c(59,20,35, 24, 46, 56, 55, 45, 27, 22, 27, 58, 54,
  40, 50, 32, 36, 29, 35, 39)
```

> breaks = seq(20, 60, 5)

> a = cut(x, breaks, right = FALSE)

> b = table(a)

> c = transform(b)

>c

	a	Freq
1	[20, 25)	3
2	[25, 30)	2
3	[30, 35)	1
4	[35, 40)	4
5	[40, 45)	1
6	[45, 50)	3
7	[50, 55)	2
8	[55, 60)	4

~~Ax/2111~~

TOPIC:- Probability Distribution

PRACTICAL-02

Q Check whether following are P.M.F or not

n	$P(n)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

$\because P(2) = -0.5$, it can't be a probability mass function, since in P.M.F, $P(n) = 0$ for n .

n	1	2	3	4	5
$P(n)$	0.2	0.2	0.3	0.2	0.2

It cannot be a P.M.F as in P.M.F

$$\sum P(n) \neq 1$$

Code:- $\text{prob} \Rightarrow c(0.2, 0.2, 0.3, 0.2, 0.2)$
 $\Rightarrow \text{sum(prob)}$

$$[1] 1.1$$

3

u	10	20	30	40	50
$P(u)$	0.2	0.2	0.35	0.15	0.1

It is a Probability mass function as
in P.M.F $\sum P(u) = 1$

Code :- Prob=c(0.2, 0.2, 0.35, 0.15, 0.1)

Sum(Prob)

[1] 1

Q.2) a) Find C.D.F for following P.M.F and States the graph.

x	10	20	30	40	50
$P(u)$	0.2	0.2	0.35	0.15	0.1

Code :-

Prob=c(0.2, 0.2, 0.35, 0.15, 0.1)

sum(Prob)

[1] 1

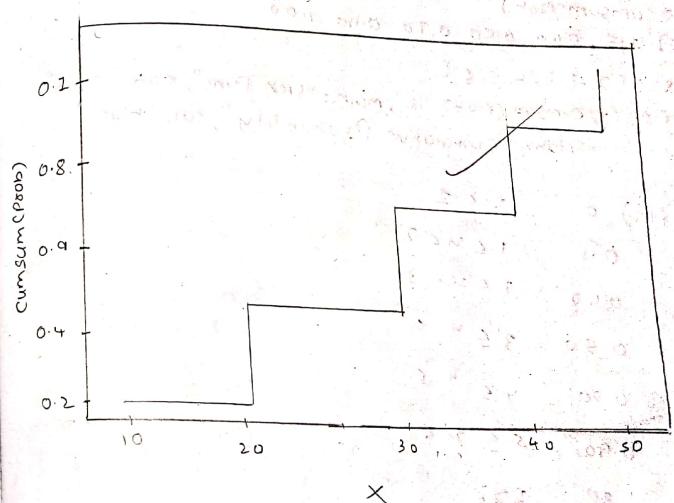
cumsum(Prob)

[1] 0.20 0.40 0.75 0.90 1.00

$x=c(10, 20, 30, 40, 50)$

plot(x, cumsum(Prob), "S")

$$\begin{aligned} f(u) &= 0 & u < 10 \\ &0.2 & 10 \leq u < 20 \\ &0.4 & 20 \leq u < 30 \\ &0.75 & 30 \leq u < 40 \\ &0.95 & 40 \leq u < 50 \\ &1.0 & u \geq 50 \end{aligned}$$



480

u	1	2	3	4	5	6
$p(u)$	0.15	0.25	0.1	0.2	0.2	0.1

Code:

```
> Prob=c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)
> Sum(Prob)
```

[1] 1

```
> Cumsum(Prob)
```

[1] 0.15 0.40 0.50 0.70 0.90 1.00

```
> x=c(1, 2, 3, 4, 5, 6)
```

```
> plot(x, Cumsum(Prob), "s", main="Step Func", xlab="Values",
       ylab="Cumulative Probability", col="blue")
```

$$f(x) = 0 \quad u < 1$$

$$0.15 \quad 1 \leq u < 2$$

$$0.40 \quad 2 \leq u < 3$$

$$0.50 \quad 3 \leq u < 4$$

$$0.70 \quad 4 \leq u < 5$$

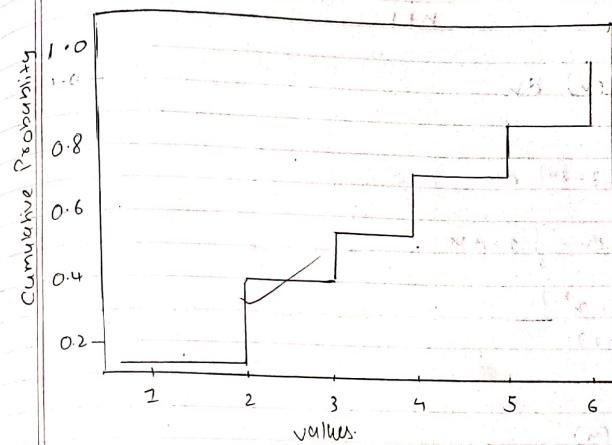
$$0.90 \quad 5 \leq u < 6$$

$$1.00 \quad u \geq 6$$

055

Graph:-

Step Func



(ii) Check whether the following is P.d.f or not.

$$\text{(i)} \quad f(u) = 3 - 2u ; \quad 0 \leq u \leq 1$$

$$\text{(ii)} \quad f(u) = 3u^2 ; \quad 0 \leq u \leq 1$$

Formula:-

$$u^n du = \frac{u^{n+1}}{n+1}$$

i) $\int_0^1 f(u) du$

$$\int_0^1 (3 - 2u) du$$

$$\int_0^1 3 du - \int_0^1 2u du$$

$$= [3u - u^2]$$

$$= [3 - 1]$$

$$= 2$$

ii) $\int_0^1 f(u)$

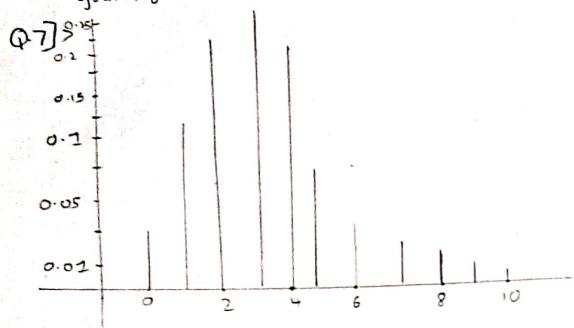
$$\int_0^1 (3u^2) du$$

$$\left[\frac{3u^3}{3} \right]_0^1$$

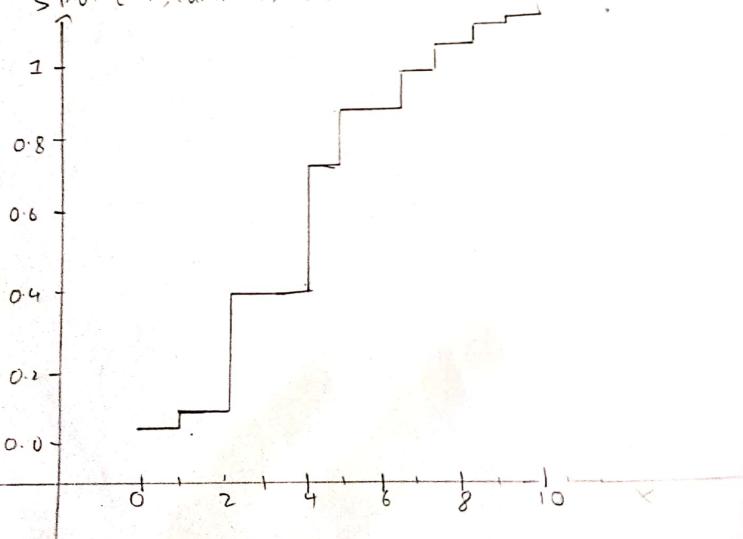
$$\cancel{\text{P.D.}} \cdot \cancel{u^2}^9$$

$$= 2$$

Graph :- $\rightarrow (n, p_{\text{binom}}, "u")$



$\rightarrow \text{plot } (x, \text{cumprob}, "s")$



TOPIC :- Binomial Distribution

PRACTICAL - 03

i) $p(x=u) = \text{dbinom}(u, n, p)$
 $\rightarrow \text{dbinom}(10, 100, 0.1)$
 $\rightarrow 0.1328653$

ii) $p(x \leq u) = P_{\text{binom}}(u, n, p)$
iii) $p(x > u) = 1 - P_{\text{binom}}(u, n, p)$
iv) If u is unknown
 $P_1 = p(x \leq u) \dots \text{(given)}$
 ~~$q_{\text{binom}}(P_1, n, p)$~~

- a1) Find the Probability of exactly 10 success in 100 trials with $p = 0.1$
 $\rightarrow \text{dbinom}(10, 100, 0.1)$
 $\rightarrow 0.1328653$

- a2) Suppose there are 12 MCA. Each question has 5 option out of which 1 is correct. Find the Probability of:-
i) Exactly 4 correct answers
ii) Almost 4 correct answers
iii) More than 5 correct answer
 $\rightarrow \text{dbinom}(4, 12, 1/5)$
 $\rightarrow 0.1328756$
ii) $P_{\text{binom}}(4, 12, 1/5)$
 $\rightarrow 0.0274445$
iii) $1 - P_{\text{binom}}(4, 12, 1/5)$
 $\rightarrow 0.0725555$

Q3) Find the complete distribution when $n=5$, $P=0.1$

$\rightarrow > \text{dbinom}(0.15, 5, 0.1)$

[2] 0.59049

0.32805

0.07290

0.00810

0.00045

0.0001

Q4) $n=12$, $P=0.25$

Find :- i) $P(X=5)$, ii) $P(X \leq 5)$, iii) $P(X \geq 7)$, iv) $P(5 \leq X \leq 7)$

$\rightarrow > \text{dbinom}(5, 12, 0.25)$

[2] 0.1032414

v) $> \text{pbinom}(5, 12, 0.25)$

[2] 0.9455978

vi) $> 1 - \text{pbinom}(5, 12, 0.25)$

[2] 0.00278151

vii) $> \text{dbinom}(6, 12, 0.25)$

[2] 0.04014445.

Q5) Probability of Salesman making a sell to customer 0.15 . Find the probability of :-

i) no sells out of 10 customer

ii) More than 3 sells out of 20 customer

$\rightarrow > \text{dbinom}(0, 10, 0.15)$

[2] 0.1968744

v) $1 - \text{pbinom}(3, 20, 0.15)$

[2] 0.3522748.

Q6) A Salesman has a 20% probability of making a sell to a customer out of 30 customers. What minimum no of sells he can make 88% probability.

$\rightarrow > \text{qbinom}(0.88, 30, 0.2)$

[2] 9

Q7) X followed binomial distribution with

$n=10$ $P=0.3$

plot the graph of P.mf. and cdf

$\rightarrow > n=10$

$\rightarrow > p=0.3$

$\rightarrow > u=0.1^n$

$\rightarrow > \text{prob} = \text{dbinom}(u, n, p)$

$\rightarrow > \text{cumprob} = \text{pbinom}(u, n, p)$

$\rightarrow > \text{df} = \text{data.frame("x values" = u, "Probability" = prob)}$

$\rightarrow > \text{print(df)}$

x values	Probability
1	0.0282475249
2	0.1210608210
3	0.2334744405
4	0.2668279320
5	0.2001209490
6	0.1029193452
7	0.0367569090
8	0.0090016920
9	0.0014467005
10	0.000137810
11	0.000059048

Source Code :-

```

Q.1) > M=12, S=3
    > P1=pnorm(15,12,3)
    [1] 0.8413447

    > P2=pnorm(13,12,3)-pnorm(10,12,3)
    [2] 0.3780661
    cat("P(10<=x<=13) = ", P2)
    P(10<=x<=13) = 0.3780661

    > P3=1-pnorm(14,12,3)
    [2] 0.2524925
    cat("P(x>14) = ", P3)
    P(x>14) = 0.2524925

    > rnorm(5,12,3)
    [2] 16.380316 13.539877 13.050514 4.181289

```

(Q.2)

```

    > P1=pnorm(7,10,2)
    [1] 0.0668072
    > P2=pnorm(12,10,2)-pnorm(5,10,2)
    [2] 0.8351351
    > P3=1-pnorm(12,10,2)
    [2] 0.1586553
    > rnorm(10,10,2)
    [2] 9.856516 10.298521 7.140323 11.081558 11.662138
    11.662138 11.186453 9.782776 9.926634 9.595926
    > qnorm(0.4,10,2)
    [2] 9.493306

```

TOPIC :- Normal Distribution

Practical - 04

$$P(X=\mu) = \text{dnorm}(\mu, \mu, \sigma)$$

$$P(X \leq \mu) = \text{pnorm}(\mu, \mu, \sigma)$$

$$P(X > \mu) = 1 - \text{pnorm}(\mu, \mu, \sigma)$$

To generate random numbers from the normal distribution (n random numbers) the R code is
 $\text{rnorm}(n, \mu, \sigma)$

Q.1 A random variable x follows a normal distribution with mean $\mu=12$ and Standard Deviation $(\sigma)=3$.
 Find :- i) $P(x \leq 15)$ ii) $P(10 \leq x \leq 13)$ iii) $P(x > 14)$
 iv) Generate 5 observation (random numbers)

Q.2 x follows normal distribution with $\mu=10, \sigma=2$
 Find :- i) $P(x \leq 7)$ ii) $P(5 \leq x \leq 12)$ iii) $P(x > 12)$
 iv) Generate 10 Observation (random numbers)
 v) Find k such that $P(x < k) = 0.4$

Q.3 Generate five random numbers from a normal distribution $\mu=15, \sigma=4$
 Find :- Sample mean, median, SD and print it

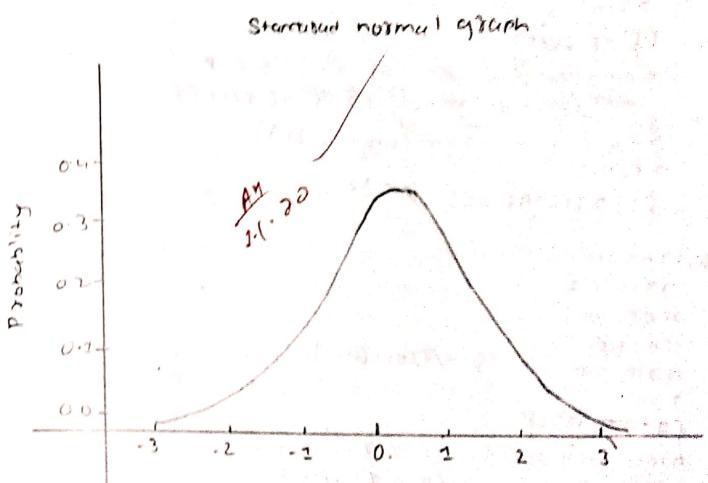
Q.4 x follows normal $x \sim N(30, 100)$
 Find :-

Q20

- i) $P(X \leq 40)$
ii) $P(X > 35)$
iii) $P(25 \leq X \leq 35)$
iv) Find K such that $P(X \leq K) = 0.6$
- Q3) i) $pnorm(40, 30, 10)$
[2] 0.8413447
- ii) $1 - pnorm(35, 30, 10)$
[2] 0.3085375
- iii) $pnorm(35, 30, 10) - pnorm(25, 30, 10)$
[2] 0.3829249
- iv) $qnorm(0.6, 30, 10)$
[2] 32.53347
- Q4) i) $X \sim \mathcal{N}(12, 4)$
[2] 5.734772 15.554360 8.161930 13.176196 13.919685
ii) $\text{cm} = \text{mean}(x)$ cat("Sample mean is:", cm)
[2] 12.29629 Sample mean is 12.29619
n = 5
- iv) $\text{variance} = (n-1)^* \text{var}(x)/n$
 variance
[2] 13.03186
- v) $\text{sd} = \text{sqrt}(\text{variance})$ cat("Sample sd is:", sd)
sd
[2] 3.63254 Sample sd is 3.63254
- vi) $\text{me} = \text{median}(x)$ cat("Sample median is:", me)
[2] 13.1702 Sample median is 13.1702

Q60

Q5] plot the standard normal graph
 $x = seq(-3, 3, by = 0.1)$
 $y = dnorm(x)$
plot(x, y, main = "21 values", ylab = "Probability",
main = "standard normal graph")



080

source code :-

```

Q1] >mu=15
>mx=14
>sd=3
>n=400
>zcal=(mx-mu)/(sd/(sqrt(n)))
>zcal
[1]-6.6667
>cat("calculated value of z is:",zcal)
calculated value of z is:-6.6667
>pvalue=2*(1-pnorm(qbs(zcal)))
>pvalue
[1] 2.616796e-11

Q2] >mu=10
>mx=10.2
>sd=2.25
>n=400
>zcal=(mx-mu)/(sd/sqrt(n))
>zcal
[1] 1.77778
>cat("calculated value of z is:",zcal)
calculated value of z is 1.77778
>pvalue=2*(1-pnorm(qbs(zcal)))
>pvalue
[1] 0.67544036
  
```

TOPIC: Normal & t-test

081

Practical - 05

Q1) Test of Hypothesis :-

 $H_0: M = 15$ $H_1: M \neq 15$

A random sample is drawn of size 400 and it is calculated the sample mean is 14 and Standard deviation is 3. Test the hypothesis at 5% level of Significance.

Since pvalue is less than 0.05 we reject $H_0: M = 15$.

Q2) Test the hypothesis $H_0: M = 0$, $H_1: M \neq 10$.

A random sample of size 400 is drawn with sample mean 10.2 and sd 2.25. Test the hypothesis at 5% level of significance.

Since pvalue is greater than 0.05 we accept $H_0: M = 15$.

- Q3) Test the hypothesis H_0 proportion of smokers in a college is 0.2. A sample is collected and it is calculated the sample proportion, calculated as 0.125. Test the hypothesis at 5% level of significance (sample size is 400)

Since P value is less than 0.05 we reject H_0

- Q4) Last Year farmers lost 20% of their crop. A random sample of 60 field fields are collected and it is found that 9 fields crops are insect polluted. Test the hypothesis of 1% level of Significance.

Since P value is greater than 0.05 we accept H_0

R>P=0.2
 >p=0.125
 >n=400
 >Q=1-P
 $\gt z_{cal} = (p - P) / (\sqrt{P(1-P)/n})$
 >zcal

[1]-3.75
 $\gt pvalue = 2 * (1 - pnorm(zcal))$
 >pvalue

[1] 0.0001768346
 $\gt cat("calculated value of z is:", zcal)$
 $\gt cat("calculated value of z is:", -3.75)$

Q4>P=0.2
 >p=0.160
 >n=60
 >Q=1-P
 $\gt z_{cal} = (p - P) / (\sqrt{P(1-P)/n})$
 >zcal

[1] -0.9682458
 $\gt cat("calculated value of z is:", zcal)$
 $\gt cat("calculated value of z is:", -0.9682458)$

>pvalue=>(1-pnorm(zcal))
 >pvalue
 [1] 0.3329216

(Q8) $x = c(12.25, 12.97, 12.15, 12.08, 12.31, 12.28, 12.94,$
 $12.89, 12.16, 12.04)$

$>n = \text{length}(x)$

$>n$

[2] 10

$>mx = \text{mean}(x)$

$\text{variance} = (n-1) * \text{var}(x)/n$

$>sd = \text{sqrt}(\text{variance})$

$>t = (mx - m0) / (sd / \text{sqrt}(n))$

$>t$

[2] -8.89 4.909

$>pvalue = 2 * (1 - \text{pnorm}(|t|))$

$>pvalue$

[2] 0.000226 0

(Q5) Test the hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of significance.

Since P value is less than 0.05 we reject H_0

AN
 (61.2)

Topic :- Large Sample Test

23/01/20

Practical - 06

- (Q1) Let the population mean (the amount spent per customer in a restaurant) is 250. A sample of 100 customers selected. The sample mean is calculated 275 and S.D 30. Test the hypothesis that population mean is 250 or not at 5% level of significance.

- (Q2) In a random sample of 1000 students it is found that 750 use blue pen. Test the hypothesis that the population proportion is 0.8 at 1% level of significance.

code :- $H_0: M = 250$ against $H_1: M \neq 250$

$$\begin{aligned} Q.1) & m_0 = 250 \\ & \bar{x} = 275 \\ & S.d = 30 \\ & n = 100 \\ & z_{cal} = (\bar{x} - m_0) / (S.d / \sqrt{n}) \\ & z_{cal} \\ & [Q] 8.333 \end{aligned}$$

\Rightarrow cal("Calculated value of \bar{z} is =", z_{cal})
 Calculated value of \bar{z} is = 8.333
 $\rightarrow p\text{value} = 2 * (1 - \text{norm}(z_{cal}))$
 $\rightarrow p\text{value}$

[Q] 0

$P\text{value} = 0.000$, we reject H_0 at 5% level of significance.

$H_0: P = 0.8$ against $H_1: P \neq 0.8$

064

$$\begin{aligned} Q.1) & P = 0.8 \\ & \bar{P} = 0.750 \\ & n = 1000 \\ & z_{cal} = (\bar{P} - P) / (\sqrt{P(1-P)/n}) \\ & z_{cal} \\ & [Q] 5.224 - 3.952847 \\ & \Rightarrow \text{cal("Calculated value of } z \text{ is =", } z_{cal} \text{)} \\ & \text{calculated value of } z \text{ is = } 5.224 - 3.952847 \\ & \rightarrow p\text{value} = 2 * (1 - \text{norm}(z_{cal})) \\ & \rightarrow p\text{value} \\ & [Q] 7.72268e-0.5 \\ & \Rightarrow p\text{value is greater than 0.05 we accept } H_0 \end{aligned}$$

- (Q3) Two random sample of size 1000 and 2000 are drawn from two population with the same S.D 2.5. The sample means are 67.5 and 68. respectively. Test the hypothesis $H_0: M_1 = M_2$ at 5% level of significance.

- (Q4) A study of noise level in two hospital is given below test the claim that the two hospitals have same level of noise at 1% level of significance.

	Hospital A	Hospital B
Size	84	34
Mean	61.2	59.4
S.D	7.9	7.5

Q3) In a sample of 600 students in a college 600 like blue ink. In another college from a sample of 900 students 450 like blue ink. Test the hypothesis that the proportion of student liking blue ink in two colleges are equal or not at 1% level of significance.

$$Q3) H_0: p_1 = p_2 \text{ vs } H_1: p_1 \neq p_2$$

$$n_1 = 600$$

$$n_2 = 900$$

$$\hat{p}_{m1} = 0.6667$$

$$\hat{p}_{m2} = 0.5$$

$$\hat{s}_{p1} = 0.05$$

$$\hat{s}_{p2} = 0.05$$

$$\hat{Z}_{cal} = (\hat{p}_{m1} - \hat{p}_{m2}) / \sqrt{\hat{p}_{m1}(1 - \hat{p}_{m1})/n_1 + \hat{p}_{m2}(1 - \hat{p}_{m2})/n_2}$$

$$\hat{Z}_{cal}$$

$$= 5.763978$$

$$P\text{value} = 2 * (1 - \text{pnorm}(\hat{Z}_{cal}))$$

$$P\text{value}$$

$$= 2.417564e-07$$

$\therefore P\text{value} = 2.417564e-07 < 0.05$, we accept $H_0: p_1 = p_2$

at 5% level of significance.

✓

$H_0: p_1 = p_2 \text{ against } H_1: p_1 \neq p_2$

$$n_1 = 600$$

$$n_2 = 900$$

$$\hat{p}_{m1} = 0.6722$$

$$\hat{p}_{m2} = 0.5944$$

$$\hat{s}_{p1} = 0.0291$$

$$\hat{s}_{p2} = 0.0316$$

$$\hat{Z}_{cal} = (\hat{p}_{m1} - \hat{p}_{m2}) / \sqrt{\hat{p}_{m1}(1 - \hat{p}_{m1})/n_1 + \hat{p}_{m2}(1 - \hat{p}_{m2})/n_2}$$

$$\hat{Z}_{cal}$$

$$= 1.62528$$

$$P\text{value} = 2 * (1 - \text{pnorm}(\hat{Z}_{cal}))$$

$$P\text{value}$$

$$= 0.2450222$$

$\therefore P\text{value} = 0.2450222 > 0.05$, we ~~reject~~ accept $H_0: p_1 = p_2$

at 5% level of significance.

✓

$H_0: p_1 = p_2 \text{ against } H_1: p_1 \neq p_2$

$$n_1 = 600$$

$$n_2 = 900$$

$$\hat{p}_{m1} = 0.6667$$

$$\hat{p}_{m2} = 0.5$$

$$\hat{p} = (n_1 * \hat{p}_{m1} + n_2 * \hat{p}_{m2}) / (n_1 + n_2)$$

$$\hat{q} = 1 - \hat{p}$$

$$P = 0.566617$$

$$\hat{Z}_{cal} = 2 * (1 - \text{pnorm}(\hat{Z}_{cal}))$$

$$P\text{value}$$

$$\hat{Z}_{cal} = (\hat{p}_{m1} - \hat{p}_{m2}) / \sqrt{\hat{p}_{m1}(1 - \hat{p}_{m1})/n_1 + \hat{p}_{m2}(1 - \hat{p}_{m2})/n_2}$$

$$\hat{Z}_{cal}$$

$$= 6.381534$$

$\text{>} p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(2 * \text{ca}1)))$
 $\text{>} p\text{value}$
 $[1] 1.753222e-10$
 $\text{pvalue} = 1.753222e-10 < 0.05$, we reject
 $p_1 = p_2$ at 5% level of significance.

 Q6) $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$
 $\text{>} n_1 = 200$
 $\text{>} n_2 = 200$
 $\text{>} p_1 = 44/200$
 $\text{>} p_2 = 30/200$
 $\text{>} p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$
 $\text{>} p$
 $[1] 0.185$
 $\text{>} q = 1 - p$
 $\text{>} 2 * \text{ca}1$
 $\text{>} 2 * \text{ca}1 * (p_1 - p_2) / (\sqrt{n_1 * p_1 * (1 - p_1)} + \sqrt{n_2 * p_2 * (1 - p_2)})$
 $\text{>} 2 * \text{ca}1$
 $[1] 1.802741$
 $\text{>} p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(2 * \text{ca}1)))$
 $\text{>} p\text{value}$
 $[1] 0.0714288$
 $\text{p value} = 0.0714288$, we accept $p_1 = p_2$ at
 5% level of significance

TOPIC 8: Small Sample Test

066

PRACTICAL 8 07

Q1) The marks of 10 students are given as 63, 63, 66, 67, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from a population of average marks 66.

Solution:-

$\text{>} u = c(63, 63, 66, 67, 68, 69, 70, 70, 71, 72)$

$\text{>} t.test(u)$

One Sample t-test

data: u

$t = 68.319$, $df = 9$, $p\text{-value} = 1.558e-13$ $\text{alternative hypothesis: mean is not equal to } 66$
 confidence interval: 65.65171 70.14829

Sample estimates:

mean of u

67.9

Since $p\text{-value}$ is less than 0.05 we reject hypothesis
 at 5% level of significance.

$\text{>} \text{lo}5 = 0.05$

$\text{>} \text{pvalue} = 1.558e-13$

$\text{>} \text{if}(\text{pvalue} > 0.05) \{ \text{cat}("accept H0") \}$

$\text{else} \{ \text{cat}("reject H0") \}$

reject H0?

- Q2] Two groups of students score the following marks. Test the hypothesis that there is no significant difference between the two groups.
- group1 = 18, 22, 21, 17, 20, 17, 23, 20, 22, 27
 group2 = 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

Solution:

H_0 : There is no difference between two groups.

$> u = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 27)$

$> y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$

$> t.test(u, y)$

Welch Two Sample t-test

data: x and y

$t = 2.2573$, $df = 16.376$, $p\text{-value} = 0.03798$.

Alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval:

0.1628205 5.0371795

Sample Estimates:

mean of x mean of y

20.1 17.5

$> pvalue = 0.0379$

$> \text{if}(pvalue > 0.05) \{ \text{cat}("Accept } H_0") \}$
 $\text{else} \{ \text{cat}("Reject } H_0") \}$

(reject H_0)

Since P-value is less than 0.05 we reject hypothesis at 5% level of significance.

- Q3] The sales data of six shops before and after a special campaign are given below:
- Before : 53, 28, 31, 48, 50, 42.
 After : 58, 29, 30, 55, 56, 45.

Test the hypothesis that the campaign is effective or not.

Solution:- H_0 : There is no significant difference of sales before and after the campaign

$> u = c(53, 28, 31, 48, 50, 42)$

$> y = c(58, 29, 30, 55, 56, 45)$

$> t.test(u, y, paired = T, alternative = "greater")$

Paired t-test

data: u and y

$t = -2.7815$, $df = 5$, $p\text{-value} = 0.0806$

Alternative hypothesis: true difference in means is greater than 0

95 percent confidence interval

- 6.035547 Inf

Sample Estimates:

mean of the difference

-3.5

$> pvalue = 0.0806$

```
> if(pvalue > 0.05) {cat("accept H0")}
else {cat("reject H0")}
accept H0
Since p-value is greater than 0.05 we accept hypothesis at 5% level of Significance.
```

(Q4) Two median are applied to the two group of patient respectively

Group 1: 10, 12, 13, 11, 14
Group 2: 8, 9, 12, 14, 15, 10, 9

Is there any significance difference between two medicions?

Solution:-

```
> u=c(10, 12, 13, 11, 14)
> y=c(8, 9, 12, 14, 15, 10, 9)
> t.test(u, y)
```

Welch Two Sample t-test

data: u and y

t = -0.80384, df = 9.7894, p-value = 0.4406

alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval:

-1.781171 3.71171

Sample estimates:

Mean of u and y:

12 11

pvalue = 0.4406

```
> if(pvalue > 0.05) {cat("accept H0")}
else {cat("reject H0")}
reject H0
```

(Q5) The following are the weight before and after the diet program effective.

Before: 120, 125, 115, 130, 123, 119

After: 100, 114, 95, 90, 115, 99

Solution:- H0: There is no significant difference

> u=c(120, 125, 115, 130, 123, 119)

> y=c(100, 114, 95, 90, 115, 99)

> t.test(u, y, paired=T, alternative="less")

Paired t-test
data: u and y

t = -4.3458, df = 5, p-value = 0.9963

alternative hypothesis: true difference in means is less than 0

95 percent confidence interval:

-Inf 29.0295

Sample estimates:

mean of the differences

19.83333

pvalue = 0.9963

820

> if (pvalue > 0.05) { cut("accept H0") }

else { cut("reject H0") }

Accept H0 >

Since the p-value is greater than 0.05, we accept the hypothesis at 5% of significance.

M

PRACTICAL : 08

Practical 08 Large and Small Sample tests

Q.1 The arithmetic mean of a sample of 100 items from a large population is 52. If the standard deviation is 7, test the hypothesis that the population mean is 55 against the alternative it is more than 55 at 5% LOS.

Q.2 In a big city 350 out of 700 males are found to be smokers. Does the information supports that exactly half of the males in the city are smokers? Test at 1% LOS.

Q.3 Thousand articles from a factory A are found to have 2% defectives, 1500 articles from a 2nd factory B are found to have 1% defective. Test at 5% LOS that the two factories are similar or not.

Q.4. A sample of size 400 was drawn at a sample mean is 99. Test at 5% LOS that the sample comes from a population with mean 100 and variance 64.

Q.5. The flower stems are selected and the heights are found to be (cm) 63, 63, 68, 69, 71, 71, 72 test the hypothesis that the mean height is 66 or not at 1% LOS.

Q.6. Two random samples were drawn from 2 normal populations and their values are A- 66, 67, 75, 76, 82, 84, 88, 90, 92 B- 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97. Test whether the populations have the same variance at 5% LOS.

7. A company producing light bulbs finds that mean life span of the population of bulbs is 1200 hours with s.d. 125. A sample of 100 bulbs have mean 1150 hours. Test whether the difference between population and sample mean is significantly different?

8. From each of two consignments of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples in two assignments are significantly different at 1% LOS?

	Sample size	No. of bad apples
Consignment 1	200	44
Consignment 2	300	56

070

Answer:

$$[1] H_0: \mu = 55$$

$$H_1: \mu > 55$$

$$n = 100$$

$$m = 52$$

$$s.d. = 7$$

$$z_{cal} = (m - \mu) / (s.d / (\sqrt{n}))$$

$$z_{cal}$$

$$[-4.285174]$$

$$p-value = 2 * (1 - \text{pnorm}(z_{cal}))$$

$$p-value$$

$$[1] 1.82153e-05$$

z_{cal} calculated \geq value is $= z_{cal}$ calculated \geq value
 $is = -4.285174$

$$p-value = 2 * (1 - \text{pnorm}(z_{cal}))$$

$$p-value$$

$$[1] 1.82153e-05$$

Since p-value is less than 0.05 we reject the hypothesis at 5% level of significance.

$$[1] H_0: \mu$$

$$p = 0.5$$

$$H_1: p \neq 0.5$$

$$p = 350 / 100$$

$$n = 700$$

$$z_{cal} = (p - \mu) / (\sqrt{\mu(1-\mu)/n})$$

$$z_{cal}$$

$$[1] 0$$

\gttext{zcal} ("calculated z value is = ", $zcal$) calculated z value is = 0.

$\gttext{P value}$ = $2 * (1 - \text{pnorm}(\text{abs}(zcal)))$
 $\gttext{P value}$.

[1] 1

Since p value is greater than 0.05 we accept hypothesis at 1% level of significance

Q3) $H_0: P_1 = P_2$ vs $H_1: P_1 \neq P_2$

$\gttext{n}_1 = 1000$

$\gttext{n}_2 = 1500$

$\gttext{p}_1 = 0.02$

$\gttext{p}_2 = 0.01$

$\gttext{P} = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

\gttext{P}

[1] 0.014

$\gttext{q} = 1 - P$

\gttext{q}

$\gttext{zcal} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$

\gttext{zcal}

[1] 2.084842

$\gttext{P value} = 2 * (1 - \text{pnorm}(\text{abs}(zcal)))$
 $\gttext{P value}$

[1] 0.03708364.

Since p value is less than 0.05, we reject the hypothesis.

a4) $H_0: M = 100$

$\gttext{m}_1 = 99$

$\gttext{m}_0 = 100$

$\gttext{s}_d = 8$

$\gttext{n} = 400$

$\gttext{zcal} = (m_1 - m_0) / (s_d / \sqrt{s_d^2 + n})$

\gttext{zcal}

[1] -2.5

$\gttext{P value} = 2 * (1 - \text{pnorm}(\text{abs}(zcal)))$
 $\gttext{P value}$

[1] 0.02241933

Since p value is less than 0.05, we reject the hypothesis at 5% of Significance

a5) $x = c(63, 63, 68, 69, 71, 71, 72)$

$\gttext{t.test}(x)$

One Sample t-test

data: x

t = 47.94, df = 6, p-value = 5.522e-09

alternative hypothesis: true mean is not equal to
95 percent confidence interval:

150

64.66479 71.62092
 Sample estimate:
 mean of x
 68.14286
 $H_0: \mu = 62$
 $x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$
 $y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$
 $\text{var.test}(x, y)$

F test to compare two variances

data: x and y
 $F = 0.70686$, num df = 8, denom df = 10, p-value
 $= 0.6359$.

Alternative hypothesis: true ratio of variances
 is not equal to 1

95 percent confidence interval:
 $0.183362 \quad 3.0360393$

Sample estimates:
 ratio of variances
 0.7068567

$p\text{value} = 0.6359$
 $\text{if } (\text{pvalue} > 0.05) \{ \text{cat}("Accept H}_0 \text{") \} \text{ else } \{ \text{cat}("reject") \}$
 Accept H_0

Since p-value is greater than 0.05 we
 accept hypothesis at 5% level of
 significance.

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(7) $H_0: \mu = 1200$
 $\mu_{\text{min}} = 1150$
 $\mu_{\text{max}} = 1200$
 $n = 100$
 $s_d = 125$
 $z_{\text{cal}} = (\bar{x} - \mu_0) / (s_d / (\sqrt{n}))$
 z_{cal}
 $[1] -4$
 $p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 $p\text{value}$
 $[1] 6.334248e-05$
 $\text{cat}("Calculated z value is = -4")$
 Since p-value is less than 0.05 we
 reject hypothesis.

(8) $H_0: p_1 = p_2$
 $n_1 = 200$
 $n_2 = 300$
 $p_1 = 44/200$
 $p_2 = 56/300$
 $p = (n_1 + p_1 + n_2 + p_2) / (n_1 + n_2)$
 p
 $[1] 0.2$
 $q = 1 - p$
 $z_{\text{cal}} = (p_1 - p_2) / \text{sqrt}(p * q * (1/n_1 + 1/n_2))$
 z_{cal}

550

```
[1] 0.9128709  
>>cat("calculated z value is : ", 2e-01)  
calculated z value is : 0.9128703  
>pvalue=2*(1-pnorm(abs(zval)))  
>pvalue  
[1] 0.3613104  
Since pvalue is greater than 0.05  
∴ we accept the hypothesis.
```

My 2nd

073

PRACTICAL 8 09

TOPIC :- CHI² TESTS AND ANOVA

Q1) USE THE FOLLOWING DATA TO TEST WHETHER THE CONDITION OF THE HOME AND CONDITION OF CHILD ARE INDEPENDENT OR NOT

	Clean	Dirty
Clean	70	50
Fairly	80	20
Dirty	35	40

H0: Condition of the Home and Child independent

>>u=c(70, 80, 35, 50, 20, 40)

>m=3

>n=2

>y=matrix(u, nrow=m, ncol=n)

>y

```
[1] [2]  
[1,] 70 50  
[2,] 80 20  
[3,] 35 40
```

>pv=chisq.test(y)

>pv

Pearson's Chi-square test

data: y

X-Squared = 25.646, df = 2, P-value = 2.698e-06

\because P-value is less than 0.05 we reject the hypothesis at 5% level of Significance.

(Q.2) Test the hypothesis that the vaccination and the disease are independent or not.

Vaccine	
AF	Not AF
AFF	70
NA	35

\rightarrow H_0 : Disease and vaccination are independent

$\geq x = c(70, 35, 46, 37)$

$\geq m = 2$

$\geq n = 2$

$\geq y = matrix(x, nrow = m, ncol = n)$

$\geq y$

$\begin{bmatrix} 1,1 & 1,2 \\ 2,1 & 70 & 46 \\ 2,2 & 35 & 37 \end{bmatrix}$

$\geq p_value = chisq.test(y)$

$\geq p_value$

Pearson's Chi-Squared test with Yate's continuity correction

data: y

X-squared = 2.0275, df = 1, p-value = 0.1545

\therefore P-value is more than 0.05 we cannot reject the hypothesis at 5% level of Significance

(Q.3) Perform a ANOVA for the following data.

Type	Observation
A	50, 52
B	53, 55, 53
C	60, 58, 57, 56
D	52, 54, 54, 55

$\rightarrow H_0$: Means are equal for A, B, C, D

$\geq u_1 = c(50, 52)$

$\geq u_2 = c(53, 55, 53)$

$\geq u_3 = c(60, 58, 57, 56)$

$\geq u_4 = c(52, 54, 54, 55)$

$\geq d = stack(list(u_1 = u_1, u_2 = u_2, u_3 = u_3, u_4 = u_4))$

$\geq names(d)$

$\geq \{1\} "values" "ind"$

$\geq one-way.test(values ~ ind, data = d, var.equal = T)$

One-way analysis of means

data: values and ind

F = 11.735, num df = 3, denom df = 9, p-value = 0.00183

$\geq anova = aov(values ~ ind, data = d)$

DF	Sum Sq	mean Sq	F value	Pr(>F)
ind	3	71.06	23.688	11.73 0.00183*
Residuals	9	18.17	2.019	

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 '

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since p-value is less than 0.05 we reject the hypothesis at 5% level of significance.

(Q4) The following data of the life of the tyre of four brand

Types	life
A	20, 23, 18, 17, 22, 24
B	19, 15, 17, 20, 16, 17
C	21, 19, 22, 17, 20
D	15, 14, 16, 18, 14, 16

→ H₀: The average life of tyre is equal!

A, B, C, D

> x2=c(20, 23, 18, 17, 22, 24)

> u2=c(19, 15, 17, 20, 16, 17)

> x3=c(21, 19, 22, 17, 20)

> u4=c(15, 14, 16, 18, 14, 16)

> d=stacklist(b1=x1, b2=x2, b3=x3, b4=u4)

> names

[2] "values" "ind"

> oneway.test(values~ind, data=d, var.eq.yes=T)

One-way analysis of means

data: values and ind

F = 7.4403, num df = 3, denom df = 19, P-value = 0.001

since p-value is less than 0.05 we reject the hypothesis at 5% level of significance

075

Q5) Import excel file in R software.

> x=read.csv("C:/Users/admin/Desktop/marks.csv")

	STATS	MATHS
1	46	68
2	45	48
3	42	47
4	25	20
5	37	25
6	36	27
7	49	57
8	59	58
9	20	25
10	27	27

> am=mean(x\$STATS)

> am

[2] 37

> me=median(x\$STATS)

> me

[2] 38.5

> n=length(x\$STATS)

> sd=sqrt((n-1)*var(x\$STATS)/n)

> sd

[2] 12.64911

250

> $\text{cm} = \text{mean}(x\$MATHS)$

> cm

[1] 40.2

> $\text{me} = \text{median}(x\$MATHS)$

> $\text{me} = 37$

> $n = \text{length}(x\$MATHS)$

> $s^2 = \text{sqrt}((n-1) * \text{var}(x\$MATHS)/n)$

> s^2

[1] 16.42437

> $\text{cor}(x\$STATS, x\$MATHS)$

[1] 0.7802508

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29
90

PRACTICAL: 10

TOPIC:- Non Parametric Test

- Q1] Following are the amount of sulphur oxide emitted by industry in 20 days. Apply sign test to test the hypothesis that the population median is 21.5 at 5% of significance

17, 15, 20, 29, 18, 22, 25, 27, 9, 24, 20,
17, 6, 24, 14, 15, 23, 24, 26

H0:

Population median is 21.5

> u=c(17..., 26)

> length(u)

[1] 20

> me=21.5

> sp=length(u[u>me])

> sn=length(u[u<me])

> n=sp+sn

> pv=pbinom(sp, n, 0.5)

> PV

[1] 0.4219015

Since p value is more than ~~0.05~~ 0.05, we accept the hypothesis of 5% of level of significance

Note: If the alternative is median not equal to ($H_1 \neq m_e$) then $P_U = \text{binom}(SP, n, 0.5)$ and if ($H_1 > m_e$) then $P_U = \text{binom}(SN, n, 0.5)$.

- Q.2] Following is the data of ten observations applying Sign Test to test the hypothesis that the population median is 625, begins the alternative it is more than 625.

$x = [612, 619, 631, 628, 643, 640, 655, 649, 670, 663]$

H_0 : Population median is 625

$\geq n = c(612 \dots 663)$

$\geq \text{length}(n)$

[1] 10

$\geq m_e = 625$

$\geq SP = \text{length}(x[x > m_e])$

$\geq SN = \text{length}(n[n > m_e])$

$\geq n = SP + SN$

$\geq P_U = \text{binom}(SN, n, 0.5)$

$\geq P_U$

[1] 0.0546875

Since pvalue is more than 0.05, we accept the hypothesis of 5% of significance value

Q.3) Following are values of a sample test the hypothesis that a population median is 600 against the alternative it is more than 600 at 5% level of significance using Wilcoxon Signed Ranked Test

$x = [63, 65, 60, 89, 61, 71, 58, 57, 69, 62, 63, 39, 72, 69, 48, 66, 72, 63, 87, 69]$

$\rightarrow H_0$: Population median is 600

$\geq x = c(63 \dots 69)$

$\geq \text{length}(x)$

[1] 20

$\geq \text{wilcox.test}(x, alter = "greater", mu = 60)$

Wilcoxon signed rank test with continuity correction

data: x

V = 145, P-value = 0.02298

Alternative hypothesis: true location is greater than 600

Since pvalue is less than 0.05, we reject the hypothesis of 5% of significance value

NOTE: If the alternative is less then alter = "less"
and if it is not equal the alter = "two-side"

q.4) Using W.S.R. Test population median is 12 or less than 12.

$x = c(15, 17, 24, 25, 20, 21, 32, 28, 25, 24, 26)$

H₀: Population median is 12
H₁: Population median is less than 12

$> length(x)$

[1] 12

$> wilcox.test(x, alter = "less", mu = 12)$

Wilcoxon Signed Rank test with continuity correction
data: x

V = 66, p-value = 0.9986

Alternative hypothesis: true location is less than 12.

Since the p-value is greater than 0.05 we accept the hypothesis at 5% level of significance

(a) The weight of the students before and after they stop smoking below. Using W.S.R. test
that there is no significant change.

Before (x)	(y) After
65	
75	72
75	74
62	72
72	66
	73

H₀: Before and after there is no significant change

H₁: There is change

$> u = c(65, 75, 75, 62, 72)$

$> y = c(72, 74, 72, 66, 73)$

$> d = x - y$

$> d$

[1] -7 2 3 -4 -1

$> wilcox.test(u, alter = "two-side", mu = 0)$

Wilcoxon Signed Rank test with continuity

data: x

V = 15, p-value = 0.05791

Alternative hypothesis: true location is not equal to

Since p-value is greater than 0.05, we accept the hypothesis at 5% level of significance

AT 5%
It is ~