PROBLEM SET 7: BINOMIAL THEOREM AND VIETA'S FORMULAS BASICS

CS 198-087: Introduction to Mathematical Thinking

UC BERKELEY EECS SPRING 2019

This homework is due on Sunday, April 14th, at 11:59 PM on Gradescope. As usual, this homework is graded on participation, but it is in your best interest to put full effort into it. This is a good opportunity to learn how to use LATEX.

1. Binomial Theorem — General Term

Let
$$g(x) = (2x^5 - 3x^2)^7$$
.

- a. What is the sum of the coefficients of the expansion of g(x)?
- b. Find the general term of the expansion of g(x).
- c. What is the coefficient on x^{20} ?
- d. What is the coefficient on x^{18} ?
- 2. Approximations with the Binomial Theorem

Use the first three terms of the binomial expansion to approximate each of the following values. Use a calculator to simplify immediate steps if need be, but only when absolutely necessary.

Compare your results with the true values.

- a. 5.02^3
- b. $31^{-\frac{1}{5}}$
- 3. Sums of Coefficients
 - a. Three roots of $x^4 + ax^2 + bx + c = 0$ are 9, -3 and 2. Determine a + b + c. (Hint: What is the coefficient of x^3 ?)
 - b. Suppose P(x) is a polynomial such that

$$x^{23} + 23x^{17} - 18x^{16} - 24x^{15} + 108x^{14} = (x^4 - 3x^2 - 2x + 9)P(x)$$

Determine the sum of the coefficients of P(x).